Chi-Squared

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```
# Create a data frame with the given data
exam_data <- data.frame(Year = c(1996, 1997, 1998, 1999, 2000, 2001,
                                  2002, 2003, 2004, 2005, 2006, 2007,
                                  2008, 2009, 2010, 2011, 2012, 2013,
                                  2014, 2015),
                         N = c(6964, 7173, 7348, 7311, 7048, 6802,
                               7074, 6751, 7056, 7051, 7006, 7090,
                               7194, 7226, 7335, 7337, 7303, 7482,
                               7601, 7839),
                         PassRate = c(0.82, 0.85, 0.84, 0.85, 0.86,
                                      0.88, 0.87, 0.92, 0.92, 0.92,
                                      0.91, 0.94, 0.91, 0.88, 0.87,
                                      0.84, 0.85, 0.86, 0.87, 0.89) )
head(exam_data)
##
     Year
             N PassRate
## 1 1996 6964
                   0.82
## 2 1997 7173
                   0.85
## 3 1998 7348
                    0.84
## 4 1999 7311
                   0.85
## 5 2000 7048
                   0.86
## 6 2001 6802
                   0.88
# Calculate Pass Count and Fail Count
exam_data$PassCount <- round(exam_data$N * exam_data$PassRate)</pre>
exam_data$FailCount <- exam_data$N - exam_data$PassCount
head(exam_data)
##
     Year
             N PassRate PassCount FailCount
## 1 1996 6964
                    0.82
                              5710
                                        1254
                              6097
                                        1076
## 2 1997 7173
                    0.85
## 3 1998 7348
                   0.84
                              6172
                                        1176
## 4 1999 7311
                   0.85
                              6214
                                        1097
## 5 2000 7048
                   0.86
                              6061
                                         987
## 6 2001 6802
                   0.88
                              5986
                                         816
# Create Contingency Table 1
table1 <- matrix(c(sum(exam_data$PassCount[exam_data$Year < 2003]),</pre>
```

```
sum(exam_data$FailCount[exam_data$Year < 2003]),</pre>
                   sum(exam_data$PassCount[exam_data$Year >= 2003 & exam_data$Year < 2011]),</pre>
                   sum(exam_data$FailCount[exam_data$Year >= 2003 & exam_data$Year < 2011])),</pre>
                 nrow = 2, byrow = TRUE,
                 dimnames = list(c("Pass", "Fail"), c("Before 2003", "2003-2010")))
table1
        Before 2003 2003-2010
##
              42394
                         7326
## Pass
## Fail
              51517
                         5192
# Chi-Squared test
chisq.test(table1)
##
## Pearson's Chi-squared test with Yates' continuity correction
##
## data: table1
## X-squared = 793.98, df = 1, p-value < 2.2e-16
# Create Contingency Table 2
table2 <- matrix(c(sum(exam_data$PassCount[exam_data$Year < 2011]),</pre>
                   sum(exam_data$FailCount[exam_data$Year < 2011]),</pre>
                   sum(exam_data$PassCount[exam_data$Year >= 2011]),
                   sum(exam_data$FailCount[exam_data$Year >= 2011])),
                 nrow = 2, byrow = TRUE,
                 dimnames = list(c("Pass", "Fail"), c("Before 2011", "2011-2015")))
table2
        Before 2011 2011-2015
## Pass
              93911
                        12518
## Fail
              32396
                         5166
# Chi-Squared test
chisq.test(table2)
##
## Pearson's Chi-squared test with Yates' continuity correction
##
## data: table2
## X-squared = 102.02, df = 1, p-value < 2.2e-16
```