

Towards a miniKanren with fair search strategies

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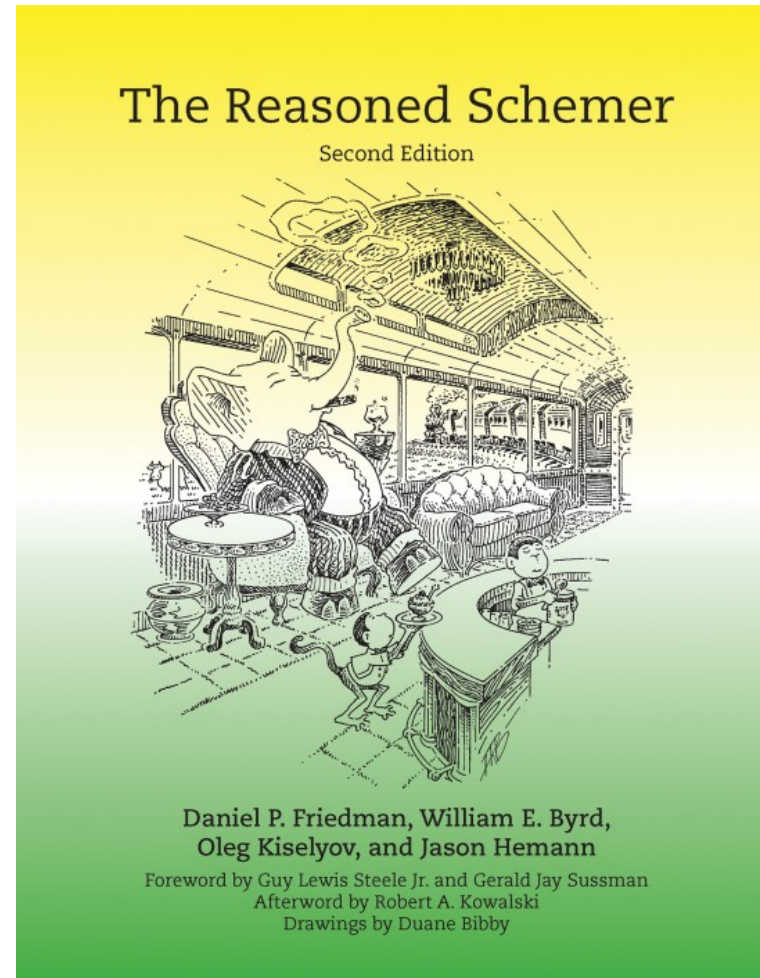
Content

- Background
- Contributions
- The Behavior of Strategies
- The Implementations of Strategies
- Conclusion

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The Reasoned Schemer, 2nd Edition



Commandments for miniKanren Programmers

- Within each sequences of goals, move non-recursive goals before recursive goals
- If your miniKanren program is slow, fiddle with its **cond^e**-lines.

(interleaving DFS, the strategy of  and μ Kanren, has unfair disjunction)

Cases Where We Might Want Other Strategies

- teaching new miniKanren programmers
- writing relational definitions that run in different running modes

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Fairness

- fairness in disjunctions: unfair, almost-fair, fair
- fairness in conjunctions: unfair, fair

Search Strategies

strategy	disj	conj
interleaving DFS	unfair	unfair
balanced interleaving DFS	almost-fair	unfair
fair DFS	fair	unfair
BFS[1]	fair	fair

[1] Seres, Silvija, J. Michael Spivey, and C. A. R. Hoare. "Algebra of Logic Programming." ICLP. 1999.

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(repeat^o x l)

- **x** is an arbitrary term.
- **l** is a list of one or more **x** s.

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```
(defrel (repeato x l)  
  (conde  
    [(== `(,x) l)]  
    [(fresh (res)  
      (== (cons x res) l)  
      (repeato x res))]))
```

`(repeat° x l)`

- `x` is an arbitrary term.
- `l` is a list of one or more `x` s.

```
(defrel (repeat° x l)
  (conde
    [(== `(,x) l)]
    [(fresh (res)
      (== (cons x res) l)
      (repeat° x res))]))
```

```
> (run 3 q
  (repeat° 'λ q))

'((λ) (λ λ) (λ λ λ))
```

Interleaving DFS (Unfair Disjunction)

```
> (run 15 q
  (conde
    [(repeato 'λ q)]
    [(repeato '🐑 q)]
    [(repeato '🐏 q)]
    [(repeato '🐱 q)]
    [(repeato '🐱 q)])))
```

```
' ((λ) (λ λ) (🐑) (λ λ λ) (λ λ λ λ)
   (🐑 🐑) (λ λ λ λ λ) (🐏)
   (λ λ λ λ λ λ) (🐑 🐑 🐑)
   (λ λ λ λ λ λ λ) (λ λ λ λ λ λ λ λ)
   (🐑 🐑 🐑 🐑) (λ λ λ λ λ λ λ λ λ)
   (🐏 🐏))
```

Balanced-interleaving DFS (Almost-fair Disjunction)

