

LOgisTIC

Mi



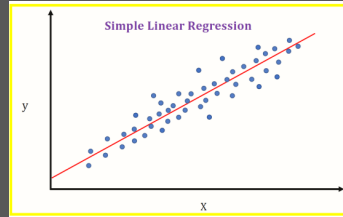
Regression

Discussion classCfication

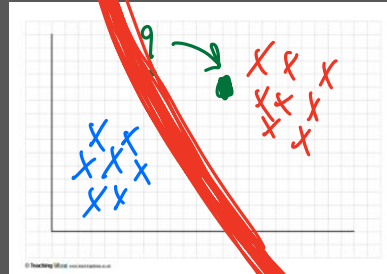
What is logictic regression?

But before that, let's make sure you understand these two terminologies

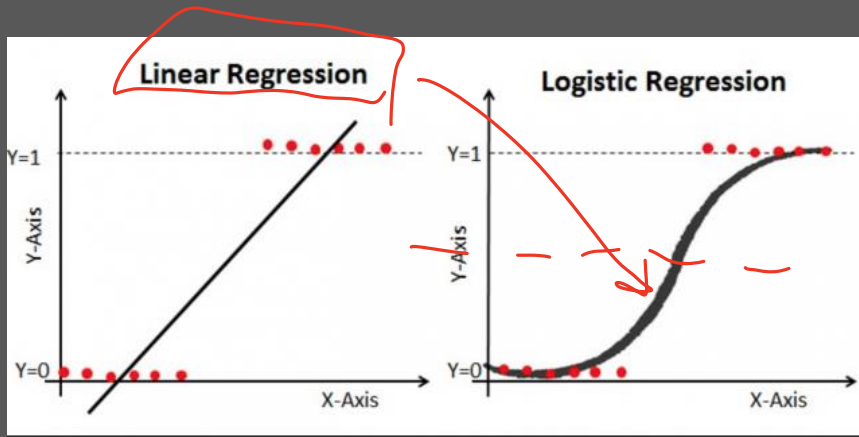
Regression: predicting a continuous quantity output. Basically, finding a trend line



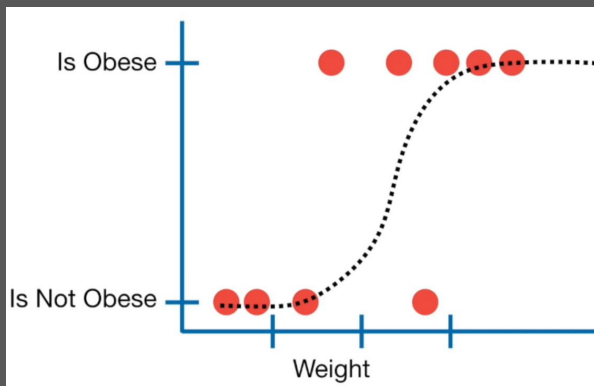
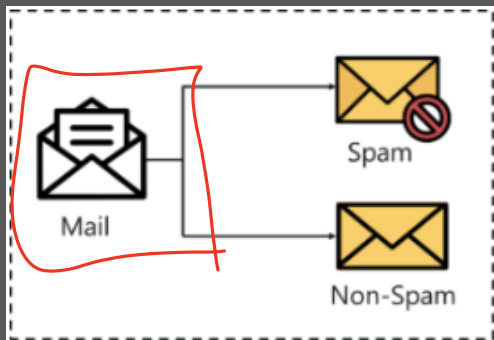
Classification: predicting whether a data belongs to a certain class or not. Basically, find if the output is either in class 0 or class 1



