

DIGITAL ELECTRONICS

1 Course Outline

Definition

Number systems - Decimal - Binary - Octal - Hexadecimal

Binary Number System.

Binary Coded Number System.

8421 BCD

2421 BCD

Excess 3 BCD

GRAY CODE Number System.

2 Logic Circuits.

Definition

Logic circuit and logic gate

Classification of logic circuits.

- Combination circuits

- Circulation circuits

Combination Circuit - Logic gates

Arithmetic Logic Gates - Binary addition

- " subtraction

- " comparator

Code Converters.

Logic Circuit design tools

- Boolean algebra

- Karnaugh map

Arithmetic Logic Circuit Adder

- Binary adder - Subtraction operator.

- Binary subtractor

- " comparator

Code Converter.

SEQUENTIAL CIRCUITS

Definition

Classification

- Asynchronous circuit

- Synchronous circuits.

Components:

FLIP FLOPs

- R-S / S-R flip flop

- Clocked S-R flip flop

- J-K flip flop

Xynchronous circuits

- Binary counters

Synchronous circuits

- Counters

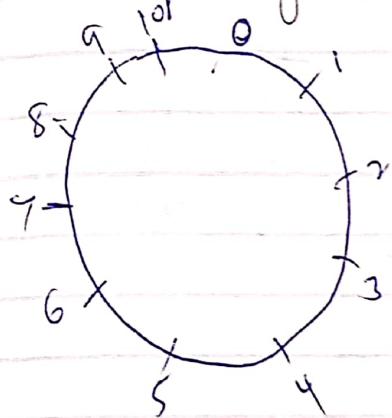
- Registers.

Digital Electronics

Base 10 numbers ~~are system~~

has 10 steps in the counting cycle. Each step is represented by a unique symbol.

The unique symbols (0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10) ^{symbols are known} as digits



The ten counting steps in a decimal counting cycle with the ten unique symbols of representation after each step.

This is a weighted number system. In case of combination of digits the least to the most significant the digits will be occupying the position weight as, 0.10, 10, 100.

Indecimal number system : This is a natural
and given number system.

Decimal Arithmetic

Addition

$$0_{10} + 0_{10} = 0_{10}$$

$$0_{10} + 1_{10} = 1_{10}$$

$$1_{10} + 0_{10} = 1_{10}$$

$$1_{10} + 1_{10} = 2_{10}$$

$$9_{10} + 1_{10} = 10_{10}$$

Multiplication

$$0_{10} \times 0_{10} = 0_{10}$$

$$0_{10} \times 1_{10} = 0_{10}$$

$$1_{10} \times 0_{10} = 0_{10}$$

$$1_{10} \times 3_{10} = 3_{10}$$

$$3_{10} \times 1_{10} = 3_{10}$$

Subtraction

$$0_{10} - 1_{10} = \text{Impossible.}$$

$$1_{10} - 0_{10} = \text{Not possible, } 0_{10}$$

$$1_{10} - 0_{10} = 1_{10}$$

$$1_{10} - 1_{10} = 0_{10}$$

$$13_{10} - 5_{10} = 8_{10}$$

Division

$$0_{10} \div 0_{10} = 0_{10}$$

$$0_{10} \div 1_{10} = \text{Impossible (0)}$$

$$1_{10} \div 0_{10} = \text{Impossible or } \infty$$

$$1_{10} \div 1_{10} = 1_{10}$$

$$3_{10} \div 2_{10} =$$

Binary Digits

It is a weighted number system. The weighting is such that the positional value is obtained by having the base of the number for this case 2 to the power of the bit position.

$$0_2 + 0_2 = 0_2$$

$$0_2 + 1_2 = 1_2$$

$$0_2 + 1_2 = 1_2$$

$$1_2 + 1_2 = 10_2$$

$$11_2 + 1_2 = 100_2$$

$$(0 - 0)_2 = 0_2$$

$$(0 - 1)_2 = 0_2 \text{ Not possible}$$

$$(1 - 0)_2 = 1_2$$

$$(1 - 1)_2 = 0_2$$

$$(10 - 1)_2 =$$

Binary Multiplications.

