

# Online Appendix of “Haste Makes Waste? Quantity-Based Subsidies under Heterogeneous Innovations”

(Not for Publication)

## A Appendix: Data and Facts

### A.1 Institutional Background and Patent Quantity

Table A.1 lists quantity targets set by Chinese central and local governments in the late 2000s and early 2010s.

Table A.1: Quantity Targets set by the Central and Selected Local Governments

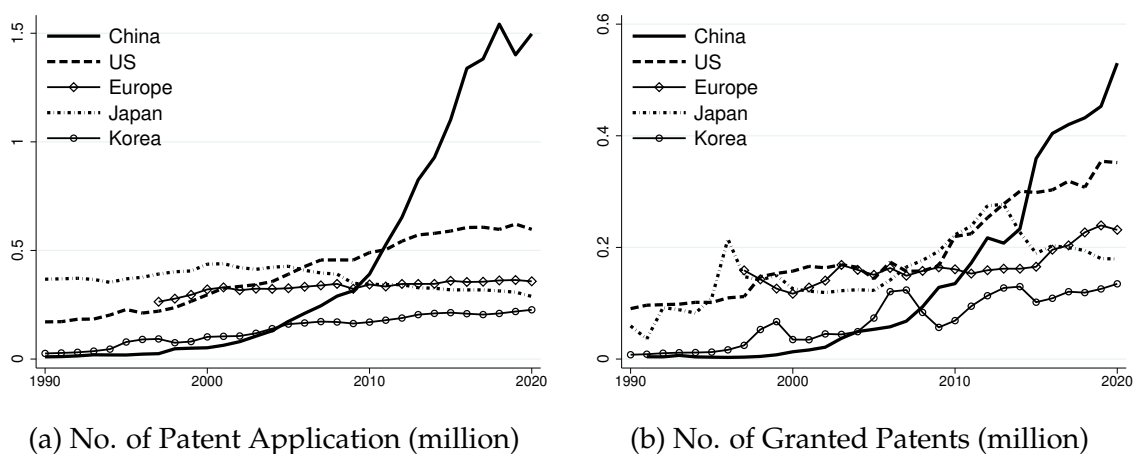
Policy Year	Target Period	Quantity Target
<i>Central Government</i>		
2010	2011-20	Patents to reach 2 mil. & rank Top 2 in the world in 2015 Patents per 1 mil. pop. to increase by 100% by 2015 and 300% by 2020
<i>Beijing City</i>		
2010	2011-15	Patent applications ( <i>resp.</i> grants) per 10,000 pop. to reach 20 ( <i>resp.</i> 8) by 2015
2015	2016-20	Patents per 10,000 pop. to reach 80 by 2020
<i>Shanghai City</i>		
2010	2011-20	Patent grants per 1 mil. pop. to reach 600, and patents per 10,000 pop. to reach 30, in 2015; both criteria to double in 2020
<i>Guangdong Province</i>		
2007	2007-20	Patent applications per 1 mil. pop. to reach 200 in 2010 and to increase more than 15% annually
<i>Heilongjiang Province</i>		
2011	2011-20	Patents per 10,000 pop. to surpass 2.1 by 2015
<i>Guizhou Province</i>		
2017	2016-20	Patents per 10,000 pop. to reach 2.5 by 2020

Data Source: The national targets are from National Patent Development Strategy 2011-2020. Local targets are from local Intellectual Property Development Strategy or Five Year Plans.

Figure A.1 presents the number of applied & granted patents in China and other major patent-holding countries. Table A.2 presents the number of researchers per million

inhabitants in China and selected countries. Figure A.2 shows the number of patent applications per researcher in China, the US, and G5 countries. Lastly, Figure A.3 shows the patent grant rate and number of patents that have been eventually granted per researcher.

Figure A.1: No. of Applied and Granted Patents in China and Advanced Economies



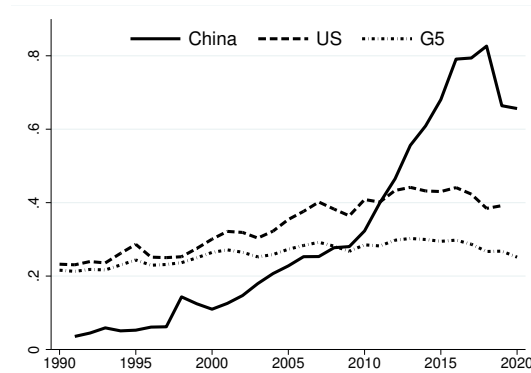
Note: X-axis: year. This figure shows the number of applied and granted patents in China and other major patent-holding economies. The data source is World Intellectual Property Office (WIPO) IP Statistics Data Center.

Table A.2: Researchers per million Inhabitants, 2013

	China	US	Europe	Japan	France	Germany
(1)	1071.1	3984.4	2941.9	5194.8	4124.6	4355.4
(2)	0.2%	1.5%	1.8%	1.2%	1.7%	2.7%

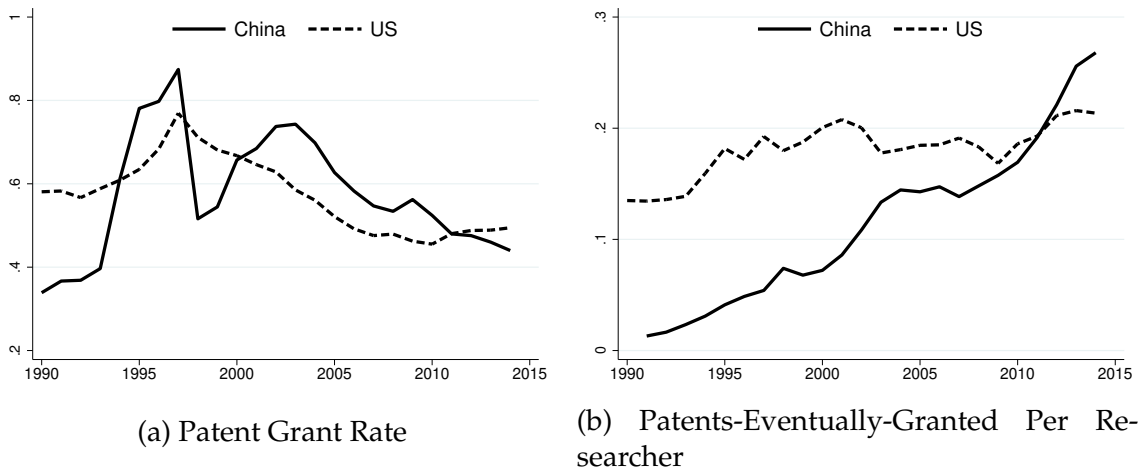
Note: Row (1) shows full-time equivalent researchers per million Inhabitants in 2013, and row (2) the share of Ph.D. degree holders in the labor force. Data source: USESCO.ORG.

Figure A.2: No. of Patent Applications per Researcher in China, US, and G5



Note: X-axis: year. Data source for No. of patents is WIPO, and for No. of full-time equivalent researchers is from OECD.Stat. This figure shows the evolution of patent applications per researcher over time. G5 includes the US, the UK, France, Germany, and Canada. It does not contain Japan or Italy as data on No. of researchers for these two countries in the OECD.Stat database are under different definitions.

Figure A.3: Patent Grant Rate and Number of Patents-Eventually-Granted Per Researcher



Note: X-axis: year. This figure shows the patent grant rate, which is the fraction of applied patents in a given year that are eventually granted before Oct. 2020 (panel (a)), and patents-eventually-granted per researcher, which is the number of patent applications that are eventually granted per researcher (panel (b)). No. of patents that are eventually granted is calculated from patent-level data from *Innography* and *PatentsView* databases. To avoid the truncation issue, the figure only shows patents that were applied in or before 2014.

## A.2 Firm-Level Sample: Data Source, Construction, and Results

### A.2.1 Data Source

**Annual Survey of Industrial Enterprises (ASIE).** Annual Survey of Industrial Enterprises (ASIE), conducted by the National Bureau of Statistics of China (NBS), contains financial information for all state-owned enterprises, and private firms with sales above 5 million RMB before 2011 and 20 million RMB since 2011 in the industrial sector (also referred to as the “above scale” industrial firms) for the periods 1998-2013.

**Innography.** Innography Patent Database covers information on over one hundred million patents from various countries. In this paper, we restrict attention to patents that are applied and eventually granted in China. If a patent is filed in China in year  $t$  and eventually granted in year  $t + 1$ , it consists of our sample of newly applied Chinese patents in year  $t$ . We supplement the Innography database with patent data from Orbis Intellectual Property.

**Firm Innovation Activity Database.** Firm Innovation Activity Database contains information on innovation costs and R&D expenditures, and tax cuts from the Recognition of High-Tech Enterprises, for all industrial firms that have innovation activities for the 2008-2013 period. There are in total 394,381 observations within the seven-year time period, covering approximately 120,000 unique firms.

### A.2.2 Sample Construction

To construct the firm-level sample, we merge different data sources to ASIE manufacturing firms. The sample construction process consists of the following three major steps.

**Step 1: Construct the 1998-2013 ASIE Sample.** We follow [Brandt et al. \(2012\)](#) to create an unbalanced panel of firms between 1998 and 2013. We restrict the ASIE sample to the

manufacturing industries, that all 4-digit CIC codes between 1300 and 4400. We drop all firms with missing firm identification numbers, province, industry, age, or employment, and drop those with negative values of age or revenue. The final ASIE sample, consisting of 4,037,866 firm-level observations, is the foundation of our firm-level sample.

**Step 2: Attach Patent Information to the ASIE Sample.** We merge the patent-level Innography Database to the ASIE sample by using information on institutional applicants of patents. Table A.3 presents the number of patents for all and domestic firms. We restrict attention to domestic firms which are favored when Chinese governments give out subsidies (Haley and Haley, 2013).

Table A.3: Number of Patents in the Sample

Year	All firms				Domestic firms		
	Application	Grant	G/A	Firm No.	Grant	% in all	Firm No.
1998	687	412	59.97%	238	364	88.35%	217
1999	1,144	737	64.42%	316	623	84.53%	281
2000	1,831	1225	66.90%	449	1,068	87.18%	408
2001	3,011	2,169	72.04%	610	1,750	80.68%	549
2002	6,272	4,564	72.77%	963	3,066	67.18%	848
2003	9,916	6,360	64.14%	1,357	4,536	71.32%	1,189
2004	14,087	8,343	59.22%	1,799	5,901	70.73%	1,541
2005	19,751	12,124	61.38%	2,291	8,849	72.99%	1,930
2006	28,801	17,274	59.98%	3,192	12,672	73.36%	2,594
2007	37,106	22,122	59.62%	4,068	15,864	71.71%	3,238
2008	46,201	26,871	58.16%	6,071	19,533	72.69%	4,976
2009	53,886	31,431	58.33%	7,303	22,829	72.63%	5,940
2010	72,905	40,133	55.05%	10,422	29,689	73.98%	8,496
2011	98,555	52,366	53.13%	12,266	39,853	76.10%	10,020
2012	136,026	71,726	52.73%	15,565	55,273	77.06%	12,804
2013	165,874	87,304	52.64%	18,790	69,733	79.87%	15,785

Note: The “Grant” column denotes the number of patents that are applied and eventually granted. “% in all” for domestic firms is the fraction of grant patents by domestic firms in all firms.

**Step 3: Attach the Firm Innovation Activities Database to the ASIE Sample.** For calibration purposes, we further merge a supplementary Firm Innovation Activity Database, available from 2008 to 2013, to the ASIE sample by using firms' organization codes and Chinese names.

### **A.2.3 Variable Construction**

**Types of Patents.** In the benchmark, we label a Chinese patent as radical if (1) it has been cited by at least one US patent, and (2) the gap of the application year between the cited and citing patent lies within 5 years. Incremental patents are those that are not radical.

**Types of Firms.** Firms are classified into two types: high- and low-type firms. High-type firms are those with at least one radical patent from 2008-2013; otherwise, firms are labeled as low-type.

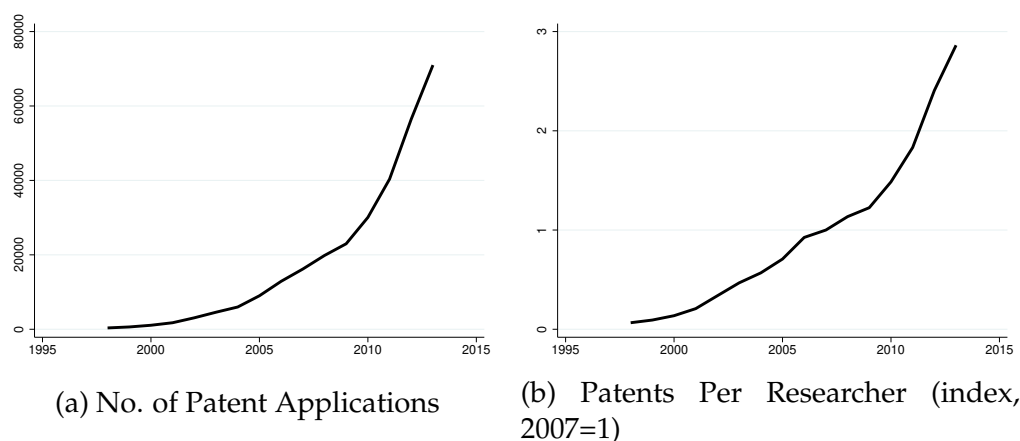
**SOE and Foreign Firms.** A firm is a state-owned enterprise (*resp.* a foreign firm) if either (a) the controlling shareholder is the state (*resp.* foreign or from Hong Kong, Macau, and Taiwan), or (b) the share of state (*resp.* foreign capital and capital from Hong Kong, Macau, and Taiwan) in total capital is greater than 50%.

