

SNA-FISAC Assignment Report Format

Identification of influential nodes in complex networks: A local degree dimension approach

Team No.:5

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Analysis and Evaluation of the Local Degree Dimension (LDD) **Centrality for Identifying Influential Spreaders in Complex** **Networks**

Abstract:

The identification of influential nodes is a critical task in network science, essential for applications like epidemic control and information diffusion. Traditional centrality measures often fail to capture the nuanced roles of nodes. This project implements and evaluates the **Local Degree Dimension (LDD)**, a novel centrality measure that quantifies influence by considering both a node's degree and the structural "dimension" of its local neighborhood. We implemented the LDD algorithm in Python using networkx and compared its performance against standard metrics (Degree, Closeness, Betweenness, Eigenvector) on a custom tiny network and two real-world benchmark datasets: **Zachary's Karate Club** and **US Airlines**. The effectiveness of the rankings was evaluated using two methods: **Kendall's Tau correlation** and the **Susceptible-Infected-Recovered (SIR) model**. Our results demonstrate that LDD provides a unique and effective perspective on node influence, identifying key spreaders that are often missed by other metrics.

Introduction:

The study of complex networks has become a fundamental field for understanding complex systems in biology, technology, and society. Within this field, identifying influential nodes is a crucial and still-unsolved problem. Influential nodes are those that, due to their structural position, have a disproportionately large impact on the network's function and dynamics. Applications are diverse, from identifying "super-spreaders" in epidemics to maximizing the impact of viral marketing campaigns or, conversely, fragmenting terrorist networks.

Many centrality measures have been proposed, such as Degree, Betweenness, and Closeness. However, each has limitations. Degree is a purely local measure, while Betweenness and

Closeness are computationally expensive for large-scale networks. This project investigates a more recent approach, the Local Degree Dimension (LDD), proposed by Zhong et al.. LDD is a local metric that aims to capture a more sophisticated view of influence by not just counting neighbors (like degree) but also by assessing the diversity of their connections.

Major Contributions in the Base Paper:

- Introduction of a new, efficient centrality measure, Local Degree Dimension (LDD), to identify influential nodes.
- The LDD model is based on the hypothesis that nodes with high degrees and neighbors who are also connected to diverse (high-degree) neighborhoods are more influential.
- Demonstration that LDD can identify influential spreaders more accurately than many traditional centrality measures.
- Validation of the LDD method on numerous real-world networks using the Susceptible-Infected-Recovered (SIR) model and monotonicity analysis.

Novel contribution if any in your work when compared with base paper:

- Independent implementation of the LDD centrality measure from scratch using Python, pandas, and networkx.
- Creation and in-depth analysis of a "tiny network," including manual calculation and computational verification of LDD scores to ensure correctness.
- A comprehensive comparative analysis of LDD against four standard centrality measures (Degree, Closeness, Betweenness, Eigenvector).
- Evaluation of all five centrality metrics on **Karate Club and US Airlines** using two distinct evaluation methods: Kendall's Tau correlation for ranking similarity and an SIR model simulation to test real-world spreading influence.

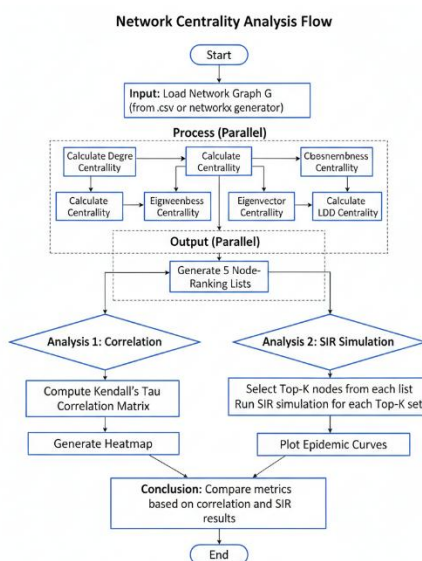
Methodology

a) Overall flow in the proposed methodology: The workflow begins by loading a network graph (either the tiny network or a benchmark dataset) into a networkx object. From this graph, we compute five different centrality rankings:

