

# CSE 12 – Basic Data Structures and Object-Oriented Design

## Lecture 10

Greg Miranda, Fall 2020

# Announcements

- Quiz 10 due Monday @ 9am
- Survey 3 due tonight @ 11:59pm
- PA3 due Wednesday @ 11:59pm → practice → submit after
- Exam 1 next Friday •
  - Released @ 8am on Friday
  - Closes @ 12pm on Saturday
  - More details to be released on Piazza soon

} 28 hours → 60 minutes

# Topics

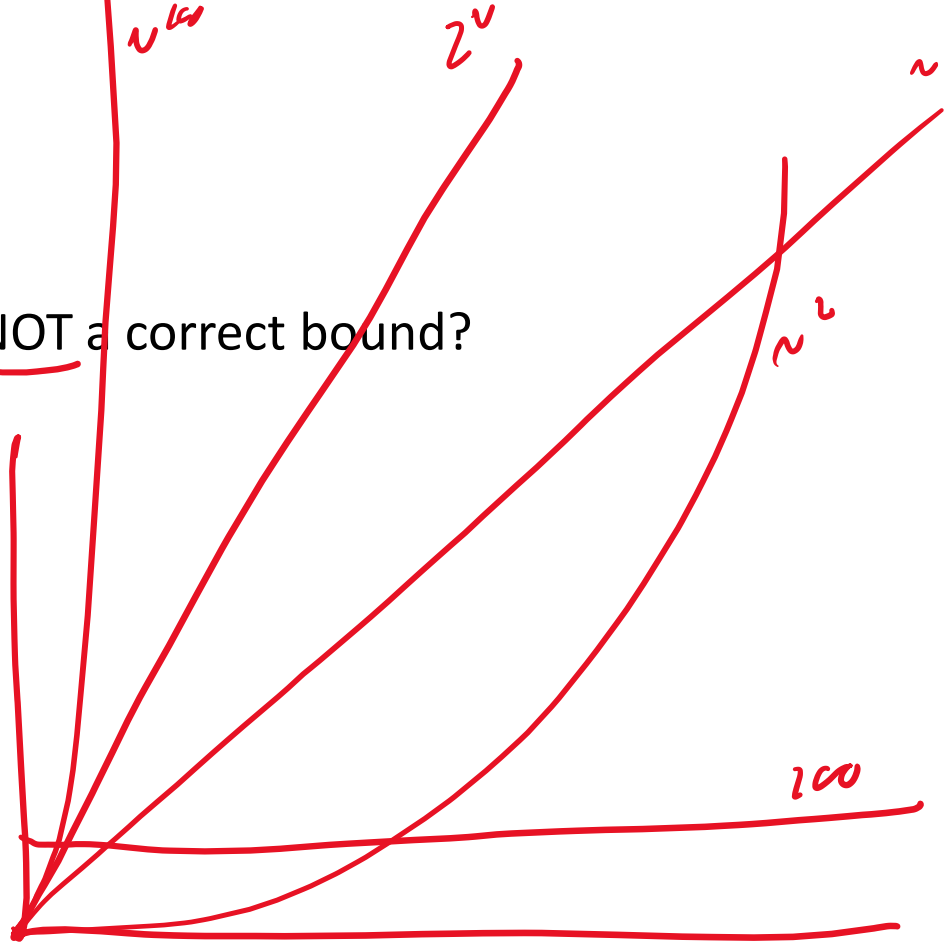
- Questions on Lecture 10?
- Big O

Questions on Lecture 10?

Let  $f(n) = 100$

• Which of the following is NOT a correct bound?

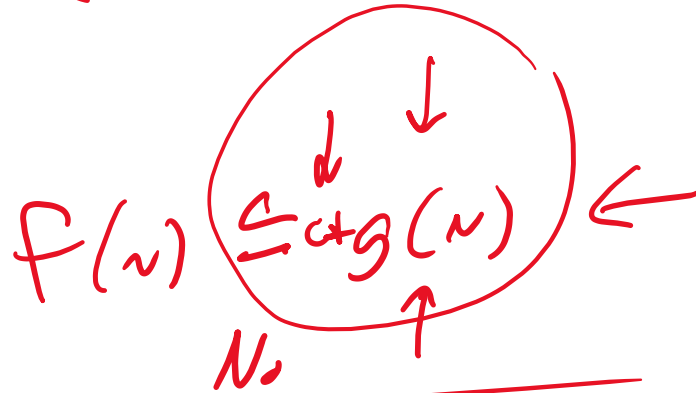
- 2 A.  $f(n)$  is  $O(2^n)$   
B.  $f(n)$  is  $O(n^2)$   
C.  $f(n)$  is  $O(n)$   
D.  $f(n)$  is  $O(n^{100})$   
18 E. None of these



For each function in the list below, it is related to the function below it by  $O$ , and the reverse is **not** true. That is,  $n$  is  $O(n^2)$  but  $n^2$  is **not**  $O(n)$ .