**Skill Composition.** We define the employment engaging in scientific activities (*keji huodong ren yuan*) as R&D personnel. Among all R&D personnel, we further categorize those with medium or high professional titles (*zhonggaoji zhicheng*) as skilled personnel. Skill intensity is then defined as the ratio of skilled personnel to total R&D personnel.

## A.2.4 Additional Tables and Figures

Figure A.4 shows the total number of patents and patents per researcher in our firm-level sample. Same as the aggregate trend shown in Figure 2.1, there appears a speedup in patents per researcher among ASIE firms since the late 2000s. Table A.4 shows the distribution in forward citation codes of Chinese patents. Overall, more than 90% of forward citations for Chinese patents come from other patents applied in China. US patents are the second largest source of citations for Chinese patents, accounting for 7.22% of total forward citations and much larger than the share for other areas.

Figure A.4: Patent Quantity For Industrial Firms



Note: X-axis: year. This figure shows the number of patents and patents per researcher (index, 2007=1) for ASIE firms. There is no information on the number of researchers for industrial firms before 2011. By assuming that the share of researchers in industrial firms in total researchers is constant, we divide the number of ASIE patents by the number of national researchers, normalize such that the value in 2008 is 1, and present the results in the right panel.

Table A.4: Distribution of Forward Citations for Chinese Patents

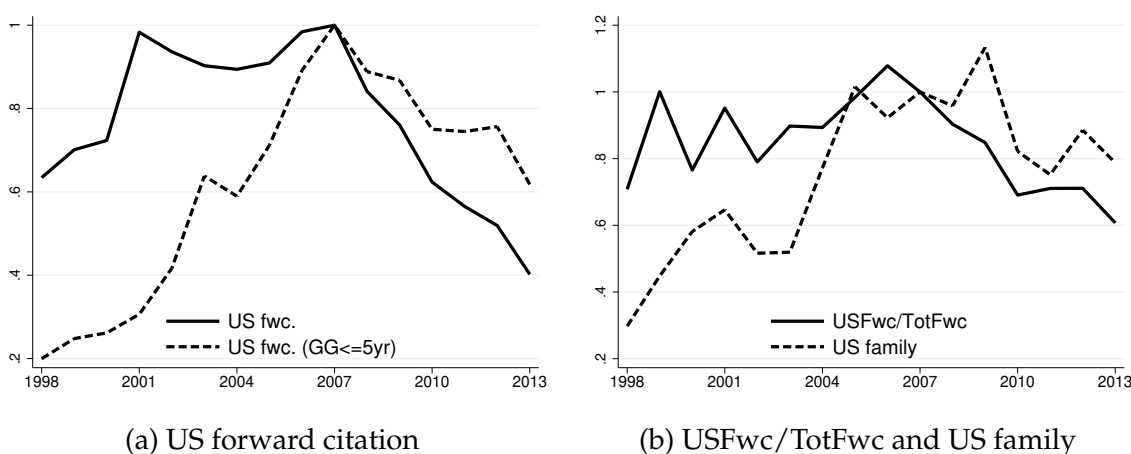
Code	CN	US	TW	JP	EP	KR	GB	DE	AU	FR
Fraction, %	90.73	7.22	0.73	0.44	0.32	0.17	0.07	0.03	0.03	0.03

Data source: Innography and Orbis Intellectual Property

## A.2.5 Robustness Check on Patent Quality Decline

**Aggregate Trend: Alternative Definitions.** Figure A.5 presents the trend of the share of radical patents under four alternative definitions: (a) radical patents are those with at least one forward citation from a US patent; (b) the condition in (a) plus that the gap between grant years of the cited and citing patents are within 5 years; (c), the ratio of No. of US forward citations and No. of all forward citations; (d) radical patents are defined as those with a US patent as its family member. Definition (a) might suffer from truncation bias, while (b)-(d) do not. Though the magnitude varies across different definitions, there displays a rise-then-decline trend in all four series.

Figure A.5: Share of Radical Patents (Index, 2007=1) under Alternative Definitions



Note: X-axis: year, Y-axis: index, 2007=1. For 'US fwc.', a patent is defined as radical if it is even being cited by a US patent; For 'US fwc. (GG<=5)', a patent is defined as radical if it is ever being cited by a US patent, and the gap in grant year between the cited and citing patent is within 5 years; For 'US family', a patent is defined as radical if it has one US patent as its simple family member; 'USFwc/TotFwc' denotes the fraction of US forward citations in total forward citations.

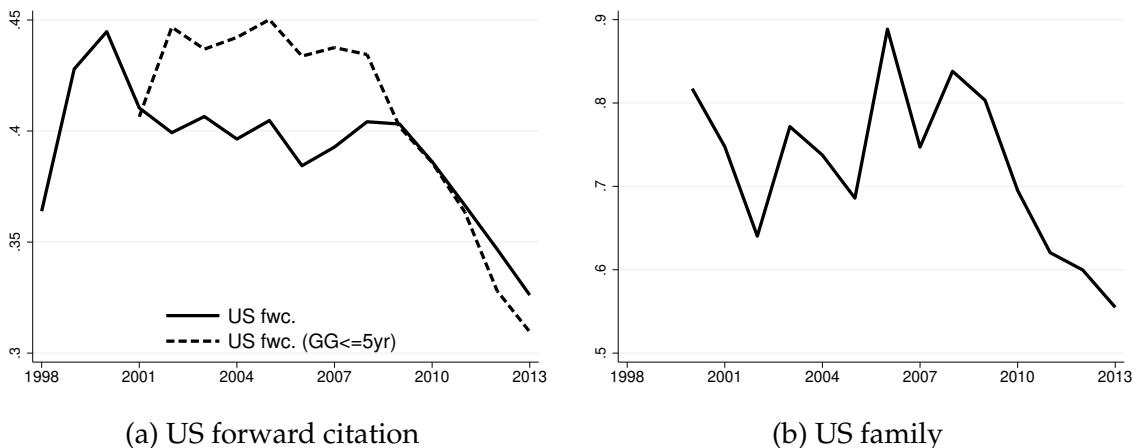
Figure A.6 presents the trend of the relative quality of incremental to radical patents under definitions (a), (b), and (d),<sup>1</sup> all showing a similar flat-then-decline pattern. In Table A.5, we further restrict to incremental patents and regress the log of forward citations received at the patent level on IPC class-level incremental patent stocks, controlling for IPC class-level radical patent stocks, IPC class, and year fixed effects. The results indicate a

<sup>1</sup>Under definition (c), one cannot properly label whether a patent is radical or incremental.



significantly negative impact of incremental patent stock on incremental patents' quality.

Figure A.6: Relative Quality of Incremental to Radical Patents



Note: X-axis: year. See note of Figure A.5 for more details.

Table A.5: Patent-Level Log Number of Forward Citations Received

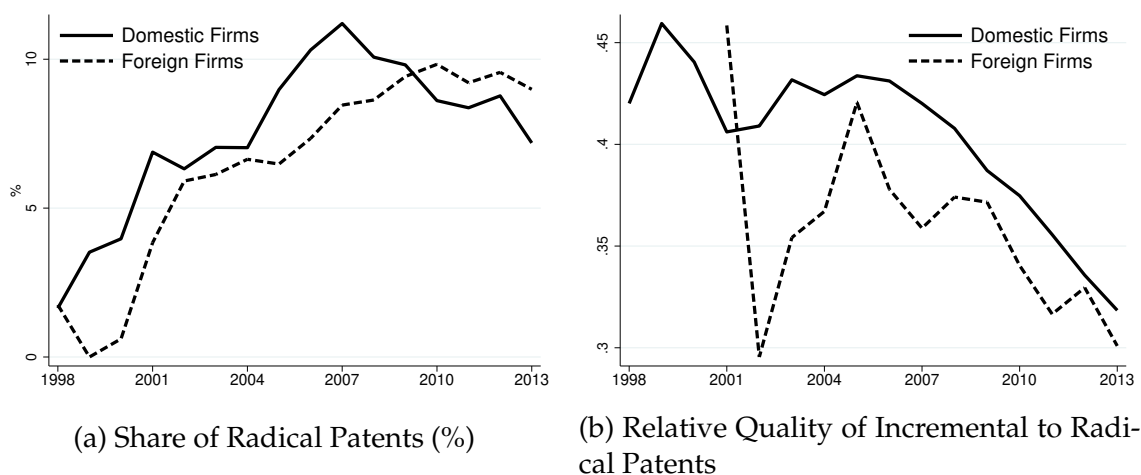
	(1)	(2)	(3)
IPC class-level log incremental patent stock	-0.216*** (-5.14)	-0.146*** (-4.19)	-0.294*** (-6.64)
IPC class-level log radical patent stock	Yes	Yes	Yes
Year FE	Yes	Yes	Yes
Patent Class FE	Yes	Yes	Yes
$R^2$	0.065	0.069	0.064
Observations	297552	300076	272864

Note:  $t$  statistics in parentheses; \*  $p < 0.10$ , \*\*  $p < 0.05$ , \*\*\*  $p < 0.01$ . This table shows results regressing the log of forward citations received at the patent level, of incremental patents, on IPC class-level incremental patent stocks, with IPC class-level radical patent stocks, IPC class, and year fixed effects controlled. Columns [1], [2], and [3] define incremental patents as without US citations within a five-application-year window, without US family applications, and without US citations, respectively. Robust standard errors clustered at the patent class level.

Next, we stick to the baseline definition, i.e., radical patents are cited by at least one US patent, and the gap between the application years of the cited and citing patent is within 5 years, and confirm the robustness of the aggregate trend at more disaggregated levels.

**Domestic versus Foreign.** Figure A.7 presents the two measures of patent quality for domestic and foreign firms. For radical patent shares (in panel (a)), both firms experience a rising trend in the late 1990s and early-to-middle 2000s. For the post-2008 period, while there is a clear decline for domestic firms, the trend for foreign firms is less visible. That the decline is more significant among domestic firms is consistent with existing research pointing out that China favors indigenous firms when giving out subsidies (Haley and Haley, 2013). As shown in panel (b), the decline in the relative quality of incremental to radical patents is also more significant for domestic firms.

Figure A.7: Evolution of Patent Quality for Domestic and Foreign Firms



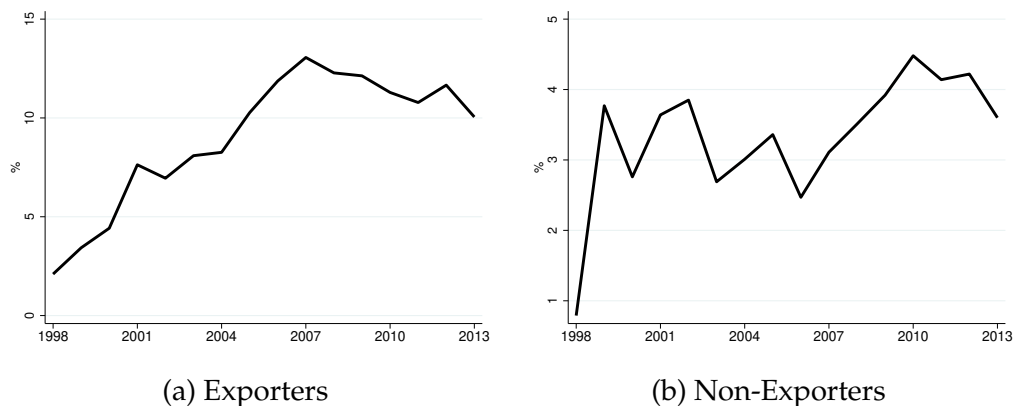
Note: X-axis: year. A firm is defined as foreign when the share of registered capital held by foreigners is no less than 50% or when foreigners is the controlling shareholder, and defined as domestic otherwise.

**Exporters versus Non-Exporters.** A firm is defined as an exporter if it ever exports from 1998 to 2013.<sup>2</sup> Defined this way, exporters account for 65.59% of all patents. Figure A.8 presents the share of radical patents for exporters and non-exporters. The radical patent share for exporters is greater than for non-exporters, which is not surprising since exporters are typically larger in size and more intensive in R&D. The trend for exporters is quite similar to the aggregate one. For non-exporters, the radical patent share does not

<sup>2</sup>We also tried to define exporters as firms that have an export-revenue ratio exceeding 50% in at least 1 year from 1998 to 2013. The results are qualitatively similar to patterns shown in the text.

