QUESTION 10)

STABILITY

$$\frac{V_{j}^{n+1}}{2} = \frac{\left(V_{j+1}^{n} + V_{j-1}^{n}\right)}{2} - \frac{\Delta k}{\Delta \times} \left(V_{j+1}^{n} - V_{j-1}^{n}\right)$$

 $U_n^k = \overline{V}_n^k + \epsilon_n^k$

$$\Rightarrow \tilde{y}_{j}^{n+1} + \tilde{\epsilon}_{j}^{n+1} = \left(\frac{\tilde{y}_{j+1}^{n} + \tilde{\xi}_{j+1}^{n} + \tilde{y}_{j-1}^{n} + \tilde{\xi}_{j-1}^{n}}{2}\right) - 2\tilde{\Delta}_{x} \left(\tilde{y}_{j+1}^{n} + \tilde{\xi}_{j+1}^{n} - \tilde{y}_{j-1}^{n} - \tilde{\xi}_{j-1}^{n}\right)$$

$$=> \epsilon_{j}^{n+1} = \left(\frac{\epsilon_{j+1}^{n} + \epsilon_{j-1}^{n}}{2}\right) - \frac{c \Delta t}{2 \Delta x} \left(\epsilon_{j+1}^{n} - \epsilon_{j-1}^{n}\right)$$

$$\epsilon_{n}^{k} = e^{-k} e^{ik_{n}n} \quad j \quad c\Delta t = 0$$

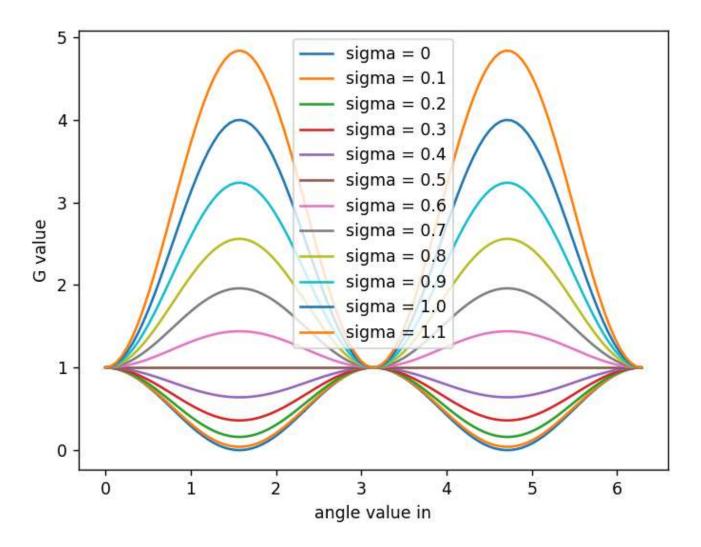
$$\Rightarrow G = \underbrace{\frac{e^{\lambda} - 1}{i}}_{C_{i}} = \underbrace{1}_{V} \underbrace{\left(\frac{e^{\lambda t} e^{iR_{\lambda}(x + \lambda x)}}{e^{\lambda t} e^{iR_{\lambda}(x)}} + \frac{e^{\lambda t} e^{iR_{\lambda}(x + \lambda x)}}{e^{\lambda t} e^{iR_{\lambda}(x)}}\right)}_{C_{i}} - \underbrace{\left(\frac{e^{\lambda t} e^{iR_{\lambda}(x + \lambda x)}}{e^{\lambda t} e^{iR_{\lambda}(x)}} - \frac{e^{\lambda t} e^{iR_{\lambda}(x + \lambda x)}}{e^{\lambda t} e^{iR_{\lambda}(x)}}\right)}_{C_{i}}$$

$$\Rightarrow G = \frac{1}{2} \left(e^{ik_m \Delta x} + e^{-ik_n \Delta x} \right) - G \left(e^{ik_m \Delta x} - e^{ik_m \Delta x} \right)$$

WE SEE ONTHE GRAPH THAT SIGMA SHOULD B

COWER THAN O.S.

