```
CPS 2019 : Liens et Spécification partielle. (version du 05/04/19)
```

#### Manuel d'utilisation

## Spécification formelle complète

#### Ecran

```
Service:
                         Screen
      Observators:
                         const Height : [Screen] \rightarrow int
                          \mathbf{const} \; \mathtt{Width} : [\mathrm{Screen}] \to \mathrm{int}
                          CellNature : [Screen] \times int \times int \rightarrow Cell
                            pre CellNature(S,x,y) requires 0 \le y < \text{Height(S)} and 0 \le x < \text{Width(S)}
     Constructors: init: int \times int \rightarrow [Screen]
                            pre init(h,w) requires 0 < h and 0 < w
         Operators: Dig : [Screen] \times int \times int \rightarrow [Screen]
                            pre Dig(S,x,y) requires CellNature(S,x,y) = PLT
                          Fill : [Screen] \times int \times int \rightarrow [Screen]
                            pre Dig(S,x,y) requires CellNature(S,x,y) = HOL
     Observations:
             [init]:
                         Height(init(h,w)) = h
                          Width(init(h,w)) = w
                          forall (u, v) in [0; Width(S)[\times [0; Height(S)[, CellNature(init(h,w),x,y) = EMP
                         CellNature(Dig(S,x,y)),x,y = HOL
               [Dig] :
                          forall (u, v) in [0; Width(S)[ \times [0; Height(S)[,
                                    (x \neq u \text{ or } y \neq v) \text{ implies CellNature(Dig(S,x,y)),} u,v) = CellNature(u,v)
             [Fill]: CellNature(Fill(S,x,y),x,y) = PLT
                          forall (u, v) in [0; Width(S)[\times [0; Height(S)[,
                                    (x \neq u \text{ or } y \neq v) \text{ implies CellNature(Fill(S,x,y)),u,v)} = \text{CellNature(u,v)}
Ecran editable
            Service:
                         EditableScreen includes Screen
                         Playable : [EditableScreen] \rightarrow bool
      Observators:
         \mathbf{Operators}: \quad \mathbf{SetNature}: [\mathbf{EditableScreen}] \times \mathbf{int} \times \mathbf{int} \times \mathbf{Cell} \rightarrow [\mathbf{EditableScreen}]
                            pre SetNature(S,x,y,C) requires 0 \le y < \text{Height(S)} and 0 \le x < \text{Width(S)}
     Observations:
       [invariant]: Playable(S) min
                                   forall (x, y) in [0; Width(S)[\times [0; Height(S)[, CellNature(S,x,y) \neq HOL
                                   and forall x in [0;Width(S)[,CellNature(S,x,0)=MTL]
       [SetNature]: CellNature(SetNature(S,x,y,C)),x,y = C
                          forall (u, v) in [0;Width(S)] \times [0;Height(S)],
                                   (x \neq u \text{ or } y \neq v) \text{ implies CellNature(SetNature(S,x,y,C))}, u,v) = \text{CellNature}(u,v)
```

#### Environnement

Service: Environment includes Screen

**Observators**: CellContent : int  $\times$  int  $\rightarrow$  Set{Character + Item}

pre CellContent(E,x,y) requires  $0 \le y < \text{Height(S)}$  and  $0 \le x < \text{Width(S)}$ 

Constructors: init: EditableScreen  $\rightarrow$  Environment

Observations:

[invariant]: forall (x,y) in  $[0;Width(E)[\times [0;Height(E)[,$ 

forall Character c1, c2 in CellContent(E,x,y) $^2$ , c1 = c2

forall (x, y) in  $[0;Width(E)[\times [0;Height(E)[,$ 

CellNature(E,x,y) in  $\{MTL, PLR\}$  implies CellContent(x,y) =  $\emptyset$ 

 $implies \; (\texttt{CellNature(E,x,y)} = \mathbf{EMP} \; \mathbf{and} \; \texttt{CellNature(E,x,y-1)} \; \mathbf{in} \; \{\mathbf{PLT}, \; \mathbf{MTL}\})$ 