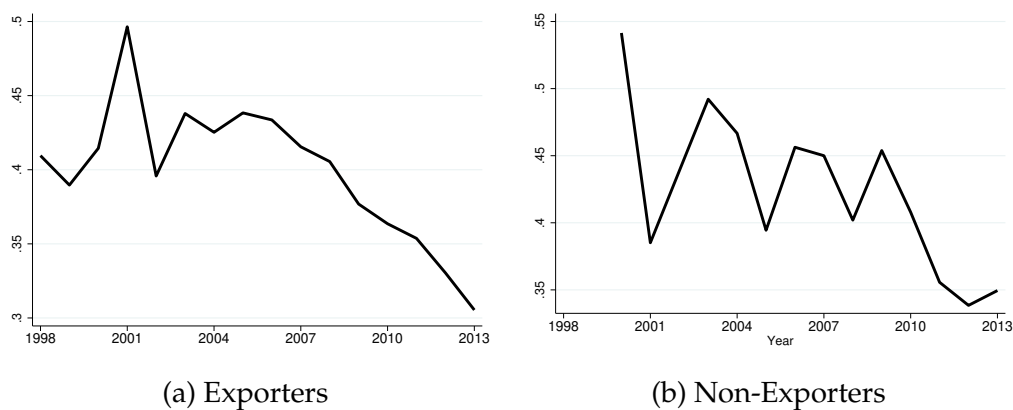
show a clear pre-2008 trend, suggesting a much smaller learning effect for this group. The post-2008 decline for non-exporters is also less significant, though there is a visible decline since the year 2010. Figure A.9 shows the relative quality of incremental to radical patents. Again, the post-2008 decline in relative quality is mainly driven by exporters.

Figure A.8: Share of Radical Patents for Exporters and Non-Exporters



Note: X-axis: year. A firm is defined as an exporter if it ever exports from 1998 to 2013.

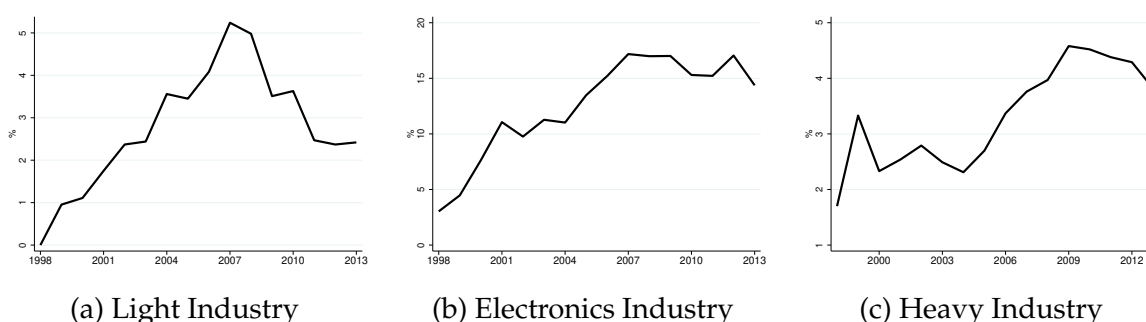
Figure A.9: Relative Quality of Incremental to Radical Patents for Exporters and Non-Exporters



Note: X-axis: year. See note of Figure A.8 for more details.

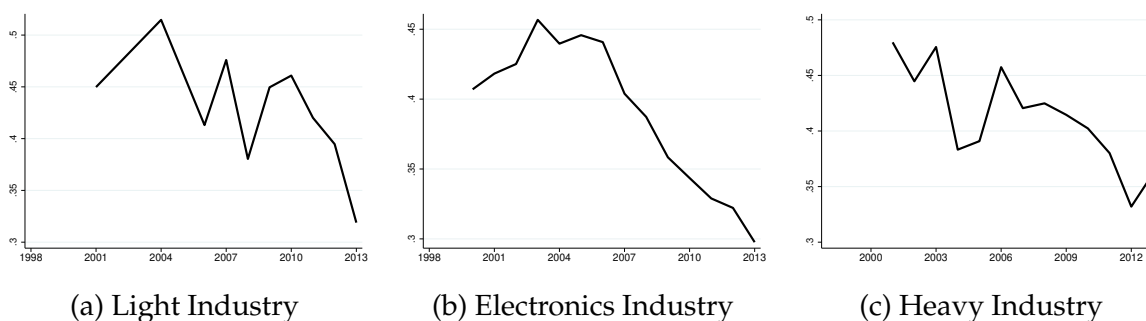
**Industry Heterogeneity.** Figure A.10 presents the radical patent share for the light, electronics, and heavy industries. There is a clear rise-then-decline pattern for the light and heavy industries. Radical patent share for electronics is roughly stable or shows a mild decline in the post-2008 period. It, however, displays a clear decline compared to the pre-2008 trend. In Figure A.11, we confirm that the relative quality of incremental to radical patents is relatively stable before the mid-to-late 2000s and declines thereafter in all three industries.

Figure A.10: Share of Radical Patents of Different Industries



Note: X-axis: year. This figure shows the radical patent share of the light, electronics, and heavy industries.

Figure A.11: Relative Quality of Incremental to Radical Patents of Different Industries



Note: X-axis: year. This figure shows the relative quality of incremental to radical patents of the light, electronics, and heavy industries.

**Different Patent Categories.** Table A.6 shows patent numbers and shares for eight 1-digit IPC section symbols, which we refer to as “categories”. There are eight categories, with symbols ranging from A to H. Category A refers to “Human Necessities”; Category B refers to “Performing Operation, Transporting”; Category C refers to “Chemistry, Metallurgy”; Category D refers to “Textiles, Paper”; Category E refers to “Fixed Constructions”; Category F refers to “Mechanical Engineering, Lighting, Heating, Weapons, Blasting”; Category G refers to “Physics”; Category H refers to “Electricity”. The largest categories are H, C, and B, which account for 30.30%, 17.81%, and 17.20% of total patents created by industrial firms.

Table A.6: No. and Share of Patents for Different Categories, 2000-2013

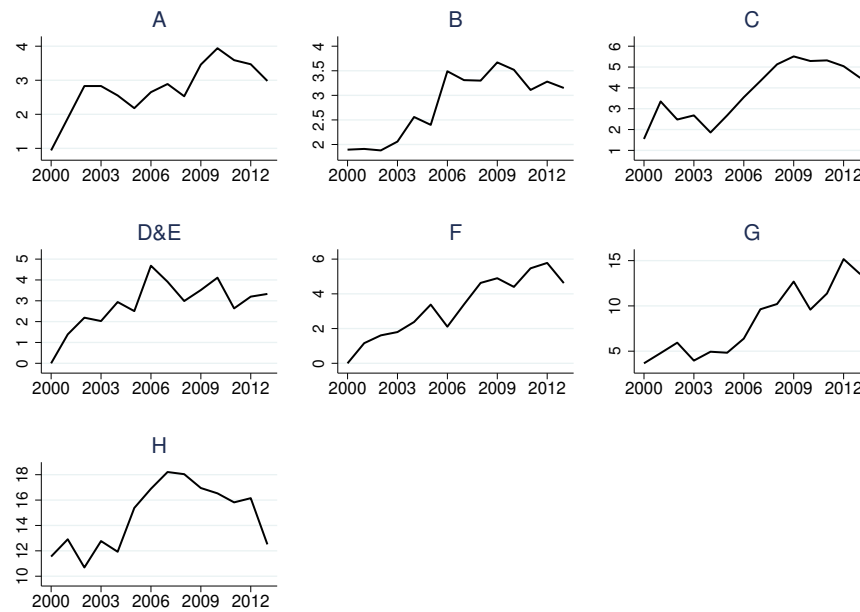
Category	A	B	C	D	E	F	G	H
No.	25,170	50,786	52,582	6,766	7,688	22,234	40,571	89,466
Share	8.52%	17.20%	17.81%	2.29%	2.60%	7.53%	13.74%	30.30%

Note: This table shows the number of patents and the share in total for each patent category (IPC Section Symbols). Category A refers to “Human Necessities”; Category B refers to “Performing Operation, Transporting”; Category C refers to “Chemistry, Metallurgy”; Category D refers to “Textiles, Paper”; Category E refers to “Fixed Constructions”; Category F refers to “Mechanical Engineering, Lighting, Heating, Weapons, Blasting”; Category G refers to “Physics”; Category H refers to “Electricity”.

Figure A.12 shows the radical patent share for 7 patent categories (i.e., 1-digit IPC Section Symbols) from 2000-2013.<sup>3</sup> As the number of patents in categories D and E is significantly less than others, containing 6-7 thousand patents in total and less than 500 patents in most of the sample years, we merge those two categories as a single one. For categories A, B, C, D&E, H, or 5 out of the 7 categories, there is a decline in the post-2008 period especially compared to the pre-2008 trend. Together, patents from these five categories account for over 80% of the total patents. As for the relative quality of incremental to radical patents, the flat-then-decline pattern exists for almost all patent classes, as shown in Figure A.13.

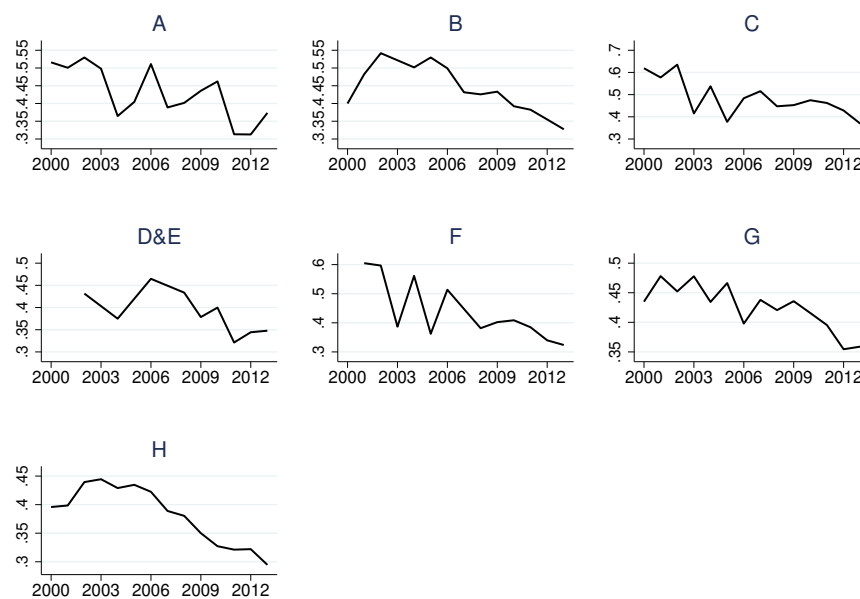
<sup>3</sup>We start from 2000 as there are less than 100 patents for most patent categories in 1998 and 1999. In rare cases that the quality measure for a category in year  $t$  is significantly different from year  $t - 1$  and  $t + 1$ , we interpolate to obtain the value in year  $t$ .

Figure A.12: Radical Patent Share for Different Categories



Note: X-axis: year. Unit for Y-axis: %. This figure shows the trend of radical patent share for different patent categories (IPC Section Symbols). See note of Table A.6 for detailed meanings of each patent category.

Figure A.13: Relative Quality of Incremental to Radical Patents for Different Categories



Note: X-axis: year. This figure shows the trend of the relative quality of incremental to radical patents for different patent categories (IPC Section Symbols). See note of Table A.6 for detailed meanings of each patent category.

**Entrants versus Incumbents.** A firm is defined as an entrant in year  $t$  if its first (eventually-granted) patent is applied in year  $t$ , and as an incumbent otherwise. Table A.7 shows the number and share of patents owned by incumbents and entrants from 1998 to 2013. By definition, entrants' patent share equals 100% in 1998. Overall, the share of patents accounted for by entrants does not show a rising trend over the post-2008 period. This result, however, should be interpreted under the caveat that the data we use is for above-scale industrial firms and it does not contain very small firms.

