## CS2223 D Term 2020 Quiz 22

(1 point) Question 1: "My brain is open...."

I pledge that I am taking this quiz on my own, with help from no one else and no notes:

(3 points) Question 2: The matrix below is not a legitimate **Ranking Matrix** for finding a Stable Marriage of 5 hockey players and 5 positions. Why not?

|         | LeftWing | Center   | RightWing | LeftDefense | RightDefense |
|---------|----------|----------|-----------|-------------|--------------|
| Adrian  | 1,1      | 2,2      | 3,3       | 4,4         | 5,5          |
| Bobby   | 2,2      | 1,1      | $3,\!4$   | 5,2         | 4,2          |
| Chip    | 3,3      | $^{2,3}$ | $3,\!5$   | 1,3         | 3,3          |
| Denver  | 4,4      | $^{2,5}$ | 3,1       | 1,1         | 5,4          |
| Everett | 5,5      | $^{4,4}$ | $^{3,2}$  | 1,5         | $2,\!1$      |

- a.) (1,1) cannot appear more than twice in a valid ranking matrix, but it's here thrice.
- b.) The first entries under the 'Right Wing' column are all 3's. That's impossible.
- c.) Chip doesn't have a least-favorite/worst position.
- d.) Hockey requires 6 players the Goalie is left out!
- e.) It is, indeed, a valid Ranking Matrix.

(3 points) Question 3: The ranking matrix below represents the expected top three players and cities for the upcoming National Ultimate Frisbee League draft. Which pair constitutes a blocking pair of the suggested marriage in the ranking matrix below?

| a.) | (Hailey, Atlanta) |        | Atlanta  | Boston   | Chicago |
|-----|-------------------|--------|----------|----------|---------|
| b.) | (Hailey, Boston)  | Hailey | 1,3      | $^{2,2}$ | 3,1     |
| c.) | (Hailey, Chicago) | Izzy   | $^{2,2}$ | 3,1      | 1,2     |
| d.) | (Izzy, Chicago)   | Joey   | $^{2,1}$ | 1,3      | 3,3     |
| e.) | (Joev. Chicago)   |        |          |          |         |

(3 points) Question 4: Which of the following constitutes a stable marriage based on the ranking matrix above?

- a.) (Hailey, Atlanta), (Izzy, Boston), (Joey, Chicago)
- b.) (Hailey, Atlanta), (Izzy, Chicago), (Joey, Boston)
- c.) (Hailey, Boston), (Izzy, Boston), (Joey, Boston)
- d.) (Izzy, Atlanta), (Izzy, Boston), (Izzy, Chicago)
- e.) No stable marriage exists for this ranking matrix.

(1 point) Bonus Question: Another stable marriage for the ranking matrix above is: (Hailey, Boston), (Izzy, Chicago), (Joey, Atlanta). It is:

- a.) City-Optimal
- b.) Player-Optimal
- c.) Neither Player-Optimal nor City-Optimal
- d.) Both Player-Optimal and City-Optimal
- e.) A stable marriage with a blocking pair.