## kaldi-matrix.h

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```
// matrix/kaldi-matrix.h
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 4
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   //
 5
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20
21
22
   #ifndef KALDI MATRIX KALDI MATRIX H
23
   #define KALDI MATRIX KALDI MATRIX H 1
24
25
   #include "matrix/matrix-common.h"
26
27
   namespace kaldi {
28
30
33
    template<typename Real>
34
    Real TraceMatMat(const MatrixBase<Real> &A, const MatrixBase<Real> &B,
35
                     MatrixTransposeType trans = kNoTrans);
37
40
44
   template<typename Real>
    class MatrixBase {
45
    public:
46
47
      // so this child can access protected members of other instances.
      friend class Matrix<Real>;
48
      // friend declarations for CUDA matrices (see ../cudamatrix/)
49
      friend class CuMatrixBase<Real>;
50
51
      friend class CuMatrix<Real>;
52
      friend class CuSubMatrix<Real>;
53
      friend class CuPackedMatrix<Real>;
54
55
      friend class PackedMatrix<Real>;
56
      inline MatrixIndexT NumRows() const { return num_rows_; }
58
59
      inline MatrixIndexT NumCols() const { return num_cols_; }
61
62
64
      inline MatrixIndexT Stride() const { return stride_; }
65
67
      size_t SizeInBytes() const {
        return static_cast<size_t>(num_rows_) * static_cast<size_t>(stride_) *
68
69
            sizeof(Real);
70
      }
71
      inline const Real* Data() const {
73
74
        return data ;
75
76
      inline Real* Data() { return data_; }
78
79
      inline Real* RowData(MatrixIndexT i) {
81
        KALDI_ASSERT(static_cast<UnsignedMatrixIndexT>(i) <</pre>
82
                     static_cast<UnsignedMatrixIndexT>(núm_rows_));
83
        return data_ + i * stride_;
84
```

```
85
       }
 86
 88
       inline const Real* RowData(MatrixIndexT i) const
 89
         KALDI_ASSERT(static_cast<UnsignedMatrixIndexT>(i) <</pre>
 90
                       static_cast<UnsignedMatrixIndexT>(num_rows_));
         return data_ + i * stride_;
 91
 92
 93
       inline Real& operator() (MatrixIndexT r, MatrixIndexT c) {
 96
 97
         KALDI_PARANOID_ASSERT(static_cast<UnsignedMatrixIndexT>(r) 
 98
                                static_cast<UnsignedMatrixIndexT>(num_rows_) &&
 99
                                static_cast<UnsignedMatrixIndexT>(c) <</pre>
100
                                static_cast<UnsignedMatrixIndexT>(num_cols_));
101
         return *(data_ + r * stride_ + c);
102
105
       Real &Index (MatrixIndexT r, MatrixIndexT c) { return (*this)(r, c); }
106
109
       inline const Real operator() (MatrixIndexT r, MatrixIndexT c) const {
         KALDI_PARANOID_ASSERT(static_cast<UnsignedMatrixIndexT>(r) <</pre>
110
111
                                static_cast<UnsignedMatrixIndexT>(num_rows_) &&
112
                                static_cast<UnsignedMatrixIndexT>(c) <</pre>
113
                                static_cast<UnsignedMatrixIndexT>(num_cols_));
114
         return *(data_ + r * stride_ + c);
115
116
            Basic setting-to-special values functions. */
117
118
120
       void SetZero();
       void Set(Real);
122
124
       void SetUnit();
126
       void SetRandn();
128
       void SetRandUniform();
129
130
          Copying functions. These do not resize the matrix! */
131
132
       template<typename OtherReal>
134
135
       void CopyFromMat(const MatrixBase<OtherReal> & M,
136
                         MatrixTransposeType trans = kNoTrans);
137
139
       void CopyFromMat(const CompressedMatrix &M);
140
142
       template<typename OtherReal>
143
       void CopyFromSp(const SpMatrix<OtherReal> &M);
144
       template<typename OtherReal>
146
147
       void CopyFromTp(const TpMatrix<OtherReal> &M,
148
                        MatrixTransposeType trans = kNoTrans);
149
       template<typename OtherReal>
151
       void CopyFromMat(const CuMatrixBase<OtherReal> &M,
152
153
                         MatrixTransposeType trans = kNoTrans);
154
158
       void CopyRowsFromVec(const VectorBase<Real> &v);
159
161
       void CopyRowsFromVec(const CuVectorBase<Real> &v);
162
163
       template<typename OtherReal>
164
       void CopyRowsFromVec(const VectorBase<OtherReal> &v);
165