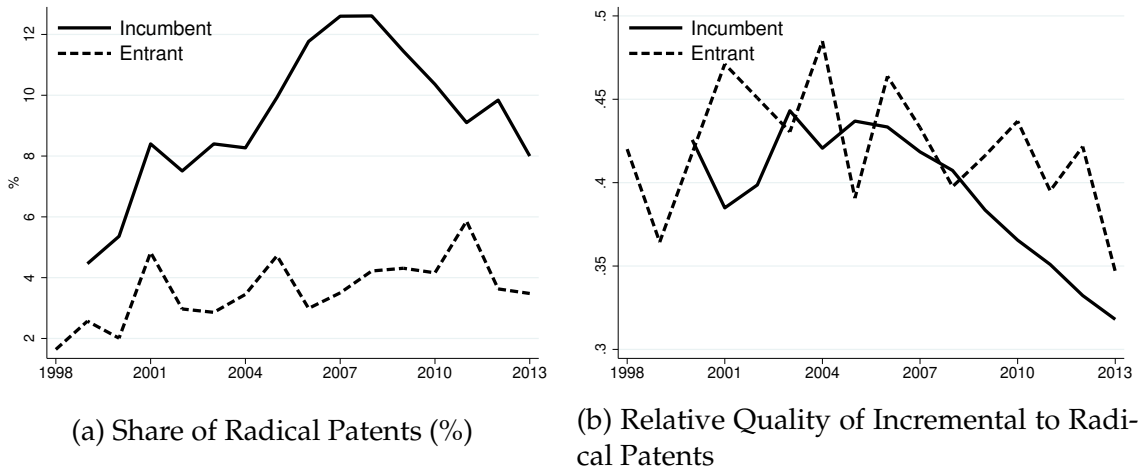
Table A.7: No. and Share of Patents by Entrants

Year	1998	2001	2004	2007	2009	2010	2011	2012	2013
No.	365	746	1,538	2,483	5,286	8,477	9,059	9,712	12,604
Share	100.00%	42.43%	25.69%	15.34%	23.00%	28.20%	22.45%	17.20%	17.75%

Note: A firm is defined as entrant in year  $t$  if its first (eventually-granted) patent is applied in year  $t$ .

Figure A.14 shows the trend of patent quality for incumbent firms and entrants. As seen in panel (a), the rise-then-decline pattern in radical patent share is predominantly driven by incumbents. For entrants, we actually find a flat or slightly rising trend from 1998-2013. Confining to the later 2008-2013 period, there is no clear decline for entrants. If we take away the jump in 2011, there is a moderate decline for entrants, but with a magnitude much smaller than that of incumbents. In panel (b), the flat-then-decline trend in the relative quality of incremental to radical patents is also predominantly driven by incumbents. No clear trend can be discerned for entrants.

Figure A.14: Evolution of Patent Quality for Incumbent Firms and Entrants



Note: X-axis: year. A firm is defined as an entrant in year  $t$  if its first (eventually-granted) patent is applied in year  $t$ .

**Regressions With versus Without Firm Fixed Effects.** To examine more closely the post-2008 decline in radical patent share, we run a patent-level regression of the radical patent dummy against year (a trend variable) with [column (a)] and without [column (b)] fixed effects. Table A.8 shows the results. The ratio between the coefficient in column (b) and that in column (a) is informative on how much the aggregate decline is explained by the within-firm component. The ratio is 74% for the 2010-2013 period, implying that the post-2009 decline mainly occurs within firms.

Table A.8: Patent-Level Regression with and without Firm Fixed Effects

Period	2010-2013	
	(a)	(b)
Year	-0.0047*** (0.0006)	-0.0035*** (0.0007)
Firm FE	N	Y
Obs.	197,885	186,101

Note: This table shows regression results in which the dependent variable is the radical patent dummy and the main independent variable is the year trend. Note that firms that appear only once in the sample are automatically dropped in the regression with firm fixed effects.



We also try to use the full sample data from 1998-2013 and regress the radical patent dummy against year dummies with and without firm fixed effects. Then using coefficients for the year dummies, we estimate a pre-2008 trend and compare the relative deviation of the actual coefficients in the post-2008 period from the predicted values extrapolated from the pre-2008 trend. The average deviation from 2011-2013 is 1.07 in the case without firm fixed effects, and 0.71 in the case with firm fixed effects. The latter accounts for 66% of the former, which is consistent with the results in Table A.8.

For decline in the radical patent share that is not “within-firm”, one component is the increase in the patent share of low-type firms. By definition, the radical patent share for low-type firms is always zero, so there can be no within-firm decline for these firms. On the other hand, creating more incremental patents by a high-type firm not only reduces the radical patent share within the firm, but also increases its patent share among all firms, therefore simultaneously leading to a within-firm and cross-firm effect, a property featured in the data and captured by our model.

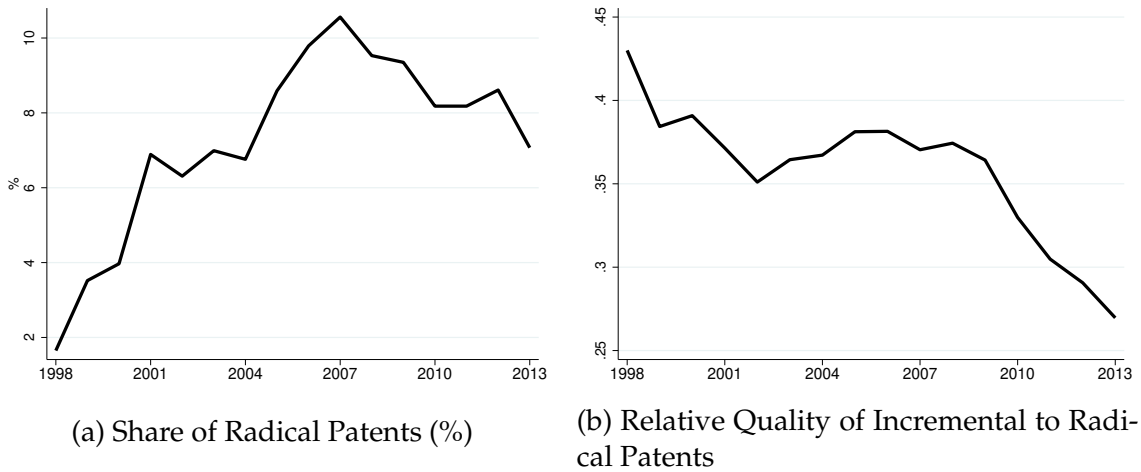
**Internal versus External Patents.** All (eventually granted) patents are used in the baseline. We follow Akcigit and Kerr (2018) to divide all patents into internal versus external ones based on backward citations. Specifically, we define the self-citation rate as the fraction of *self-citation* in its total backward citations, with *self-citation* of a patent applied by firm  $i$  in year  $t$  containing all backward citations that are applied between 1998 and year  $t$  by firm  $i$ . Patents with a self-citation rate greater than 50% are defined as internal patents. External patents are those that are not internal. Patents without backward citations are regarded as external patents. As shown in Table A.9, the vast majority of Chinese patents are external under the definition above. It is not surprising that both the radical patent share and the relative quality of incremental to radical patents among external patents are quite similar to that for all patents, as seen in Figure A.15.

Table A.9: No. and Share of External Patents for Domestic Industrial Firms

Period	No. of external patents	No. of patents	Share of external patents
1998-2013	279,800	296,254	94.45%
2011-2013	159,490	167,823	95.03%

Note: External patents are defined as those with a self-citation rate no greater than 50%.

Figure A.15: Evolution of Patent Quality among External Patents



Note: X-axis: year. External patents are defined as those with a self-citation rate no greater than 50%.

## A.2.6 Skill Intensity for High- and Low-Type Firms

Table A.10 shows the average skill intensity for high- and low-type firms. It is clear that high-type firms are more skill-intensive.

Table A.10: Skill Intensity for Firms of Different Types

	2011	2012	2013	Average
Skill intensity of high-type firms	34.91%	34.53%	33.02%	34.12%
Skill intensity of low-type firms	26.83%	25.19%	24.69%	25.42%

Note: Skill intensity is defined as the fraction of R&D personnel with a medium or senior professional title. To clear the effects of age and size, we first run a firm-level regression of skill intensity against age and log(employment) and then use the residual to obtain the numbers above.

## B Appendix: Model Derivations and Proofs

### B.1 Education

With the presence of education subsidy  $b_e$  and skilled labor subsidy  $b_h$ , young people choose to invest in education and become skilled if and only if

$$\frac{e^{-(r-g+d)}}{r-g+d} \frac{w^h}{1-b_h} - (1-b_e) \frac{1-e^{-(r-g+d)}}{r-g+d} \frac{1}{\theta \bar{\xi}} \frac{w^h}{1-b_h} \geq \frac{w^\ell}{r-g+d},$$

that is, obtaining education if and only if her type is above the threshold

$$\theta^* \equiv \max \left\{ \frac{1-b_e}{\bar{\xi}} \left[ 1 - e^{-(r-g+d)} \right] \left( e^{-(r-g+d)} - (1-b_h) \frac{w^\ell}{w^h} \right)^{-1}, 1 \right\}.$$

We can further derive the mass of the four types of people in the economy: students, skilled workers employed in education, skilled workers employed in the R&D sector, and unskilled workers

$$h^{\text{student}} = \theta^{*-2} (1 - e^{-d}) L;$$

$$h^{\text{teacher}} = \frac{2\theta^{*-3}}{3\bar{\xi}} (1 - e^{-d}) L;$$

$$h^{\text{R\&D}} = \theta^{*-2} e^{-d} L - h^{\text{teacher}};$$

$$\ell^{\text{supply}} = (1 - \theta^{*-2}) L.$$

## B.2 Step-Size and Firm Size Distribution

Start with the step-size distribution of incremental innovations. Denote  $D_\tau$  the fraction of product lines of distance  $\tau$ , with  $\tau = 1$  representing a product line where the latest innovation is radical. Under an invariant distribution,

STATE:	INFLOW	OUTFLOW
$\tau = 1:$	$(1 - D_1)\delta_d$	$= D_1\delta_m$
$\tau \geq 2:$	$D_{\tau-1}\delta_m$	$= D_\tau(\delta_d + \delta_m)$

where  $\delta_d$  and  $\delta_m$  are aggregate creative destruction from radical and incremental innovations, respectively. Denote  $\delta$  the aggregate creative destruction rate, that is,  $\delta \equiv \delta_d + \delta_m$ . Under the invariant distribution, inflow equals outflow for each  $\tau \geq 1$ . It follows that,

$$D_\tau = \frac{\delta_d}{\delta} \left( \frac{\delta_m}{\delta} \right)^{\tau-1}, \quad \tau = 1, 2, \dots$$

From this distribution, we can calculate the expected step-size of an incremental innovation as

$$\bar{\eta} = \sum_{\tau=1}^{\infty} D_\tau \eta \alpha^{\tau-1} = \eta / \left( \alpha + \frac{1-\alpha}{\delta_d/\delta} \right).$$

For the firm size distribution, denote  $p_H = p^*$ ,  $p_L = 1 - p^*$ ,  $x_H = x_{Hd} + x_{Hm}$  and  $x_L = x_{Lm}$ . Then for firms of type  $j$ , stationarity implies that

STATE:	INFLOW	OUTFLOW
$n = 0:$	$\mu_{j,1} \times \delta$	$= p_j \times x_E$
$n = 1:$	$p_j \times x_E + \mu_{j,2} \times 2\delta$	$= \mu_{j,1} \times (x_j + \delta)$
$n \geq 2:$	$\mu_{j,n-1} \times (n-1)x_j + \mu_{j,n+1} \times (n+1)\delta$	$= \mu_{j,n} \times n(x_j + \delta)$

For  $n = 0$ , the inflow occurs when firms with only 1 product line are destroyed, and the outflow is the successful innovations by entrants. For  $n = 1$ , the inflow contains firms originally with 2 product lines losing 1 line and the entrants who successfully add 1 line; while the outflow consists of 1-line firms that innovate and obtain additional lines or lose existing lines due to creative destruction. A similar interpretation applies for  $n \geq 2$ . From these expressions, we have

$$\mu_{j,n} = \frac{p_j x_E}{\delta} \left( \frac{x_j}{\delta} \right)^{n-1} \frac{1}{n},$$

and

$$\sum_{n=1}^{\infty} \mu_{j,n} \times n = \frac{p_j x_E}{\delta - x_j}.$$

### B.3 Proof of Proposition 1

For a more general theoretical property, let's assume that there are  $J \geq 2$  many types of firms in the economy. And define  $\text{Line}_j \equiv \sum_n \mu_{j,n} \times n$ , that is, the total number of product lines owned by type  $j$  firms.

As shown in B.2, stationarity requires that  $\forall j \in \{1, 2, \dots, J\}$ ,

$$\text{Line}_j = \frac{p_j x_E}{\delta - x_j}.$$

We plug in the definition of  $\delta$  and get

$$\text{Line}_j = \frac{p_j x_E}{\sum_{j'} \text{Line}_{j'} x_{j'} + x_E - x_j} \quad (\text{eqn-[j]})$$

with the requirement of

$$\sum_j \text{Line}_j = 1. \quad (\text{eqn-[x]})$$

This is a system of  $J$  unknowns  $\{\text{Line}_j\}_{j=1}^J$ , and  $J + 1$  equations.

Seemingly, we need an extra free variable such that it is a system of  $J + 1$  unknowns and  $J + 1$  equations. However, we are going to prove that, for any given combinations of  $x_E > 0$ ,  $\{p_j\}_{j=1}^J \in (0, 1)$  and  $\{x_j\}_{j=1}^J > 0$ , there always exists a  $\{\text{Line}_j\}_{j=1}^J$  such that the above  $J + 1$  equations hold. The remaining is to show that, when eqn-[1] to eqn-[J-1] hold and eqn-[x] is satisfied, the last equation, eqn-[J], shall hold automatically.