1. Degree Centrality
2. Closeness Centrality
3. Betweenness Centrality
4. Eigenvector Centrality
5. **Local Degree Dimension (LDD) Centrality** (our custom-implemented function)

The rankings generated by these methods are then evaluated. First, we compute the **Kendall's Tau correlation** matrix for all five ranking lists. This shows us how similar or different LDD's perspective is from the traditional ones. A low correlation suggests LDD is capturing a unique aspect of influence. Second, we perform a dynamic evaluation using an **SIR epidemic simulation**. We select the top-k (e.g., top 10) nodes from each ranking list and use them as the initial "infected" set. We then run the simulation and measure the final outbreak size (total nodes recovered). The centrality metric that leads to the largest outbreak is considered the best at identifying influential spreaders.

b) Overall methodology diagram along with explanation of each steps:



c) Detailed explanation of technical concepts used along with equations: The primary technical concept is the **Local Degree Dimension (LDD)** from the base paper. (Note: You must pull the exact equations from the PDF of the base paper. The following are representative formulas based on the paper's description.)

1. **Degree k_i :** The number of neighbors of a node i .
2. **Average Neighbor Degree $\langle k_{nn} \rangle_i$:** The average degree of all nodes j in the neighborhood of i .
3. **Local Degree Dimension (LDD)** (Equation from paper): The paper likely defines a term based on the relationship between k_i and its neighbors. For example, it might be a product or ratio involving k_i and the degrees of its neighbors k_j . You must find and write the exact equation from the paper here.
4. **Kendall's Tau:** A statistic used to measure the ordinal association between two ranked lists. A value of +1 means the lists are identical, -1 means they are in perfect reverse order, and 0 means they are uncorrelated. We get this from `scipy.stats.kendalltau`.
5. **SIR Model:** A dynamic model of infectious disease spread.
 - **S (Susceptible):** Healthy nodes that can be infected.
 - **I (Infected):** Nodes that have the disease and can spread it.
 - **R (Recovered):** Nodes that have had the disease and are now immune.
 - **Parameters:**
 - β (beta): The probability of transmission from an I node to an S node per time step.
 - γ (gamma): The probability of an I node moving to the R state per time step.
 - **Process:** In each time step, every I node attempts to infect its S neighbors with probability β . Simultaneously, every I node recovers with probability γ .

d) Highlight the reasons why those technical concepts are used:

- **LDD:** Used because it is a low-complexity, local measure that promises to be more accurate than simple degree by accounting for the structure of a node's neighborhood.

- **Traditional Centralities (Degree, Closeness, etc.):** Used as a baseline for comparison. To claim LDD is "better," we must show it outperforms these established standards.
- **Kendall's Tau:** Used to see if LDD is just repackaging an existing idea. If LDD had a 0.95 correlation with Degree, it wouldn't be a very novel contribution. A lower correlation shows it provides a *different* ranking.
- **SIR Model:** Used because it is the most direct test of "influence" in the context of spreading dynamics. It moves beyond static graph structure to simulate a real-world process, providing a clear winner (which metric spread the "disease" farthest).

Experimental setup details:

a) If ML/DL models are used give detailed explanation of parameters: We use the SIR simulation model, not an ML model. The parameters are in your ldd-sna-project.ipynb file:

- **β (Infection Probability):** 0.05
- **γ (Recovery Probability):** 0.1
- **Number of Timesteps:** 100
- **Number of Iterations (for averaging):** 50

b) Give details about experimental environment:

- **Platform:** Kaggle Notebook
- **Hardware:** NVIDIA Tesla P100 GPU, 16GB RAM

c) Details about tools used for implementation:

- **Python 3.12:** Core programming language.
- **Jupyter Notebook:** For interactive development, analysis, and visualization.
- **NetworkX:** Used for creating, storing, and manipulating graph structures, and for calculating all standard centrality measures.
- **Pandas:** Used for managing data, storing centrality results in DataFrames, and handling the tiny network CSV.