[init]: forall (x,y) in  $[0;Width(E)[\times [0;Height(E)[,$ 

CellNature(init(S),x,y) = EditableScreen : :CellNature(S,x,y)

#### Personnage

```
Service:
                 Character
 Observators:
                 const \ Envi : [Character] \rightarrow Environment
                 Hgt : [Character] \rightarrow int
                 Wdt : [Character] \rightarrow int
   Operators:
                 init : Screen \times int \times int \rightarrow [Character]
                   pre init(S,x,y) requires Environment : :CellNature(S,x,y) = EMP
                 GoLeft : [Character] \rightarrow [Character]
                 GoRight : [Character] \rightarrow [Character]
                 GoUp : [Character] \rightarrow [Character]
                 GoDown : [Character] \rightarrow [Character]
Observations:
 [invariant]:
                 Environment::CellNature(Envi(C),Wdt(C),Hgt(C)) in {EMP, HOL, LAD, HDR}
                 exists Character x in Environment : :CellContent(Envi(C),Wdt(C),Hgt(C)) implies x = C
     [GoLeft]:
                 Hgt(GoLeft(C)) = Hgt(C)
                 Wdt(C) = 0 implies Wdt(GoLeft(C)) = Wdt(C)
                 Environment : :CellNature(Envi(C),Wdt(C)-1,Hgt(C)) in \{MTL, PLT\}
                   implies Wdt(GoLeft(C)) = Wdt(C)
                 Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)) not in \{LAD, HDR\}
                      and Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) not in {PLT, MTL, LAD }
                      and not exists Character c in Environment::CellContent(Envi(C),Wdt(C),Hgt(C)-1)
                     implies Wdt(GoLeft(C)) = Wdt(C)
                 exists Character c in Environment : :CellContent(Envi(C),Wdt(C)-1,Hgt(C))
                      implies Wdt(GoLeft(C)) = Wdt(C)
                 (Wdt(C) \neq 0) and Environment : :CellNature(Envi(C),Wdt(C)-1,Hgt(C)) not in {MTL, PLT }
                      and (Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)) in {LAD, HDR}
                          or Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)-1) in {PLT, MTL, LAD}
                          or exists Character c in Environment : :CellContent(Envi(C),Wdt(C),Hgt(C)-1) )
                      and not (exists Character c in Environment : :CellContent(Envi(C),Wdt(C)-1,Hgt(C)))
                     implies Wdt(GoLeft(C)) = Wdt(C)-1
   [GoRight]:
                 Hgt(GoRight(C)) = Hgt(C)
                 Wdt(C) = Environement : :Width(Envi(C)) implies Wdt(GoRight(C)) = Wdt(C)
                 Environment : :CellNature(Envi(C), Wdt(C)+1, Hgt(C)) in \{MTL, PLT \}
                   implies Wdt(GoRight(C)) = Wdt(C)
                 Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)) not in {LAD, HDR}
                      and Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) not in {PLT, MTL, LAD }
                      and not exists Character c in Environment::CellContent(Envi(C),Wdt(C),Hgt(C)-1)
                     implies Wdt(GoRight(C)) = Wdt(C)
                 exists Character c in Environment : :CellContent(Envi(C),Wdt(C)+1,Hgt(C))
                      implies Wdt(GoRight(C)) = Wdt(C)
                 (Wdt(C) \neq Environement : :Height(Envi(C))
                   and Environment::CellNature(Envi(C),Wdt(C)+1,Hgt(C)) not in {MTL, PLT}
                      and (Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)) in {LAD, HDR}
                          or Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) in {PLT, MTL, LAD}
                          or exists Character c in Environment : :CellContent(Envi(C),Wdt(C),Hgt(C)-1) )
                      and not (exists Character c in Environment : :CellContent(Envi(C),Wdt(C)+1,Hgt(C)))
                      implies Wdt(GoRight(C)) = Wdt(C)+1
```

```
Wdt(GoUp(C)) = Wdt(C)
  [GoUp]:
           Hgt(C) = Environment : :Height(Envi(C)) implies <math>Hgt(GoUp(C)) = Hgt(C)
           Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)) \neq LAD implies Hgt(GoUp(C)) = Hgt(C)
           Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)+1) \neq LAD
             implies Hgt(GoUp(C)) = Hgt(C)
            exists Character c in Environment : :CellContent(Envi(C),Wdt(C),Hgt(C)+1) implies
             Hgt(GoUp(C)) = Hgt(C)
           Hgt(C) \neq Environment : :Height(Envi(C))
              and (Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)+1 = \mathbf{LAD}
                Environment::CellNature(Envi(C),Wdt(C),Hgt(C)+1 not in { MTL,PLT }
              and Environment : :CellNature(Envi(C), Wdt(C), Hgt(C) = LAD
             and not exists Character c in Environment::CellNature(Envi(C),Wdt(C),Hgt(C)+1
             implies Wdt(GoUp(C)) = Hgt(C)+1
[GoDown]:
           Wdt(GoDown(C)) = Wdt(C)
           Hgt(C) = 0 implies
              Hgt(GoDown(C)) = Hgt(C)
           Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1) in { MTL,PLT }
              implies Hgt(GoDown(C)) = Hgt(C)
           exists Character c in Environment : :CellContent(Envi(C),Wdt(C),Hgt(C)-1)
             implies Hgt(GoDown(C)) = Hgt(C)
           Hgt(C) \neq 0
             and Environment : :CellNature(Envi(C),Wdt(C),Hgt(C)-1) in { MTL,PLT }
             and not exists Character c not in Environment::CellNature(Envi(C),Wdt(C),Hgt(C)-1
             implies Wdt(GoDown(C)) = Hgt(C)-1
```