Eqn-[j] indicates that

$$(p_j - \text{Line}_j)x_E = \text{Line}_j \left( \sum_{j'} \text{Line}_{j'} x_{j'} - x_j \right),$$

sum them up from  $j = 1$  to  $J - 1$ . Then use the fact  $p_J = 1 - \sum_{j=1}^{J-1} p_j$ , together with eqn-[x],

$\text{Line}_J = 1 - \sum_{j=1}^{J-1} \text{Line}_j$ , we have

$$(\text{Line}_J - p_J)x_E = (1 - \text{Line}_J) \left( \sum_{j'} \text{Line}_{j'} x_{j'} \right) - \sum_{j=1}^{J-1} \text{Line}_j x_j.$$

For the R.H.S., we rearrange terms and get

$$(\text{Line}_J - p_J)x_E = (1 - \text{Line}_J)\text{Line}_J x_J - \text{Line}_J \sum_{j=1}^{J-1} \text{Line}_j x_j,$$

which is exactly the same as eqn-[J]

$$(p_J - \text{Line}_J)x_E = \text{Line}_J \left( \sum_{j=1}^J \text{Line}_j x_j - x_J \right).$$

## B.4 Value Functions and Proof of Proposition 2

As discussed in the main text, we focus on high-type firms which face a trade-off between radical and incremental innovations. Again, for expositional convenience, we drop the firm type subscript  $j$ . Guess that the value function takes the following form

$$V(Q, \bar{q}) = \sum_{\omega} Aq_{\omega} + nB\bar{q}.$$

Substituting this conjectured form into the Bellman equation, we have

$$\begin{aligned} r \left( \sum_{\omega} Aq_{\omega} + nB\bar{q} \right) - gnB\bar{q} = & \max_{x_d, x_m} \sum_{\omega} [\pi q_{\omega} - \delta(Aq_{\omega} + B\bar{q})] + nx_d[A(1 + \lambda) + B]\bar{q} \\ & + nx_m[A(1 + \bar{\eta}) + B]\bar{q} - nR(x_d, x_m; z_d, z_m) + nb_n\bar{q}. \end{aligned}$$

It follows that coefficients  $A$  and  $B$  satisfy the following conditions

$$\begin{aligned} A &= \frac{\pi}{r + \delta}; \\ (r - g + \delta)B &= \max_{x_d, x_m} x_d[A(1 + \lambda) + B] + x_m[A(1 + \bar{\eta}) + B] - \hat{R}(x_d, x_m) + b_n, \end{aligned}$$

where  $\hat{R} \equiv R/\bar{q}$  is the detrended R&D cost per line. One can see that  $B$  is increasing in  $b_n$ . With the value function's form, equation (10) in Proposition 2 follows immediately from the first-order conditions with respect to  $x_d$  and  $x_m$ .

If the quantity-based subsidy is posted on the number of new patents instead of the stock, i.e.,  $nx \times b_x \bar{q}$ , the value function and the relation between subsidy and  $B$  remain unaltered. The only difference is that “innovation return” now becomes

$$\frac{A(1 + \lambda) + B + b_x}{A(1 + \bar{\eta}) + B + b_x}.$$

## C Appendix: Calibration

### C.1 External Parameters

Table C.1 summarizes the values of all externally calibrated parameters and their sources.

Table C.1: Externally Calibrated Parameters

Para	Value	Equation	Meaning	Source
$\rho$	0.02	(1)	time discount rate	literature
$\nu$	3	(1)	intertemporal elasticity of substitution	literature
$\epsilon$	0.22	(2)	E.o.S. in final good production	profitability
$L$	1		total population	normalization
$\phi$	0.49	(3)	innovation elasticity w.r.t. R&D	external estimation
$\eta$	$\alpha\lambda$	(5)	initial step-size of incremental inno.	assumption
$d$	0.03		death rate of the population	years of working
$u$	25%		corporate tax rate	documentations
$b_r$	150%		R&D tax credit multiplier	documentations

### C.2 Connect Innovation Step-Size to Patents' Number of Forward Citations

In this section, we follow [Akcigit and Kerr \(2018\)](#) and show the map between innovation step-size in the model and the number of forward citations in the patent data. Assume that radical and incremental innovations ( $s = \lambda, \eta\alpha^{\tau-1}$ ) obtain a citation from each subsequent patent with probability  $s\kappa$ . A radical innovation starts a new technology cluster, which future citations build on, and renders older technology clusters obsolete. Denote  $m(\omega, t)$  the number of citable patents in product line  $\omega$ , and  $M(t) = \int_0^1 m(\omega, t)d\omega$  total citable patents in period  $t$ . As  $m(\omega, t)$  satisfies

$$m(\omega, t + \Delta t) = [m(t) + 1]\delta_m\Delta t + 1 * \delta_d\Delta t + (1 - \delta_m\Delta t - \delta_d\Delta t)m(t),$$

The law of motion for  $M(t)$  is



$$M(\omega, t + \Delta t) = [M(t) + 1]\delta_m \Delta t + 1 * \delta_d \Delta t + (1 - \delta_m \Delta t - \delta_d \Delta t)M(t).$$

Imposing  $M(\omega, t + \Delta t) = M(\omega, t)$  in steady state, we have  $M = \frac{\delta}{\delta_d}$ . Denote  $\Phi_{\tau,n}$  the fraction of incremental patents with step-size  $s_\tau = \eta\alpha^{\tau-1}$  and  $n$  citations, among all patents. The inflow and outflow are

STATE:	INFLOW	OUTFLOW
$n = 0:$	$G_{\tau-1}\delta_m =$	$M\Phi_{\tau,0}\delta_d + M\Phi_{\tau,0}\eta\alpha^{\tau-1}\kappa\delta_m$
$n = 1:$	$M\Phi_{\tau,n-1}\eta\alpha^{\tau-1}\kappa\delta_m =$	$M\Phi_{\tau,n}\delta_d + M\Phi_{\tau,n}\eta\alpha^{\tau-1}\kappa\delta_m$

It follows that  $\Phi_{\tau,0} = \frac{G_{\tau-1}\delta_m}{M\delta_d + Ms_\tau\kappa\delta_m}$ , and  $\Phi_{\tau,n} = \Phi_{\tau,0}\left(\frac{s_\tau\kappa\delta_m}{\delta_d + s_\tau\kappa\delta_m}\right)^n$ . Note that at any point in time, the **number** of  $\tau - th$  incremental patents is  $G_\tau = M\frac{\delta_d}{\delta}\left(\frac{\delta_m}{\delta}\right)^\tau$ . Then at this point of time, the **fraction** of incremental patents that have citation  $n$ , among all incremental patents, is

$$\tilde{f}(n; \alpha, \eta\kappa) = \frac{\sum_{\tau=1}^{\infty} M\Phi_{\tau,n}}{\sum_{\tau=1}^{\infty} G_\tau} = \sum_{\tau=1}^{\infty} \frac{\delta_d}{\delta} \left(\frac{\delta_m}{\delta}\right)^{\tau-1} \frac{\delta}{\delta_d + s_\tau\kappa\delta_m} \left(\frac{s_\tau\kappa\delta_m}{\delta_d + s_\tau\kappa\delta_m}\right)^n$$

Matching this distribution with that from data produces an estimate for  $\alpha$  and  $\eta\kappa$ .

The average citation for  $\tau - th$  incremental patents is  $\sum_{n=0}^{\infty} \Phi_{\tau,n}n / \sum_{n=0}^{\infty} \Phi_{\tau,n} = s_\tau\kappa\delta_m / \delta$ . It follows that the average citation for all incremental patents is  $\bar{\eta}\kappa\delta_m / \delta$ .

Similarly, denote  $\Phi_{\lambda,n}$  the fraction of radical innovations with  $n$  citations. The associated inflow and outflow are

STATE:	INFLOW	OUTFLOW
$n = 0:$	$\delta_d$	$= M\Phi_{\lambda,0}\delta_m + M\Phi_{\lambda,0}\lambda\kappa\delta_m$
$n = 1:$	$M\Phi_{\lambda,n-1} [\lambda\kappa\delta_m + \psi\lambda\kappa\delta_d]$	$= M\Phi_{\lambda,n}\delta + M\Phi_{\lambda,n}\lambda\kappa\delta_m$

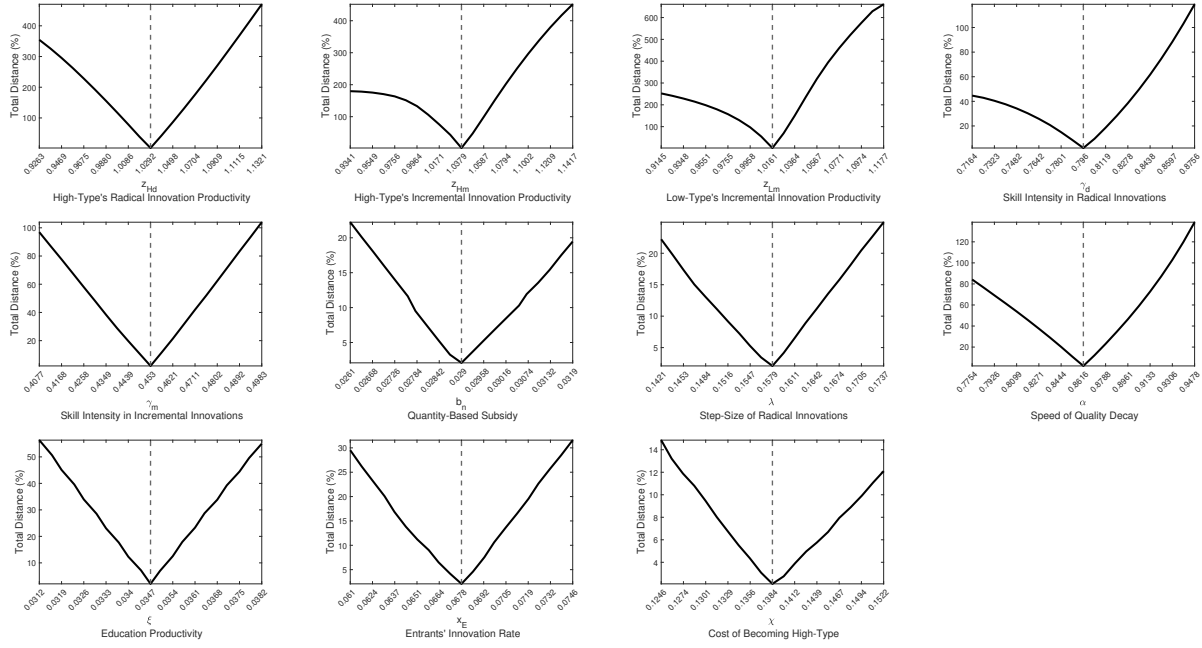
We then have that  $\Phi_{\lambda,0} = \frac{\delta_d}{M\delta_m + M\lambda\kappa\delta_m}$  and  $\Phi_{\lambda,n} = \left[ \frac{\lambda\kappa\delta_m}{\delta_m + \lambda\kappa\delta_m} \right]^n \Phi_{\lambda,0}$ . The average citation for radical innovations are  $\sum_{n=0}^{\infty} \Phi_{\lambda,n} n / \sum_{n=0}^{\infty} \Phi_{\lambda,n} = \frac{\lambda\kappa\delta_m}{\delta}$ . Therefore, we can use the ratio between average forward citations received by incremental and radical patents to infer the  $\bar{\eta}/\lambda$  ratio.

### C.3 Identification

To formally illustrate the identification of internally calibrated parameters, we conduct two exercises. First, we show how the total sum of distance changes as we move one parameter away from its benchmark value while keeping the others unchanged. Figure C.1 summarizes the results. One can check that the total distance is well V-shaped with respect to all parameters, with its minimum achieved at the benchmark value (dash line), which implies that the identification is clear.

