

**tutor\_week4**

# import random

## random.sample(sequence, k)

作用： 从给定的sequence中随机选择k个不重复的元素，并以列表形式返回这些元素。

sequence： 待抽样的序列，可以是列表、元组、字符串或集合等。

k： 抽取元素的数量。

```
# sequence is list
import random
list1 = [1,2,3,4,5]
random_list_num = random.sample(list1,2)
random_list_num
```

✓ 0.0s

[5, 1]

```
# sequence is tuple
import random
tuple1 = (1,2,3,4,5)
random_tuple_num = random.sample(tuple1,2)
random_tuple_num
```

✓ 0.0s

[4, 5]

# import random

## random.sample(sequence, k)

作用： 从给定的sequence中随机选择k个不重复的元素，并以列表形式返回这些元素。

sequence： 待抽样的序列，可以是列表、元组、字符串或集合等。

k： 抽取元素的数量。

```
# sequence is str
import random
str1 = '12345'
random_str_num = random.sample(str1, 2)
random_str_num
```

✓ 0.0s

['3', '2']

```
# sequence is set
import random
set1 = {3, "apple", 4.5}
random_set_num = random.sample(set1, 2)
random_set_num
```

✓ 0.0s

## dict.fromkeys(keys, values)

作用：创建一个新字典

参数：

keys: 键的列表

values: 或有，可以不传入，默认为None.

字典 (dict)：键值对集合，可变、**键不可重复**、无序。例如：{"name": "John", "age": 30}。

```
keys = ['a', 'b', 'c']
new_dict = dict.fromkeys(keys)
new_dict
```

✓ 0.0s

```
{'a': None, 'b': None, 'c': None}
```

```
keys = ['a', 'b', 'a']
new_dict = dict.fromkeys(keys)
new_dict
```

✓ 0.0s

```
{'a': None, 'b': None}
```

## 共享值的问题与解决

注意:

当使用`dict.fromkeys()`为所有键指定一个可变对象（如列表）作为值时，需要注意所有的键将共享这个可变对象的同一实例。

```
keys = ['a', 'b', 'c', 'd']
value = []
new_dict = dict.fromkeys(keys, value)
print(new_dict)
```

```
# 向这个共享列表添加一个元素
new_dict['a'].append(1)
print(new_dict)
new_dict['b'] = [4]
print(new_dict)
```

✓ 0.0s

```
{'a': [], 'b': [], 'c': [], 'd': []}
{'a': [1], 'b': [1], 'c': [1], 'd': [1]}
{'a': [1], 'b': [4], 'c': [1], 'd': [1]}
```

## value\_cross\_sec\_momentum(horizon,frequency,shift=0) 函数细节详解:

```
def value_cross_sec_momentum(horizon,frequency,shift=0):  
    # Compute dates at which portfolio is rebalanced  
    rebalancing_dates = [dates[shift+(i+1)*frequency] for i in range(n_dates)]
```

```
def value_cross_sec_momentum(horizon,frequency,shift=0):  
    rebalancing_dates = []  
    for i in range(n_dates):  
        the_rebal_date = dates[shift+(i+1)*frequency]  
        rebalancing_dates.append(the_rebal_date)  
    rebalancing_dates
```

列表解析式与for循环的对应关系

## value\_cross\_sec\_momentum(horizon,frequency,shift=0) 函数细节详解:

```
def value_cross_sec_momentum(horizon,frequency,shift=0):  
    # Initialize "old units" to 0  
    units_old = np.zeros([len(tickers)])
```

### np.zeros(shape, dtype=float, order='C')

作用: 返回一个给定形状和类型的用0填充的数组;

shape: 返回的形状

dtype: 数据类型, 默认numpy.float64。 dtype=int, 返回整数0

order: 可选参数, c代表与c语言类似, 行优先; F代表列优先

```
import numpy as np  
units_old = np.zeros(8,dtype = int)  
units_old
```

✓ 0.0s

```
array([0, 0, 0, 0, 0, 0, 0, 0])
```

```
import numpy as np  
units_old = np.zeros((2,2),dtype = float)  
units_old
```

