

ENGN1218 Introduction to Electronics

Full-wave Rectifier Analysis

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Abstract

A diode-bridge full wave power rectifier circuit was designed and constructed. The aim was to achieve a 12V DC output with 10% tolerance. A theoretical analysis of two types of diode-bridge full-wave rectifiers—with and without a capacitor—was conducted, and results confirmed using a computer simulation. The construction process was documented, and all output parameters measured. The aim was successfully achieved, with all output parameters matching the predicted values within an acceptable error bound.

1 Introduction

Most forms of power are supplied in the form of AC current. As most electronics devices and systems require DC current it is necessary that there be a means to convert AC to DC. Power rectifier circuits allow this and function using diodes, which ideally only allow the passage of current in one direction—typically the positive direction.

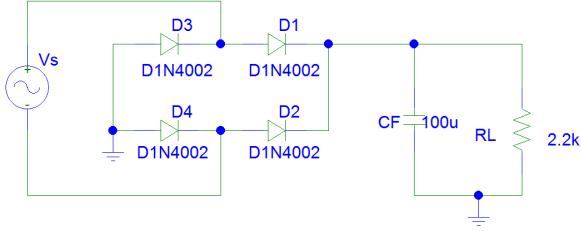
There are several types of rectifier circuits that can be used to convert from AC to DC current but only the full wave rectifier or bridge rectifier will be discussed in this report. The bridge rectifier circuit—as per Figure 1a—is designed such that current during both the negative and positive cycles pass through the load site in the same direction, which means that the voltage across the load site is always of the same sign. Although this configuration of diodes succeeds in inverting the voltage in the negative cycle, the voltage is not the constant DC voltage that is desired. In order to reduce this voltage variation a capacitor is added in series with the load site. The capacitor charges when the voltage from the source is increasing and discharges when the voltage from the source is decreasing, thus smoothing the output waveform.

The analysis of the full-wave rectifier was conducted using multiple techniques, which are detailed in the body of the report. In the theoretical analysis several equations were used to approximate the output and ripple voltages of the voltage across the load resistor in the circuit. These same values were then calculated using a PSPICE simulation. The simulation was also used to observe the effect of various diode malfunctions on the function of the rectifier circuit. In the implementation section, the method used to construct the physical rectifier is described and how

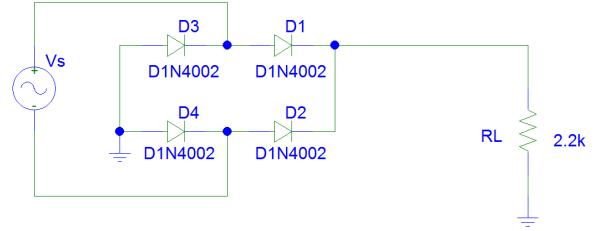
the output and ripple voltages of the load resistor were measured. Photos of the soldered and functioning circuit are also included. The results of each of the analyses are then compared and discussed in the discussion section.

2 Theoretical Analysis

Two versions of a full-wave rectifier circuit were analysed, with and without a smoothing capacitor, schematics shown in Figures 1a and 1b respectively.



(a) Full-wave rectifier with a capacitor filter.



(b) Full-wave rectifier without a capacitor filter.

Figure 1: Schematics.

To predict the output of the rectifier circuit, formulas from the lecture notes were used (Kim). The value for the input voltage V_{in} ¹ was taken to be equal to the actual output of the transformer used during testing (see Section 4). The output voltage of a rectifier without a capacitor filter was calculated in Equation 1, and the voltage ripple and DC voltage output of the rectifier with a smoothing capacitor—in Equations 2 and 3 respectively.

$$\begin{aligned} V_{out} &= V_{in} - 2 \times 0.7 \\ &= 18.8 - 1.4 \\ &= 17.4V \end{aligned} \tag{1}$$

Note that in the above case, in the absence of the smoothing capacitor, $V_r = V_{out}$. The addition of a capacitor has no effect on the output peak voltage, but decreases ripple.

$$\begin{cases} V_r = \frac{V_{DC}}{2fR_L C} \\ V_{DC} = V_{out} - \frac{1}{2}V_r \end{cases} \Leftrightarrow V_r = \frac{2V_{out}}{4fR_L C + 1} = \frac{2 \times 17.4}{4 \times 50 \times 2.2 \times 10^3 \times 10^{-4} + 1} = 0.773V \tag{2}$$

$$\begin{aligned} V_{DC} &= V_{out} - \frac{1}{2}V_r \\ &= 17.4 - \frac{0.773}{2} \\ &= 17.01V \end{aligned} \tag{3}$$

¹Unless explicitly stated otherwise, all AC voltage values are peak-to-peak.