$$0 \times 0 = 0_2$$

$$0 \times 1 = 0_2$$

$$1 \times 0 = 0_2$$

$$1 \times 1 = 1_2$$

$$11 \times 10 = 110$$

Division

$$0 \div 0 = 0$$

$$0 \div 1 = \text{Not possible}$$

$$1 \div 0 = ???$$

$$1 \div 1 = 1$$

$$11 \div 10$$

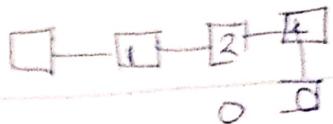
$$(10 \overline{)110} = 1\%_0$$

Decimal to Binary Conversion

$$100 \rightarrow x_2$$

$$\begin{array}{r} 100 \\ 2 \overline{)100} \\ -100 \\ \hline 0 \end{array}$$

$$\begin{array}{r} 2 | 100 \\ \hline 2 | 00 \\ \hline 00 \end{array}$$



Binary to Decimal.

(111)₂

$$(2^0 + 2^1 + 2^2)$$

$$1 + 2 + 4 = 7$$

Decimal	Binary
0	0 0 0 0
1	0 0 0 1
2	0 0 1 0
3	0 0 1 1
4	0 1 0 0
5	0 1 0 1
6	0 1 1 0
7	0 1 1 1
8	1 0 0 0
9	1 0 0 1
10	1 0 1 0
11	1 0 1 1
12	1 1 0 0
13	1 1 0 1
14	1 1 1 0
15	1 1 1 1
16	1 0 0 0 0
17	1 0 0 0 1
18	1 0 0 1 0
19	1 0 0 1 1
20	1 0 1 0 0

Octal Number System. It's a base 8 number system.
 Has 8 steps in its counting cycle rep by 8 unique symbols. (0, 1, 2, 3, 4, 5, 6, 7). The symbols are known as digits. This is a weighted number system. The weighting is such that the weight of the number system is raised to the power of the digit position starting from the LSCD to MCD i.e $8^0, 8^1, 8^2, \dots, 8^n$.
 It is a shorthand form for the binary no. system.

Decimal To Octal.

E.g. $\begin{array}{r} 8 \\ \overline{)8} \\ 8 \quad \rightarrow 0 \\ \hline 1 \\ 0 \quad \rightarrow 1 \end{array}$

$$8_{(10)} = \frac{(10)}{8} \quad 10_{(8)}$$

1×8
 $8 - 8 = 0$

$$28_{(10)} \quad \underline{\text{Sd}}_8 \quad \begin{array}{r} 8 \mid 28 \\ 8 \quad | \\ 3 \quad | \\ 0 \quad 3 \end{array} \quad \begin{array}{l} 4 \uparrow \\ 3 \end{array}$$

$8 \times 0 = 0$
 $3 - 0 = 3$

$$= 34_{(8)}$$

Conversion Table.

Decimal	Octal.	Decimal	Octal
0	0	13	15
1	1	14	16
2	2	15	17
3	3	16	20
4	4	17	21
5	5		
6	6		
7	7		
8	10		
9	11		
10	12		
11	13		
12	14		
13	15		

64TB = 64,000,000 bytes

Octal To Decimal.

$$10_8 \equiv (8)_{10}$$

$$\begin{array}{r} 1 \\ 8 \\ 8 \\ 8 \\ 1 \\ 0 \\ \hline 8+0 = 8_{10} \end{array}$$

$$32 \equiv (0)_{10}$$

$$\begin{array}{r} 3 \\ 3 \\ 3 \\ 3 \\ 1 \\ 0 \\ \hline 3+0 = 3_{10} \end{array}$$

$$24+0 = 24_{10}$$

Octal to Binary

V. Decimal, Power applied

e.g 1

$$6_8 \equiv ()_2$$

$$6_8 \equiv (6)_{10}$$

$$\begin{array}{r} 6 \\ 8 \\ 8 \\ 1 \\ 6 \\ 6 \\ \hline 6 \end{array}$$

Divide by 3 ...