✓ 0.0s

```
array([[0., 0.],  
       [0., 0.]])
```



## value\_cross\_sec\_momentum(horizon,frequency,shift=0) 函数细节详解:

```
def value_cross_sec_momentum(horizon,frequency,shift=0):
    for i in range(len(rebalancing_dates)):
        ## We don't trade, if we don't have enough data about past performance available yet
        if (i+1)*frequency<horizon:
            continue
        # Initialize units to 0
        units = np.zeros_like(rel_ma)
```

**np.zeros\_like(array, dtype = None, order = 'K', subok = True, shape = None)**

作用: 返回一个给定形状和类型的用0填充的数组

array: 一定形状和数据类型的数组, 如果没有传入shape, 全0数组依据array形状和数据类型创建。

dtype: 数据类型。如果没有指定, 返回数组的数据类型会和数组a相同。 dtype=int, 返回整数0

order: 可选参数, {'C','F','A', or 'K'}, 指定数组在内存中的存储顺序。默认是'K', 保持与数组array相同的存储顺序。

subok: bool 类型, 默认为True。 subok = False, 表示返回一个基础类型数组 (即, 总是返回一个基础的、非子类化的数组)。

shape: 指定返回的形状

```
import numpy as np
# 创建一个3x3的整数数组
a = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
# 使用np.zeros_like创建一个形状相同的全零数组
b = np.zeros_like(a)
b
```

✓ 0.0s

```
array([[0, 0, 0],
       [0, 0, 0],
       [0, 0, 0]])
```

```
import numpy as np
# 创建一个3x3的整数数组
a = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])
# 使用np.zeros_like创建一个形状相同的全零数组
b = np.zeros_like(a, dtype = float, shape = (2,2))
print(b)
```

✓ 0.0s

```
[[0. 0.]
 [0. 0.]
```



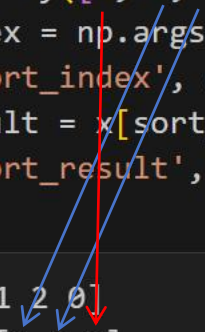
## value\_cross\_sec\_momentum(horizon,frequency,shift=0) 函数细节详解:

```
def value_cross_sec_momentum(horizon,frequency,shift=0):  
    for i in range(len(rebalancing_dates)):  
        ## We don't trade, if we don't have enough data about past performance available yet  
        if (i+1)*frequency<horizon:  
            continue  
        # Sort stocks according to past performance  
        sort_ind = np.argsort(rel_ma)
```

```
x = np.array([3, 1, 2])  
sort_index = np.argsort(x)  
print('sort_index', sort_index)  
sort_result = x[sort_index]  
print('sort_result', sort_result)
```

✓ 0.0s

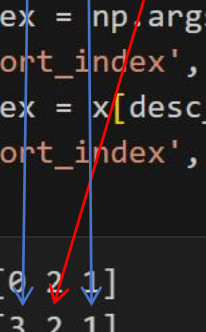
sort\_index [1 2 0]  
sort\_result [1 2 3]



```
x = np.array([3, 1, 2])  
desc_sort_index = np.argsort(-x) #按降序排列  
print('desc_sort_index', desc_sort_index)  
desc_sort_index = x[desc_sort_index]  
print('desc_sort_index', desc_sort_index)
```

✓ 0.0s

desc\_sort\_index [0 2 1]  
desc\_sort\_index [3 2 1]



## value\_cross\_sec\_momentum(horizon,frequency,shift=0) 函数细节详解:

```
def value_cross_sec_momentum(horizon,frequency,shift=0):  
    # Compute dates at which portfolio is rebalanced  
    rebalancing_dates = [dates[shift+(i+1)*frequency] for i in range(n_dates)]  
  
    for i in range(len(rebalancing_dates)):  
        ## We don't trade, if we don't have enough data about past performance available yet  
        if (i+1)*frequency<horizon:  
            continue # 退出本次循环
```

```
# break 跳出整个循环  
number = 0  
for number in range(5):  
    if number == 3:  
        break  
    print("number is",number)  
print("end loop")
```

