

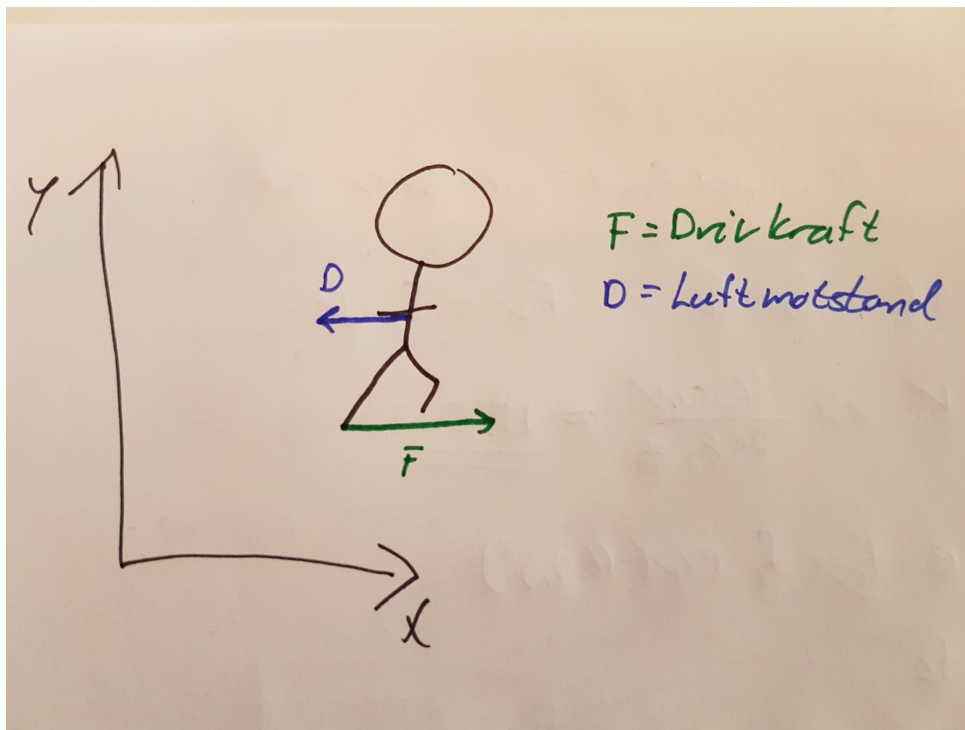
FYS-MEK 1110 Obligatorisk oppgave 1

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Innhold

a)



Figur 1: Free body diagram.

b)

I will start by solving this analytical, then numerical.

$F = ma$ this gives us $a = \frac{F}{m}$ where $F = 400N$, $m = 80kg$

We put this in our equation that gives us

$$a = \frac{400N}{80kg} = 5 \frac{m}{s^2}$$

We know from motion-equations that $x(t) = v_0t + \frac{1}{2}at^2$ The start velocity in this situation is zero ($v_0 = 0$) therefore the equation becomes $x(t) = \frac{1}{2}at^2$ we know **a** so no matter the value of time **t** we can find the position **x(t)**.

Numerical solution is:

```

1 import numpy as np
2
3 F = 400 # Enhhet kgm/s
4 m = 80.0 # Enhhet meter[m]
5 time = 10 # Enhhet sekund[s]
6 dt = 1./100; n = int(time/dt)
7 a = np.zeros(n)
8 x = np.zeros(n)
9 v = np.zeros(n)
10 t = np.zeros(n)
11 v[0] = 0; x[0] = 0
12 for i in range(int(n-1)):
13     a[i] = F/m
14     v[i+1] = v[i] + a[i]*dt
15     x[i+1] = x[i] + v[i+1]*dt
16     t[i+1] = t[i] + dt
17     if x[i+1] > 100:
18         q = i + 1
19         break

```

Here I have used Euler-Cromer method,. I have chosen a time-intervall and I have given my code an objektive to stop the for loop when the runner hits 100 meters.

c)

I will use the motion equation I used in exercise b.

$$x(t) = \frac{1}{2}at^2 \Rightarrow t^2 = \frac{2x}{a} \Rightarrow t = \sqrt{\frac{2x}{a}}$$

To achieve the solution we insert the value of **a** and **x** in the equation above.

$$t = \sqrt{\frac{2 * 100}{5}} \approx 6.3s$$

d)

I will use Newtons 2 law.