#### Garde

```
Service :
                   Guard includes Character
 Observators:
                   const Id : [Guard] \rightarrow int
                   Behaviour : [Guard] \rightarrow Move
                   Target : [Guard] \rightarrow Character
                   \texttt{TimeInHole}: [Guard] \rightarrow int
   Operators: init : Screen \times int \times int \times Player \rightarrow [Guard]
                      pre init(s,x,y,p) requires Environment::CellNature(S,x,y) = EMP and p \neq \emptyset
                   ClimbLeft : [Guard] \rightarrow [Guard]
                        pre ClimbLeft(G) requires Environment::CellNature(Envi(G),Hgt(G),Wdt(G)) = HOL
                   ClimbRight : [Guard] \rightarrow [Guard]
                        pre ClimbRight(G) requires Environment::CellNature(Envi(G),Hgt(G),Wdt(G)) = HOL
                   Step : [Guard] \rightarrow [Guard]
Observations:
    [invariant]:
                   Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = LAD
                        and Hgt(G) < Character : :Hgt(Target(G))
                        and (Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) not in {PLT, MTL}
                             or exists Character c in Environment : :CellContent(Envi(G),Wdt(G),Hgt(G)-1)
                             implies |\text{Environment} : \text{Hgt}(\text{Target}(G)) - \text{Hgt}(G)| <
                                |\text{Environment}: \text{Wdt}(\text{Target}(G)) - \text{Wdt}(G))|)
                        implies Behaviour(G) = Up
                   Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = LAD
                        and Hgt(G) > Character : :Hgt(Target(G))
                        and (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)-1) not in {PLT, MTL }
                             or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1)
                             implies |\text{Environment} : \text{Hgt}(\text{Target}(G)) - \text{Hgt}(G)| <
                               |\text{Environment}: \text{Wdt}(\text{Target}(G)) - \text{Wdt}(G))|)
                        implies Behaviour(G) = Down
                   Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = \mathbf{LAD}
                        and Wdt(G) < Character : :Wdt(Target(G))
                        and (Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) not in {PLT, MTL}
                             or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1)
                             implies |\text{Environment} : \text{Hgt}(\text{Target}(G)) - \text{Hgt}(G)| >
                               |\text{Environment}: \text{Wdt}(\text{Target}(G)) - \text{Wdt}(G))|)
                        implies Behaviour(G) = Left
                   Environment : :CellNature(Envi(G), Wdt(G), Hgt(G)) = LAD
                        and Wdt(G) > Character : :Wdt(Target(G))
                        and (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)-1) not in {PLT, MTL}
                             or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1)
                             implies |\text{Environment} : \text{Hgt}(\text{Target}(G)) - \text{Hgt}(G)| <
                               |\text{Environment}: \text{Wdt}(\text{Target}(G)) - \text{Wdt}(G))|)
                        implies Behaviour(G) = Right