$$\begin{array}{r} 6 \\ 3 \\ 2 \\ 2 \\ 1 \\ 1 \\ \hline 1 \end{array} \quad \begin{array}{r} 110 \\ / / \\ 110 \end{array}$$

e.g 2

$$15_8 \equiv x_2$$

$$15_8 \equiv x_{10}$$

$$\begin{array}{r} 15 \\ 8 \\ 8 \\ 8 \\ 1 \\ 5 \\ \hline 8+5 = 13_{10} \end{array}$$

$$13_{10}$$

$$\begin{array}{r} 13 \\ 2 \\ 2 \\ 2 \\ 2 \\ 0 \\ \hline 1 \end{array} \quad \begin{array}{r} 101 \\ \uparrow \uparrow \\ 101 \end{array}$$

$$1101_2$$

Cramer's Approach.

$$6_8 \equiv (?)_{10}$$

$$8 = 2^3$$

$$6_8 \equiv 110$$

$$6_8 = ?$$

$$8 = 2^3$$

Example 2

$$15_8 \equiv (?)_2$$

$$8 = 2^3$$

$$\begin{array}{r} 1 \quad 5 \\ 001 \quad 101 \end{array} \left| \begin{array}{l} \text{We concatenate} \\ \hline 001101_2 \end{array} \right. \Rightarrow 15_8 \equiv 1101_2$$

Binary To Octal Conversion.

- There are 3 methods of approach
① Through decimal
② Cramer's approach
③ (c)

Through Decimals.

Binary to decimal

Decimal to octal

The resultant combination of the digit is the octal equivalent of the given binary number.

Example.

$$① 111_2 \equiv (?)_8$$

$$② 1011_2 \equiv (?)_8$$

$$\begin{array}{r} 1 \quad 0 \quad 1 \quad 1 \\ 2 \quad 2 \quad 2 \quad 2 \end{array}$$

$$8 + 0 + 2 + 1$$

$$= 11_{10}$$

$$11_{10} \equiv (?)_8$$

$$\begin{array}{r} 11 \\ 8 \longdiv{11} \\ \quad 8 \\ \quad \quad 3 \\ \quad \quad 0 \end{array}$$

$$= 13_8$$

Cramars approach.

$$10_2 \equiv (?)_8$$

$$2^3 = 8$$

No of bits we combine to map a single unique octal digit.

$$10_2 \equiv (?)_8$$

Grouping the bits in the binary number starting from the most sigf to the least sigf into groups of three bits. Should any fail short of the number three, add zeros to make the no. three. Make the no 3 from the conversion table interpret the value of each group. The combination of the digits is the octal equivalent of the binary numbers.

(i) $\frac{010}{2}$

$$10_2 \equiv (?)_8$$

(ii) Eg $111_2 \equiv (?)_8$

$$2^3 = 8$$

3 bits in each digit

$$\frac{111}{7}$$

$$111_2 = 7_8$$

(iii) $1011_2 \equiv (?)_8$

$$2^3 = 8$$

$$\frac{\underline{001} \underline{011}}{1 \quad 3}$$

$$1011_2 = 13_8$$

Hexadecimal: Base 16 no-system
+ has 16 counting steps in its counting cycle.
Lack of the 16 steps is rep by a unique symbol.
The 16 unique symbols are 0, 1, ..., F, known as digits.

Dec Hex

It is also known as alphanumeric number systems.

This is a weighted number system. The digit position are such as from LSD to MSD in the form $16^0 \cdot 16^1 \cdot 16^2 \cdot 16^3 \cdots 16^n$

Decimal To Hexadecimal Conversion:
Decimal is standard Hex is not.

$$\begin{array}{r} 8_{10} = (?)_{16} \\ 16 \overline{) 8} \\ \quad 0 - 8 \\ \hline 8_{10} = 8_{10} \end{array}$$

$$15_{10} = (?)_{16}$$

$$\begin{array}{r} 16 \overline{) 15} \\ \quad 0 \rightarrow 15 \\ \hline 15_{10} = F_{16} \end{array}$$

$$43_{10} = (?)_{16}$$

$$\begin{array}{r} 16 \overline{) 43} \\ \quad 4 \end{array}$$

$$75_{10} = (?)_{16}$$

$$\begin{array}{r} 16 \overline{) 75} \\ \quad 4 \\ \hline 0 \end{array}$$

$$75_{10} = 4B_{16} / 4B_{16}$$

Hexadecimal to Binary

$$37C_{16} \Rightarrow (?)_{10}$$

$$3 C 7_{16} \Rightarrow (?)_{10}$$

$$\begin{array}{r} 16^2 \quad 16^1 \quad 16^0 \\ 256 \quad 16 \quad 1 \\ \times 3 \quad \times 7 \\ \hline 768 + 192 + 7 \end{array}$$

$$= 967_{10}$$

Hexadecimal to binary conversion.