✓ 0.0s

```
number is 0  
number is 1  
number is 2  
end loop
```

```
# continue 跳出本次循环  
number = 0  
for number in range(5):  
    if number == 3:  
        continue  
    print("number is",number)  
print("end loop")
```

✓ 0.0s

```
number is 0  
number is 1  
number is 2  
number is 4  
end loop
```

```
# pass 不做任何事情，一般用做占位语句。  
# 目前还不清楚具体是什么，提醒开发者这里将来需要添加代码。  
number = 0  
for number in range(5):  
    if number == 3:  
        pass  
    print("number is",number)  
print("end loop")
```

✓ 0.0s

```
number is 0  
number is 1  
number is 2  
number is 3  
number is 4  
end loop
```

**homework\_week4**

1. Suppose  $R$  has a bi-variate normal distribution with mean vector  $(1, 2)$  and covariance matrix with diagonal entries 1 and off-diagonal entries 0. Consider two portfolios: portfolio A with weights  $x = (-1, 2)$  and portfolio B with weights  $x = (0.5, 0.5)$ . Which of the following statements is correct?

$$\Sigma = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

- a) Portfolio A dominates Portfolio B
- b) Portfolio B dominates Portfolio A
- c) Neither of the two portfolios dominates each other.

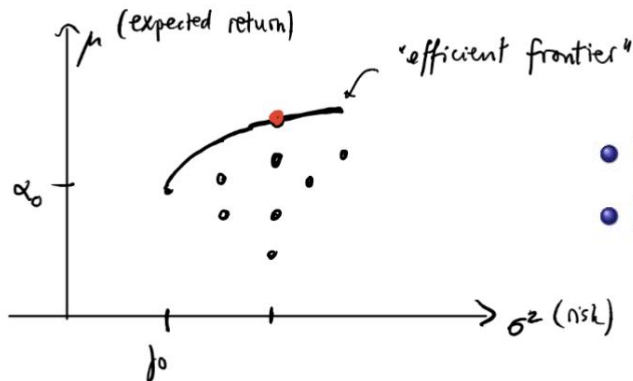
• Notice:

- $\mathbb{E}[R_p(x)] = \sum_{i=1}^n x_i \mu_i = \mu \cdot x$

$$\sigma_p^2(x) = \text{Var}(R_p(x)) = \text{Cov}(R_p(x), R_p(x)) = \text{Cov}\left(\sum_{i=1}^n x_i R_i, \sum_{j=1}^n x_j R_j\right)$$

$$= \sum_{i=1}^n \sum_{j=1}^n x_i x_j \underbrace{\text{Cov}(R_i, R_j)}_{=C_{i,j}}$$

$$= x^T C x$$



- $\text{Var}(R) < \text{Var}(\bar{R})$  and  $\mathbb{E}[R] \geq \mathbb{E}[\bar{R}]$
- $\mathbb{E}[R] > \mathbb{E}[\bar{R}]$  and  $\text{Var}(R) \leq \text{Var}(\bar{R})$

### Expected Return

The expected return for a portfolio can be calculated as:

$$E[R_x] = x \cdot \mu^T$$

- For portfolio A:  $E[R_A] = (-1, 2) \cdot (1, 2)^T = -1 * 1 + 2 * 2 = 3$
- For portfolio B:  $E[R_B] = (0.5, 0.5) \cdot (1, 2)^T = 0.5 * 1 + 0.5 * 2 = 1.5$

### Risk (Standard Deviation)

The risk (variance) for a portfolio is given by:

$$\text{Var}(R_x) = x \Sigma x^T$$

The square root of the variance gives us the standard deviation, which is the risk.

- For portfolio A:  $\text{Var}(R_A) = (-1, 2) \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} -1 \\ 2 \end{bmatrix} = (-1, 2) \cdot (-1, 2)^T = 1 * 1 + 2 * 2 = 5$ , so the risk (standard deviation) is  $\sqrt{5}$ .
- For portfolio B:  $\text{Var}(R_B) = (0.5, 0.5) \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix} = (0.5, 0.5) \cdot (0.5, 0.5)^T = 0.5 * 0.5 + 0.5 * 0.5 = 0.5$ , so the risk (standard deviation) is  $\sqrt{0.5}$ .

