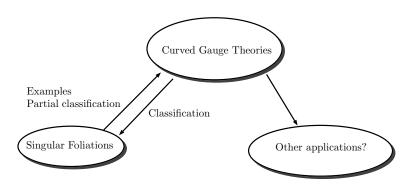
Classification of neighbourhoods of leaves of singular foliations

joint work with Camille Laurent-Gengoux (Université de Lorraine)

Simon-Raphael Fischer

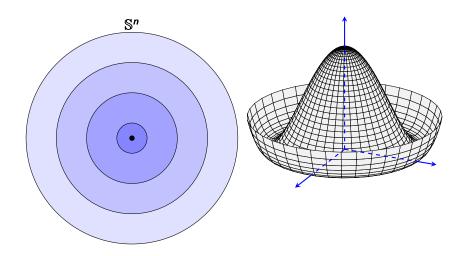


國家理論科學研究中心 National Center for Theoretical Sciences (National Taiwan University)



Remarks (Based on the following works)

- S.-R. F. and Camille Laurent-Gengoux, Classification of neighborhoods around leaves of singular foliations, arXiv:2401.05966, (2024).
- S.-R. F., Integrating curved Yang-Mills gauge theories, arXiv:2210.02924, (2022).



- Gauge Theory
- Poisson Geometry (Singular foliation of symplectic leaves)
- Lie groupoids and algebroids
- Dirac structures
- Generalised complex manifolds
- Non-commutative geometry
- ...

First idea

Definition (Partitionifolds)

Let M be a smooth manifold. A **partitionifold of** M is a partition of immersed connected submanifolds, which we call leaves.

Remarks

We will denote a partitionifold by L_{\bullet} , $p \mapsto L_p$, where L_p is the leaf through $p \in M$.

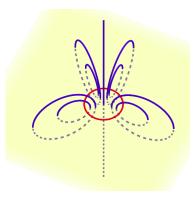


Figure: The magnetic partition

Remarks

A partitionifold with:

- All leaves are of the same dimension.
- But: It lacks regularity!

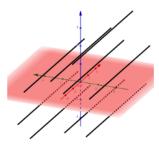


Figure: Isolated lasagna in a spaghetti dish

Remarks

A partitionifold with:

- Dimension is now different.
- But: Also no regularity!

Remarks

Isolated spaghetti in a lasagna dish: Regularity!

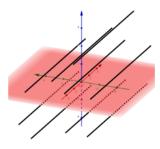


Figure: Isolated lasagna in a spaghetti dish

Remarks

A partitionifold with:

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Remarks

Isolated spaghetti in a lasagna dish: Regularity!

Definition (Smooth partitionifold)

A smooth partitionifold L_{\bullet} is smooth, if there is for all $p \in M$ and every vector $u \in T_p L_p$ a vector field X tangent to L_{\bullet} with

$$X_p = u$$
.

This definition is okay, but not widely used: It still has a problem...

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Remarks

This definition is okay, but not widely used: It still has a problem...

Example (Vector fields not necessarily finitely generated)

Consider the following smooth partitionifold:

 \bullet $M=\mathbb{R}$:

0-dimensional leaves:

$$\{1\}, \left\{\frac{1}{2}\right\}, \left\{\frac{1}{3}\right\}, \dots, \left\{\frac{1}{n}\right\}, \dots, \{0\};$$

• 1-dimensional leaves: Remaining open intervals.

One has a sort of "infinitesimal leaf" next to $\{0\}$.

Technically: Tangent vectors of L_{\bullet} are locally not finitely generated

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Remarks

One has a sort of "infinitesimal leaf" next to $\{0\}$.

Technically: Tangent vectors of L_{\bullet} are locally not finitely generated around 0.

Recall:

Theorem (Frobenius Theorem)

Every integrable subbundle E of TM corresponds to a regular foliation in M.

Remarks

Integrable:

$$[X, Y] \in \Gamma(E)$$

for all $X, Y \in \Gamma(E)$.

Remarks

Alternatively: An involutive submodule of $\mathfrak{X}(M)$, or equivalently of $\mathfrak{X}_c(M)$.

Recall:

Singular Foliations

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Definition

Singular Foliations

Definition (Smooth singular foliation)

A smooth singular foliation \mathcal{F} on a smooth manifold M is a subspace of $\mathfrak{X}_{c}(M)$ so that

- it is involutive.
- it is stable under $C^{\infty}(M)$ -multiplication,
- it is locally finitely generated.