3 Simulation

A series of PSPICE simulations were conducted to verify the validity of the theoretical analysis. The results are recorded in Table 1, and the input against output waveform graph of a full-bridge rectifier (Figure 1a) is shown in Figure 2a.

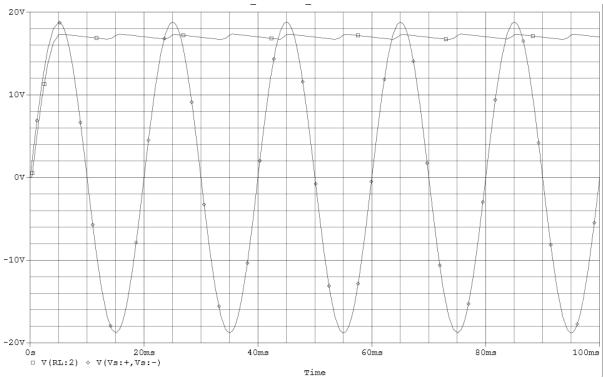
Table 1: Simulation results.

	V_{out}	V_R
Single resistor	17.339V	0.613V
Double resistors	17.332V	1.229V

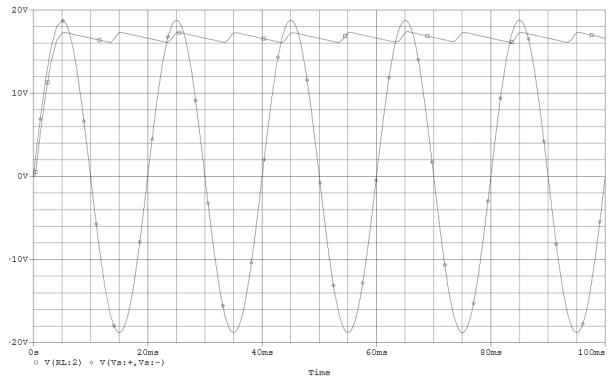
When a second resistor of equivalent resistance was connected in parallel with the load resistor, the result in the PSPICE simulation was a doubling in the magnitude of the ripple voltage. This is to be expected as the result of placing two equivalent resistors in parallel is that the net resistance is halved. (Equation 4). Consequently the RC constant halved—that is the capacitor was able to discharge faster—and as a result the amount that the voltage ripple between peaks was doubled (Figure 2b). This behaviour is described in Equation 5, which shows that peak to peak ripple voltage (V_r) is inversely proportional to RC .

$$\begin{aligned} R_{total} &= \frac{1}{\frac{1}{R} + \frac{1}{R}} \\ &= \frac{R}{2} \end{aligned} \quad (4)$$

$$V_r = \frac{V_{DC}}{2fRC} \quad (5)$$



(a) Normal rectifier with a capacitor.



(b) Rectifier with two parallel load resistors.

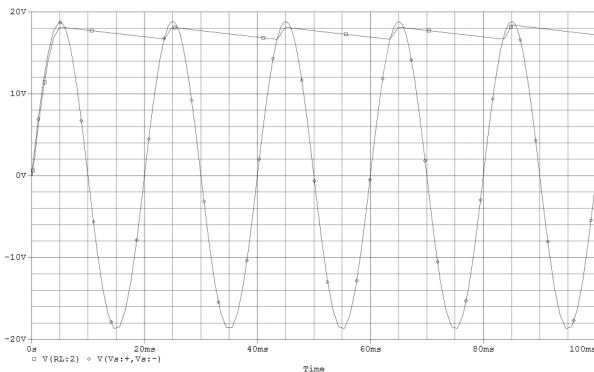
Figure 2: Simulation results.

PSPICE was also used to predict the outcome in the case of a faulty diode. To do this two scenarios were simulated, one in which the diode acts as an open circuit and one in which the diode acts as a short circuit. For these simulations, diode 4 (D4) was varied (Figure 1a).