$$\sum F = ma$$

$\sum F = Fd - D$ where Fd = driving force and D = air resistance.

$$ma = Fd - D \Rightarrow a = \frac{Fd - D}{m}$$

$D = \frac{1}{2}\rho C_D A(v-w)^2$ (v = velocity and w = velocity of air) and $Fd = 400N$ we insert this in our equation and get that the acceleration is given by

$$a = \frac{400N - \frac{1}{2}\rho C_D A(v-w)^2}{m}$$

e)

```

1 import numpy as np, matplotlib.pyplot as plt
2 from math import *
3
4 F = 400      # kraft Newton[N]
5 m = 80.0     # masse [kg]
6 p = 1.293    # [kg/m^3]
7 A = 0.45     # [m^2]
8 Cd = 1.2     # Drag koeffisienten
9 w = 0        # Luft hastighet
10 time = 8     # Tid sekunder[s]
11 dt = 1./100  #dette er hva jeg har valgt som delta t
12 n = int(time/dt)
13 a = np.zeros(n); t = np.zeros(n)
14 x = np.zeros(n); v = np.zeros(n)
15 x[0] = 0; v[0] = 0 #initial verdien til posisjon og hastighet
16 q = 0
17
18 for i in range(int(n-1)):
19     a[i] = (400 - 0.5*p*Cd*A*(v[i]-w)**2)/m
20     v[i+1] = v[i] + a[i]*dt
21     x[i+1] = x[i] + v[i+1]*dt
22     t[i+1] = t[i] + dt
23     if x[i+1] > 100:
24         q = i + 1
25         break
26
27 plt.subplot(3,1,1)      #lager tre separate grafer i samme plott
28 plt.title( 'Bevegelses diagram' )
29 plt.plot(t[0:q],x[0:q]) #[0:q]=henter tall verdiene fra 0 til q
30 plt.ylabel( 'x [m]' )
31 plt.subplot(3,1,2)
32 plt.plot(t[0:q],v[0:q])
33 plt.ylabel( 'v [m/s]' )
34 plt.subplot(3,1,3)
35 plt.plot(t[0:q],a[0:q])
36 plt.ylabel( 'a [m/s^2]' )
37 plt.xlabel( 't [sekund]' )
38 plt.show()

```

I chose Δt to be small ($\frac{1}{100}$) because my graph would become more accurate. I thought about measurement uncertainty but the assignment tells us that we do not have a test subject. This is therefore only theoretical calculation. You can see my plot in figure 2 on the following page

f)

If we implement `print t[q]` in my code we get the eksakt time the runner used to run 100 m in my modell

$$t[q] = 6.79s$$

g)

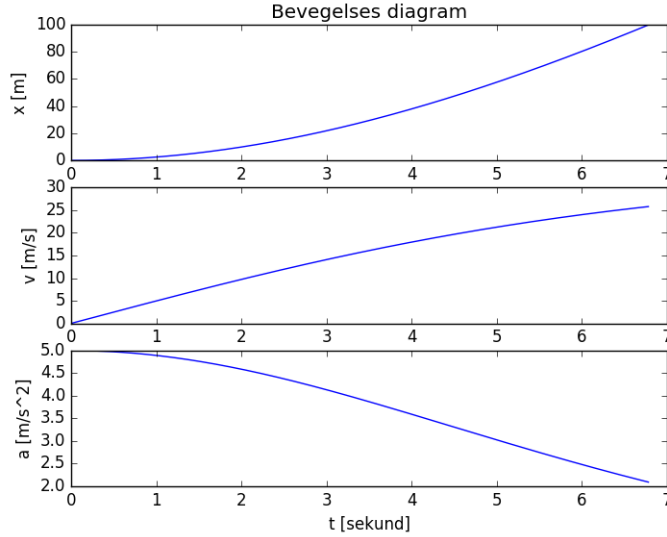


Figure 2: Graphs of $x(t)$, $v(t)$ og $a(t)$

To find the maximum velocity of a runner driven by only these forces we can use $\sum F = Fd - D$ I know that to find the maximum velocity we can use Newtons 1 law. With this we get

$$\sum F = Fd - D = 0 \Rightarrow Fd = D$$

If $D = \frac{1}{2}\rho C_D A(v - w)^2$, $Fd = F$ and $w = 0$ we get

$$F = \frac{1}{2}\rho C_D A v^2 \Rightarrow 2F = \rho C_D A v^2 \Rightarrow v^2 = \frac{2F}{\rho C_D A} \Rightarrow v = \sqrt{\frac{2F}{\rho C_D A}}$$

h)