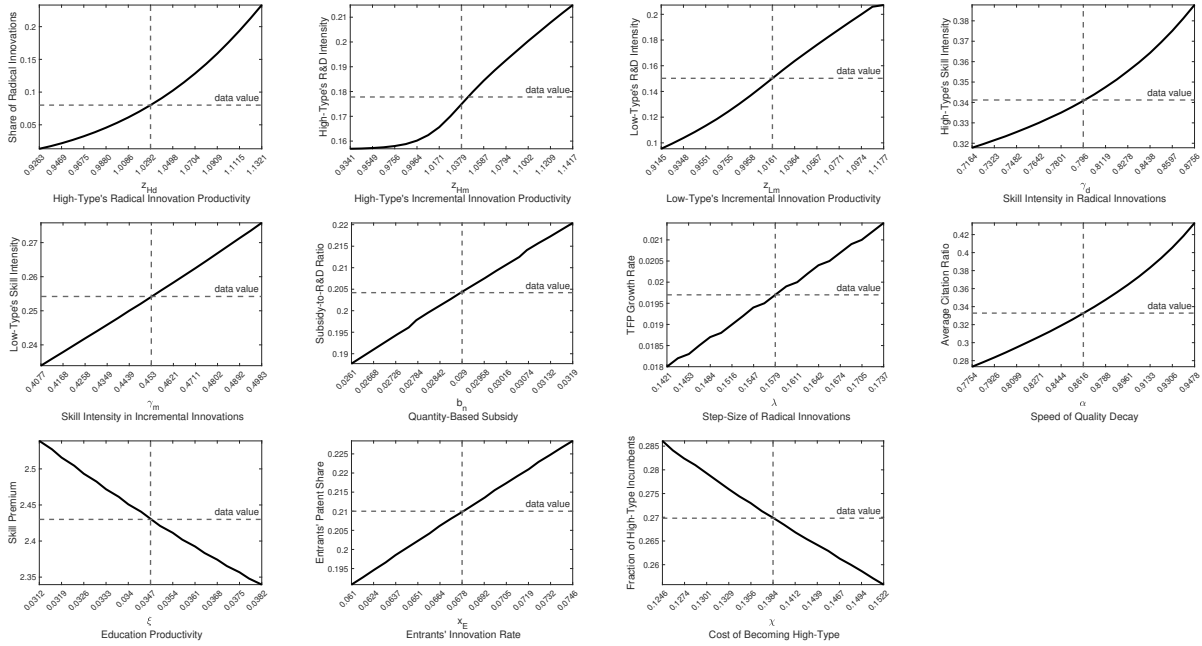
Second, in the main text, we picked a most informative moment for each of the parameters based on model implications, despite the fact that all 11 parameters are jointly identified. To support this argument, we check each of the 11 model-generated moments as a function of the corresponding parameter. Figure C.2 shows the results, the identification is clear as well.

Figure C.1: Total Distance w.r.t. Each Parameter



Note: This figure shows how the total sum of distance (Y-axis) changes as we move each of the 11 parameters (X-axis) away from its benchmark value, up and down by 10%, while keeping the others unchanged.

Figure C.2: Informative Moment w.r.t. Each Parameter



Note: This figure checks the sensitivity of each of the 11 model-generated moments (Y-axis) as a function of the corresponding parameter (X-axis). Again, each parameter is moved up and down by 10% from its benchmark value, while keeping the others unchanged.

## C.4 More on Model Fit: Patent Stock, Relative Firms Size and the Quantity-Quality Trade-off

**Active Patent Stock.** We construct the stock of active patents using patents' forward citation information. More specifically, we define the lifespan of a patent as the period from its application year to the last year it receives a forward citation. The idea here is essentially to regard an old patent as "inactive" or "dead" when it no longer contributes to society's knowledge creation.

For an eventually granted patent that was applied in year  $t_0$ , if the application year associated with its latest forward citation is  $t$ , then this patent is treated as "active" between year  $t_0$  and  $t$ . If a patent does not receive any forward citation, we assume that it is active only in its application year and becomes inactive in the subsequent periods. For any given year, we then construct the patent-level creative destruction rate as the ratio of newly granted patents and the active patent stock. As the active patent stock grows rapidly, we tried the active patent stock in the current year, the active patent stock in the previous year, and the two-year moving averages of the active patent stock in the two consecutive years, which gives us a range of values. The average creative destruction rate ranges from 30% to 34% in the 2011-2013 period. Since we look at patent-level creative destruction and China experienced a patent surge in that period, we consider the relatively high rate reasonable.

**Relative Firm Size.** The model predicts that firms with a higher innovation intensity have a larger expected size. Under the calibrated parameter values, the size ratio between average high- and low-type firms, measured by employment, revenue, or profit, is 1.332. Table C.2 shows the relative size ratio from 2011-2013 firm-level data. Our calibration captures the size difference well.

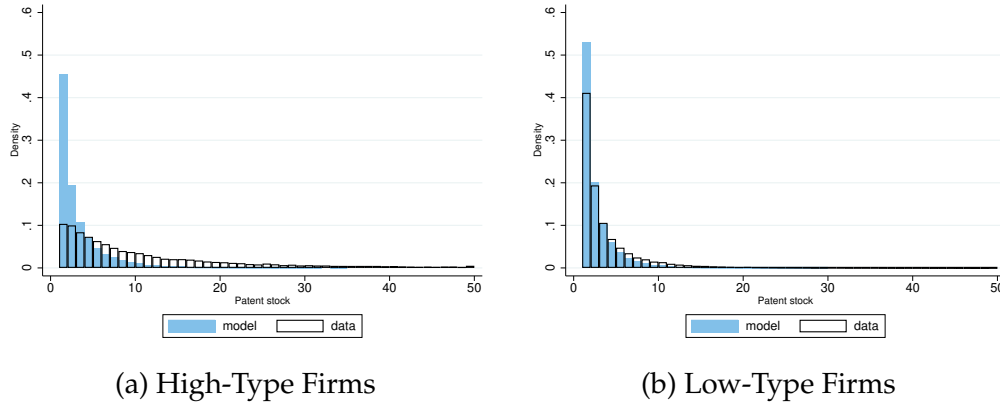
Table C.2: Size Ratio between High- and Low-Type Firms in the Data and the Model

	Employment	Revenue	Profit
Data	1.139	1.249	1.420
Model	1.332	1.332	1.332

Note: This table reports the relative ratio for variables of interest, between average high- and low-type firms in the 2011-2013 period, and we trim the bottom and the top 5 percent of the sample.

We then check the model's performance on the number of patents distributed among innovating firms. In the model, the number of patents corresponds to the number of product lines,  $n$ . Similar to the measurement of patent-level creative destruction, we calculate the patent stock of an individual firm in 2011-2013 by summing all active patents. Figure C.3 shows the distribution of active patent stock among high- and low-type firms. We underestimate the number of patents for high-type firms, but overall, the model matches the data pattern well.

Figure C.3: Distribution of Patent Number among High- and Low-Type Firms



Note: This figure shows the distribution of patent numbers among high- (panel (a)) and low-type (panel (b)) firms. Patent stock is calculated as the sum of all active patents within the 2011-2013 period, and the distribution of patent stock is then estimated for the two sub-groups.

**Magnitude of Quantity-Quality Trade-off.** We provide evidence that the model-implied magnitude of quantity-quality trade-off under the calibrated parameters is in line with data, by exploiting firm-level variations from the Innocom Program. China initiated many policies that aim to promote firm innovations around the mid-2000s. A critical subsidy program China has initiated to promote firm innovations around the mid-2000s is the recognition of High-Tech Enterprises (HTEs) under the InnoCom Program.<sup>4</sup> Certified HTEs enjoy corporate tax cuts and various types of research and development subsidies such as research grants and patent subsidies, which presumably affect their choices over radical and incremental patents.

We employ a Difference-in-Difference (DID) methodology to examine the impact of HTE recognition on high-type firms' innovation choices.<sup>5</sup> Our approach involved defining a post dummy variable equal to 1 for an HTE firm if the observation year was on or after the year the firm obtained the HTE title for the first time, and 0 otherwise. In contrast, for a Non-HTE firm, the post dummy is always 0. Furthermore, we only considered HTEs with at least one prior year and one post year (including the recognition year) to enable meaningful before-after comparisons. We then regress (log) the share of radical patents on the HTE dummy, the interaction term between the HTE dummy and post dummy, which is the key variable of our interest, controlling for (log) employment, (log) revenue, (log) assets as well as year, location (province), industry, ownership types and established year fixed effects. Robust standard errors are clustered at the firm level.

Our DID regression analysis reveals a 24.10% decline in its share of radical patents after a high-type firm receives HTE recognition. We further conduct an event study using

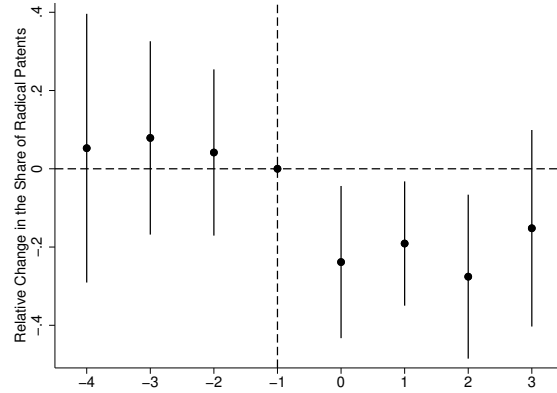
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<sup>4</sup>Among the qualifications to become an HTE, the most important criteria are: (1) firms own patents on their core technology and use such core technology on their main production lines where patents can be invented, transferred, purchased or via M&A, (2) R&D related personnel is no less than 10% of the employers, and (3) depending on the level of total sales, R&D expenses must reach a certain amount.

<sup>5</sup>By definition, low-type firms are those who create only incremental patents, so their radical patent share is unaffected.

year zero as the treatment year to confirm the parallel trends in the pre-treatment period. Figure C.4 displays the results, indicating no apparent trends during the pre-treatment periods. However, during the post-treatment periods, we observed a clear decline in the firm's radical patent share, with most of the point estimates being significant.<sup>6</sup>

Figure C.4: Event Study



Correspondingly, we extend the model to include four types of firms: high-type & HTE, high-type & non-HTE, low-type & HTE, low-type & non-HTE. On top of the general quantity-based subsidies eligible for all, HTE firms are rewarded more:  $b_n^{\text{HTE}} > b_n^{\text{non-HTE}}$ . Consistent with the data, we give each type a 55% chance of HTE recognition. We then quantify the extended model's two extra parameters,  $b_n^{\text{HTE}} = 0.034$  and  $b_n^{\text{non-HTE}} = 0.019$ , according to the observed subsidy differences between HTE and non-HTEs, while keeping the remaining parameters at their benchmark values. The extended model generates a 26.55% decline in its share of radical innovations once a high-type firm receives HTE recognition, quite close to that in the data.

<sup>6</sup>To maintain a sufficiently large sample size for our DID regression and event study, we choose not to apply the 5-year restriction in application years between the cited and citing patents. This should not cause bias as in the regression we include year fixed effects, which resolves the truncation issue. If we had imposed the 5-year restriction, though, one-third of the observations would've been lost, and the DID coefficient became -18.7%, significant at 5% level.

## **D Appendix: Quantitative Analysis**

### **D.1 Estimating the Magnitude of Patent Quantity Surge and Quality Decline**

As shown in Figure [A.4](#), the quantity of patents per researcher increases at a faster rate in the post-2008 period than in the pre-2008 period, while panel (a) in Figure 2.2 shows a clear post-2008 decline in the share of radical patents comparing to the pre-2008 trend. To estimate the magnitude of patent quantity increase above, and of radical share below, their natural trends in the post-2008 period, we first fit the pre-2008 data with a linear trend and then use that trend to extrapolate to obtain the “natural” level for years after 2008 trend. Then by calculating the deviation of the actual level from 2011 to 2013 from the predicted values in relative terms, we obtain the estimation of the magnitude of patent surge above the trend, and of radical share decline below the trend. The estimated quantity increase and radical share decline are 34.57% and 40.89% respectively. For the relative quality of incremental to radical patents (panel (b) in Figure 2.2), the pre-2008 linear trend turns out to be insignificant, so we calculate a 20.27% decline as the relative change of the 2011-2013 average from the 2006-2008 average.

### **D.2 Key Parameters for the Growth and Welfare Implications**

The baseline model finds a negative growth and welfare effect of quantity-based subsidies. The assumption of scarce research time, and parameter values about the degree of quality decay and heterogeneity in skill intensities, determine the strength of quality and quantity channels and the sign of the net impact. We counterfactually shut down each of the three margins to illustrate its importance on the findings presented in Section 4.2. Table [D.1](#) summarizes the results.



Table D.1: Pre vs. Post Changes when Corresponding Margins are Shut Down

Parameter	Margin	$\Delta_{\delta-x_E}$	$\Delta_{\delta_d/\delta}$	$\Delta_{\bar{\eta}/\lambda}$	$\Delta_g$	$\Delta_{\text{welfare}}$
$e$	research time	6.36%	-0.24%	-0.06%	0.21 p.p.	0.29%
$\alpha$	quality decay	9.34%	-41.58%	0.00%	-0.05 p.p.	-1.92%
$\gamma_d, \gamma_m$	skill intensity	8.77%	-12.49%	-8.36%	-0.04 p.p.	-1.79%
baseline results		10.14%	-22.91%	-15.28%	-0.19 p.p.	-3.31%

Note:  $\Delta$  represents changes in the variable from the counterfactual (without  $b_n$ ) to the benchmark economy (with  $b_n$ ) when the corresponding margin is shut down. We present  $\Delta_g$  in absolute percentage point (p.p.) changes, while the others are presented in relative percentage changes (%).

The first margin regards research time,  $e$ . As indicated by the R&D cost function, the scarceness of  $e$  helps generate a strong firm-level quantity-quality trade-off. Once we shut it down, i.e., taking  $e$  out from the R&D production function, both quality channels are substantially weakened, and the growth and welfare implications are completely reversed (row 1).