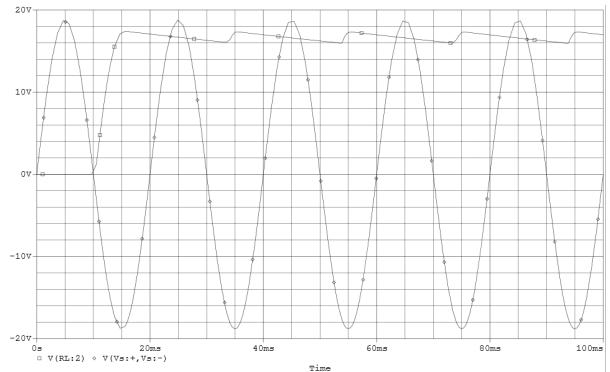
In the short circuit scenario, the rectifier functioned as a half wave rectifier that only permitted the positive half-cycle to flow across the load resistor (Figure 3a). This is because during the negative cycle, a short circuit was created between the negative and positive outputs of the source. That is, as D4 no longer blocked current, current from the negative terminal could flow through D3 and back to the source without passing over the load resistor. During the positive half cycle there is not short circuit as D3 acts as an open circuit with respect to the path of current.

In the open circuit scenario, the circuit functioned as a half wave rectifier that permitted only the negative half-cycle (Figure 3b). This is because during the positive cycle an open circuit between ground and the negative source terminal is produced, preventing current from flowing across the load resistor. However, when functioning normally D4 acts as an open circuit with respect to the path of current during the negative half-cycle and therefore the negative half-cycle is unaffected.

If the same simulations are applied to the other diodes, a faulty D1 has the same effect as D4. D3 and D2 however block the positive cycle when acting as an open circuit and the negative cycle when acting as a short circuit.



(a) Positive half-cycle only.



(b) Negative half-cycle only.

Figure 3: Fault simulation results.

4 Implementation

The rectifier circuit was first built according to Figure 1b, then modified with a smoothing capacitor (Figure 1a), and finally fitted with a voltage regulator, as shown in Figure 4. The completed circuit, with the components labeled, soldered on a PCB can be seen in Figure 5.

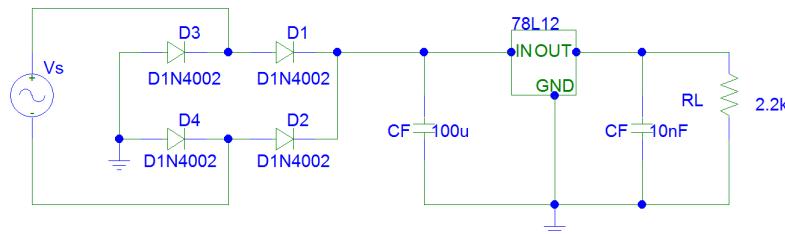
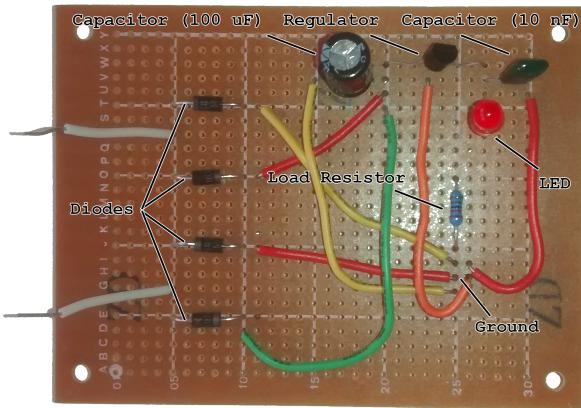
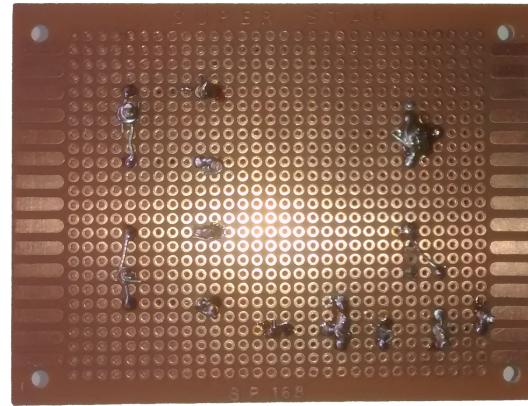


Figure 4: Rectifier with a voltage regulator.



(a) Front.



(b) Back.

Figure 5: Finished circuit.

The measurements taken from the three versions of the circuit are presented in Table 2.

Table 2: Measurements.

	$V_{in}(V)$	$V_{out}(V)$	$V_{DC}(V)$	$V_r(V)$	$R_L(\Omega)$	$f_{out}(\text{Hz})$
no capacitor	18.8	17.4	—	17.4	2197	100
with capacitor	18.8	17.4	16.9	0.7	2197	100
with regulator	18.8	12.1		0.02	2197	100

5 Discussion

6 Conclusion

References

Jon Kim. ENGN1218 intro to electronics: Response of RC and RL circuits. Lecture 11.