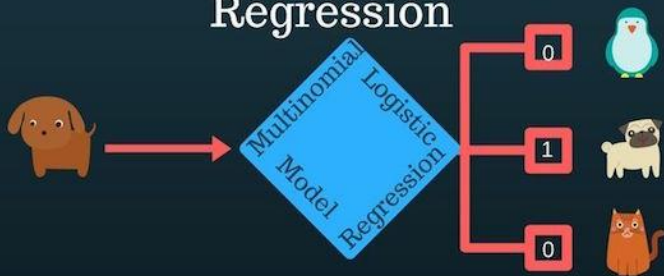
Logistic Regression



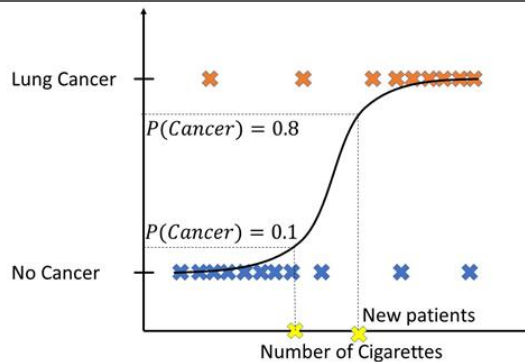
$$f(x) = \beta_0 + \beta_1 x$$



Multinomial Logistic Regression



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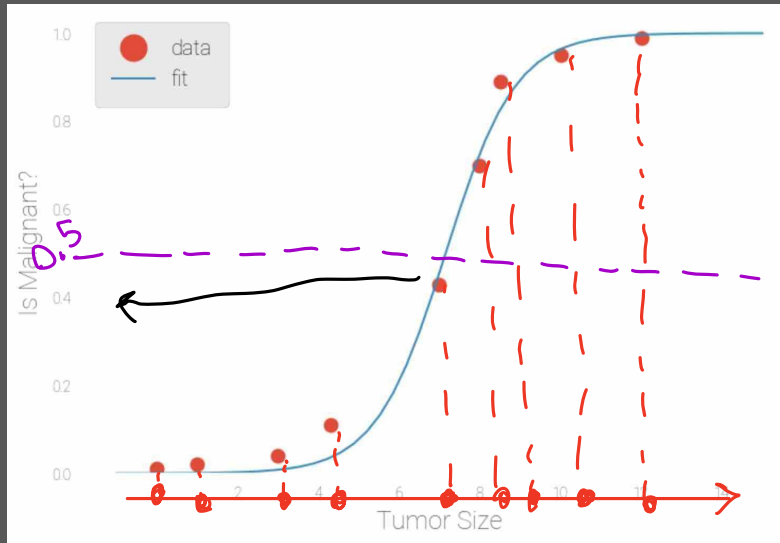


Key idea: given input, which class does this input belong to

Elaboration: given input, what is the probability of this input belongs to class A?

↓
range from $[0, 1]$

Output range is between [0,1]

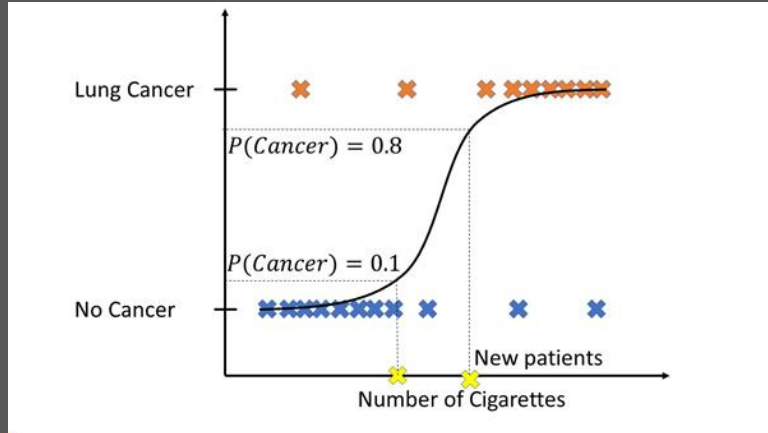


Note: we can optimize the threshold to be something other than 0.5

How to determine whether the tumor is malignant?