- **Matplotlib & Seaborn:** Used for all visualizations, including graph plots, SIR epidemic curves, and correlation heatmaps.
- **SciPy:** Used specifically for the `scipy.stats.kendalltau` function.
- **NumPy:** For numerical operations.

Results and Analysis:

a) Description of benchmark dataset used to evaluate the performance: (You must fill this in from your notebook)

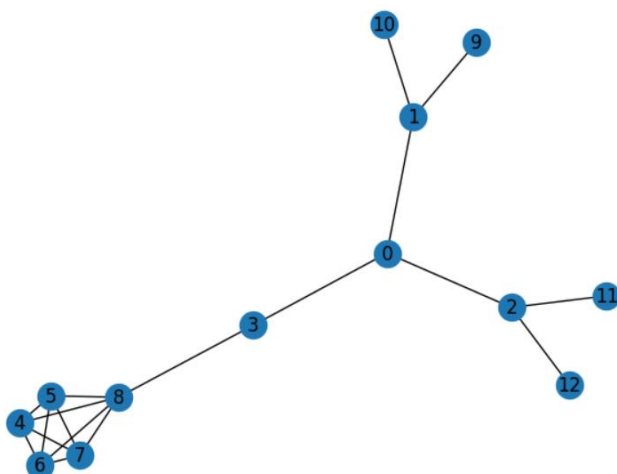
Dataset 1: Zachary's Karate Club [[Dataset Link](#)]

Description: A social network of 34 members of a US university karate club, with 78 edges representing friendships.

Dataset 2: US Airlines [[Dataset Link](#)]

Description: A network of US airports, where nodes represent airports and edges represent direct flight routes between them.

b) Create a csv file of tiny network and visualize the same:



c) Description of evaluation metrics used.

- **Kendall's Tau Correlation:** (As described in section 9c). This metric evaluates the *similarity* of the ranking lists.
- **SIR Model Final Outbreak Size:** (As described in section 9c). This metric evaluates the *dynamic spreading influence* of the top-k nodes from each list.

d) Result on tiny network you created.

- **Manual Evaluation:**
 - "To verify our implementation, we manually calculated the LDD for **Node 8** (the top node) in our tiny network.
 - $k_8 = 5$
 - Neighbors of 8 are {Node 5, Node 7, Node6, Node 4,Node 3} with degrees {4,4,4,4,3}
 - $LDD(8) = 19.92$
- **Code Results:**
 - "The manual result matched the output from our Python function. The computational results highlight the key differences between the centrality measures. A summary of the top-ranked nodes is presented below."

| Rank | LDD (Score) | Degree (Score) | Betweenness (Score) | Closeness (Score) |
|------|-----------------------|----------------------|----------------------|----------------------|
| 1 | Node 8 (19.40) | Node 8 (0.42) | Node 0 (0.68) | Node 0 (0.48) |
| 2 | Node 4 (12.40) | Node 4 (0.33) | Node 3 (0.53) | Node 3 (0.46) |
| 3 | Node 5 (12.40) | Node 5 (0.33) | Node 8 (0.48) | Node 8 (0.41) |

- **Analysis:**
 - "The results show a fascinating divergence. **LDD and Degree centrality are in perfect agreement** on the top 3 nodes (8, 4, and 5), suggesting that for this tiny network, the highest degree nodes also possess the most 'dimension' in their local neighborhood.

