

CS2223 D Term 2020 Quiz 6

(1 point) Question 1: “My brain is open...”

I pledge that I am taking this quiz on my own, with help from no one else and no notes:

(3 points) Question 2: A National League baseball team consists of 25 players.

A batting order from such a team consists of an ordered subset of 9 of the players.

How many batting orders are possible?

a.) $2^9 = 512$

b.) $9! = 362,880$

c.) $C(25, 9) = \frac{25!}{9!16!} = 2,042,975$

d.) $2^{25} = 33,554,432$

e.) $P(25, 9) = \frac{25!}{16!} = 741,354,768,000$

(3 points) Question 3: Generating Subsets

Each choice below represents all the subsets of $\{a, b, c\}$.

Which of them is in **squashed order**?

a.) $\emptyset, \{1\}, \{2\}, \{3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}$

b.) $\emptyset, \{1\}, \{2\}, \{3\}, \{2, 1\}, \{3, 1\}, \{3, 2\}, \{3, 2, 1\}$

c.) $\emptyset, \{1\}, \{2\}, \{1, 2\}, \{3\}, \{1, 3\}, \{2, 3\}, \{1, 2, 3\}$

d.) $\{1, 2, 3\}, \{1, 2\}, \{1, 3\}, \{2, 3\}, \{1\}, \{2\}, \{3\}, \emptyset$

e.) $\{3, 2, 1\}, \{2, 1\}, \{3, 1\}, \{3, 2\}, \{3\}, \{2\}, \{1\}, \emptyset$

(3 points) Question 4: Minimal-Change Requirement

Suppose we wish to generate all $5^5 = 3,125$ arrangements of the digits 0 through 4, i.e. 00000 up to 44444, and we insist on applying the minimal-change requirement (perhaps as a 5-ary Gray code rather than a binary/Boolean one).

Which of the following might appear in our list after the arrangement 01234?

a.) 01240

b.) 10000

c.) 10234

d.) 11234

e.) 12340

(1 point) Bonus Question: Binary Reflective Gray Codes

The follow is an interesting fact about our Binary Reflective Gray Code (BRGC):

- a.) Zero and One are the only integers with the same representations in Base Two and in our Binary Reflective Gray Code.
- b.) Unlike in Base Two, an integer is even if and only if its BRGC representation has an even number of 1s.
- c.) Powers of 2 larger than $2^0 = 1$ can be expressed with exactly one 1 in Base Two but require exactly two 1s in our BRGC.
- d.) As in Base Two, the length of the BRGC representation of a positive integer k can be computed as $\lceil \lg k \rceil + 1$, that is $\lceil \log_2 k \rceil + 1$
- e.) All of the Above