

# Mathematical Analysis I. Midterm Examination 2021. *Problem Set 2. Part 1*

Name \_\_\_\_\_ Group Number \_\_\_\_\_

*Solutions for each part of the examination have to be written on separate sheets! You can use a single sheet for several problems from one part of the examination (i.e. you can write solutions 1, 2 on the same sheet). Do not forget to sign **all** the sheets you submit. You can use the sheet with the tasks for solving problems as well.*

I am aware that using any electronic devices, books etc. during the examination, as well as communicating with other students, is strictly prohibited. Only one **handwritten** informational sheet is allowed. Any violation of these rules immediately leads to test cancellation. Signature \_\_\_\_\_

1. [5 points] Represent a function  $f(x) = \frac{x-1}{x^2+7x+10}$  in the neighbourhood of  $x_0 = -3$  using Taylor formula with  $o((x+3)^m)$ .
2. [6 points] Find the limit  $\lim_{x \rightarrow 0} \frac{\arctan(\sinh x) - \ln(1-x) - e^{2 \tan(x/2)} + 1 - x}{(1+x)^{2x} - \sqrt[3]{1+6x^2}}$ . *Hint: it is better not to use l'Hôpital's rule here. Use Taylor's formula with  $o(x^3)$ .*

## Mathematical Analysis I. Midterm Examination 2021. *Problem Set 2. Part 2*

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3. [4 points] Find the derivatives  $y'_x$  and  $y''_{xx}$  at point  $t_0 = 1$  if function  $y = y(x)$  is given by parametric equations  $x(t) = -\sqrt{1-t^2}$ ,  $y(t) = \arccos t - \sqrt{1-t^2}$ .
4. [4 points] Find  $y^{(m)}(x)$  if  $y = (x^2 + 4x) \sin x \cos 3x$ ,  $m \geq 3$ .

## Mathematical Analysis I. Midterm Examination 2021. *Problem Set 2. Part 3*

Name \_\_\_\_\_ Group Number \_\_\_\_\_

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5. [3 points] Find the first and the second differentials of a function  $h(x) = (5x^2 + x - 4)e^{2x}$ .
6. [4 points] Find the limit  $\lim_{x \rightarrow 1} \left( \frac{14}{1 - x^{14}} - \frac{8}{1 - x^8} \right)$ .
7. [4 points] Find the first and the second derivatives of a function  $x = x(y)$  that is inverse to a function  $y(x) = 7x + x^5$ .