

## Assignment #3 (Due Oct. 30, 2023)

For Q1 and Q2, handwriting or typing is both acceptable.

**Q1.** We call the model in Akcigit and Ates (2023 JPE) with  $f(m_{ijt}) = 1$  as the *baseline model* (notice that  $i$  denotes firm,  $j$  denotes industry, and  $t$  denotes time;  $f(m_{ijt}) = 1$  leads to  $q_{ij(t+\Delta t)} = \lambda q_{ijt}$ ). Solve the following problems with step-by-step derivations:

1. Final good producer's problem ( $Y_t, Y_{jt}, P_t, P_{jt}$ );
2. Intermediate good producer's production problem ( $p_{ijt}, z_{ijt}, y_{ijt}, l_{ijt}, mu_{ijt}, \pi_{ijt}$ , where  $mu_{ijt}$  is the markup);
3. Demand elasticity  $\varepsilon_{ijt} \equiv \frac{\partial \ln(y_{ijt})}{\partial \ln(p_{ijt})}$ ;
4. Suppose intermediate good producers produce *perfectly* substitutable varieties of goods in each industry. Recompute 1 to 3 and explain the difference.

**Q2.** Based on the *baseline model*, write down the computation algorithm for BGP equilibrium and transition dynamics. Explain the tricks or procedures you use as detailed as possible.

**Q3.** Numerically solve the BGP equilibrium of *baseline model*. Plot intermediate firms' production and innovation decision rules. In particular, plot the following:

1. How  $p_{ijt}, z_{ijt}, y_{ijt}$ , and  $\pi_{ijt}$  vary with  $m_{ijt}$ ; show the result with  $\lambda = 1.1$  and  $\lambda = 3.1$ ;
2. How  $x_{ijt}$  varies with  $m_{ijt}$ ; show the result with  $\lambda = 1.1$  and  $\lambda = 3.1$ ;
3. How  $x_{ijt}$  varies with  $m_{ijt}$ ; show the result with  $\phi = 0.01$  and  $\phi = 0.30$ ;
4. Suppose there are no entrants in the model economy. How  $x_{ijt}$  is affected? Replot 1 to 3 and explain the difference.

**Q4. (bonus)** Suppose there are no entrants in the model economy. Impose a change in knowledge diffusion  $\delta$  by 10% from initial to new BGP. Numerically solve the transition dynamics. Explain how the results differ from those in the *baseline model*. You can use parameters in Akcigit and Ates (2013 JPE) to pin down the initial BGP.