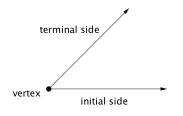
Topics: angles, degrees, radians, coterminal angles lengths of circular arcs, areas of circular sectors

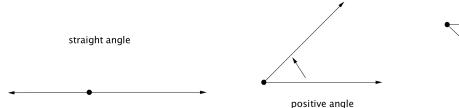
#### **Student Learning Outcomes:**

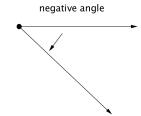
- 1. Students will be able to find degree and radian measure.
- 2. Students will be able to determine coterminal angles.
- 3. Students will be able to determine arc length and area of a sector of a circle.

## 1 Finding Degree Measure



- $\star$  An **angle** is formed by rotating a ray around its endpoint.
- ★ The original position of the ray is called the **initial side** of the angle; the ending position of the ray is called the **terminal side**.
- $\star$  The endpoint of the ray is called the **vertex**.

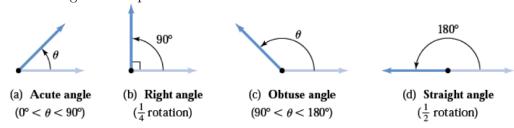




- $\star$  An angle is said to be in **standard position** if its vertex is at the origin and its initial side is on the positive x-axis.
- \* An angle is **positive** if it is rotated counterclockwise and **negative** if it is rotated clockwise.
- \* Greek letters are commonly used to name the angles:  $\alpha$  (alpha),  $\beta$  (beta),  $\theta$  (theta),  $\gamma$  (gamma),  $\phi$  (phi).
  - 1. Draw a positive angle  $\theta$  in standard position with its terminal side in Quadrant 3 and a negative angle  $\beta$  with its terminal side in Quadrant 4.

**Degree Measure** We can measure angles using degrees noted by  $^{\circ}$ .

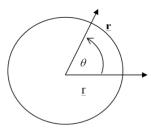
Certain angles have special names:



How many degrees is a full circle?

# 2 Finding Radian Measure

Radian Measure To define radian measure we will use a circle of radius r and the central angle  $\theta$ .  $\theta$  has a measure of **one radian** if it intercepts an arc of length equal to the radius of the circle.



2. If a circle has a radius of 5 and  $\theta$  intercepts an arc of length 10, what is  $\theta$ ?

The radian measurement of an angle is the number of radii that can be laid out on the subtended arc. In other words,  $\theta = \frac{\text{arc length } s}{\text{radius } r}$ .

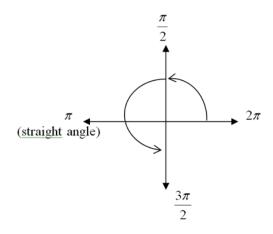
3. How do we convert degrees to radians and radians to degrees? **Answer:** We use the complete rotation of a circle.

1 rotation=360°, Circumference of a circle= $2\pi r$ 

$$\theta = \frac{s}{r} = \frac{\text{circumference}}{r} = \frac{2\pi r}{r} = 2\pi$$

Therefore, 1 rotation is  $360^{\circ} = 2\pi$  radians.

What if we divide both sides by 2?



### Conversions

To covert from degrees to radians, multiply by  $\frac{\pi}{180}$ .

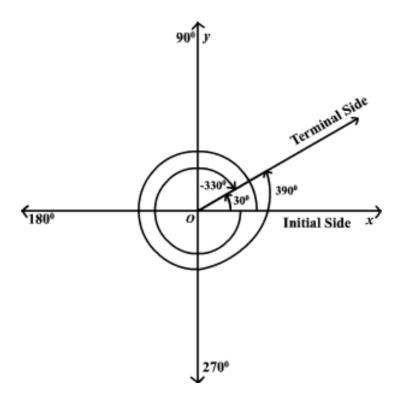
To covert from radians to degrees, multiply by  $\frac{180}{\pi}.$ 

4. Covert  $90^{\circ}, 150^{\circ}, 1^{\circ}, -135^{\circ}$  to radians.

5. Covert  $\frac{5\pi}{6}, \frac{-5\pi}{6}, 3\pi, 1$  radian to degrees.

# 3 Coterminal Angles

Coterminal Angles Two angles are coterminal angles if they have the same terminal side and initial side but different rotations.

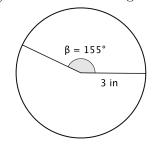


6. Find two positive angles and two negative angles coterminal to  $\theta=60^{\circ}$ .

## 4 Arc Length and Area of a Sector

If  $\theta$  is the radian measure of a central angle of a circle of radius r, and if A is the area of the circular sector determined by  $\theta$ , then  $A = \frac{1}{2}r^2\theta$ .

- 7. Determine the area of the circular sector with central angle  $\theta=120^\circ$  when the radius of the circle is 5.
- 8. (a) Determine the length of the arc subtended by the angle  $\beta$  below.



(b) Determine the area of the circular sector with central angle  $\beta$  above.

### Student Learning Outcomes Check

- 1. Can you find degree and radian measure?
- 2. Can you determine coterminal angles?
- 3. Are you able to determine arc length and area of a sector of a circle?

If any of your answers were no, please ask about these topics in class.