Two approaches

- ① Via Decimal ② Cramers Approach.

Example; $4_{16} \equiv ?_2$

$$\begin{array}{c|c|c} 4 & 4_{10} \equiv x_2 & 4_{16} \equiv 100_2 \\ \begin{array}{c} 16 \\ | \\ 16 \\ | \\ 4 \end{array} = 4_{10} & \begin{array}{c|c} 2 & 4 \\ 2 & 2 \\ 2 & 1 \\ 0 & 1 \end{array} & \begin{array}{c} 100 \\ 1 \end{array} \end{array}$$

$$4_{16} = x_2$$

$$26_{10} = x_2$$

$$4_{16} = x_{10}$$

$$\begin{array}{r} 16 \\ | \\ A \\ 16 \end{array}$$

$$\begin{array}{r} 16 \\ | \\ 10 \\ 16 + 10 \\ \hline 10 \end{array}$$

$$x_{10} = 26_{10}$$

$$\begin{array}{c|c} 2 & 26 \\ 2 & 13 \\ 2 & 6 \\ 2 & 3 \\ 2 & 1 \\ 0 & 1 \end{array} \quad 11010_2$$

$$4_{16} = 11010_2$$

Cramers Approach:

$$4_{16} \equiv x_2$$

$$16 = 2^4$$

$$\begin{array}{c} 4 \\ \hline 0 \ 1 \ 0 \ 0 \end{array}$$

$$= 100_2$$

$$4_{(16)} \equiv 100_2$$

$$1A_{16} = x_2$$

$16 = 2^4$ - rep. the no. of binary bits
for hexadecimal digit

$$\begin{array}{c|c} 1 & 0 \ 0 \ 0 \ 1 \\ \hline A & 1 \ 0 \ 1 \ 0 \end{array}$$

$$00011010$$

Binary To Hexadecimal

- Two Approaches ① via decimal ② Cramers

$$10F_2 \equiv x_{10}$$

$$\begin{array}{r} 1 \ 0 \ 1 \\ 2 \ 2 \ 2 \\ 0 \ 1 \end{array}$$

$$4+0+1=5_{10}$$

$$5_{10} \equiv x_{16}$$

$$\begin{array}{c|c} 16 & 5 \\ \hline 0 & 5 \end{array}$$

$$101_2 \equiv 5_{16}$$

$$1011101_2 = x_{16}$$

$$\begin{array}{r} 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1 \ 2^0 \\ | \quad | \quad | \quad | \quad | \quad | \quad | \\ 1 \ 0 \ 1 \ 1 \ 1 \ 0 \ 1 \\ 2^6 \ 2^5 \ 2^4 \ 2^3 \ 2^2 \ 2^1 \ 2^0 \\ 64 \ 32 \ 16 \ 8 \ 4 \ 2 \ 1 \\ \hline 1 \ 0 \ 1 \ 1 \ 1 \ 0 \ 1 \\ 64 \ 0 \ 16 \ 8 \ 4 \ 0 \ 1 = 93 \end{array}$$

$$93_{10} \rightarrow x_{14}$$

16	93
16	5
	0

13(D)

$$1011101_2 = 5D_{16}$$

Grammars Approach.

$$\textcircled{a} \quad 101_2 = x_{16}$$

$$2^4 = 16$$

$$\begin{array}{r} 0101 \\ 5 \end{array}$$

$$101_2 = 5_{16}$$

$$\textcircled{b} \quad 1011101_2 = (x)_{16}$$

$$2^6 = 16$$

$$\begin{array}{r} 010 \ 1101 \\ 5 \ D \end{array}$$

$$1011101_2 = 5D_{16}$$

Binary Classification.

Binary Code Decimal(BCD) A family member of the binary number system. Uses bits to represent the values. The ten unique decimal symbols are rep by their 4 bits binary equivalent.