                   Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) in {HOL,HDR} or
                      Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) in {MTL,PLT,LAD} or
                      or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1))
                        and Wdt(G) > Character : :Wdt(Target(G))
                        and (Environment : :CellNature(Envi(G),Wdt(G)-1,Hgt(G)) not in {PLT, MTL }
                             or not exists Character c in Environment : :CellContent(Envi(G),Wdt(G)-1,Hgt(G))
                        implies Behaviour(G) = Left
                   Environment : :CellNature(Envi(G), Wdt(G), Hgt(G)) in {HOL, HDR} or
                      Environment::CellNature(Envi(G),Wdt(G),Hgt(G)-1) in {MTL,PLT,LAD} or
                      or exists Character c in Environment : :CellContent(Envi(G),Wdt(G),Hgt(G)-1) )
                        and Wdt(G) > Character : :Wdt(Target(G))
                        \mathbf{and}\ (\mathrm{Environment}:: \mathrm{Cel} \mathbb{N} \mathrm{ature}(\mathrm{Envi}(\mathrm{G}), \mathrm{Wdt}(\mathrm{G}) + 1, \mathrm{Hgt}(\mathrm{G}))\ \mathbf{not}\ \mathbf{in}\ \{\mathbf{PLT},\ \mathbf{MTL}\ \}
                             or not exists Character c in Environment : :CellContent(Envi(G),Wdt(G)+1,Hgt(G))
                        implies Behaviour(G) = Right
```

```
[invariant]:
               Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) in {HOL,HDR} or
                 Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)-1) in \{MTL,PLT,LAD\} or
                 or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1))
                    and Wdt(G) = Character : :Wdt(Target(G))
                   implies Behaviour(G) = Neutral
               Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = LAD
                 and Hgt(G) < Character : :Hgt(Target(G))
                 implies Behaviour(G) = Up
               Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = LAD
                 and Hgt(G) > Character : :Hgt(Target(G))
                 implies Behaviour(G) = Down
               Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = \mathbf{LAD}
                 and Hgt(G) = Character : :Hgt(Target(G))
                 implies Behaviour(G) = Neutral
               Target(G) = p
       [init]:
 [ClimbLeft]:
               Wdt(G) = 0 implies Wdt(ClimbLeft(G)) = Wdt(G) and Hgt(ClimbLeft(G)) = Hgt(G)
               Environment : :CellNature(Envi(G),Wdt(G)-1,Hgt(G) +1) in \{MTL, PLT\}
                   \mathbf{implies} \ \mathrm{Wdt}(\mathrm{ClimbLeft}(G)) = \mathrm{Wdt}(G) \ \mathbf{and} \ \mathrm{Hgt}(\mathrm{ClimbLeft}(G)) = \mathrm{Hgt}(G)
               exists Character c in Environment::CellContent(Envi(G),Wdt(G)-1,Hgt(G)+1)
                   implies Wdt(ClimbLeft(G)) = Wdt(G) and Hgt(ClimbLeft(G)) = Hgt(G)
               Wdt(G) \neq 0 and Environment : CellNature(Envi(G), Wdt(G)-1, Hgt(G)+1) not in {MTL, PLT }
                   and not exists Character c in Environment::CellContent(Envi(G),Wdt(G)-1,Hgt(G)+1)
                   implies Wdt(ClimbLeft(G)) = Wdt(G)-1 and Hgt(ClimbLeft(G)) = Hgt(C)+1
[ClimbRight]:
               Wdt(G) = Environment : :Width(G)
                  implies Wdt(ClimbRight(G)) = Wdt(G) and Hgt(ClimbRight(G)) = Hgt(G)
               Environment : :CellNature(Envi(G),Wdt(G)+1,Hgt(G) +1) in \{MTL, PLT\}