```
> (run 15 q
  (conde
    [(repeato 'λ q)]
    [(repeato '🐑 q)]
    [(repeato '🐏 q)]
    [(repeato '🐱 q)]
    [(repeato '🐱 q)])))
```

```
' ((🐑) (🐏) (🐱) (λ)
   (🐑 🐑) (🐏 🐏) (🐱 🐱) (🐱)
   (🐑 🐑 🐑) (🐏 🐏 🐏) (🐱 🐱 🐱) (λ λ)
   (🐑 🐑 🐑 🐑) (🐏 🐏 🐏 🐏) (🐱 🐱 🐱 🐱))
```


Fair DFS & BFS (Fair Disjunction)

```
> (run 15 q
  (conde
    [(repeato 'λ q)]
    [(repeato '🐏 q)]
    [(repeato '🐑 q)]
    [(repeato '🐱 q)]
    [(repeato '🐱 q)])))
```

```
' ((λ) (🐏) (🐑))
  (🐱) (🐱)
  (λ λ) (🐏 🐏) (🐑 🐑)
  (🐱 🐱) (🐱 🐱)
  (λ λ λ) (🐏 🐏 🐏) (🐑 🐑 🐑)
  (🐱 🐱 🐱) (🐱 🐱 🐱) )
```

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Review

- a **goal** is a function from a **state** to a **space**
- a **state** is a way to satisfy some relations
- a (search) **space** is a collection of **state** s

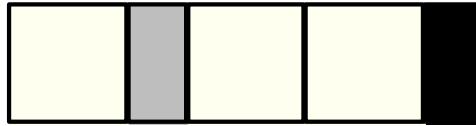
(Search) Space

Space ::= Null | (\rightarrow Space) | (Pair State Space)