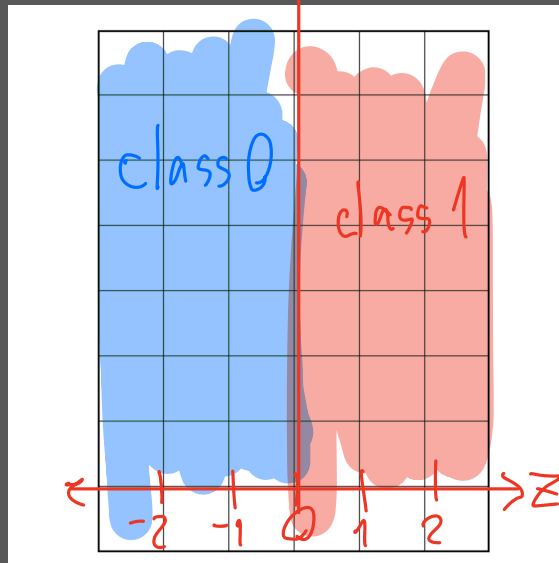
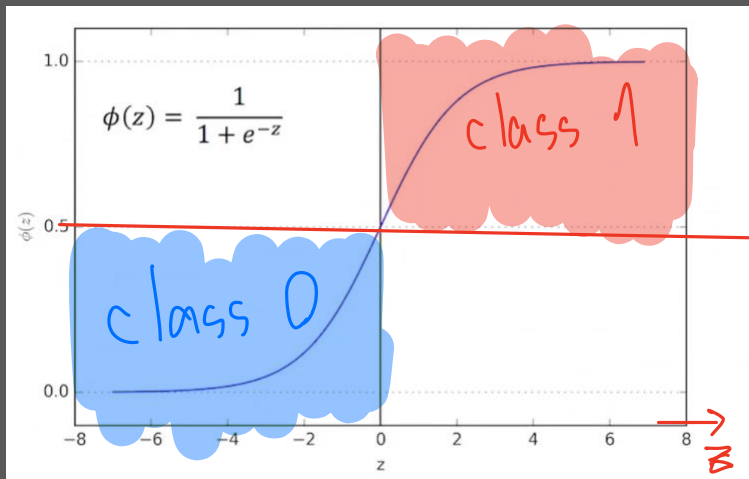
if $y < 0.5 \rightarrow \text{class } 0 \rightarrow \text{benign}$
else $y \geq 0.5 \rightarrow \text{class } 1 \rightarrow \text{malignant}$

Problem: see the “jump gap” here? How can we make the curve?



$$z = f(x) = \beta_0 + \beta_1 x_1$$

Solution: logistic function



So from this, can we classify which class the input belongs to?

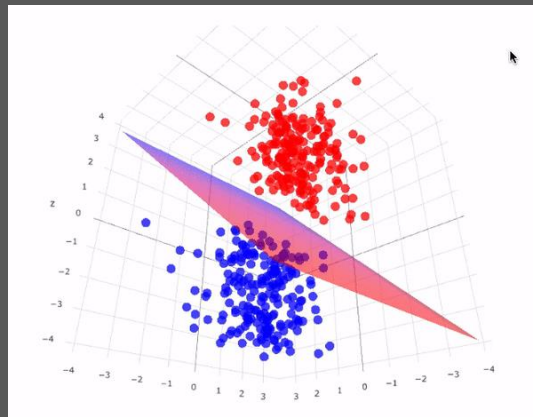
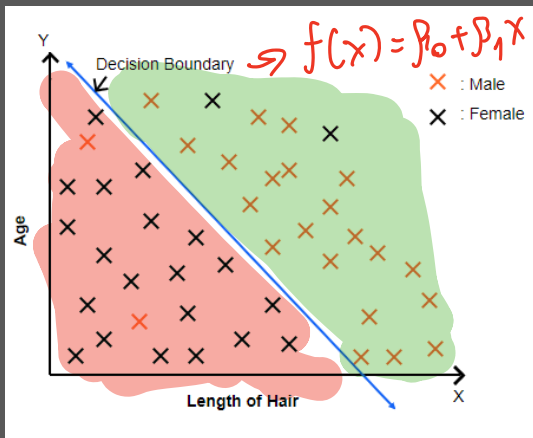
if $z > 0 \rightarrow \phi(z) \geq 0.5 \rightarrow$ belong to class 1

else $z < 0 \rightarrow \phi(z) < 0.5 \rightarrow$ belong to class 0



sion boundary

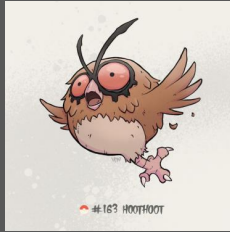
Deoxys



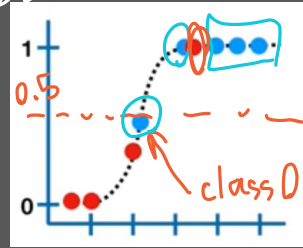
which curve's slope/steepness

Problem: how to we know ~~which model is the~~ best one to classify data?