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- it is stable under $C^{\infty}(M)$ -multiplication, i.e. $fX \in \mathcal{F}$ for all $f \in C^{\infty}(M)$ and $X \in \mathcal{F}$,
- it is **locally finitely generated**, i.e. around each $p \in M$ there is an open neighbourhood U and a finite family $(X^i)_{:}^r$ $(X^i \in \mathcal{F})$ such that for all $X \in \mathcal{F}$ there are $f_i \in C^{\infty}(M)$ satisfying on U.

$$X=\sum_i f_i X^i.$$

Remarks (Leaves)

Singular Foliations

We have an induced smooth partitionifold L_{\bullet} ,

$$\mathscr{F}\Rightarrow L_{\bullet},$$

but ${\mathcal F}$ also encodes the information about the generators,



Why locally finitely generated?

Singular Foliations

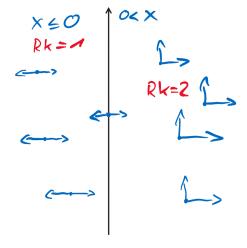
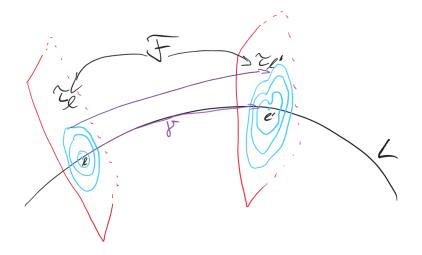
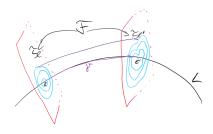


Figure: Infinite comb

First step towards classification



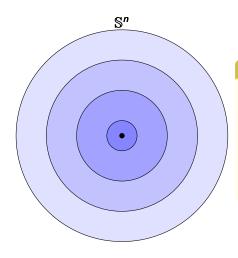


Theorem $(\mathscr{F} ext{-connections})$

There is a connection on the normal bundle of a leaf L:

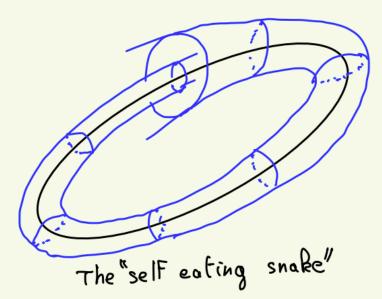
- Horizontal vector fields are in F.
- Parallel transport PT_{γ} has values in $\mathsf{Sym}(\tau_{l}, \tau_{l'})$.
- For a contractible loop γ_0 at I: PT_{γ_0} values in $Inner(\tau_I)$.

Example of a transverse foliation τ :



Remarks

- Inner (τ_I) maps each circle to itself
- Sym (τ_I) allows to exchange circles
- Both preserve τ_l and fix the origin



Other example: Regular foliation

Recovering the ordinary definition Foliation | Connection Regular | Flat lift Singular | Family of possibly curved lifts

Remarks

Inner(τ_I): Trivial.

 $\operatorname{\mathsf{Sym}}(\tau_I)$: The image of a group morphism $\pi_1(L) \to \operatorname{\mathsf{Diff}}_0(\mathbb{R}^d)$.

Remarks

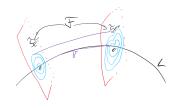
 $Sym(\tau_l)$ and $Inner(\tau_l)$ are in general infinite-dimensional!

Definition (Formal foliation)

 $X \in \mathcal{F}$ induces a derivation on $C^{\infty}(L)/C_0^{\infty}(L)$. The image of \mathcal{F} under this is the **formal singular foliation**.

Remarks

- τ_l a formal singular foliation.
- L a manifold (connected immersed submanifold of M).



Remarks (F-connection)

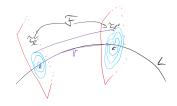
For $\phi \in \operatorname{Sym}(\tau_l)$ we have an induced parallel transport

$$\mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi) \coloneqq \mathsf{PT}_{\gamma} \circ \phi \circ \mathsf{PT}_{\gamma}^{-1}.$$

Then, on the normal bundle $\pi \colon \mathcal{T} \to L$,

$$\mathsf{PT}_{\gamma}(\phi \cdot p) = \mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi) \cdot \mathsf{PT}_{\gamma}(p)$$
 $\mathsf{PT}_{\gamma_0}(p) = \varphi \cdot p$

for all $p \in \mathcal{T}_I$, $\phi \in \text{Sym}(\tau_I)$, and for some $\varphi \in \text{Inner}(\tau_I)$.