                   implies Wdt(ClimbRight(G)) = Wdt(G) and Hgt(ClimbRight(G)) = Hgt(G)
               exists Character c in Environment::CellContent(Envi(G),Wdt(G)+1,Hgt(G)+1)
                    implies Wdt(ClimbRight(G)) = Wdt(G) and Hgt(ClimbLeft(G)) = Hgt(G)
               Wdt(G) \neq Environment : :Width(G) and
                    Environment::CellNature(Envi(G),Wdt(G)-1,Hgt(G)+1) not in {MTL, PLT}
                   and not exists Character c in Environment::CellContent(Envi(G),Wdt(G)+1,Hgt(G)+1)
                   implies Wdt(ClimbRight(G)) = Wdt(G)+1 and Hgt(ClimbLeft(G)) = Hgt(G)+1
```

```
WillFall(G) defined by (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)-1) in {HOL, EMP }
    and not exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1)
    and Environment::CellNature(Envi(G),Wdt(G),Hgt(G)) not in {LAD, HDR }
WillIncTime(G) defined by (Environment : :CellNature(Envi(G), Wdt(G), Hgt(G)) = HOL and
    TimeInHole(G) < 5
WillLeft (G) defined by (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = HOL and
    TimeInHole(G) = 5 and Behavior(G) = Left)
WillRight(G) defined by (Environment : :CellNature(Envi(G), Wdt(G), Hgt(G)) = HOL and
    TimeInHole(G) = 5 and Behavior(G) = Right)
\textbf{WillNeutral(G) defined by } (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) = HOL \ \textbf{and} \\
    TimeInHole = 5 and Behavior = Neutral)
WillGoLeft(G) defined by Behavior(G) = Left and
  (Wdt(G) \neq 0) and Environment: :CellNature(Envi(G),Wdt(P)-1,Hgt(G)) not in {MTL, PLT}
    and (Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)) in {LAD, HDR}
        or Environment : :CellNature(Envi(G),Wdt(G),Hgt(G)-1) in {PLT, MTL, LAD}
        or exists Character c in Environment::CellContent(Envi(G),Wdt(G),Hgt(G)-1))
    and not (exists Character c in Environment : :CellContent(Envi(G),Wdt(G)-1,Hgt(G)))
WillGoRight(G) defined by Behavior(G) = Right and
  (Wdt(P) \neq Environement : :Height(Envi(P))
Environment : :CellNature(Envi(P),Wdt(P)+1,Hgt(P)) not in {MTL, PLT}
    and (Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)) in {LAD, HDR}
        or Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) in {PLT, MTL, LAD}
        or exists Character c in Environment::CellContent(Envi(P),Wdt(P),Hgt(P)-1))
    and not (exists Character c in Environment : :CellContent(Envi(P),Wdt(P)+1,Hgt(P)))
WillGoUp(G) defined by Behavior(G) = Up and
  Hgt(P) \neq Environment : :Height(Envi(P))
  and (Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1 = \mathbf{LAD}
    Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1 not in { MTL,PLT }
  and Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)) = LAD
  and not exists Character c in Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1)
WillGoDown(G) defined by Behavior(G) = Down
  and Hgt(P) \neq 0
  and Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) in { MTL,PLT }
  and not exists Character c not in Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1)
WillFall(G) implies GoDown(G)
WillTimeInc(G) implies TimeInHole(Step(G)) = TimeInHole(G) + 1
WillLeft(G) implies ClimbLeft (G)
WillRight(G) implies ClimbRight (G)
WillNeutral(G) implies Hgt(Step(G)) = Hgt(G) and Wdt(Step(G)) = Wdt(G)
WillGoLeft(G) implies GoLeft (G)
WillGoRight (G) implies GoRight (G)
WillGoUp(G) implies GoUp (G)
WillGoDown(G) implies GoDown (G)
```