Solution: Likelihood
(likelihood)



hoothoot



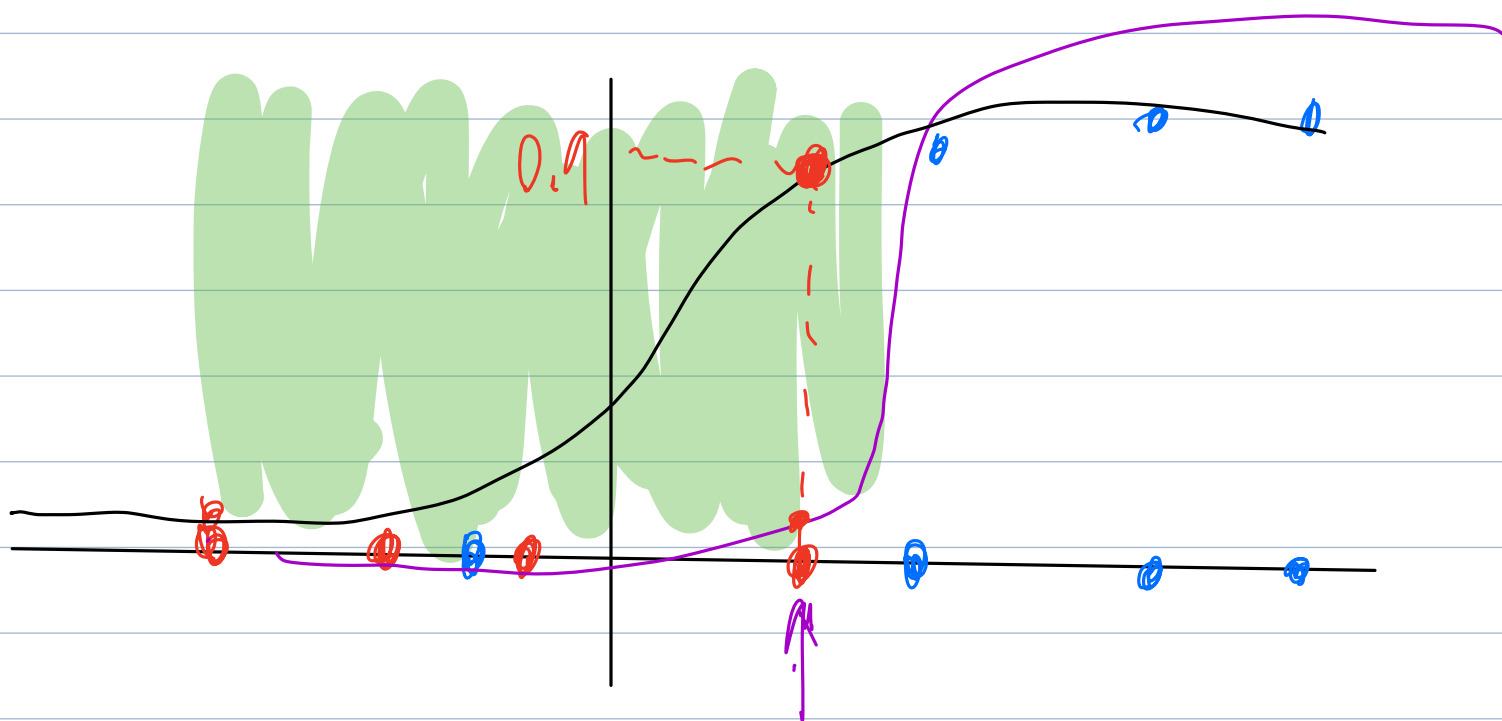
■ = class 1
■ = class 0

$$\begin{aligned} L &= 0.9 \times 0.9 \times 0.9 \\ &\quad \times 0.8 \times 0.4 \\ &\quad \times (1 - 0.1) \times (1 - 0.1) \\ &\quad \times (1 - 0.3) \times \\ &\quad \quad (1 - 0.9) \\ &= 0.013 \end{aligned}$$

$$L = \left[\text{product of } \phi(z_i) \text{ of points in class 1} \right] \times \left[\text{product of } (1 - \phi(z_i)) \text{ of points in class 0} \right]$$

