
Algorithm 1 her-CPRAND

Initialization : Choose $\beta_0 \in (0, 1)$, $\eta \geq \gamma \geq \bar{\gamma} > 1$, and 2 sets of initial factor matrices $(A_0^{(1)}, \dots, A_0^{(N)})$ and $(\hat{A}_0^{(1)}, \dots, \hat{A}_0^{(N)})$. Set $\bar{\beta}_0 = 1$ and $k = 1$.

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1: repeat
2:   for  $n = 1, \dots, N$  do
3:     Define sampling operator  $\mathcal{S} \in \mathbf{R}^{S \times \prod_{m \neq n} I_m}$  with  $S = \text{card}(\mathcal{S})$ 
4:      $Z_s \leftarrow SKR(\mathcal{S}, \hat{A}_{k-1}^{(1)}, \dots, \hat{A}_{k-1}^{(n-1)}, \hat{A}_{k-1}^{(n+1)}, \dots, \hat{A}_{k-1}^{(N)})$ 
5:      $X_s^T \leftarrow \mathcal{S} X_n^T$ 
6:     Update :  $A_k^{(n)} \leftarrow \text{argmin}_A \|Z_s A^T - X_s^T\|_F$ 
7:     Normalize columns of  $A_k^{(n)}$  and update  $\lambda$ 
8:     Extrapolate :  $\hat{A}_k^{(n)} = A_k^{(n)} + \beta_{k-1}(A_k^{(n)} - A_{k-1}^{(n)})$ 
9:   end for
10:  Compute  $\hat{F}_k = F(A_k^{(N)}; \hat{A}_k^{(l \neq N)})$ .
11:  if  $\hat{F}_k > \hat{F}_{k-1}$  for  $k \geq 2$  then
12:    Set  $\hat{A}_k^{(i)} = A_k^{(i)}$  for  $i = 1, \dots, N$ 
13:    Set  $\bar{\beta}_k = \beta_{k-1}$ ,  $\beta_k = \beta_{k-1}/\eta$ 
14:  else
15:    Set  $A_k^{(i)} = \hat{A}_k^{(i)}$  for  $i = 1, \dots, N$ 
16:    Set  $\bar{\beta}_k = \min\{1, \bar{\beta}_{k-1}\bar{\gamma}\}$ ,  $\beta_k = \min\{\bar{\beta}_{k-1}, \gamma\beta_{k-1}\}$ 
17:  end if
18:  Set  $k=k+1$ 
19: until some criteria is satisfied
20: return  $\lambda$ , factor matrices  $\{A_k^{(n)}\}$ 
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