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a space with three states



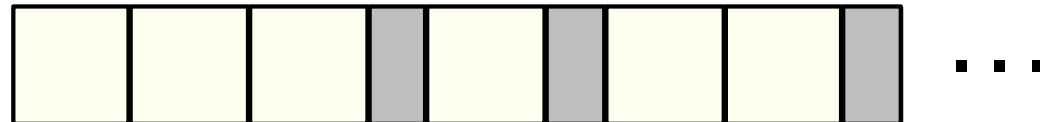
(Search) Space

Space ::= Null | (\rightarrow Space) | (Pair State Space)

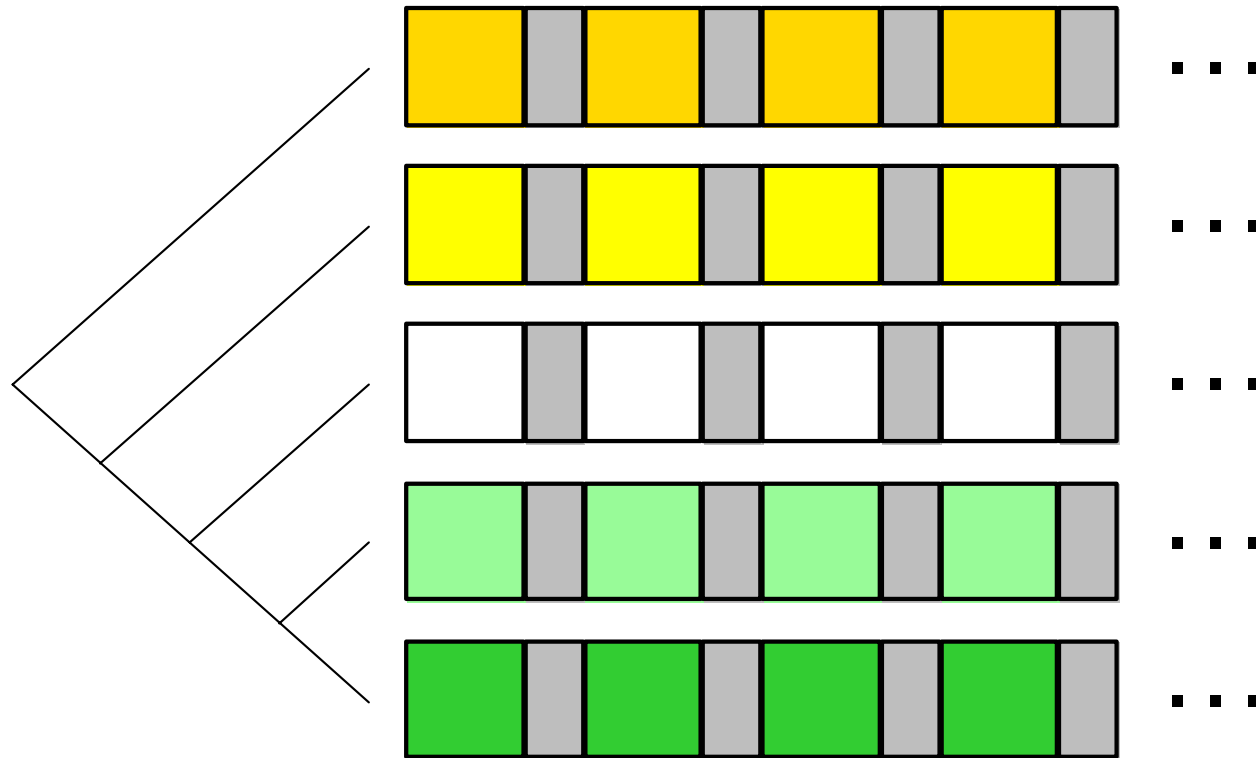
a space with three states



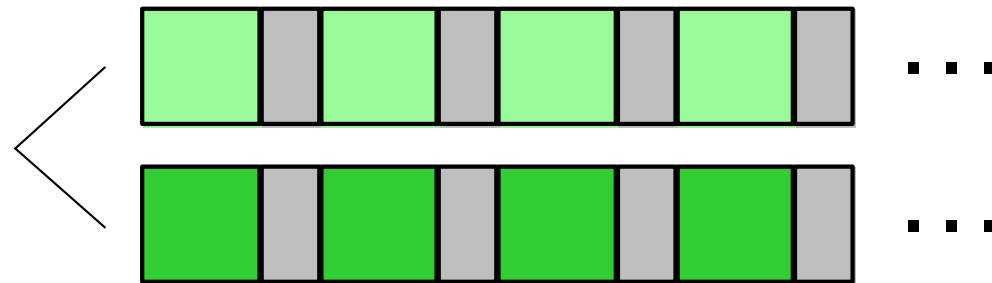
a space with possibly infinite states



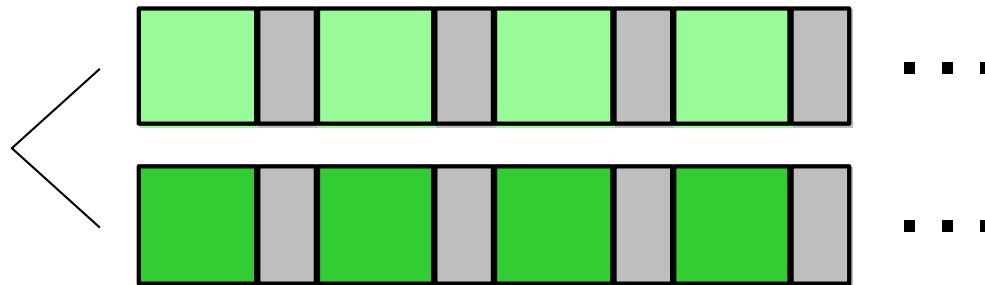
Implementation of Unfair Disjunction