       void CopyColsFromVec(const VectorBase<Real> &v);
169
170
       void CopyColFromVec(const VectorBase<Real> &v, const MatrixIndexT col);
172
174
       void CopyRowFromVec(const VectorBase<Real> &v, const MatrixIndexT row);
176
       void CopyDiagFromVec(const VectorBase<Real> &v);
177
178
       /* Accessing of sub-parts of the matrix. */
179
181
       inline const SubVector<Real> Row(MatrixIndexT i) const {
182
         KALDI_ASSERT(static_cast<UnsignedMatrixIndexT>(i) <</pre>
183
                       static_cast<UnsignedMatrixIndexT>(num_rows_
184
         return SubVector<Real>(data_ + (i * stride_), NumCols());
185
       }
186
       inline SubVector<Real> Row(MatrixIndexT i) {
188
```

```
189
         KALDI_ASSERT(static_cast<UnsignedMatrixIndexT>(i) <</pre>
190
                       static_cast<UnsignedMatrixIndexT>(num_rows_));
191
         return SubVector<Real>(data_ + (i * stride_), NumCols());
192
193
195
       inline SubMatrix<Real> Range(const MatrixIndexT row_offset,
196
                                     const MatrixIndexT num rows,
197
                                     const MatrixIndexT col_offset,
198
                                     const MatrixIndexT num_cols) const {
         return SubMatrix<Real>(*this, row_offset, num_rows,
199
200
                                 col offset, num cols);
201
202
       inline SubMatrix<Real> RowRange(const MatrixIndexT row_offset,
203
                                        const MatrixIndexT num_rows) const {
         return SubMatrix<Real>(*this, row_offset, num_rows, 0, num_cols_);
204
205
       inline SubMatrix<Real> ColRange(const MatrixIndexT col_offset,
206
207
                                        const MatrixIndexT num_cols) const {
         return SubMatrix<Real>(*this, 0, num_rows_, col_offset, num_cols);
208
209
       }
210
       /* Various special functions. */
211
213
       Real Sum() const;
215
       Real Trace(bool check_square = true) const;
216
       // If check_square = true, will crash if matrix is not square.
217
219
       Real Max() const;
221
       Real Min() const;
222
224
       void MulElements(const MatrixBase<Real> &A);
225
227
       void DivElements(const MatrixBase<Real> &A);
228
       void Scale(Real alpha);
230
231
233
       void Max(const MatrixBase<Real> &A);
234
237
       void MulColsVec(const VectorBase<Real> &scale);
238
241
       void MulRowsVec(const VectorBase<Real> &scale);
242
246
       void MulRowsGroupMat(const MatrixBase<Real> &src);
247
       Real LogDet(Real *det_sign = NULL) const;
249
250
       void Invert(Real *log_det = NULL, Real *det_sign = NULL,
254
                   bool inverse_needed = true);
255
260
       void InvertDouble(Real *LogDet = NULL, Real *det_sign = NULL,
261
                            bool inverse_needed = true);
262
264
       void InvertElements();
265
269
       void Transpose();
270
276
       void CopyCols(const MatrixBase<Real> &src,
                      const std::vector<MatrixIndexT> &indices);
277
278
284
       void CopyRows(const MatrixBase<Real> &src
285
                      const std::vector<MatrixIndexT> &indices);
286
288
       void ApplyFloor(Real floor_val);
289
291
       void ApplyCeiling(Real ceiling_val);
292
294
       void ApplyLog();
295
297
       void ApplyExp();
298
300
       void ApplyPow(Real power);
301
306
       void ApplyPowAbs(Real power, bool include_sign=false);
307
312
       void ApplyHeaviside();
313
       void Eig(MatrixBase<Real> *P,
328
```

```
329
                VectorBase<Real> *eigs_real,
330
                VectorBase<Real> *eigs_imag) const;
331
       bool Power(Real pow);
339
340
       void DestructiveSvd(VectorBase<Real> *s, MatrixBase<Real> *U,
352
353
                            MatrixBase<Real> *Vt); // Destroys calling matrix.
354
359
       void Svd(VectorBase<Real> *s, MatrixBase<Real> *U,
       MatrixBase<Real> *Vt) const;
void Svd(VectorBase<Real> *s) const { Svd(s, NULL, NULL); }
360
362
363
364
366
       Real MinSingularValue() const {
         Vector<Real> tmp(std::min(NumRows(), NumCols()));
367
368
         Svd(&tmp);
369
         return tmp.Min();
370
371
       void TestUninitialized() const; // This function is designed so that if any
372
373
       // if the matrix is uninitialized memory, valgrind will complain.