Remarks (Sym-connection)

For $\phi \in \operatorname{Sym}(\tau_I)$ we have an induced parallel transport

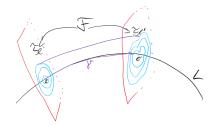
$$\mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi) \coloneqq \mathsf{PT}_{\gamma} \circ \phi \circ \mathsf{PT}_{\gamma}^{-1}.$$

Then

$$\mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi \circ \phi') = \mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi) \circ \mathsf{PT}^{\mathsf{Sym}}_{\gamma}(\phi')$$
$$\mathsf{PT}^{\mathsf{Sym}}_{\gamma_0}(\phi) = \varphi \circ \phi \circ \varphi^{-1}$$

for all $\phi, \phi' \in \text{Sym}(\tau_l)$, and for some $\varphi \in \text{Inner}(\tau_l)$.

Idea

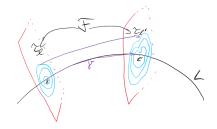


Idea

Generators of \mathcal{F} given by:

$$\mathbb{H}(X) + \overline{\nu},$$

where $X \in \mathfrak{X}(L)$, $\mathbb{H}(X)$ its projectable horizontal lift, $\nu \in \Gamma(\operatorname{inner}(\tau))$ and $\overline{\nu}$ its fundamental vector field.



Idea

Fix I and given τ_I : Reconstruct \mathscr{F} .

$$[\mathbb{H}(X) + \overline{\nu}, \mathbb{H}(X') + \overline{\mu}] = \mathbb{H}([X, X']) + \dots$$

$$= \underbrace{[\mathbb{H}(X), \mathbb{H}(X')]}_{\text{\sim curvature}} + \underbrace{[\mathbb{H}(X), \overline{\mu}] - [\mathbb{H}(X'), \overline{\nu}]}_{\text{\sim connection}} + \overline{[\nu, \mu]}$$

Idea

Fix I and given τ_I : Reconstruct \mathscr{F} .

$$\begin{split} \left[\mathbb{H}(X) + \overline{\nu}, \mathbb{H}(X') + \overline{\mu}\right] &= \mathbb{H}(\left[X, X'\right]) + \dots \\ &= \underbrace{\left[\mathbb{H}(X), \mathbb{H}(X')\right]}_{\text{\sim curvature}} \\ &+ \underbrace{\left[\mathbb{H}(X), \overline{\mu}\right] - \left[\mathbb{H}(X'), \overline{\nu}\right]}_{\text{\sim connection}} + \overline{\left[\nu, \mu\right]} \end{split}$$

Idea $(\ldots \in \tau)$

We need:

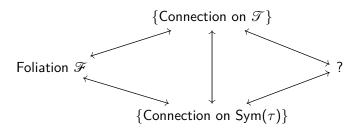
- **1** Lie algebra bundle τ with structure τ_I
- $oldsymbol{2}$ A horizontal lift $\mathbb H$ into $\mathcal T$ satisfying

Curvature:
$$\left[\mathbb{H}(X),\mathbb{H}(X')\right]-\mathbb{H}\left(\left[X,X'\right]\right)\in au$$

Connection:

 $[\mathbb{H}(X), \overline{\mu}] \in \tau$

Summary



Remarks

Connections

- preserve group bundle action,
- and their curvatures follow corresponding orbits.

The pair of connections may **not** be unique for a given \mathcal{F} !

Multiplicative Yang-Mills connections

Curved Yang-Mills gauge theories:

Classical Curved Lie group G Lie group bundle \mathscr{G}



Usually, the field strength F is given by (abelian, for simplicity)

$$F := \mathrm{d}A = \mathrm{d}^{\nabla^0}A.$$

 \rightarrow We will use a general connection ∇ instead of ∇^0 , and ∇ may not be flat.

Curved Yang-Mills gauge theories:

Classical Curved Lie group G Lie group bundle \mathcal{E}



Remarks (Why a "curved theory"?)

Usually, the field strength F is given by (abelian, for simplicity)

$$F := \mathrm{d}A = \mathrm{d}^{\nabla^0}A.$$

 \leadsto We will use a general connection ∇ instead of ∇^0 , and ∇ may not be flat.