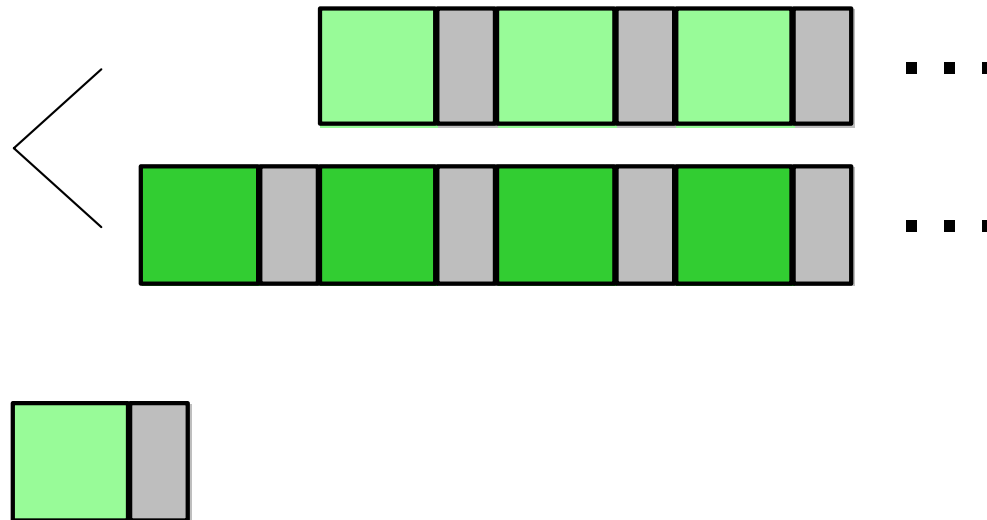
Implementation of Unfair Disjunction



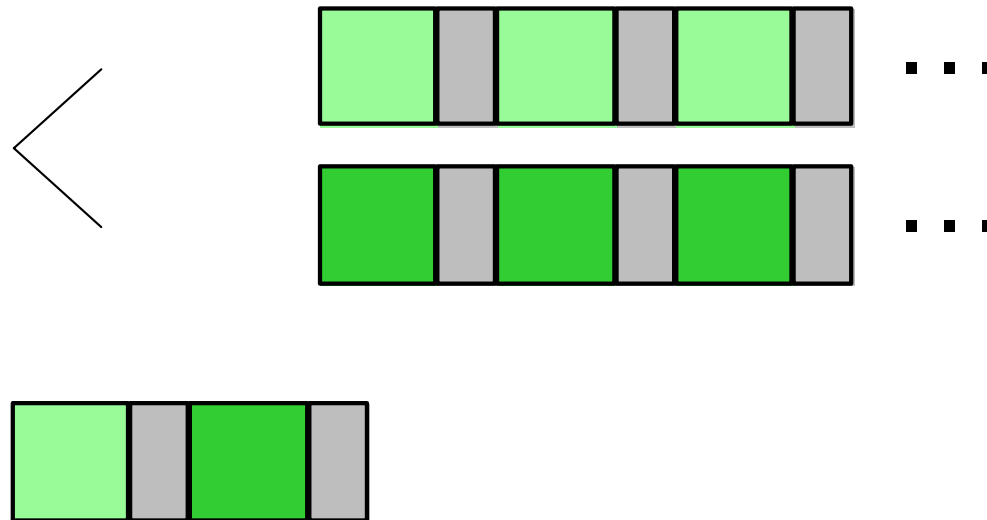
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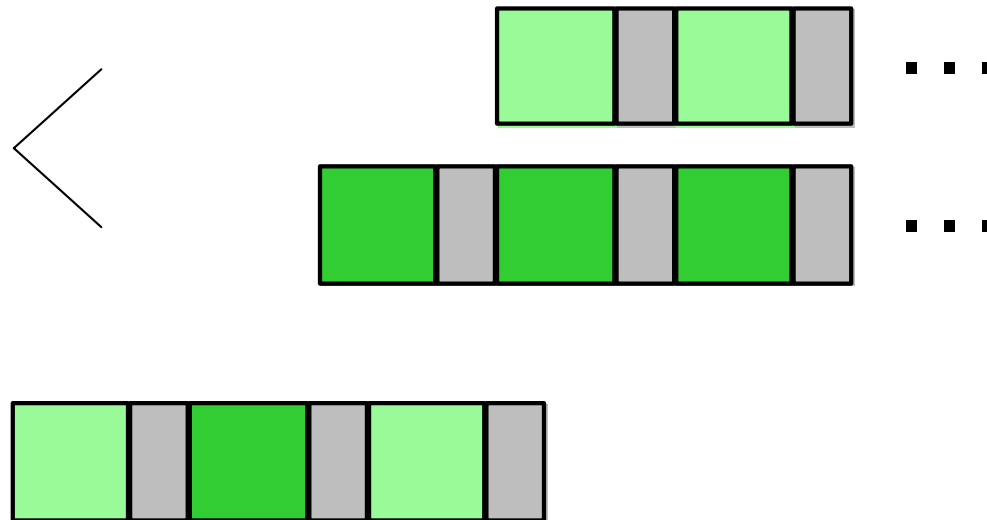
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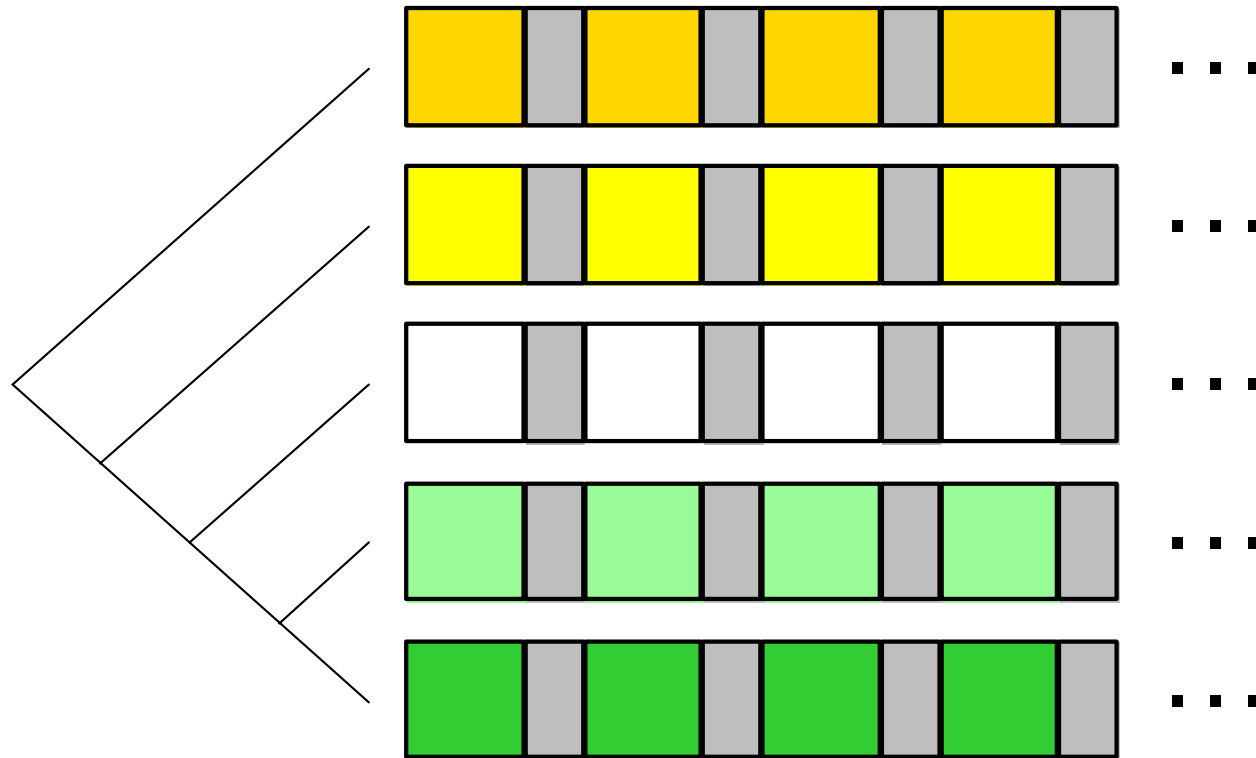
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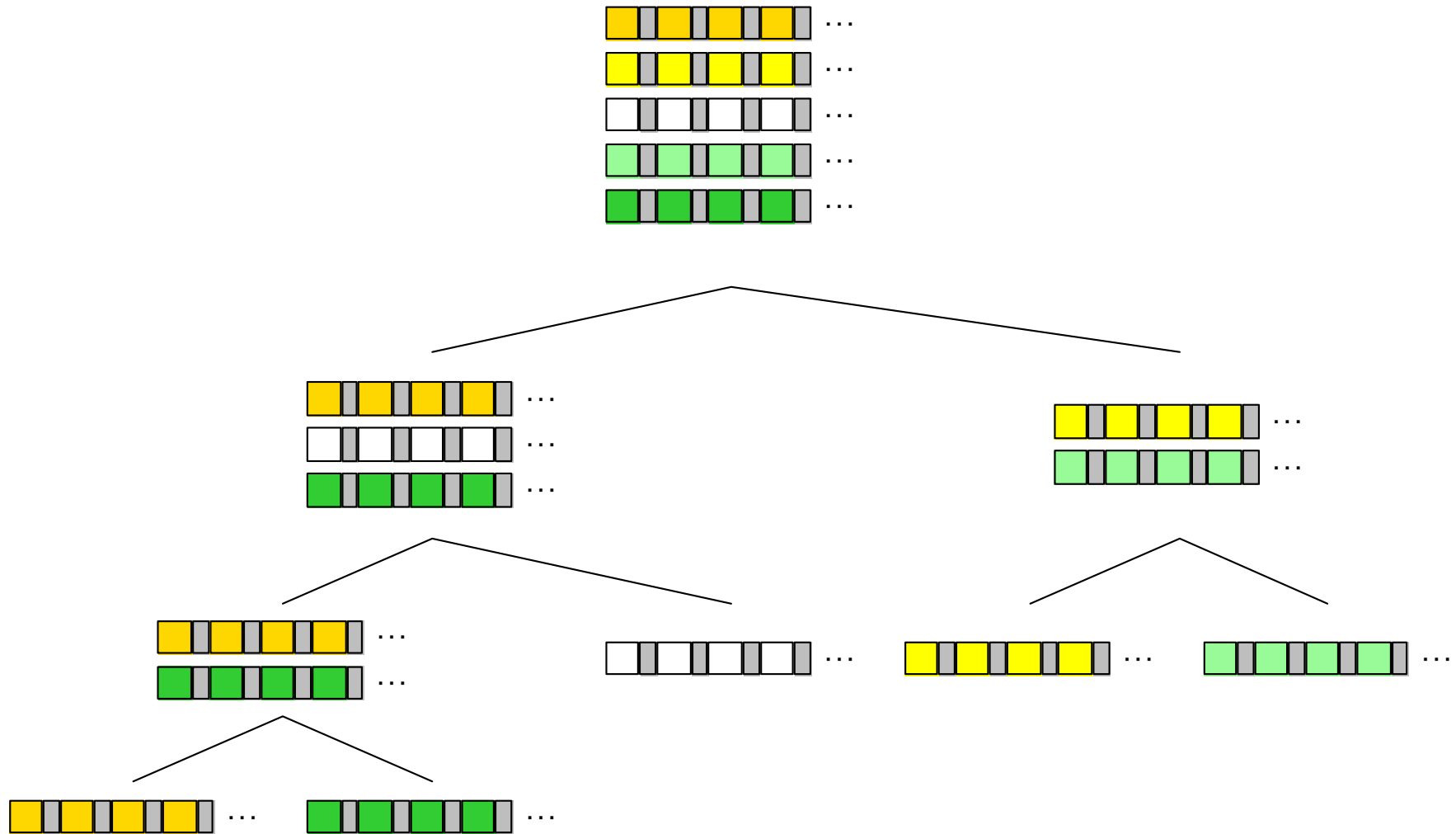


Implementation of Unfair Disjunction