$$6 = \frac{C\Delta t}{2\Delta X} = 7 \qquad \frac{C\Delta h}{\Delta x} = CFC < 1$$



ACCU RACK

$$v_{j}^{n+1} = \frac{\left(v_{j+1}^{n} + v_{j-1}^{n}\right)}{2} - \frac{cDt}{2\Delta x} \left(v_{j+1}^{n} - v_{j-1}^{n}\right) \quad (1)$$

$$\int_{J}^{m+1} \mathcal{N}_{J}^{n} + \mathcal{N}_{J}^{n} + \frac{\partial \mathcal{N}_{J}}{\partial \mathcal{N}_{J}} + \frac{\partial \mathcal{N}_{J}}{\partial \mathcal{N}_{J}} + \frac{\partial \mathcal{N}_{J}}{\partial \mathcal{N}_{J}} + \frac{\partial \mathcal{N}_{J}}{\partial \mathcal{N}_{J}} + \dots \quad (2)$$

$$U_{j+1}^{n} = U_{j}^{n} + \Delta \times \frac{\partial u}{\partial x} + \frac{\Delta^{2}}{2} \frac{\partial^{2} u}{\partial x^{2}} + \frac{\Delta^{2}}{6} \frac{\partial^{2} u}{\partial x^{2}} + \dots$$

$$V_{j-1}^{7} = V_{j}^{7} - D \times \frac{\partial u}{\partial x} + \frac{\Delta x^{2}}{2} \frac{\partial^{2} u}{\partial x^{2}} - \frac{\Delta x^{3}}{6} \frac{\partial^{3} u}{\partial x^{3}} + \dots$$

=)
$$v_{j+1}^{n} + v_{j-1}^{n} = 2v_{j}^{n} + 2\frac{\Delta x^{2}}{2}\frac{2u}{\partial x^{2}} + 2\frac{\Delta x^{4}}{24}\frac{2u}{\partial x^{4}} + \dots$$
 (3)

$$=) \frac{1}{2} \frac{1}{120} \frac{1$$

$$= \frac{1}{100} + \frac{$$

$$= \frac{\partial^{2}}{\partial t} = \frac{\Delta x^{2}}{2At} \frac{\partial^{2}}{\partial x} + \frac{\Delta x^{4}}{2ADt} \frac{\partial^{2}}{\partial x^{4}} - \left(\left(\frac{\partial}{\partial x} + \frac{\Delta x^{2}}{6} \frac{\partial^{3}}{\partial x} + \frac{\Delta x^{4}}{2} \frac{\partial^{5}}{\partial x} + \frac{\Delta x^{4}}{2} \frac{\partial^{$$

$$\frac{\partial^{2} + Q_{0}}{\partial x^{2}} = \frac{\Delta x^{2}}{2At} \frac{\partial^{2} v}{\partial x} + \frac{\Delta x^{2}}{2ADt} \frac{\partial^{2} v}{\partial x^{2}} - \left(\frac{\Delta x^{2}}{6} \frac{\partial^{3} v}{\partial x} + \frac{\Delta x^{2}}{100} \frac{\partial^{2} v}{\partial x} + \dots \right) - \frac{\Delta t}{2} \frac{\partial^{2} v}{\partial x} - \frac{\Delta t^{2}}{6} \frac{\partial^{2} v}{\partial x}$$

$$= O\left(\frac{\Delta x^2}{\Delta t}\right) + O(\Delta t) \quad P$$

CONSISTENCY

lin $\frac{\Delta x^{2}}{\partial x} \frac{\partial^{2} u}{\partial x} + \frac{\partial x^{1}}{\partial x} \frac{\partial^{2} u}{\partial x^{2}} - \left(\frac{\Delta x^{2}}{\partial x} \frac{\partial^{3} u}{\partial x} + \frac{\partial x^{4}}{\partial x} \frac{\partial^{2} u}{\partial x} + \frac{\partial x^{2}}{\partial x} \frac{\partial^{2} u}{\partial$