Definition (LGB actions)

$$\mathscr{T} \xrightarrow{\pi} L$$

A **right-action of** \mathscr{G} **on** \mathscr{T} is a smooth map

 $\mathcal{T}*\mathcal{G}\coloneqq\mathcal{T}_{\pi}\times_{\pi_{\mathcal{G}}}\mathcal{G}\to\mathcal{T}$, $(p,g)\mapsto p\cdot g$, satisfying the following properties:

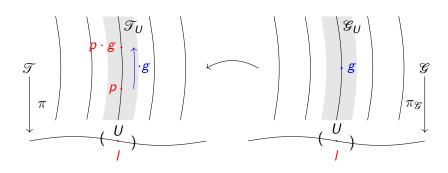
$$\pi(p \cdot g) = \pi(p), \tag{1}$$

$$(p \cdot g) \cdot h = p \cdot (gh), \tag{2}$$

$$p \cdot e_{\pi(p)} = p \tag{3}$$

for all $p \in \mathcal{T}$ and $g, h \in \mathcal{G}_{\pi(p)}$, where $e_{\pi(p)}$ is the neutral element of $\mathcal{G}_{\pi(p)}$.

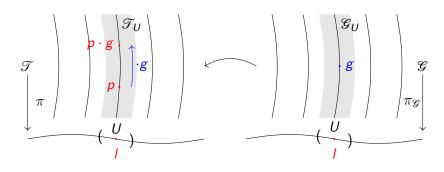
Connection on \mathcal{T} : Idea



But:

$$r_g \colon \mathcal{T}_I o \mathcal{T}_I$$
 $D_p r_g$ only defined on vertical structure

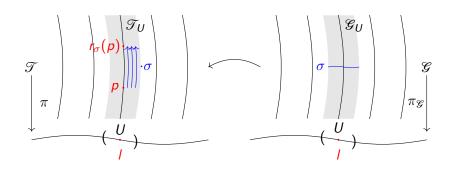
Connection on \mathcal{T} : Idea



But:

$$r_g\colon \mathcal{T}_I o \mathcal{T}_I$$
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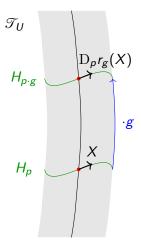
Connection on \mathcal{T} : Idea



Use
$$\sigma \in \Gamma(\mathcal{G})$$
: $r_{\sigma}(p) := p \cdot \sigma_{I}$

Connection on \mathcal{T} : Revisiting the classical setup

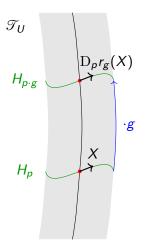
If \mathcal{G} is trivial, $\sigma \equiv g$ constant, and H a connection:



Singular Foliations

Connection on \mathcal{T} : Revisiting the classical setup

If \mathscr{G} is trivial, $\sigma \equiv g$ constant, and H a connection:



Remarks (Integrated case)

Parallel transport $PT_{\gamma}^{\mathcal{T}}$ in \mathcal{T} :

$$\mathsf{PT}_{\gamma}^{\mathscr{T}}(p\cdot g) = \mathsf{PT}_{\gamma}^{\mathscr{T}}(p)\cdot g$$

where $\gamma: I \to L$ is a base path

Connection on \mathcal{T} : General case

Remarks (Integrated case)

Ansatz: Introduce connection on \mathcal{G} ,

$$\mathsf{PT}_{\gamma}^{\mathscr{T}}(p \cdot g) = \mathsf{PT}_{\gamma}^{\mathscr{T}}(p) \cdot \mathsf{PT}_{\gamma}^{\mathscr{G}}(g).$$

Recovering the ordinary definition

- $\mathfrak{g}\cong L\times G$
- 2 Equip \mathcal{G} with canonical flat connection

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General notion of Ehresmann and Yang-Mills connections

Definition (Ehresmann/Yang-Mills connection, [C. L.-G., S.-R. F.])

A surjective submersion $\pi\colon \mathcal{T}\to L$ so that one has a commuting diagram



Ehresmann connection:

$$\mathsf{PT}_{\gamma}^{\mathscr{T}}(p \cdot g) = \mathsf{PT}_{\gamma}^{\mathscr{T}}(p) \cdot \mathsf{PT}_{\gamma}^{\mathscr{G}}(g)$$

Yang-Mills connection: Additionally

$$\mathsf{PT}^{\mathscr{T}}_{\gamma_0}(p) = p \cdot \mathsf{g}_{\gamma_0}$$

for some $g_{\gamma_0} \in \mathcal{G}^0_{\pi(p)}$, where γ_0 is a contractible loop.

Definition (Multiplicative YM connection, [S.-R. F.])