```
(define (append-inf s-inf t-inf)
  (cond
    ((null? s-inf) t-inf)
    ((pair? s-inf)
     (cons (car s-inf)
            (append-inf (cdr s-inf) t-inf)))
    (else (lambda ()
              (append-inf t-inf (s-inf))))))
```

Implementation of Almost-fair Disjunction

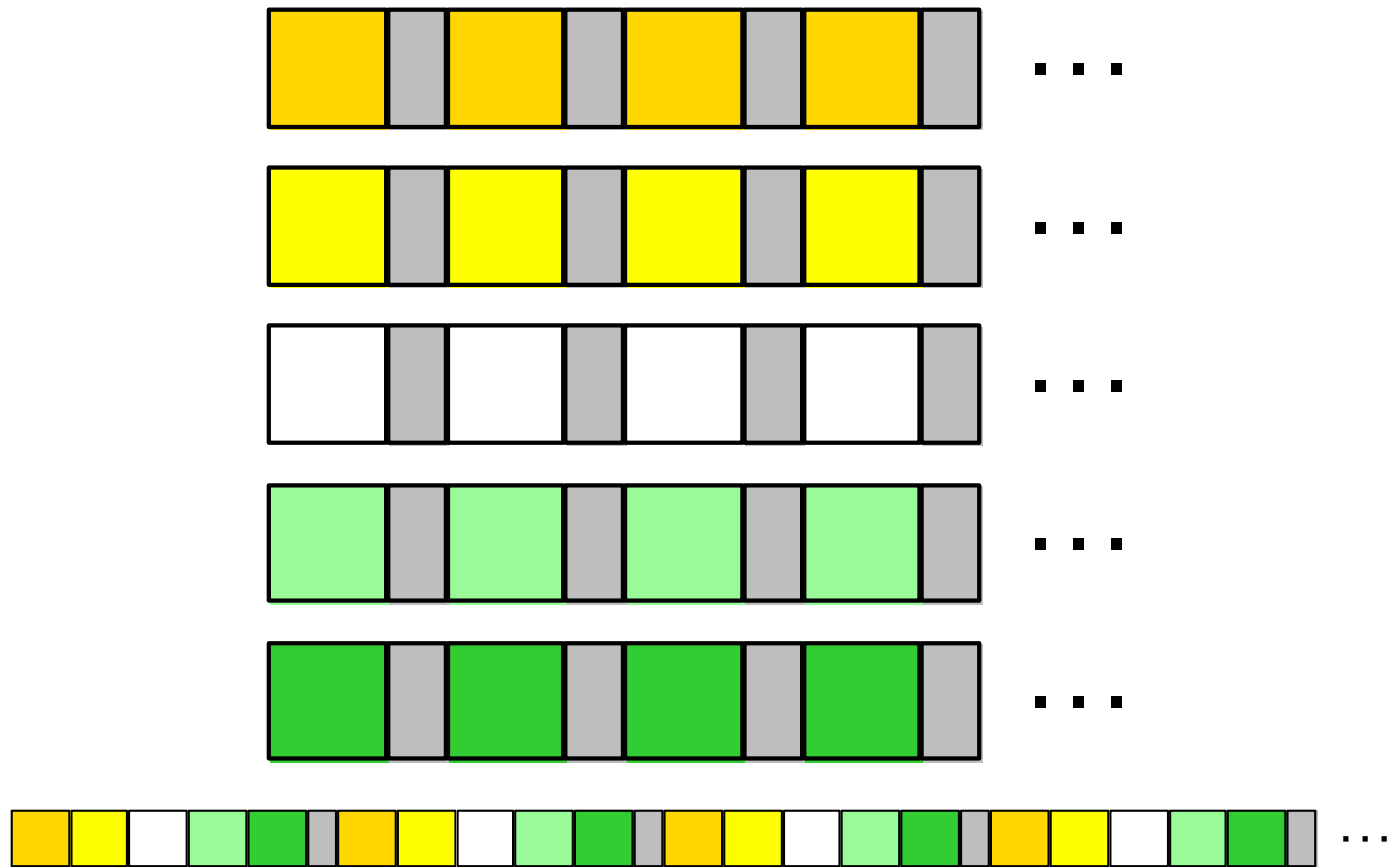


Balanced-interleaving DFS (Almost-fair Disjunction)