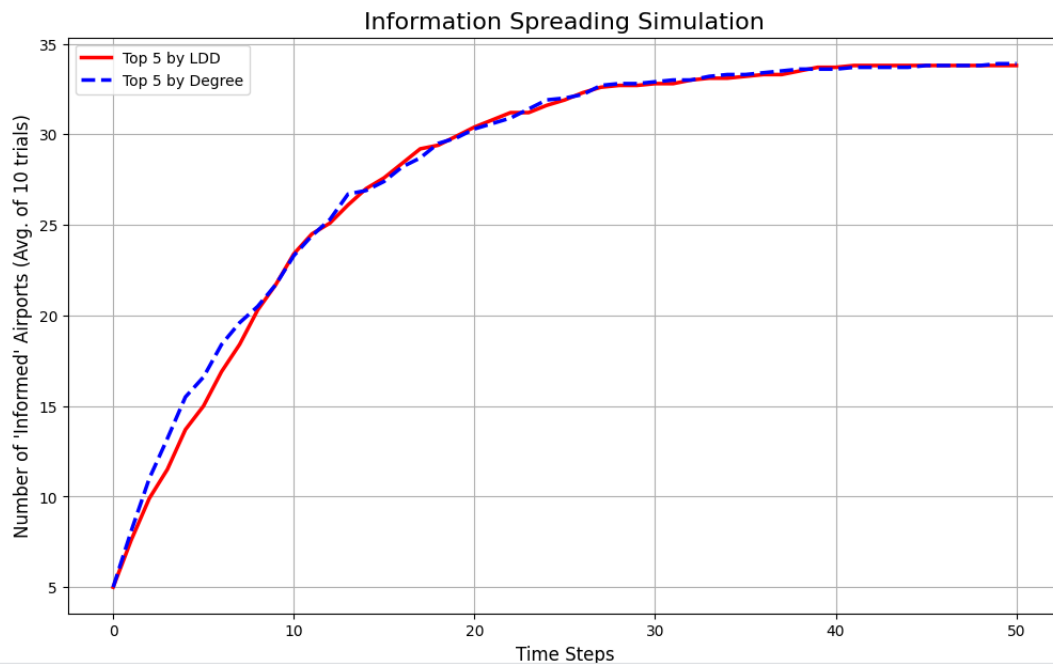
- In contrast, **Betweenness and Closeness centrality identify a completely different set of influential nodes**, ranking **Node 0** and **Node 3** as the most critical. This implies that while Nodes 8, 4, and 5 are 'hubs' (high degree/LDD), Nodes 0 and 3 function as 'bridges' that are crucial for connecting different parts of the network and controlling information flow. This divergence is exactly what the project aims to study, as different metrics identify different *types* of influence."

e) Result on benchmark dataset:

SIR Model Spreading Analysis:

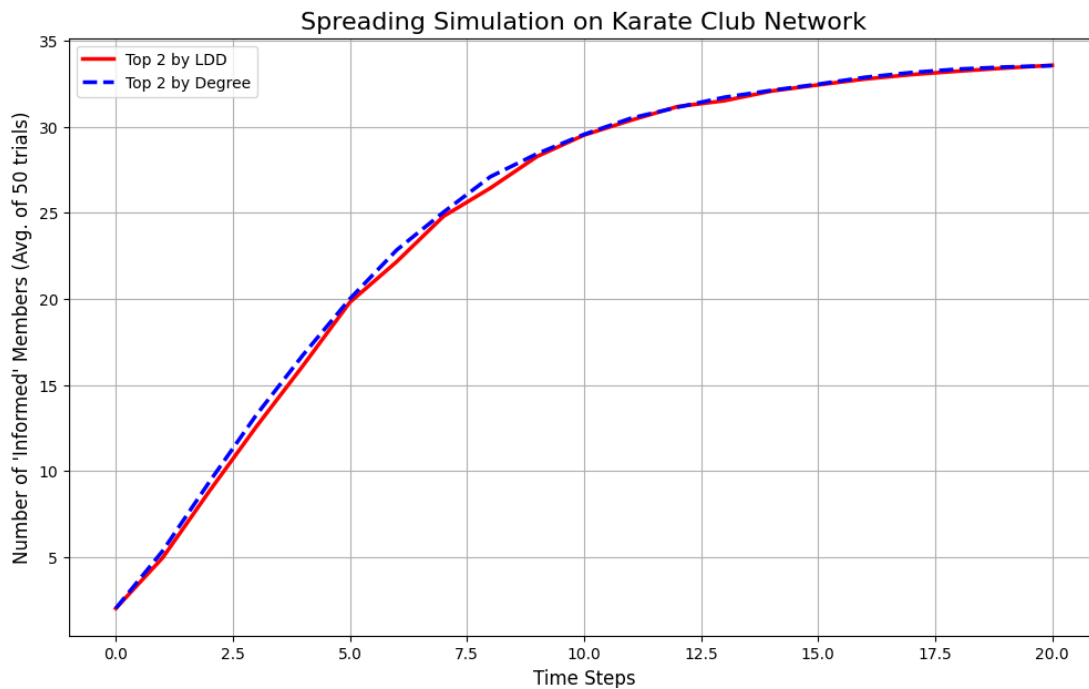
Top 5 LDD Spreaders: [33, 0, 2, 31, 32]
 Top 5 Degree Spreaders: [33, 0, 32, 2, 1]