Four bit system is fixed so that all the decimal digits that need to be are comfortably covered. The largest unique digit in binary is 1001_2 . In this number sys each of the decimal digit is represented by the four bits equivalent. It is a weighted no. system.

$$\begin{array}{r} 2^3 \ 2^2 \ 2^1 \ 2^0 \\ 0 \ 0 \ 0 \ 0 \end{array}$$

8 4 2 1 BCD

The weighting of this binary number system is such that the MSB is weighted 2^3 , to 2^2 , 2^1 , 2^0 to form 8 4 2 1 BCD.

Dec	Binary	BCD
0	0	0000
1	1	0001
2	10	0010
3	11	0011
4	100	0100
5	101	0101
6	110	0110
7	111	0111
8	1000	1000
9	1001	1001
10	1010	1010 XXXX

EXCESS THREE BCD

This is a BCD number. The weighting is similar to the 8421 BCD except the count of zero is elevated by a value of 3. All the other counts are elevated by the value 3.

Dec	BCD	BCD
8421		
0	0000	0011
1	0001	0100
2	0010	0101
3	0011	0110
4	0100	0111
5	0101	1000
6	0110	1001
7	0111	1010
8	1000	1011
9	1001	1100
10	* * * * X	X X X X
11	X X X X	X X X X
12	X X X X	X X X X
13	X X X X	X X X X
14	X X X X	X X X X
15	X X X X	X X X X
16	0 0 0 0	0 0 11

16

$2^4 = 16$

1101
 1110
 1111.
 0000
 0001
 0010
 0011

Gray Code Number System.

A no. of the binary system by virtue of using the two unique symbols 0 and 1 just as the ordinary binary. It is a weighted number system. It's a no. system that follows the sequence for every single step change there will be a single bit change. It is a self reflecting code number system. It has a mirror effect.

Binary	Grey Code	Binary	Grey Code
0.	000	0	0000
1.	001	10.	0001
10.	011	11.	0001
11.	010	100.	0011
100.	0110	101.	0110
101.	0111	110.	0111
111.	101	111.	1010
		1000.	1100
		1001	1101
		1010	0111
		1011	0110
		1100	01010
		1101	01011
		1110	01001
		1111	01000
		10000	11000
		10001	11001

Binary to Grey Code conversion.

$$10_2 = (?)_{\text{gray}}$$

Get the binary number

Copy the most significant bit of the binary to be the MSB of grey code number.

Compare the most significant bit of binary with the bit

If the two bits are equal the next grey code bit is a zero

If the two bits are not equal the next grey bit is a one

Compare the second binary bit with the next binary bit

If the two bits are equal, the next bit is zero

If the two bits are not equal the next grey is one

Continue until all the comparisons

Continue with the comparison until the LSB is considered. The resulting combination of Bits is the Grey code equivalent of the binary numbers.

$\begin{array}{c} 1 \\ 1 \\ 0 \\ \downarrow \\ 1 \\ 0 \end{array}$ f_2
 $\begin{array}{c} 1 \\ 1 \\ 0 \\ \downarrow \\ 1 \\ 0 \end{array}$ \ddagger_2
 $\begin{array}{c} \downarrow \\ \downarrow \\ 1 \\ 0 \end{array}$
 1011 Gray

$\begin{array}{c} 1 \\ 1 \\ 1 \\ \downarrow \\ 1 \\ 0 \end{array}$ $\{^2\}$
 1000 Gray

Gray code to Binary

$$1011_{\text{gray}} = ?_2$$

Get the gray code no.
Copy the most significant bit.
Comp the binary MSB with the gray next

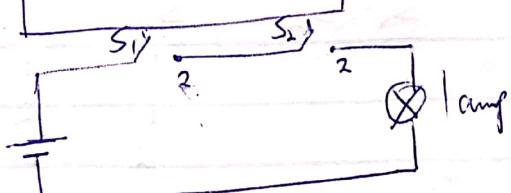
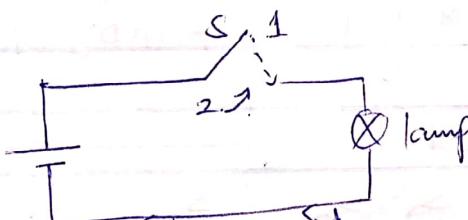
$$1011_{\text{gray}} = ?_2$$

$$\begin{array}{c} 1 \\ 0 \\ \swarrow \\ 1 \\ 0 \\ \downarrow \\ 1 \end{array} \quad 101_2 = 1101_2$$

$$\begin{array}{c} 1 \\ 1 \\ \swarrow \\ 1 \\ 1 \\ \downarrow \\ 1 \\ 0 \end{array} \quad 10_2 = 10_2 \quad \text{If same zero}$$