```
> (run 15 q
  (conde
    [(repeato 'λ q)]
    [(repeato '🐑 q)]
    [(repeato '🐏 q)]
    [(repeato '🐱 q)]
    [(repeato '🐱 q)])))
```

```
' ((🐑) (🐏) (🐱) (λ)
   (🐑 🐑) (🐏 🐏) (🐱 🐱) (🐱)
   (🐑 🐑 🐑) (🐏 🐏 🐏) (🐱 🐱 🐱) (λ λ)
   (🐑 🐑 🐑 🐑) (🐏 🐏 🐏 🐏) (🐱 🐱 🐱 🐱))
```

Implementation of Fair Disjunction



```
(define (append-inf/fair s-inf t-inf)
  (let loop ((s? #t) (s-inf s-inf) (t-inf t-inf))
    (cond
      ((null? s-inf) t-inf)
      ((pair? s-inf)
       (cons (car s-inf)
              (loop s? (cdr s-inf) t-inf)))
      (s? (loop #f t-inf s-inf))
      (else (lambda ()
                (loop #t (t-inf) (s-inf)))))))
```

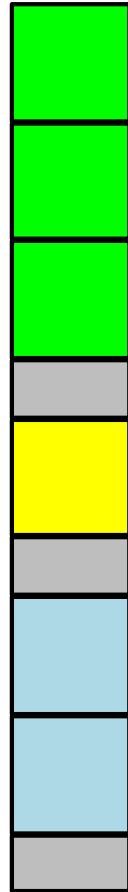
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(define (append-inf/fair s-inf t-inf)
  (let loop ((s? #t) (s-inf s-inf) (t-inf t-inf))
    (cond
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       (cons (car s-inf)
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```

Implementations of Conjunctions

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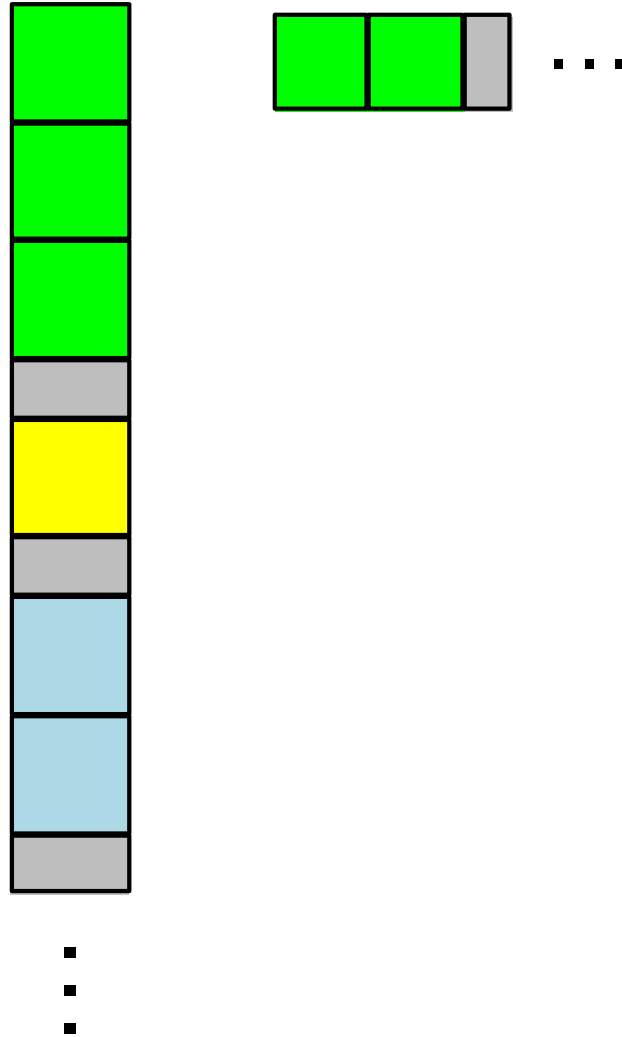
g1 **(conj2 g1 g2)**



⋮

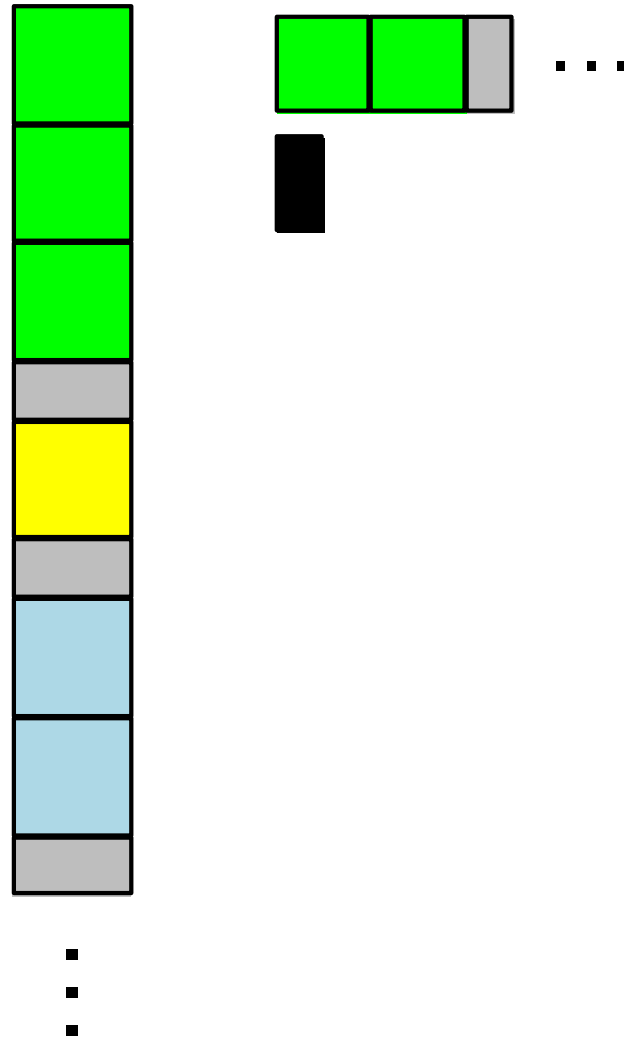