- $f(n) = 1/(n^2)$
- $f(n) = 1/n$
- $f(n) = 1$
- $f(n) = \log(n)$
- $f(n) = \text{sqrt}(n)$
- $f(n) = n$
- $f(n) = n^2$
- $f(n) = n^3$
- $f(n) = n^4$
- ... and so on for constant polynomials ...  $2^{100}$
- $f(n) = 2^n$
- $f(n) = n!$  - factorial
- $f(n) = n^n$

Big  $O$  upper bound  
 Big  $\Omega$  lower bound -  
 Big  $\Theta$  tight bound.



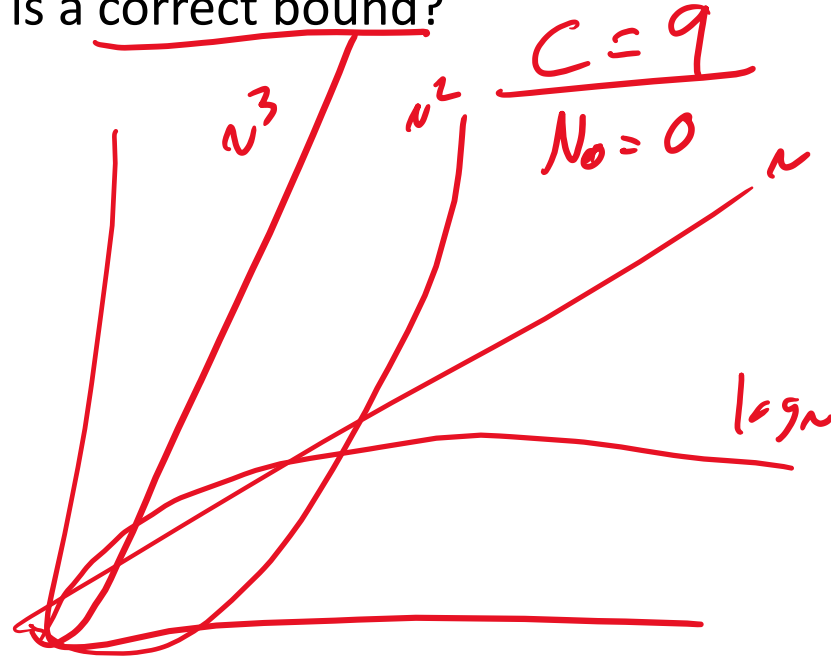
$$f(n) = \underline{3n} \rightarrow O(n) \rightarrow O(n^n) \quad O(n^2)$$

Let  $f(n) = 3n^3 + 2n + 7 \leq$

$3n^3 + 3n^3 + 3n^3 = 9n^3$

• Which of the following is a correct bound?

- A.  $f(n)$  is  $O(\log(n))$ .
- B.  $f(n)$  is  $O(n^2)$ .
- C.  $f(n)$  is  $O(n)$ .
- 19 D.  $f(n)$  is  $O(n^3)$  ←
- E. None of these



```
void printAllElementOfArray(int[] arr) {
    for (int i = 0; i < arr.length; i++) {
        printf("%d\n", arr[i]);
    }
}
```

$$1 + (n+1) + n + n$$

$$(3n) + 2$$

$$3n + 3n = 6n$$

• Which of the following is a correct bound?

- ~~A.  $f(n)$  is  $O(\log(n))$~~
- 1 B.  $f(n)$  is  $O(n^2)$  ✓
- 12 C.  $f(n)$  is  $O(n)$  ✓
- D.  $f(n)$  is  $O(n^3)$  ✓
- 9 E. More than one of these

$$\leq \underline{6n}$$



```

void printAllPossibleOrderedPairs(int arr[]) {
    for (int i = 0; i < arr.length; i++) {
        for (int j = 0; j < arr.length; j++) {
            printf("%d = %d\n", arr[i], arr[j]);
        }
    }
}

```

$$1 + (n+1) + n + \underline{n(1 + (n+1) + n + n)}$$

$$2 + 2n + \underline{n(2 + 3n)}$$

• Which of the following is a correct bound?

- 1 ~~A.~~ f(n) is  $O(\log(n))$
- 4 B. f(n) is  $O(n^2)$  ✓
- 0 ~~C.~~ f(n) is  $O(n)$
- 3 D. f(n) is  $O(n^3)$  ✓
- 15 E. More than one of these

$$2 + 2n + 2n + 3n^2$$

$$\underline{2 + 4n + 3n^2}$$

```
int fibonacci(int num) {
    if (num <= 1) return num;
    return fibonacci(num - 2) + fibonacci(num - 1);
}
```



• Which of the following is a correct bound?

8 A.  $f(n)$  is  $O(2^n)$

1 ~~B.~~  $f(n)$  is  $O(n^2)$

2 ~~C.~~  $f(n)$  is  $O(n)$

1 ~~D.~~  $f(n)$  is  $O(n^3)$

8 ~~E.~~ More than one of these



$$\underline{f(n)} = 1 + \underline{f(n-2)} + \underline{f(n-1)}$$

$$= 1 + (1 + f(n-4) + f(n-3)) + (1 + f(n-3) + f(n-2))$$

4  
8  
16  
32

$$\rightarrow f(n) \rightarrow \underline{2^N}$$