Exercise 6
Clustering Algorithms

Distance measurements

Euclidean distance	$d(A, B) = \sqrt{\sum_{i=1}^{n} (A_i - B_i)^2}$
Manhattan distance	$d(A, B) = \sum_{i=1}^{n} \lvert A_i - B_i \rvert$
Hamming distance	$d(A, B) = \#\{ i : A_i \neq B_i \}$

k-means Algorithm:

Inputs: D: Dataset; k: the number of clusters to form;
Outputs: D: Labeled dataset;
Begin
  Randomly choose k instances as centroids.
  Repeat
    Calculate the distance between each instance D[i] and the k centroids;
    Assign each instance D[i] to the cluster closest to its center;
    Calculate the new center of each cluster and modify the centroid;
  Until D[i] is the same as D[i-1]**;**
Return D;
End.

Questions :

Let's ignore the "*Exercise*" and “ep (ms)” and “ID” attributes.

1- Re-use the distance function seen in TP 5.
2- Write a function to calculate the centroid of a set of instances.
3- Write a function to find the cluster to which a given instance is the closest.
4- Implement the k-means algorithm.
5- Test the algorithm with k=2, k=5 and k=6. Suggest an interpretation of the obtained clustering.

Have fun !