The second margin regards innovation quality decay,  $\alpha$ . From the growth decomposition in Table 4.4, we already demonstrated that the negative quality-crowding channel is quantitatively dominant. Slightly different from what we did with that decomposition, here we shut down the quality decay margin by setting  $\alpha = 1$  and fixing  $\eta = 0.053$ , i.e., the baseline level of  $\bar{\eta}$ . As a result, the quality-crowding channel is eliminated, and the growth and welfare implications are largely weakened (row 2).

The last is a pair of parameters regarding skill intensity,  $\gamma_d$  &  $\gamma_m$ . As explained by Proposition 2, the skill intensity difference is through which the general equilibrium skill premium effect works. We shut down this margin by setting  $\gamma_d = \gamma_m = 0.453$ , that is, the baseline value of  $\gamma_m$ .<sup>7</sup> To make a reasonable comparison, we also adjust  $z_{Hd} = 0.970$  to

<sup>7</sup>Results remain similar if we set  $\gamma_d$  and  $\gamma_m$  to the baseline value of  $\gamma_d = 0.796$ , so we don't present them here.

restore the baseline level of radical innovation share  $\delta_d/\delta$ . Consequently, both quality channels are largely weakened, and so are the growth and welfare implications (row 3).

Other parameters, or margins, may also affect the growth and welfare implications to some extent. For example, the entrant's overhead investment, or the R&D tax credit multiplier. However, their effects are secondary compared to the three key parameters mentioned above.

### D.3 Extension: Decreasing Return to Scale

In the baseline model, innovation cost scales up linearly with firm size, so that size of a firm does not impact its innovation intensities. While this simplification delivers a clean characterization of the firm-level quantity-quality trade-off and facilitates aggregation, it might lead to bias in policy evaluations. To alleviate this concern, we extend the baseline model to decreasing return to scale (D.R.S.) and re-evaluate the effects of quantity-based innovation subsidies.

**Setting.** We assume a more general innovation production function with size-dependent R&D productivity

$$X_i = z_i(n) n^{1-\phi} \left( e_i h_i^{\gamma_i} \ell_i^{1-\gamma_i} \right)^\phi,$$

where  $z_i(n) = z_i n^{-\psi_i}$ , for  $i = d, m$ . Parameters  $\psi_d, \psi_m > 0$  govern the speed of productivity decay w.r.t. firm size.<sup>8</sup> Similarly, we can derive the function of R&D cost per line

$$R(x_d, x_m; n) = \left[ \Theta_d(n)^{\frac{1}{2}} + \Theta_m(n)^{\frac{1}{2}} \right]^2,$$

but  $\Theta_d$  and  $\Theta_m$  are now size-dependent

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<sup>8</sup>This specification is effectively assuming  $X_i = z_i n^{1-\phi-\psi_i} \left( e_i h_i^{\gamma_i} \ell_i^{1-\gamma_i} \right)^\phi$ , for  $i = d, m$ .

$$\Theta_i(n) = \Delta_i \left( w^h \right)^{\gamma_i} \left( w^\ell \right)^{1-\gamma_i} \left( \frac{x_i}{z_i(n)} \right)^{\frac{1}{\phi}}, \text{ for } i = d, m.$$

Now that the R&D cost per line is size-dependent, the value function takes the form

$$V(Q, \bar{q}) = \sum_{\omega} A q_{\omega} + B_n \bar{q}.$$

To make a comparison, our benchmark case is where  $B_n = n \times B$ .

Again, it is easy to verify that

$$A = \frac{\pi}{r + \delta},$$

while the sequence  $B_n$  solves

$$\begin{aligned} (r - g) \frac{B_n}{n} &= \delta(B_{n-1} - B_n) + b_n \\ &+ \max_{x_d, x_m} x_d [A(1 + \lambda) + B_{n+1} - B_n] \\ &+ x_m [A(1 + \bar{\eta}) + B_{n+1} - B_n] - \hat{R}(x_d, x_m, n), \end{aligned}$$

where  $\hat{R} \equiv R/\bar{q}$  is the detrended R&D cost per line. Lastly, a similar but generalized version of Proposition 2 can be derived, that is

$$\frac{x_d(n)}{x_m(n)} \propto \underbrace{\frac{A(1 + \lambda) + B_{n+1} - B_n}{A(1 + \bar{\eta}) + B_{n+1} - B_n}}_{\text{innovation return}} \times \underbrace{\left( \frac{w^h}{w^\ell} \right)^{-(\gamma_d - \gamma_m)}}_{\text{input structure}} \times \underbrace{\frac{z_d(n)}{z_m(n)}}_{\text{R\&D productivity}}.$$

Here we have an extra ‘‘R&D productivity’’ term, as the relative productivity ratio is no longer a constant. In conclusion, the change does not alter the quantity-quality trade-off facing innovating firms, except that the magnitude now depends on firm size.

**Calibration.** We assume identical  $\psi_m$  for both high- and low-type firms to reduce parameters. To discipline the values of  $\psi_d$  and  $\psi_m$ , we first estimate two regressions regarding the elasticity of innovation quantity and quality w.r.t. firm size

$$\frac{New\ Patent_{f,t}}{emp_{f,t}} = \beta_0 - \underbrace{0.0411^{***}}_{(s.e. 0.0011)} \times \ln(emp_{f,t}) + FE_{f,t}^1 + \varepsilon_{f,t};$$

$$Radical\ Patent\ Share_{f,t} = \beta_0 - \underbrace{0.0293^{***}}_{(s.e. 0.0024)} \times \ln(emp_{f,t}) + FE_{f,t}^2 + \varepsilon_{f,t},$$

where  $FE_{f,t}^2$  contains year and industry fixed effects, and  $FE_{f,t}^1$  further includes a dummy for high-type firms. We then calibrate the values of  $\psi_d$  and  $\psi_m$  to match the two elasticity coefficients in the model and the data.

**Results.** The calibrated  $\psi_d = 0.061$  and  $\psi_m = 0.055$ , which suggest a rather mild D.R.S. among Chinese innovating firms, comparing to the values,  $\psi_d = \psi_m = 0.105$ , reported in [Akcigit and Kerr \(2018\)](#) regarding US firms. For better comparison with the baseline case, we also apply a common factor  $\psi_z = 1.066$  to scale up values of R&D productivity, to restore the baseline level of aggregate creative destruction rate. All the rest of the parameters are kept at their baseline values. Table D.2 & D.3 replicate the growth and welfare implications of quantity-based subsidies, i.e., Table 4.3 & 4.4 in the main text. The results are quite close to the baseline case.

Table D.2: Impact of Quantity-based Subsidies on Innovation Quantity and Quality under D.R.S.

Variable	Meaning	Model	C.F.	$\Delta_{Model}$	$\Delta_{Data}$	$\frac{\Delta_{Model}}{\Delta_{Data}}$
$\delta - x_E$	incumbent innovation	25.43%	23.16%	9.80%	34.57%	28.35%
$\delta_d / \delta$	radical share	7.37%	9.51%	-22.50%	-40.89%	55.03%
$\bar{\eta} / \lambda$	step-size ratio	31.45%	37.20%	-15.46%	-20.27%	76.27%

Note:  $\Delta_{Model}$  represents changes from the counterfactual to the model benchmark,  $\Delta_{Data}$  is changes between the pre- and post-2008 period, both columns are presented in relative terms. Step-size ratio denotes the relative step-size of incremental to radical innovations.

Table D.3: Growth Decomposition under D.R.S.

$\Delta_{\text{Growth}}$	(i) quantity	(ii) quality-composition	(iii) quality-crowding	
-0.18	0.15	-0.06	-0.24	(p.p.)
	-83.33%	33.33%	133.33%	

Note: For each of the channels, we add the corresponding change in (i)  $\delta$ ; (ii)  $\delta_d/\delta$ ; (iii)  $\bar{\eta}$  to the pre-2008 economy, and see how it affects the aggregate growth rate. The second row shows the contribution of each channel, calculated by dividing the corresponding number by -0.18 p.p.

## D.4 Extension: Internal Innovations

In the baseline model, all innovations (patents) trigger creative destruction, i.e., being external. We made this assumption based on the observation that the vast majority of Chinese patents are external ones (Table A.9). In this section, we explore how the model would perform when internal innovations are allowed.

**Setting.** We add a third *internal* innovation choice for all incumbent firms, high- or low-type. In particular, internal innovations arrive at the following Poisson flow rate

$$X_s = z_s n^{1-\phi} \left( h_s^{\gamma_s} \ell_s^{1-\gamma_s} \right)^\phi,$$

where the subscript  $s$  stands for “self-improvement”. The arrival of an internal innovation improves the quality of a product line owned by the firm by a fixed step-size  $\lambda_s > 0$ . The setup gives us an R&D cost per line similar to that assumed in Akcigit and Kerr (2018)

$$R(x_d, x_m, x_s; z_d, z_m, z_s) = \underbrace{\left[ \Theta_d(x_d)^{\frac{1}{2}} + \Theta_m(x_m)^{\frac{1}{2}} \right]^2}_{\text{external innovation cost}} + \underbrace{\Theta_s(x_s)}_{\text{internal innovation cost}},$$

where  $\Theta_i(x_i) \equiv \Delta_i (w^h)^{\gamma_i} (w^\ell)^{1-\gamma_i} (x_i/z_i)^{\frac{1}{\phi}}$  and  $\Delta_i \equiv \gamma_i^{-\gamma_i} (1 - \gamma_i)^{\gamma_i-1}$ , for  $i = d, m, s$ .

The value function still takes the form  $V(Q, \bar{q}) = \sum_{\omega} A q_{\omega} + n B \bar{q}$ , and the return for internal innovations is  $A \lambda_s$ . Quantity-based subsidies affect the relative return of internal vs.

external innovations through competing forces, e.g.,  $B$  and  $\bar{\eta}$ . The overall effect, however, is an issue we address quantitatively.

Before quantifying the model, we introduce some extra notations regarding internal innovations and aggregation. Denote  $\iota_s$  the aggregate internal innovation rate, we have

$$\iota_s = \sum_j \sum_n \mu_{j,n} \times nx_{js},$$

where  $x_{js}$  denotes the internal innovation intensity of the type  $j = H, L$  firm.

The economy's aggregate innovation rate is  $\iota = \delta_d + \delta_m + \iota_s$ , while  $\delta = \delta_d + \delta_m$  still denotes the aggregate creative destruction rate. The aggregate growth rate is given by

$$g = \delta_d \lambda + \delta_m \bar{\eta} + \iota_s \lambda_s.$$

We follow the baseline approach to decompose changes in  $g$  into three channels

$$\begin{aligned} \Delta g = & \underbrace{\Delta \iota \times \left( \frac{\delta_d}{\iota} \lambda + \frac{\delta_m}{\iota} \bar{\eta} + \frac{\iota_s}{\iota} \lambda_s \right)}_{\text{(i) quantity}} + \underbrace{\iota \times \frac{\delta}{\iota} \times \left[ \Delta \frac{\delta_d}{\delta} \times (\lambda - \bar{\eta}) \right] + \iota \times \Delta \frac{\delta}{\iota} \times \left( \frac{\delta_d}{\delta} \lambda + \frac{\delta_m}{\delta} \bar{\eta} - \lambda_s \right)}_{\text{(ii) quality-composition}} \\ & + \underbrace{\iota \times \frac{\delta}{\iota} \times \left[ \left( 1 - \frac{\delta_d}{\delta} \right) \times \Delta \bar{\eta} \right]}_{\text{(iii) quality-crowding}}. \end{aligned}$$

The *quantity* channel now refers to change in the aggregate innovation rate  $\iota$ ; the *quality-composition* channel summarizes changes in the weights  $\delta_d/\delta$  and  $\delta/\iota$ ;<sup>9</sup> the *quality-crowding* channel still refers to the change in the average productivity impact of incremental innovations,  $\bar{\eta}$ .

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<sup>9</sup>The former is the weight of radical innovations within external innovations, while the latter is the weight of external innovations among total innovations. Under our calibration, the *quality-composition* effect is mainly driven by its first component.

**Calibration.** We assume identical  $\gamma_s, z_s, \lambda_s$  for both high- and low-type firms to reduce the number of parameters. We further assume  $\gamma_s = \gamma_m$ , i.e., internal innovations have the same skill intensity as the external incremental ones. That leaves us with two parameters,  $z_s$  and  $\lambda_s$ , which we calibrate jointly by matching the share of internal innovations and the average citation ratio between internal and external radical patents. For better comparison with the baseline case, we also apply a common scale factor  $\psi_z$  on  $z_{Hd}, z_{Hm}$  and  $z_{Lm}$ , to restore the baseline level of aggregate innovation rate. All the rest of the parameters are kept at their baseline values.

**Results with CN Internal Patent Share.** We first take the model to the Chinese patent data. In 2011-2013, the share of internal patents in China is 4.97%, and the average citation ratio between internal and external radical patents is 0.403. These moments produce an internal innovation productivity of  $z_s = 1.294$  and a step-size of  $\lambda_s = 6.36\%$ . The common scale factor required to restore the baseline aggregate innovation rate is  $\psi_z = 0.951$ .