On \mathcal{G} there is also the notion of **multiplicative Yang-Mills** connections, that is,

$$\mathsf{PT}_{\gamma}^{\mathscr{G}}(q \cdot g) = \mathsf{PT}_{\gamma}^{\mathscr{G}}(q) \cdot \mathsf{PT}_{\gamma}^{\mathscr{G}}(g), \ \mathsf{PT}_{\gamma_0}^{\mathscr{G}}(q) = g_{\gamma_0} \cdot q \cdot g_{\gamma_0}^{-1}$$

Remarks

Compare this with the Maurer-Cartan form and its curvature equation!

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Compare this with the Maurer-Cartan form and its curvature equation!

Remarks

On the Lie algebra bundle g we have a connection ∇ with

$$\nabla ([\mu, \nu]_{\mathcal{G}}) = [\nabla \mu, \nu]_{\mathcal{G}} + [\mu, \nabla \nu]_{\mathcal{G}},$$

$$R_{\nabla} = \operatorname{ad} \circ \zeta.$$

Example

Consider the Atiyah sequence of a principal *G*-bundle *P*:

$$(P \times \mathfrak{g})/G \longrightarrow \mathsf{T}P/G \xrightarrow{\downarrow} \mathsf{T}L$$

with splitting $\mathbb{H} \colon \mathrm{T} L \to E$, where \mathfrak{g} is the Lie algebra. Then

$$\nabla_{X}\nu = [\mathbb{H}(X), \nu]_{\mathsf{T}P/G},$$

$$\zeta(X, X') = [\mathbb{H}(X), \mathbb{H}(X')]_{\mathsf{T}P/G} - \mathbb{H}([X, X']).$$

Remarks

On the Lie algebra bundle q we have a connection ∇ with

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Consider the Atiyah sequence of a principal G-bundle P:

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Theorem ([C. L.-G., S.-R. F.])

Given a multiplicative Yang-Mills connection on $\mathcal G$ and a Yang-Mills connection $\mathbb H$ on $\mathcal T$, then there is a natural foliation on $\mathcal T$ generated by

$$\mathbb{H}(X) + \overline{\nu},$$

where $X \in \mathfrak{X}(L)$ and $\nu \in \Gamma(g)$.

Proof

We have

$$[\mathbb{H}(X), \overline{\nu}] = \overline{\nabla_X \nu},$$
$$[\mathbb{H}(X), \mathbb{H}(X')] = \mathbb{H}([X, X']) + \overline{\zeta(X, X')},$$

where $\zeta \in \Omega^2(L; q)$.

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Fix a point $l \in L$ with transverse model (\mathbb{R}^d, τ_l) :

- \bigcirc P a principal G-bundle, equipped with an ordinary connection

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- ① $\mathcal{T} := \left(P \times \mathbb{R}^d\right) / G$, the normal bundle

Fix a point $l \in L$ with transverse model (\mathbb{R}^d, τ_l) :

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- **3** $\mathscr{G} := (P \times G) / G$, the inner group bundle
- $\mathscr{T} := (P \times \mathbb{R}^d) / G$, the normal bundle

Remarks

- ullet Think of the induced connection on ${\mathcal T}$ as the ${\mathcal F}$ -connection.
- \bullet $\mathscr G$ acts on $\mathscr T$ (canonically from the left).

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- P a principal G-bundle, equipped with an ordinary connection
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Remarks

- ullet Think of the induced connection on $\mathcal T$ as the $\mathcal F$ -connection.
- \mathscr{G} acts on \mathscr{T} (canonically from the left).

Proposition ([C. L.-G., S.-R. F.])

The associated connection on $\mathcal G$ is a multiplicative Yang-Mills connection and the one on $\mathcal T$ is a corresponding Yang-Mills connection.

Remarks

Thus, we have a singular foliation on \mathcal{T} , which, by construction, admits L as a leaf and τ_l as transverse data.

Proposition ([C. L.-G., S.-R. F.])

The reconstructed foliation is independent of the choice of connection on P.

Proof.

- The adjoint bundle of P, $Ad(P) := (P \times \mathfrak{g})/G$, is the Lie algebra bundle of \mathscr{G}
- $\tau = \overline{\mathrm{Ad}(P)}$
- Difference of two connections on P has values in Ad(P)

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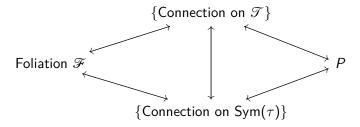
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- Difference of two connections on P has values in Ad(P)

Summary

Remarks ([C. L.-G., S.-R. F.])

In the simply connected case, the following are equivalent:

- ullet Singular foliations with leaf L and transverse model $\left(\mathbb{R}^d, au_I
 ight)$
- Principal Inner(τ_I)-bundles P over L



Summary

Examples

Thank you!