## THE UNITED REPUBLIC OF TANZANIA CERTIFICATE OF SECONDARY EDUCATION EXAMINATION

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## SECTION A (60 marks)

Answer ALL questions in this section. All working for each question must be shown clearly.

1. (a) The functions f and g are defined by

$$f: x \rightarrow 5x + 4$$

$$g:x \to 6x-k$$

where  $x \in R$  and k is a constant. Find the value of k for which fog(x) = gof(x).

(3 marks)

- (b) The expression  $3x^3 + 2x^2 bx + a$  is divisible by (x 1) and it leaves a remainder of when divided by x + 1. Find the values of a and b. (3 marks)
- 2. (a) Prove that  $(\sin\theta + \cos\theta)(1 \sin\theta\cos\theta) = \sin^3\theta + \cos^3\theta$ . (3 marks)
  - (b) Find the value of  $\sin^2 A \csc(\frac{\pi}{2} A) \cot^2(\frac{\pi}{2} A)\cos A$  (3 marks)
- 3. (a) If  $\underline{u} = 2\underline{i} \underline{j}$ ,  $\underline{v} = 6\underline{i} 3\underline{j}$ 
  - (i) find u + v
  - (ii) show that  $|\underline{u} + \underline{v}| = |\underline{u}| + |\underline{v}|$

(3 marks)

- (b) In a triangle OAB,  $\overrightarrow{OA} = \underline{a}$  nd  $\overrightarrow{OB} = \underline{b}$ . Given that P and Q are the midpoints of OA and OB respectively, express  $\overrightarrow{PQ}$  and  $\overrightarrow{AB}$  in terms of  $\underline{a}$  and  $\underline{b}$ . State the geometrical relationship between  $\overrightarrow{PQ}$  and  $\overrightarrow{AB}$ . (3 marks)
- 4. (a) Find the inverse A<sup>-1</sup> of the matrix  $A = \begin{bmatrix} 3 & -8 \\ 7 & 5 \end{bmatrix}$  (3 marks)
  - (b) Using the result of (a) above, and not otherwise solve the following system of simultant equations:

$$\begin{cases} 3x - 1 - 8y = 0 \\ 7x = 26 - 5y \end{cases} = 0$$

(3 marks)

The following table summarises the masses measured to the nearest gram of 200 animals from the 5. same species:

Mass (g)	Frequency
75 - 79	7
80 - 84	30
85 - 89	66
90 - 94	57
95 - 99	27
100 - 104	
100 - 104	13

Calculate the median and upper quartile of the distribution.

(6 marks)

A social committee is to transport 20 boys and 32 girls to a place for a picnic. The committee can hire either a taxi which can carry 2 boys and 1 girl or a mini bus which can carry 2 boys and 4 girls. It costs sh.4000 to hire a taxi and sh 3000 for a mini bus. Find the cheapest means of transport.

(6 marks)

Differentiate with respect to x (a) 7.

(i) 
$$\frac{\sin x}{1 + \tan x}$$
 (ii)  $\sqrt{x^2 + 2x}$ 

(4 marks)

Evaluate (b)

$$\int_{0}^{\pi/2} (2\cos^2\theta + 3\sin^2\theta)d\theta \qquad (2 \text{ marks})$$

- Show how the biconditional  $p \leftrightarrow q$  can be written in terms of the original three 8. (a) (2 marks) connectives v, A and ~.
  - Using a truth table verify that (b)

(i) 
$$\sim (p \rightarrow q) \equiv p \land \sim q$$

(i) 
$$\sim (p \rightarrow q) = p \land q$$
  
(ii)  $\sim (p \leftrightarrow q) \equiv \sim p \leftrightarrow q$   
(4 marks)

(3 marks) 9.  $\int e^x \cos 3x dx$ (a)

Find the value of p and q such that (b)

$$\int_{0}^{3x} (pt - q)dt = 9x^{2} + 9x$$
(3 marks)
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Solve the following system of simultaneous equations: 10.

$$\begin{cases} 2x - 5y + 2z = 14 \\ 9x + 3y - 4z = 13 \\ 7x + 3y - 2z = 3 \end{cases}$$
 (6 marks)

## SECTION B (40 marks)

Answer FOUR (4) questions from this section. All workings must be shown clearly.

Find the 2 x 2 matrix that will transform the point (1, 2) to (3, 3) and the point (-1, 1) 11. (a)

All the points on the line y = 2x - 3 have been transformed by the matrix (b)

$$\begin{bmatrix} 2 & 1 \\ 3 & -1 \end{bmatrix}$$

Find the equation of the image line.

(5 marks)

- Find the equation of the circle which circumscribes the triangle with vertices 12. (10 marks) (1, 0), (2, 1) and (0, 2).
- A company that manufactures cattle food wishes to pack the food in closed cylindrical tins. What should be the dimensions of each tin, if each tin is to have a volume of  $128 \pi \, \mathrm{cm}^3$ 13. (a) (5 marks) and a minimum possible area?
  - The area of the segment cut off by y = 5 from the curve  $y = x^2 + 1$  is rotated about (5 marks) (b) y = 5. Find the volume generated.
- If A and B are independent events such that  $P(A) = \frac{5}{8}$  and  $P(\frac{B}{A}) = \frac{3}{7}$ , 14. (a) (3 marks) find P(A n B).
  - In a class of 30 boys, 15 have bicycles, 10 have motorbikes and 4 have both. If a student (b) is picked at random, what is the possibility that (7 marks)

he has neither a bicycle nor a motorbike (i)

he has a bicycle but no a motorbike. (ii)

- (2 marks) Find the modulus and argument of  $z = \frac{1}{2} - \frac{\sqrt{3}}{2}i$ 15. (a)
  - Given that z = 1 + i, show that  $z^3 = -2 + 2i$ . For this value of z, the real numbers (b) p and q are such that  $\frac{p}{1+2} = \frac{q}{1+z^3} = 2i$ . Find the values of p and q. (5 marks)
  - The complex number z satisfies the equation (c) 2zz - 4z = 3 - 6i where z is the conjugate of z. Find the two possible values of z (3 marks) in the form x + iy.
  - Newton-Raphson method with starting point 1.6 determine in two iterations a better root giving your answer to two decimal places 16.