Table D.4 reports the impact of subsidies on innovation quantity and quality, with an extra row documenting change in the share of internal innovations, while Table D.5 reports the impact on growth.<sup>10</sup>

The results remain very close to the baseline case, reaffirming our strategy of focusing on external innovations in the Chinese context. Moreover, the extended model is able to replicate the decline in the share of internal patents in China, which drops from 6.45% pre-2008 to 4.97% post-2008, or a relative decline of 22.95%. In our quantified model, the introduction of quantity-based subsidies causes firms to focus more on external innovations, which crowd out internal innovations through general equilibrium pricing effects.

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<sup>10</sup>In the Chinese sample, the radical patent share within external patents is very close to the baseline where we do not distinguish internal versus external patents, hence we stick to the baseline numbers when calculating changes in the data.

Table D.4: Impact of Quantity-based Subsidies on Innovation Quantity and Quality with CN Internal Patent Share

Variable	Meaning	Model	C.F.	$\Delta_{\text{Model}}$	$\Delta_{\text{Data}}$	$\frac{\Delta_{\text{Model}}}{\Delta_{\text{Data}}}$
$\iota - x_E$	incumbent innovation	25.55%	23.46%	8.91%	34.57%	25.77%
$\delta_d / \delta$	radical within external	8.08%	10.45%	-22.68%	-40.89%	55.47%
$\bar{\eta} / \lambda$	step-size ratio	33.47%	39.42%	-15.09%	-20.27%	74.44%
$\iota_s / \iota$	internal share	4.97%	5.79%	-14.16%	-22.95%	61.70%

Note:  $\Delta_{\text{Model}}$  represents changes from the counterfactual to the model benchmark,  $\Delta_{\text{Data}}$  is changes between the pre- and post-2008 period, both columns are presented in relative terms. Step-size ratio denotes the relative step-size of incremental to radical innovations.

Table D.5: Growth Decomposition with CN Internal Patent Share

$\Delta_{\text{Growth}}$	(i) quantity	(ii) quality-composition	(iii) quality-crowding	
-0.18	0.15	-0.07	-0.24	(p.p.)
	-83.33%	38.89%	133.33%	

Note: For each of the channels, we add the corresponding change in (i)  $\iota$ ; (ii)  $\delta_d / \delta$  and  $\delta / \iota$ ; (iii)  $\bar{\eta}$  to the pre-2008 economy, and see how it affects the aggregate growth rate. The second row shows the contribution of each channel, calculated by dividing the corresponding number by -0.18 p.p.

All the growth-decomposition channels are weakened, so as the growth and welfare loss from quantity-based subsidies. The magnitude, though, is rather small, as the share of internal innovations in China is negligible. Many Chinese firms in that period of time had very few patents of their own to cite. Mechanically, this leads to a low internal patent share. We leave a detailed discussion on why the growth-decomposition channels are weakened in the following exercise with the US internal patent share.

**Results with US Internal Patent Share.** Due to the low internal patent share in China, the quantified model generates very similar results to that in the baseline case. As a comparison, [Akcigit and Kerr \(2018\)](#) reports that the US internal patent share is 21.5%. We further conduct a numerical exercise, targeting the share of internal innovations at the US level. This gives a higher internal innovation productivity of  $z_s = 2.506$ , and a common



scale factor of  $\psi_z = 0.783$  to restore the baseline aggregate innovation rate. Tables D.6 and D.7 report the impact of subsidies on innovation quantity and quality, and on growth.

Table D.6: Impact of Quantity-based Subsidies on Innovation Quantity and Quality with US Internal Patent Share

Variable	Meaning	Model	C.F.	$\Delta_{\text{Model}}$	$\Delta_{\text{Data}}$	$\frac{\Delta_{\text{Model}}}{\Delta_{\text{Data}}}$
$\iota - x_E$	incumbent innovation	25.53%	24.31%	5.02%	34.57%	14.52%
$\delta_d / \delta$	radical within external	8.46%	10.76%	-21.38%	-40.89%	52.29%
$\bar{\eta} / \lambda$	step-size ratio	34.49%	40.11%	-14.01%	-20.27%	69.12%
$\iota_s / \iota$	internal share	21.50%	24.22%	-11.23%	-22.95%	48.93%

Note:  $\Delta_{\text{Model}}$  represents changes from the counterfactual to the model benchmark,  $\Delta_{\text{Data}}$  is changes between the pre- and post-2008 period, both columns are presented in relative terms. Step-size ratio denotes the relative step-size of incremental to radical innovations.

Table D.7: Growth Decomposition with US Internal Patent Share

$\Delta_{\text{Growth}}$	(i) quantity	(ii) quality-composition	(iii) quality-crowding	
-0.16	0.09	-0.04	-0.19	(p.p.)
	-56.25%	25.00%	118.75%	

Note: For each of the channels, we add the corresponding change in (i)  $\iota$ ; (ii)  $\delta_d / \delta$  and  $\delta / \iota$ ; (iii)  $\bar{\eta}$  to the pre-2008 economy, and see how it affects the aggregate growth rate. The second row shows the contribution of each channel, calculated by dividing the corresponding number by -0.16 p.p.

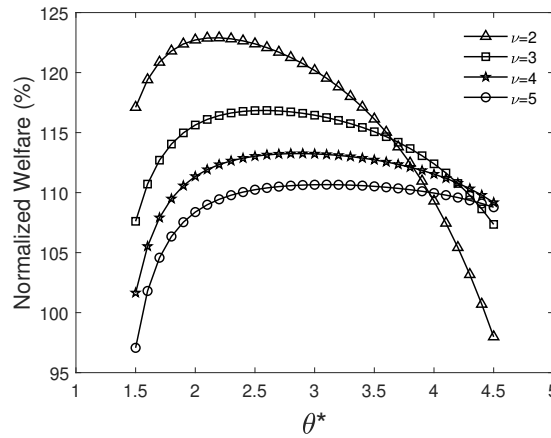
The weakening of all the growth-decomposition channels is more evident under the US calibration. As discussed, subsidies cause firms to pursue more external innovations, which pushes up wages and crowds out internal innovations in the general equilibrium. Hence the increase in total innovations  $\iota$  is smaller than that in external ones  $\delta$ , leading to a weakened quantity effect. As the decomposition formula shows, the importance of the quality effects hinges on the rate of creative destruction. Under the US calibration where internal patent share is high and creative destruction rate is relatively low, the quality-crowding effect, though still negative and dominant, inflicts less growth and welfare loss. However, even under the US calibration, the growth rate decline caused by subsidies

(-0.16 p.p.) is close to the baseline case (-0.19 p.p.), and the dominant force is still the *quality-crowding* channel. That again affirms the robustness of our baseline conclusions.

## D.5 Social Optimum under Different Values of $\nu$

We solve the planner's problem by using a brutal grid search on different values of  $\theta^*$ . At each value, the supply of skilled and unskilled labor are determined as in Appendix B.1. We then let the demand side of the markets run until they all clear. The key difference between the planner's problem and the market equilibrium is that, skill premium in the planner's problem does not necessarily yield the  $\theta_{SP}^*$  picked by the planner. We follow the literature and try  $\nu \in [2, 5]$ . Figure D.1 shows that social welfare is well hump-shaped w.r.t.  $\theta^*$ . Moreover, the smaller  $\nu$  is, the earlier welfare reaches its peak.

Figure D.1: Social Welfare as a Function of  $\theta^*$



Note: Under each value of  $\nu$ , we solve the market equilibrium and normalize the corresponding welfare level to 100%.

## D.6 Proof of Proposition 3

To implement  $\theta_{SP}^*$ , we need to find combinations of  $(b_e, b_h)$  which solve

$$\frac{1-b_e}{\xi} \left[ 1 - e^{-(r-g+d)} \right] \left( e^{-(r-g+d)} - (1-b_h) \frac{w^\ell}{w^h} \right)^{-1} = \theta_{SP}^*, \quad (1)$$

which can be rearranged to

$$b_h = -\frac{1 - e^{-(r-g+d)}}{\xi \theta_{SP}^*} \frac{w^h}{w^\ell} b_e + \frac{1 - (1 + \xi \theta_{SP}^*) e^{-(r-g+d)}}{\xi \theta_{SP}^*} \frac{w^h}{w^\ell} + 1.$$

That is, policymakers face a linear trade-off between  $b_e$  and  $b_h$  when implementing  $\theta_{SP}^*$ , while the slope of trade-off is endogenous.

To see that both  $b_e$  and  $b_h$  are necessary if  $\theta_{SP}^*$  is low, we further examine the left-hand side (LHS) of equation (1). As shown in our quantitative analysis, the social planner's allocation is featured by high growth rate  $g$  and low skill premium  $w^h/w^\ell$ . Moreover, the lower  $\theta_{SP}^*$  is, the higher (lower) growth rate (skill premium) is. One can derive

$$\text{LHS}(b_e = 0, b_h = 1) = \frac{e^{(r-g+d)} - 1}{\xi},$$

which is, the lowest  $\theta^*$  a competitive equilibrium can reach without education subsidy. As  $\theta_{SP}^*$  approaches 1, the difference between equilibrium interest rate and growth rate,  $r - g = \rho + (\nu - 1) \times g$ , becomes greater, which eventually forces  $\text{LHS}(b_e = 0, b_h = 1)$  to stay above the desired  $\theta_{SP}^*$ . Thus, education subsidy is necessary if we want to implement a low  $\theta_{SP}^*$ .

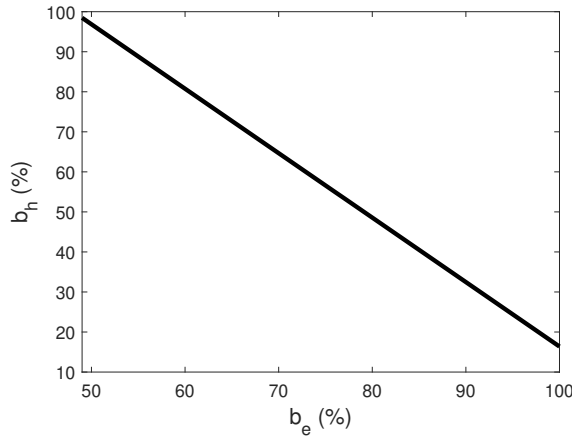
A necessary condition for equation (1) to hold is that its LHS stays positive, which in turn requires

$$\frac{w^h}{w^\ell} > (1 - b_h) e^{(r-g+d)}.$$

Without skilled labor subsidy, i.e.,  $b_h = 0$ , this condition will be violated eventually since

the skill premium approaches 1 when  $\theta_{SP}^*$  approaches 1. Thus, skilled labor subsidy is also necessary if the  $\theta_{SP}^*$  to be implemented is low. For example, to implement the socially optimal  $\theta_{SP}^*$  in our benchmark case, policymakers can choose  $(b_e, b_h)$  located on the solid line in Figure D.2. Since the  $\theta_{SP}^*$  is fairly low, policymakers need the workhorse of both subsidies to implement the desired allocation.

Figure D.2: Combinations of  $(b_e, b_h)$  to Implement  $\theta_{SP}^* = 2.6$ .



## D.7 Subsidy Comparison

Here we compare the effects of various innovation subsidies in the model. More specifically, we have four kinds of subsidies: quantity-based subsidy  $b_n$ ; generic R&D tax credit  $b_r$ ; education subsidy  $b_e$ ; and skilled labor subsidy  $b_h$ . We raise the magnitude of each subsidy by a small amount (5 percent) and check the changes in several important moments. Table D.8 summarizes the results.

The generic R&D tax credit,  $b_r$ , once strengthened, results in more R&D trials, and higher innovation quantity, but deteriorating innovation quality. Similar to the quantity-based subsidy, R&D tax credit is “quantity-biased” since it cannot distinguish between R&D

Table D.8: Effects from Strengthening the Subsidies

Variable	Meaning	B.M.	$b_n+5\%$	$b_r+5\%$	$b_e+5\%$	$b_h+5\%$
$R(x)/V_{add}$	average R&D intensity	15.84%	16.02%	16.26%	15.73%	15.75%
$\delta_d/\delta$	radical share	8.01%	7.91%	7.83%	8.63%	8.51%
$w^h/w^\ell$	skill premium	2.43	2.44	2.45	2.38	2.39
$g$	TFP growth rate	1.97%	1.96%	1.96%	2.07%	2.05%
$U$	social welfare	100%	99.80%	99.66%	101.14%	100.93%

Note: We strengthen each of the subsidies by 5 percent from the benchmark level while keeping others unchanged. The benchmark level of welfare is normalized to 100%.

expenditures on radical and incremental innovations. As a consequence, both subsidies contribute negatively to welfare if they were strengthened from their current levels.

Conversely, the two “quality-biased” subsidies,  $b_e$  and  $b_h$ , can effectively improve welfare by raising the skilled labor supply, reducing skill premium, and encouraging radical innovations. They effectively improve both the quantity and quality of innovations.

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