374
377
       Real Cond() const;
378
380
       bool IsSymmetric(Real cutoff = 1.0e-05) const; // replace magic number
381
383
       bool IsDiagonal(Real cutoff = 1.0e-05) const; // replace magic number
384
389
       bool IsUnit(Real cutoff = 1.0e-05) const;
                                                     // replace magic number
390
392
                                                     // replace magic number
       bool IsZero(Real cutoff = 1.0e-05) const;
393
396
       Real FrobeniusNorm() const;
397
       bool ApproxEqual(const MatrixBase<Real> &other, float tol = 0.01) const;
400
401
       bool Equal(const MatrixBase<Real> &other) const;
403
404
406
       Real LargestAbsElem() const; // largest absolute value.
407
       Real LogSumExp(Real prune = -1.0) const;
413
414
417
       Real ApplySoftMax();
418
420
       void Sigmoid(const MatrixBase<Real> &src);
421
423
       void SoftHinge(const MatrixBase<Real> &src);
424
427
       void GroupPnorm(const MatrixBase<Real> &src, Real power);
428
429
436
       void GroupPnormDeriv(const MatrixBase<Real> &input, const MatrixBase<Real>
     &output,
437
                             Real power);
438
439
441
       void Tanh(const MatrixBase<Real> &src);
442
443
       // Function used in backpropagating derivatives of the sigmoid function:
444
       // element-by-element, set *this = diff * value * (1.0 - value).
445
       void DiffSigmoid(const MatrixBase<Real> &value,
446
                         const MatrixBase<Real> &diff);
447
448
       // Function used in backpropagating derivatives of the tanh function:
       // element-by-element, set *this = diff * (1.0 - value^2).
449
450
       void DiffTanh(const MatrixBase<Real> &value,
451
                     const MatrixBase<Real> &diff);
452
460
       void SymPosSemiDefEig(VectorBase<Real> *s, MatrixBase<Real> *P,
461
                              Real check_thresh = 0.001);
462
463
       friend Real kaldi::TraceMatMat<Real>(const MatrixBase<Real> &A,
464
           const MatrixBase<Real> &B, MatrixTransposeType trans); // tr (A B)
465
```

```
466
       // so it can get around const restrictions on the pointer to data_.
467
       friend class SubMatrix<Real>;
468
470
       void Add(const Real alpha);
471
473
       void AddToDiag(const Real alpha);
474
476
       template<typename OtherReal>
       void AddVecVec(const Real alpha, const VectorBase<OtherReal> &a,
477
478
                       const VectorBase<OtherReal> &b);
479
481
       template<typename OtherReal>
482
       void AddVecToRows(const Real alpha, const VectorBase<0therReal> &v);
483
485
       template<typename OtherReal>
       void AddVecToCols(const Real alpha, const VectorBase<OtherReal> &v);
486
487
489
       void AddMat(const Real alpha, const MatrixBase<Real> &M,
490
                    MatrixTransposeType transA = kNoTrans);
491
495
       void SymAddMat2(const Real alpha, const MatrixBase<Real> &M,
496
                        MatrixTransposeType transA, Real beta);
497
500
       void AddDiagVecMat(const Real alpha, VectorBase<Real> &v,
501
                           const MatrixBase<Real> &M, MatrixTransposeType transM,
502
                           Real beta = 1.0);
503
506
       void AddMatDiagVec(const Real alpha,
507
                           const MatrixBase<Real> &M, MatrixTransposeType transM,
508
                           VectorBase<Real> &v,
509
                           Real beta = 1.0);
510
       void AddMatMatElements(const Real alpha,
512
513
                               const MatrixBase<Real>& A,
514
                               const MatrixBase<Real>& B,
515
                               const Real beta);
516
518
       template<typename OtherReal>
519
       void AddSp(const Real alpha, const SpMatrix<OtherReal> &S);
520
521
       void AddMatMat(const Real alpha,
                       const MatrixBase<Real>& A, MatrixTransposeType transA,
522
523
                       const MatrixBase<Real>& B, MatrixTransposeType transB,
524
                       const Real beta);
525
527
       void AddMatMatDivMat(const MatrixBase<Real>& A,
528
                              const MatrixBase<Real>& B,
529
                             const MatrixBase<Real>& C);
530
533
       void AddMatSmat(const Real alpha,
                        const MatrixBase<Real>& A, MatrixTransposeType transA,
const MatrixBase<Real>& B, MatrixTransposeType transB,
534
535
536
                        const Real beta);
537
540
       void AddSmatMat(const Real alpha,
541
                        const MatrixBase<Real>& A, MatrixTransposeType transA,
542
                        const MatrixBase<Real>& B, MatrixTransposeType transB,
543
                        const Real beta);
544
546
       void AddMatMatMat(const Real alpha,
547
                          const MatrixBase<Real>& A, MatrixTransposeType transA,
548
                          const MatrixBase<Real>& B, MatrixTransposeType transB,
549
                          const MatrixBase<Real>& C, MatrixTransposeType transC,
550
                          const Real beta);
551
       // This and the routines below are really
553
554
       // stubs that need to be made more efficient.