Implementations of Conjunctions

g1 **(conj2 g1 g2)**



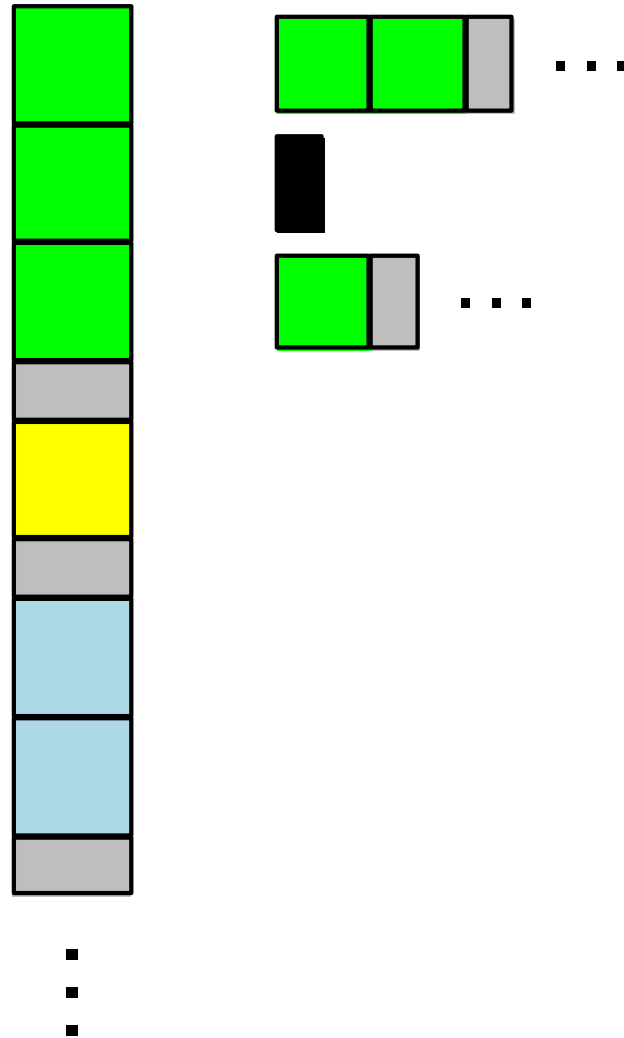
Implementations of Conjunctions

g1 **(conj2 g1 g2)**



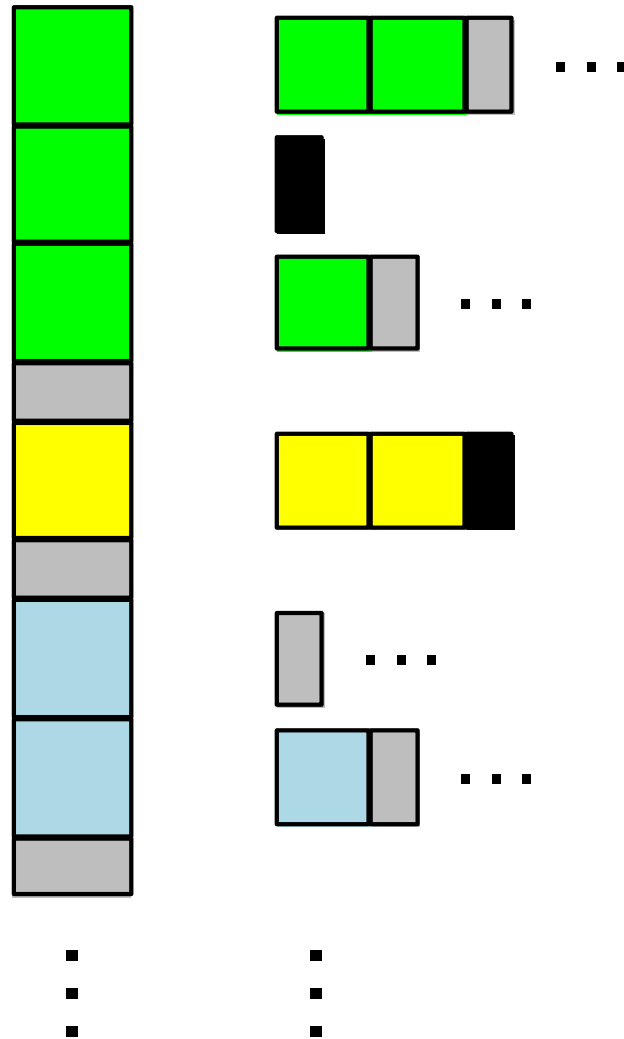
Implementations of Conjunctions

g1 **(conj2 g1 g2)**



Implementations of Conjunctions

g1 **(conj2 g1 g2)**



```
(define (append-map-inf g s-inf)
  (cond
    ((null? s-inf) '())
    ((pair? s-inf)
     (append-inf (g (car s-inf))
                  (append-map-inf g (cdr s-inf))))
    (else (lambda ()
              (append-map-inf g (s-inf))))))
```

```
(define (append-map-inf g s-inf)
  (cond
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     (append-inf (g (car s-inf))
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Quantitative Evaluation

Benchmark	DFS_i	DFS_{bi}	DFS_f	BFS_{imp}	BFS_{ser}
quine-1	41	48	33	-	-
quine-2	72	76	32	-	-
'(I love you)-1	78	70	59	254	605
'(I love you)-2	631	173	61	253	605

Why Fairness?

- resistant to permutation of **cond^e** lines.
 - need not be concerned about line order.
 - one definition for different running modes
- more understandable order of answers

Q & A