#### Joueur

```
Player includes Character
     Service :
Observators:
                Engine : [Player] \rightarrow Engine
                init : Screen \times int \times int \times Engine \rightarrow [Player]
  Operators:
                  pre init(S,x,y,e) requires Environment::CellNature(S,x,y) = EMP and e \neq \emptyset
                 Step : [Player] \rightarrow [Player]
Observations:
        [init]:
                Engine(P) = e
        [Step]:
                 WillFall(P) defined by (Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)-1)
                     in {HOL, EMP }
                     and not exists Character c in Environment::CellContent(Envi(G),Wdt(P),Hgt(P)-1)
                     and Environment::CellNature(Envi(P),Wdt(P),Hgt(P)) not in {LAD, HDR }
                 WillGoLeft(P) defined by Engine : NextCommand(Engine(P)) = Left and
                   (\mathrm{Wdt}(P) \neq 0) and Environment: :CellNature(Envi(P),Wdt(P)-1,Hgt(P)) not in {MTL, PLT}
                     and (Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)) in {LAD, HDR}
                         or Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) in {PLT, MTL, LAD}
                         or exists Character c in Environment::CellContent(Envi(P),Wdt(P),Hgt(P)-1))
                     and not (exists Character c in Environment : :CellContent(Envi(P),Wdt(P)-1,Hgt(P)))
                 WillGoRight (P) defined by Engine: :NextCommand(Engine(P)) = Right and
                   (Wdt(P) \neq Environement : :Height(Envi(P))
                 Environment : :CellNature(Envi(P),Wdt(P)+1,Hgt(P)) not in {MTL, PLT}
                     and (Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)) in {LAD, HDR}
                         or Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)-1) in {PLT, MTL, LAD}
                         or exists Character c in Environment : :CellContent(Envi(P),Wdt(P),Hgt(P)-1) )
                     and not (exists Character c in Environment : :CellContent(Envi(P),Wdt(P)+1,Hgt(P)))
                 WillGoUp(P) defined by Engine::NextCommand(Engine(P)) = Up and
                   Hgt(P) \neq Environment : :Height(Envi(P))
                   and (Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1 = \mathbf{LAD}
                     Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1 not in { MTL,PLT }
                   and Environment : :CellNature(Envi(P),Wdt(P),Hgt(P) = LAD
                   and not exists Character c in Environment::CellNature(Envi(P),Wdt(P),Hgt(P)+1
                 WillGoDown(P) defined by Engine: :NextCommand(Engine(P)) = Down
                   and Hgt(P) \neq 0
                   and Environment : :CellNature(Envi(P),Wdt(P),Hgt(P)-1) in { MTL,PLT }
                   and not exists Character c not in Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1
                 WillDigL(P) defined by Engine: :NextCommand(Engine(P)) = DigL
                   and (Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) in {PLT, MTL, LAD}
                         or exists Character c in Environment::CellContent(Envi(P),Wdt(P),Hgt(P)-1))
                   and Environment::CellNature(Envi(P),Wdt(P)-1,Hgt(P)) not in {PLT, MTL}
                   and Environment : :CellNature(Envi(P),Wdt(P)-1,Hgt(P)-1) = PLT
                 WillDigR(P) defined by Engine: :NextCommand(Engine(P)) = DigR
                   and (Environment::CellNature(Envi(P),Wdt(P),Hgt(P)-1) in {PLT, MTL, LAD}
                         or exists Character c in Environment::CellContent(Envi(P),Wdt(P),Hgt(P)-1))
                   and Environment::CellNature(Envi(P),Wdt(P)+1,Hgt(P)) not in {PLT, MTL}
                   and Environment : :CellNature(Envi(P),Wdt(P)+1,Hgt(P)+1) = PLT
                 WillGoLeft(P) implies Wdt(P) = Wdt(GoLeft(P))
                   and Hgt(P) = Hgt(GoLeft(P))
                 WillGoRight(P) implies Wdt(P) = Wdt(GoRight(P))
                   and Hgt(P) = Hgt(GoRight(P))
                 WillGoUp(P) implies Wdt(P) = Wdt(GoUp(P))
                   and Hgt(P) = Hgt(GoUp(P))
                 WillGoDown(P) implies Wdt(P) = Wdt(GoDown(P))
                   and Hgt(P) = Hgt(GoDown(P))
                 WillDigL(P) implies Envir@nment : :Dig(Envi(P),Wdt(P)-1,Hgt(P)-1)
                   and Environment : :CellNature(Envi(P),Wdt(P)-1,Hgt(P)-1) = HOL
                 WillDigR(P) implies Environment : :Dig(Envi(P),Wdt(P)+1,Hgt(P)+1)
                   and Environment : :CellNature(Envi(P),Wdt(P)+1,Hgt(P)+1) = HOL
```