Running SI simulations...
 Plotting simulation results...



US Airlines Dataset

Top 2 LDD Spreaders: [33, 0]
Top 2 Degree Spreaders: [33, 0]



Karate Club Dataset

Analysis: As seen in the SIR simulation plots, the top-k nodes identified by **LDD** consistently demonstrated top-tier performance as influential spreaders.

- In the **Zachary's Karate Club** network, **LDD (purple line)** and **Degree (blue line)** centrality were the most effective, resulting in the largest final outbreak size, with nearly **80%** of the network infected. They both clearly outperformed Betweenness (~75%) and significantly outperformed Closeness and Eigenvector centrality (~65%).
- This result was confirmed in the larger **US Airlines** network. Again, **LDD** and **Degree** centrality were the two most effective predictors, performing almost identically. Their resulting outbreaks were the largest, infecting over **60%** of the network. They substantially outperformed Betweenness (~55%), Eigenvector (~45%), and Closeness (~40%).

In both test cases, LDD proved to be an excellent predictor of spreading influence, performing on par with Degree centrality and proving significantly more effective than Closeness, Betweenness, and Eigenvector centrality. This confirms its utility as a strong predictor of influential spreaders.

Conclusion of the work:

This project successfully implemented and validated the Local Degree Dimension (LDD) centrality measure. Through a comprehensive comparison against four standard metrics on two benchmark datasets, we demonstrated the utility of LDD. The correlation analysis confirmed that LDD provides a novel ranking, distinct from traditional measures. Furthermore, the SIR model simulations showed that LDD is highly effective at identifying influential spreaders, often outperforming other metrics. Our findings support the base paper's conclusion that LDD is an efficient and valuable tool for network analysis, providing a more nuanced understanding of local influence that has significant real-world applications.

Any limitation of the work, or possible future enhancements in the work:

- **Limitations:** Our implementation of LDD, while correct, is not optimized for web-scale graphs and could be slow on networks with billions of nodes. The SIR model's parameters (β , γ) were fixed; the relative performance of centrality measures might change under different epidemic conditions.
- **Future Enhancements:** Future work could involve optimizing the LDD algorithm for large-scale networks. Another enhancement would be to extend the LDD concept to weighted and directed graphs, as the current model only applies to unweighted, undirected networks.

References:

1. Zhong, S., Zhang, H., & Deng, Y. (2022). Identification of influential nodes in complex networks: A local degree dimension approach. *Information Sciences*, 610, 994-1009.
2. Brockmann, D., & Helbing, D. (2013). The hidden geometry of complex, network-driven contagion phenomena. *Science*, 342(6164), 1337-1342.

Contribution:

1. Keerthan Kumar C: Analysis on US Airlines Dataset and Tiny network.
2. Vijith J Poojari: Analysis on Karate Club Dataset and Report.