Figure: Efficient frontier (illustration)



2. Suppose  $R$  has a bi-variate normal distribution with mean vector  $(1,1)$  and covariance matrix with diagonal entries 1 and off-diagonal entries  $-0.5$ . Consider two portfolios: portfolio A with weights  $x=(-1,2)$  and portfolio B with weights  $x=(0.5,0.5)$ . Which of the following statements is correct?

- a) Portfolio A dominates Portfolio B
- b) Portfolio B dominates Portfolio A**
- c) Neither of the two portfolios dominates each other.

$$\Sigma = \begin{bmatrix} 1 & -0.5 \\ -0.5 & 1 \end{bmatrix}$$

### Expected Return

Since the mean vector is now  $\mu = (1, 1)$ , the expected returns calculation does not change based on the mean vector but rather on the weights of the portfolios. Let's recalculate with the given weights.

- For portfolio A:  $E[R_A] = (-1, 2) \cdot (1, 1)^T = -1 + 2 = 1$
- For portfolio B:  $E[R_B] = (0.5, 0.5) \cdot (1, 1)^T = 0.5 + 0.5 = 1$

### Risk (Standard Deviation)

We calculate the variance for each portfolio using the covariance matrix to find their risks.

- For portfolio A:

$$\text{Var}(R_A) = (-1, 2) \begin{bmatrix} 1 & -0.5 \\ -0.5 & 1 \end{bmatrix} \begin{bmatrix} -1 \\ 2 \end{bmatrix} = (-1, 2) \cdot (-1, -1)^T = 1 + (-2) + (-2) +$$

So the risk (standard deviation) for A is  $\sqrt{3}$ .

- For portfolio B:

$$\text{Var}(R_B) = (0.5, 0.5) \begin{bmatrix} 1 & -0.5 \\ -0.5 & 1 \end{bmatrix} \begin{bmatrix} 0.5 \\ 0.5 \end{bmatrix} = (0.5, 0.5) \cdot (0.25, 0.25)^T = 0.5 * 0.25 +$$

So the risk (standard deviation) for B is  $\sqrt{0.25} = 0.5$ .

- $\text{Var}(R) < \text{Var}(\bar{R})$  and  $\mathbb{E}[R] \geq \mathbb{E}[\bar{R}]$
- $\mathbb{E}[R] > \mathbb{E}[\bar{R}]$  and  $\text{Var}(R) \leq \text{Var}(\bar{R})$

3. Suppose you want to modify the cross-sectional momentum strategy to only buy the 5% best-performing stocks, but not short-sell the 5% worst-performing stocks. Which adjustments do you have to make in the function “value\_cross\_sec\_momentum”?
- a) Change line 28 to `value.append(value[-1]+(np.sum(units_old*prices_date)))`
  - b) Delete line 25
  - c) Delete line 25 and change line 28 as in a)
  - d) Delete line 25 and change line 24 to `units[long_ind] = total_cap/(n_titles)`

```
9 set_cap = False # Set to False at the beginning
10 for i in range(len(rebalancing_dates)):
11     ## We don't trade, if we don't have enough data about past performance available yet
12     if (i+1)*frequency<horizon:
13         continue # 退出本次循环
14     date = rebalancing_dates[i] # Current date
15     rel_ma = moving_averages.loc[date,tickers] # Access current moving averages
16     prices_date = prices.loc[date] # Access current prices
17     sort_ind = np.argsort(rel_ma) # Sort stocks according to past performance
18     long_ind = sort_ind[len(tickers)-n_titles:] # Indices of those stocks that performed best
19     short_ind = sort_ind[:n_titles] # Indices of those stocks that performed worst
20     units = np.zeros_like(rel_ma) # Initialize units to 0
21     ## In the first iteration this will be false; we start with initial capital. Afterwards this is how much our portfolio is
22     if set_cap is True:
23         total_cap = value[-1]+np.sum(units_old*prices_date) # Previous value + gains you make from selling stocks (or buying t
24         units[long_ind] = total_cap/(2*n_titles) # Set equal weights for stocks that you buy
25         units[short_ind] = -total_cap/(2*n_titles) # Set equal weights for stocks that you shortsell
26         units = units/prices_date # Convert from proportion of wealth to actual units
27         ## Update value: liquidate previous position, build current one.
28         value.append(value[-1]+(np.sum(units_old*prices_date)-np.sum(units*prices_date)))
29         ## Set variables for next iteration
30         units_old = units
31         set_cap = True
32     ## At terminal time we liquidate the full position:
33     value.append(value[-1]+(np.sum(units*prices.loc[dates[-1]])))
```