       void AddSpMat(const Real alpha,
555
556
                      const SpMatrix<Real>& A,
557
                      const MatrixBase<Real>& B, MatrixTransposeType transB,
558
                      const Real beta) {
559
         Matrix<Real> M(A)
560
         return AddMatMat(alpha, M, kNoTrans, B, transB, beta);
561
563
       void AddTpMat(const Real alpha,
```

```
564
                     const TpMatrix<Real>& A, MatrixTransposeType transA,
565
                     const MatrixBase<Real>& B, MatrixTransposeType transB,
566
                     const Real beta) {
567
         Matrix<Real> M(A);
         return AddMatMat(alpha, M, transA, B, transB, beta);
568
569
       void AddMatSp(const Real alpha,
571
572
                     const MatrixBase<Real>& A, MatrixTransposeType transA,
573
                     const SpMatrix<Real>& B,
574
                     const Real beta) {
575
         Matrix<Real> M(B);
576
         return AddMatMat(alpha, A, transA, M, kNoTrans, beta);
577
579
       void AddSpMatSp(const Real alpha,
580
                       const SpMatrix<Real> &A,
581
                       const MatrixBase<Real>& B, MatrixTransposeType transB,
582
                       const SpMatrix<Real>& C,
583
                     const Real beta) {
584
         Matrix<Real> M(A), N(C);
585
         return AddMatMatMat(alpha, M, kNoTrans, B, transB, N, kNoTrans, beta);
586
588
       void AddMatTp(const Real alpha,
589
                     const MatrixBase<Real>& A, MatrixTransposeType transA,
590
                     const TpMatrix<Real>& B, MatrixTransposeType transB,
591
                     const Real beta) {
592
         Matrix<Real> M(B);
593
         return AddMatMat(alpha, A, transA, M, transB, beta);
594
595
597
       void AddTpTp(const Real alpha,
598
                    const TpMatrix<Real>& A, MatrixTransposeType transA,
599
                    const TpMatrix<Real>& B, MatrixTransposeType transB,
600
                    const Real beta) {
         Matrix<Real> M(A), N(B);
601
602
         return AddMatMat(alpha, M, transA, N, transB, beta);
603
604
606
       // This one is more efficient, not like the others above.
       void AddSpSp(const Real alpha,
607
608
                    const SpMatrix<Real>& A, const SpMatrix<Real>& B,
609
                    const Real beta);
610
       void CopyLowerToUpper();
612
613
615
       void CopyUpperToLower();
616
621
       void OrthogonalizeRows();
622
625
       // Will throw exception on failure.
       void Read(std::istream & in, bool binary, bool add = false);
626
628
       void Write(std::ostream & out, bool binary) const;
629
       // Below is internal methods for Svd, user does not have to know about this.
630
     #if !defined(HAVE_ATLAS) && !defined(USE_KALDI_SVD)
631
632
       // protected:
633
       // Should be protected but used directly in testing routine.
       // destroys *this!
634
       635
636
637
     #else
     protected:
638
639
       // destroys *this!
640
       bool JamaSvd(VectorBase<Real> *s, MatrixBase<Real> *U,
                    MatrixBase<Real> *V);
641
642
     #endif
643
644
     protected:
645
       explicit MatrixBase(Real *data, MatrixIndexT cols, MatrixIndexT rows,
647
     MatrixIndexT stride) :
         data_(data), num_cols_(cols), num_ro
KALDI_ASSERT_IS_FLOATING_TYPE(Real);
648
                                       num_rows_(rows), stride_(stride) {
649
650
651
       explicit MatrixBase(): data (NULL) {
654
```

```
655
         KALDI_ASSERT_IS_FLOATING_TYPE(Real);
656
657
658
       // Make sure pointers to MatrixBase cannot be deleted.
