

# Solution *Acigit* *ates* *JPE* 2023

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Consumer

Consumer solves  $V_t = \max_{C_s} \exp(-\rho(s-t)) \ln C_s$  The Bellman aligned reads  $V_t(A_t) = \max_{C_s} \ln C_s + \exp$

Set up the Hamiltonian

Final Producer

Final producer solves 
$$\max_{y_{jt}} P_t Y_t - \int_0^1 p_{jt} y_{jt} dj$$
 subject to  $\ln Y_t = \int_0^1 \ln y_{jt} dj$

The marginal profit of the Final producer should equal the marginal cost: 
$$\frac{\partial P_t Y_t}{\partial y_{jt}} = P_t \times \exp(\int_0^1 \ln y_{jt} dj) \times \frac{1}{y_{jt}} = p_{jt}$$
 
$$\Rightarrow P_t Y_t = p_{jt} y_{jt} \Leftrightarrow$$

which is the optimal demand.

Sectoral intermediate production On sectoral level, the intermediate production's optimal supply of products solves