4. Consider the time-series momentum strategy as used in the lecture. Suppose you use initial capital  $c_2 = 2000000$  instead of  $c_1 = 1000000$ . Denote by  $S_2$  the Sharpe ratio associated to  $c_2$  and by  $S_1$  the Sharpe ratio associated to  $c_1$ . How do  $S_1$  and  $S_2$  compare? (You can test this by evaluating the Sharpe ratio with the same parameters as in the lecture at shift=0 with two different initial capitals.)

a)  $S_1 > S_2$

b)  $S_1 = S_2$

c)  $S_1 < S_2$

```
sharpe=[]
out_of_sample_ind = y_train.shape[0]
for shift in range(9):
    values = np.array(value_strategy_predictor(windowsize,frequency,linear_predictor_mean,shift+out_of_sample_ind))
    returns_strat = (values[1:] - values[:-1])/values[:-1]
    mu_hat = np.mean(returns_strat)
    sigma_hat = np.std(returns_strat)
    ## returns and std are estimated based on a frequency 20/252 -> annualized sharpe ratio has factor np.sqrt(252/20)
    sharpe.append(mu_hat/sigma_hat*np.sqrt(252/frequency))
print(np.mean(sharpe))
print(sharpe)
```

$c_1 = 1000000$

✓ 0.5s

Python

0.179542374853537

[0.48441308784024656, 0.49010630745663225, 0.34320162166603346, 0.22877958085095113, 0.04163870918643329, 0.09394423556635452, -0.1480368830301871, -0.09069058293840025,

```
sharpe=[]
out_of_sample_ind = y_train.shape[0]
for shift in range(9):
    values = np.array(value_strategy_predictor(windowsize,frequency,linear_predictor_mean,shift+out_of_sample_ind))
    returns_strat = (values[1:] - values[:-1])/values[:-1]
    mu_hat = np.mean(returns_strat)
    sigma_hat = np.std(returns_strat)
    ## returns and std are estimated based on a frequency 20/252 -> annualized sharpe ratio has factor np.sqrt(252/20)
    sharpe.append(mu_hat/sigma_hat*np.sqrt(252/frequency))
print(np.mean(sharpe))
print(sharpe)
```

$c_2 = 2000000$

✓ 0.4s

Python

0.179542374853537

[0.48441308784024656, 0.49010630745663225, 0.34320162166603346, 0.22877958085095113, 0.04163870918643329, 0.09394423556635452, -0.1480368830301871, -0.09069058293840025,

5. Suppose R has a bi-variate normal distribution with mean vector (1,2) and covariance matrix with diagonal entries 1 and off-diagonal entries 0. Using the results from the lecture, what is the maximal expected return that can be achieved by an efficient portfolio with risk equal to 1?

- a) 1
- b) 1.5
- c) 2
- d) 2.5

$$\Sigma = \begin{bmatrix} 1 & 0 \\ 0 & 1 \end{bmatrix}$$

→  $\text{corr}(R_a, R_b) = 0$

$$\sigma^2 = w_1^2 \sigma_1^2 + w_2^2 \sigma_2^2$$

with  $\sigma_1^2 = \sigma_2^2 = 1$  (the variances of both assets, given by the diagonal of the covariance matrix), and the risk level squared ( $\sigma^2$ ) set to 1, we find:

$$1 = w_1^2 + w_2^2$$

$$w_1 + w_2 = 1$$

$$w_1^2 + w_2^2 = 1$$

$$w_2 = 1$$

$$w_1 = 0$$

$$E(R) = 1 \cdot 2 + 0 \cdot 1 = 2$$

• Note that we must have  $\sum_{i=1}^n x_i = 1$  for any portfolio.