659
       ~MatrixBase() { }
660
       inline Real* Data workaround() const {
666
667
         return data ;
668
669
671
       Real*
               data ;
672
                        num_cols_;
675
       MatrixIndexT
676
       MatrixIndexT
                        num_rows_;
677
       MatrixIndexT
679
                        stride_;
680
      private:
681
       KALDI_DISALLOW_COPY_AND_ASSIGN(MatrixBase);
682
683
685
     template<typename Real>
686
     class Matrix : public MatrixBase<Real> {
687
      public:
688
       Matrix();
690
691
694
       Matrix(const MatrixIndexT r, const MatrixIndexT c,
695
              MatrixResizeType resize type = kSetZero):
696
           MatrixBase<Real>() { Resize(r, c, resize_type); }
697
700
       template<typename OtherReal>
701
       explicit Matrix(const CuMatrixBase<OtherReal> &cu,
702
                        MatrixTransposeType trans = kNoTrans);
703
704
706
       void Swap(Matrix<Real> *other);
707
       void Swap(CuMatrix<Real> *mat);
709
710
713
       explicit Matrix(const MatrixBase<Real> & M,
714
                        MatrixTransposeType trans = kNoTrans);
715
717
       Matrix(const Matrix<Real> & M); // (cannot make explicit)
718
720
       template<typename OtherReal>
721
       explicit Matrix(const MatrixBase<OtherReal> & M,
722
                          MatrixTransposeType trans = kNoTrans);
723
726
       template<typename OtherReal>
       explicit Matrix(const SpMatrix<OtherReal> & M) : MatrixBase<Real>() {
727
728
         Resize(M.NumRows(), M.NumRows(), kUndefined);
729
         this->CopyFromSp(M);
730
731
733
       explicit Matrix(const CompressedMatrix &C);
734
736
       template <typename OtherReal>
737
       explicit Matrix(const TpMatrix<OtherReal> & M,
738
                        MatrixTransposeType trans = kNoTrans) : MatrixBase<Real>() {
739
         if (trans == kNoTrans) {
740
           Resize(M.NumRows(), M.NumCols(), kUndefined);
741
           this->CopyFromTp(M);
742
         } else {
           Resize(M.NumCols(), M.NumRows(), kUndefined);
this->CopyFromTp(M, kTrans);
743
744
745
       }
746
747
749
       // Unlike one in base, allows resizing.
750
       void Read(std::istream & in, bool binary, bool add = false);
751
753
       void RemoveRow(MatrixIndexT i);
754
757
       void Transpose();
758
```

```
760
       ~Matrix() { Destroy(); }
761
       void Resize(const MatrixIndexT r,
769
770
                     const MatrixIndexT c,
771
                     MatrixResizeType resize_type = kSetZero);
772
774
       Matrix<Real> & operator = (const MatrixBase<Real> & other) {
775
         if (MatrixBase<Real>::NumRows() != other.NumRows() |
              MatrixBase<Real>::NumCols() != other.NumCols())
776
            Resize(other.NumRows(), other.NumCols(), kUndefined);
777
778
         MatrixBase<Real>::CopyFromMat(other);
779
          return *this;
780
781
       Matrix<Real> & operator = (const Matrix<Real> & other)
783
         if (MatrixBase<Real>::NumRows() != other.NumRows() ||
   MatrixBase<Real>::NumCols() != other.NumCols())
Resize(other.NumRows(), other.NumCols(), kUndefined);
784
785
786
787
         MatrixBase<Real>::CopyFromMat(other);
788
         return *this;
789
790
791
792
      private:
794
       void Destroy();
795
800
       void Init(const MatrixIndexT r,
801
                  const MatrixIndexT c);
802
803
     };
805
808
811
     struct HtkHeader {
813
       int32
                 mNSamples;
815
       int32
                 mSamplePeriod;
                 mSampleSize;
817
       int16
819
       uint16
                 mSampleKind;
820
821
822
     // Read HTK formatted features from file into matrix.
823
     template<typename Real>
     bool ReadHtk(std::istream &is, Matrix<Real> *M, HtkHeader *header ptr);
824
825
826
     // Write (HTK format) features to file from matrix.
827
     template<typename Real>
828
     bool WriteHtk(std::ostream &os, const MatrixBase<Real> &M, HtkHeader htk_hdr);
829
830
     // Write (CMUSphinx format) features to file from matrix.