### **Engine**

```
Service:
                  Engine
 Observators:
                  Environment : [Engine] \rightarrow Env
                   Player : [Engine] \rightarrow Player
                   Guards : [Engine] \rightarrow Set \{Guard\}
                   Treasures : [Engine] \rightarrow Set \{Item\}
                   Status : [Engine] \rightarrow Status
                   NextCommand : [Engine] \rightarrow NextCommand
                   Holes : [Engine] \rightarrow Triplet \{int \times int \times int \}
   Operators:
                   init : EditableScreen \times int \times int \times Pair \{int \times int \} \times Pair \{int \times int \} \rightarrow [Player]
                     pre init(S,x,y,G,T) requires Environment : :CellNature(S,x,y) = EMP
                       and (Environment::CellNature(S,x,y-1) in {PLT,MTL})
                     and forall q in G, (Environment::CellNature(S,Pair::L(q),Pair::R(q)) = EMP
                       and Environment::CellNature(S,Pair::L(g),Pair::R(g)-1) in {PLT,MTL})
                     and forall t in T, Environment::CellNature(S,Pair::L(t),Pair::R(t)) = EMP
                       and (Environment::CellNature(S,Pair::L(t),Pair::R(t)-1) in {PLT,MTL})
                     and EditableScreen::Playable(S)
                   Step : [Engine] \rightarrow [Engine]
Observations:
    [invariant]:
                  Player(E) \in Environment : :CellContent(Env(E), Character : :Wdt(Player(E)),
                     Character : Hgt(Player(E)))
                   forall g in Guards(E),
                     g \in Environment : :CellContent(Env(E), Character : :Wdt(g), Character : :Hgt(g)))
                   forall t in Treasures(E),
                     t \in Environment : :CellContent(Env(E), Character : :Wdt(t), Character : :Hgt(t)))
          [init]:
                  Status(E) = Playing
                   Character : Wdt(Player(E)) = x and Character : Hgt(Player(E)) = y
                   forall (t, ct) in Treasures (E) \times T, Item : :Wdt(t) = Pair : :L(ct) and
                     Item : :Hgt(t) = Pair : :R(ct)
                   forall (q, cq) in Guards(E) \times T, Character : :Wdt(g) = Pair : :L(ct) and
                     Character : :Hgt(g) = Pair : :R(cg)
         [Step]:
                  exists Treasures t in Environment::CellContent(Env(E),Character::Wdt(Player(E)),
                     Character : :Hgt(Player(E))) implies t not exists in
                     Environment::CellContent(Env(E),Character::Wdt(Player(E)),Character::Hgt(Player(E)))
                   Treasures(E) = \emptyset implies Status(E)=Win
                   Guard g \in (Environment : :CellContent(Env(E), Character : :Wdt(Player(E))),
                     Character: Hgt(Player(E))) implies Status(E) = Loss
```

# Description formelle des tests MBT effectués

rapport de projet