## Practical Work 2

## Member in United States Electoral College: Study of the Representation of Population

- 1. Install PulP and read the documentation from the link: https://pythonhosted.org/PulP/
- 2. Solve the following LP problems in R and N with PuLP:

$$\min \left\{ -8x_1 - 5x_2 \mid x_1 + x_2 \le 6, \ 9x_1 + 5x_2 \le 45, \ x_i \ge 0 \right\}$$

$$\min \left\{ 2x_1 + 7x_2 + 2x_3 \mid x_1 + 4x_2 + x_3 \ge 10, \ 4x_1 + 2x_2 + 2x_3 \ge 13, \ x_1 + x_2 - x_3 \ge 0, \ x_i \ge 0 \right\}$$

- Watch the video from the link: https://youtu.be/7yZ5xxdkTb8
- 4. Read, understand and execute the two examples "Deciding Where to Go on Vacation" and "Creating a Reading List" from the link: https://github.com/AnnaNican/optimizers/tree/master/.ipynb\_checkpoints
- 5. Let be  $x = (x_1, ..., x_p)$ . Each coordinate of x represents the population of the state i and N the number of members at the US Electoral College. Justify that minimizing the representativity gap is to solve the following integer LP problem:

$$min \ \{u-v \mid v \le \frac{\alpha_i}{x_i} \le u, \ \sum_{1 \le i \le p} \alpha_i = N\}$$

where  $\alpha_i$  represents the number of members in US Electoral College for the state i.

- 6. Give the number of members for each state in 2016 with the criteria of representativity of the question 5.
- 7. Analyse the results of the 2016 United States presidential election.

One report for a staff of two students but each student will send the report.

The report will be presented on one page recto-verso in two-column layout + US map. You will only present the answers from question 5 to question 7.