LOGIC CIRCUITS

Logic circuit is an ~~element~~ electronic circuit they may have as many inputs as the situation may demand but will have only one output. The output may assume only one of the two logical conditions at a time. The two logical conditions are on or off, 1 or 0 upto 1, True or False.



		Functional table	
S ₂	S ₁	L	
1	1	0	
1	0	0	
0	1	0	
0	0	1	

The lamp will light up only if both switches are in position 2

S_2	S_1	L
OFF	OFF	OFF
OFF	ON	OFF
ON	OFF	OFF
ON	ON	ON

OFF \Rightarrow logic 0
ON \Rightarrow logic 1

S_2	S_1	L
0	0	0
0	1	0
1	0	0
1	1	1

Truth Table

$S_2 \& S_1$ must be at logic 1 for the output L to be logic 1.

Let us Δ : Logic 1 as the input and 0 logic 0 at the input as \bar{S} . Logic 1 at the op as L
Logic 0 at the OP as \bar{L}

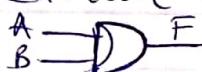
$L(S_1, S_2) = S_1 \times S_2$ AND operator.

$L(S_1, S_2) = (S_1 S_2)$ \approx A boolean expression.

LOGIC GATES.

This is an electronic circuit which may have many inputs as the situation may demand, but with a single output. Both the inputs variable and the output will each assume a logic state of 1 and 0 at any instant in time

Circuit Symbols.

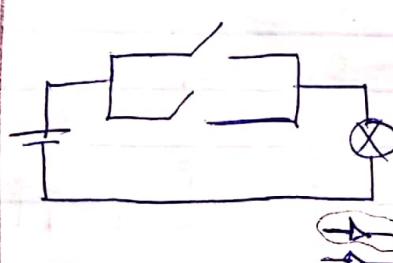


And operator.

A	B	F
0	0	0
0	1	0
1	0	0
1	1	1

Truth table

$$F(AB) = AB$$



$S_1 \setminus S_2$	S_2	S_1	L
1	1	1	OFF
1	1	2	ON
2	2	1	ON
2	2	2	ON

S_2	S_1	L
OFF	OFF	OFF
OFF	ON	ON
ON	OFF	ON
ON	ON	ON

Functional table.

The lamp will be ON when
 (1) S_1 OFF AND S_1 is ON
 or (2) S_2 ON and S_1 OFF
 or (3) S_2 ON and S_1 ON

The circuit is able to realise an OR function of the logic operation

S_1	S_2	L
0	0	0
0	1	1
1	0	1
1	1	1

Truth table
OR Gate.

Let us Δ ; S individuals out logic L

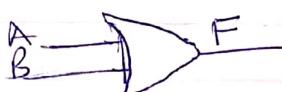
output logic L
Input logic H
Input logic H

$$L(S_2, S_1) = S_2 S_1 \text{ OR } S_2 \bar{S}_1 \text{ OR } S_2 S_1$$

⊕-logic plus operator.

$$L(S_2, S_1) = \bar{S}_2 S_1 + S_2 \bar{S}_1 + S_2 S_1$$

Grent symbol for the logic gate.



$$F(A, B) = \bar{A}B + A\bar{B} + AB$$

A	B	L
0	0	0
0	1	1
1	0	1
1	1	1

The three logic gates are namely;

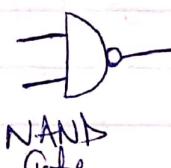
AND, OR and NOT are known as fundamental logic gates (conventional logic gates)

UNIVERSAL LOGIC GATES. These are logic gates from which the basic logic gates may be obtained by

various modes of Configuring



A	B	X	F
0	0	0	1
0	1	0	1
1	0	0	1
1	1	1	0



A	B	F
0	0	1
0	1	1
1	0	1
1	1	0