(observed value) (observed value)

Goal: We want to maximize likelihood



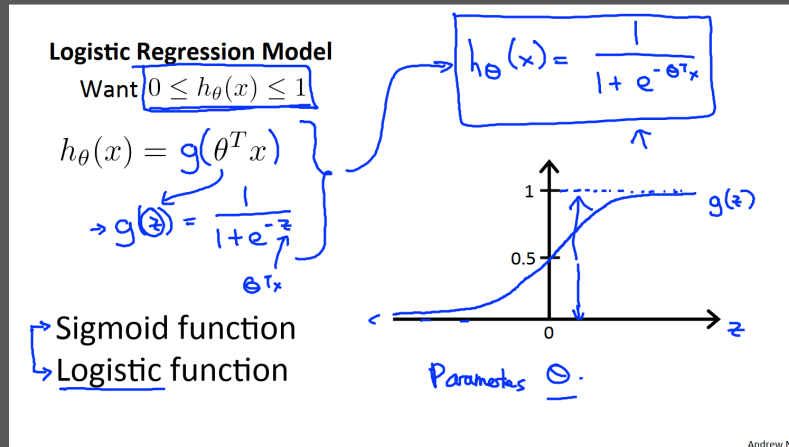
$$\begin{aligned} (1 - 0.1) &\rightarrow 0.9 \\ (1 - 0.9) &\rightarrow 0.1 \end{aligned} \quad \left. \vphantom{\begin{aligned} (1 - 0.1) &\rightarrow 0.9 \\ (1 - 0.9) &\rightarrow 0.1 \end{aligned}} \right\} >$$

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Note: technically, we want to update weight (theta), and we let $z = \text{theta} \cdot x$

$$Z = \beta_1 X + \beta_0$$

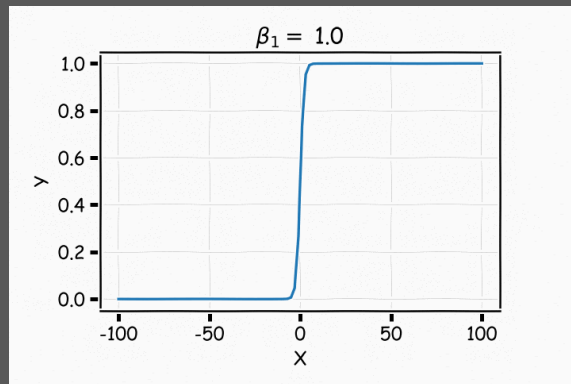
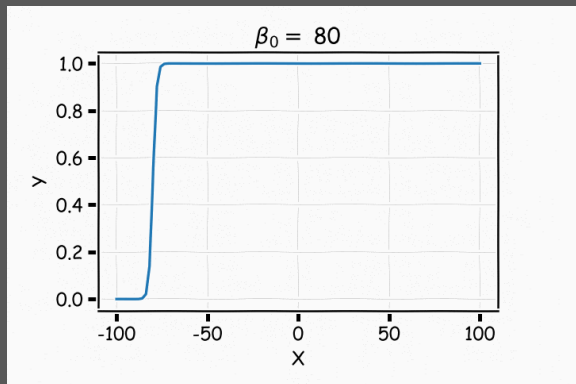
And our x-axis for sigmoid function is Z



Coefficients of the Logistic Function

- β_0 is the intercept
- β_1 is the change in log odds (kind of like slope)

$$P(Y = 1) = \frac{1}{1 + e^{-(\beta_0 + \beta_1 X)}}$$



(stole this page from stephanie's slide)

➡ **In general:** log likelihood is another alternative for finding how well the model performs. It is better than likelihood when we want to find the joint likelihood for each data, and we can simplify taking derivative
(just need to know it's easier to do complex math when working with a log)

➡ To simply put, likelihood is equivalent to logistic regression's cost function

But you know, I learned something today



- Logistic regression is a way to categorize data into a class
- We maximize the likelihood to get the best logistic regression model