831
     template<typename Real>
832
     bool WriteSphinx(std::ostream &os, const MatrixBase<Real> &M);
833
835
843
     template<typename Real>
844
     class SubMatrix : public MatrixBase<Real> {
845
      public:
846
       // Initialize a SubMatrix from part of a matrix; this is
847
       // a bit like A(b:c, d:e) in Matlab.
848
       // This initializer is against the proper semantics of "const"
       // SubMatrix can change its contents. It would be hard to implement
// a "const-safe" version of this class.
849
850
       SubMatrix(const MatrixBase<Real>& T,
851
852
                  const MatrixIndexT ro, // row offset, 0 < ro < NumRows()</pre>
                                            // number of rows, r > 0
853
                  const MatrixIndexT r,
                                             // column offset, 0 < co < NumCols()</pre>
854
                  const MatrixIndexT co,
855
                  const MatrixIndexT c);
                                              // number of columns, c > 0
856
       // This initializer is mostly intended for use in CuMatrix and related
857
858
       // classes. Be careful!
       SubMatrix(Real *data,
859
                  MatrixIndexT num_rows,
860
861
                  MatrixIndexT num_cols,
862
                  MatrixIndexT stride);
863
       ~SubMatrix<Real>() {}
864
865
```

```
SubMatrix<Real> (const SubMatrix &other):
868
869
       MatrixBase<Real> (other.data_, other.num_cols_, other.num_rows_,
870
                          other.stride_) {}
871
      private:
872
874
       SubMatrix<Real> &operator = (const SubMatrix<Real> &other);
875
877
880
881
     // Some declarations. These are traces of products.
882
883
884
     template<typename Real>
885
     bool ApproxEqual(const MatrixBase<Real> &A,
886
                       const MatrixBase<Real> &B, Real tol = 0.01) {
887
       return A.ApproxEqual(B, tol);
888
     }
889
890
     template<typename Real>
     inline void AssertEqual(const MatrixBase<Real> &A, const MatrixBase<Real> &B,
891
892
                              float tol = 0.01) {
893
       KALDI_ASSERT(A.ApproxEqual(B, tol));
894
895
897
     template <typename Real>
898
     double TraceMat(const MatrixBase<Real> &A) { return A.Trace(); }
899
900
902
     template <typename Real>
903
     Real TraceMatMatMat(const MatrixBase<Real> &A, MatrixTransposeType transA,
904
                            const MatrixBase<Real> &B, MatrixTransposeType transB
                            const MatrixBase<Real> &C, MatrixTransposeType transC);
905
906
908
     template <typename Real>
     Real TraceMatMatMatMat(const MatrixBase<Real> &A, MatrixTransposeType transA,
909
                               const MatrixBase<Real> &B, MatrixTransposeType transB,
910
                               const MatrixBase<Real> &C, MatrixTransposeType transC,
const MatrixBase<Real> &D, MatrixTransposeType transD);
911
912
913
915
916
919
920
     template<typename Real> void SortSvd(VectorBase<Real> *s, MatrixBase<Real> *U,
928
                                            MatrixBase<Real>* Vt = NULL,
929
930
                                            bool sort_on_absolute_value = true);
931
938
     template<typename Real>
939
     void CreateEigenvalueMatrix(const VectorBase<Real> &real, const VectorBase<Real>
     &imag,
940
                                  MatrixBase<Real> *D);
941
946
     template<typename Real>
     bool AttemptComplexPower(Real *x_re, Real *x_im, Real power);
947
948
949
950
952
955
     template<typename Real>
956
     std::ostream & operator << (std::ostream & Out, const MatrixBase<Real> & M);
957
958
     template<typename Real>
959
     std::istream & operator >> (std::istream & In, MatrixBase<Real> & M);
960
961
     // The Matrix read allows resizing, so we override the MatrixBase one.
962
     template<typename Real>
963
     std::istream & operator >> (std::istream & In, Matrix<Real> & M);
964
965
966
     template<typename Real>
     bool SameDim(const MatrixBase<Real> &M, const MatrixBase<Real> &N) {
967
       return (M.NumRows() == N.NumRows() && M.NumCols() == N.NumCols());
968
969
970
972
```

```
973
974
975
976
977
978
// we need to include the implementation and some
979
// template specializations.
980
981
981
982
983 #endif // KALDI_MATRIX_KALDI_MATRIX_H_
```