If the runner is subject only to the forces F and Fv then $\sum Fd = F + Fv$ According to the assignment $Fv = -f_v * v$ where v = velocity. If we apply our previous findings in exercise **g** we find that

$$F = f_v * v \Rightarrow v = \frac{F}{f_v}$$

We know from the exercise that $F = 400N$ and $f_v = 25.8sN/m$ We insert the numbers that we are given. We will then find that his maximum velocity is $v = \frac{400}{25.8} \approx 15.5$

i)

```

1 #i)
2 import numpy as np, matplotlib.pyplot as plt
3
4 F = 400; fc = 488; fv = 25.8 #kreftene som vikrere [N], fv = psykisk ←
   kraft [sN/M]
5 m = 80.0 # [kg]
6 p = 1.293 #luft tetthet
7 A = 0.45 #Arealet til loeperen
8 Cd = 1.2 #Drag koeffisient
9 w = 0 #Luft hastighet
10 time = 10 #tid
11 tc = 0.67 #tids koeffisient som er brukt til aa regne ut funksjoner
12 dt = 1./1000; #tids steg
13 n = int(time/dt)
14 a = np.zeros(n); t = np.zeros(n)
15 x = np.zeros(n); v = np.zeros(n)
16 v[0] = 0; x[0] = 0; t[0] = 0 #initial verdier
17 q = 0 #teller, naar den naar hundre stopper for loopen
18
19 D = lambda t,v: A*(1 - 0.25*np.exp(-(t/tc)**2))*0.5*p*Cd*(v-w)**2 #←
   luftmotstand
20 Fv = lambda v: -v*fV #Psykisk
21 Fc = lambda t: fc*np.exp(-(t/tc)**2) #fra kroket til staande funksjon
22
23 for i in range(int(n-1)):
24     a[i] = (F + Fc(t[i]) + Fv(v[i]) - D(t[i],v[i]))/m
25     v[i+1] = v[i] + a[i]*dt
26     x[i+1] = x[i] + v[i+1]*dt
27     t[i+1] = t[i] + dt
28     if x[i+1] > 100:
29         q = i + 1
30         break
31
32 plt.subplot(3,1,1)
33 plt.title( Bevegelses diagram )
34 plt.plot(t[0:q],x[0:q])
35 plt.ylabel( x [m] )
36 plt.subplot(3,1,2)
37 plt.plot(t[0:q],v[0:q])
38 plt.ylabel( v [m/s] )
39 plt.subplot(3,1,3)
40 plt.plot(t[0:q],a[0:q])
41 plt.ylabel( a [m/s^2] )
42 plt.xlabel( t [sekund] )
43 plt.show()

```

If we look at the figure 3 on the next page we can now see that this simulation is much more realistic.

j)

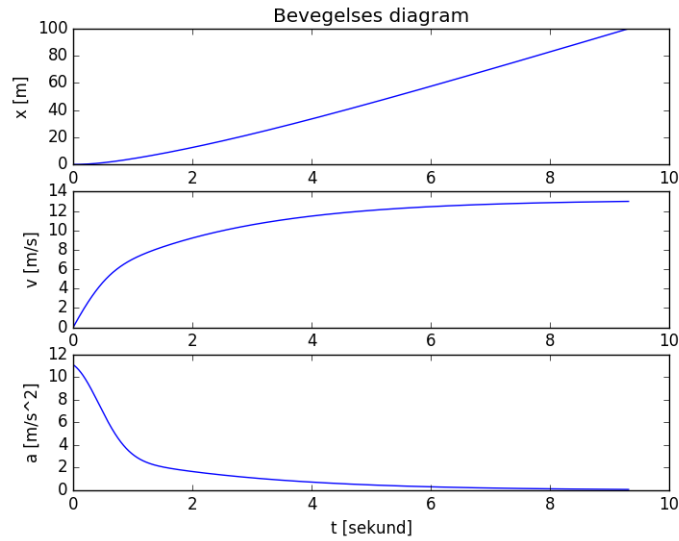
If we set $t[q]$ we find the eksakt time the runner used. According to my numerical solution $t[q] = 9.32$

The runner runs 100 meters in 9.32 seconds. Not bad considering the world record is 9.58s

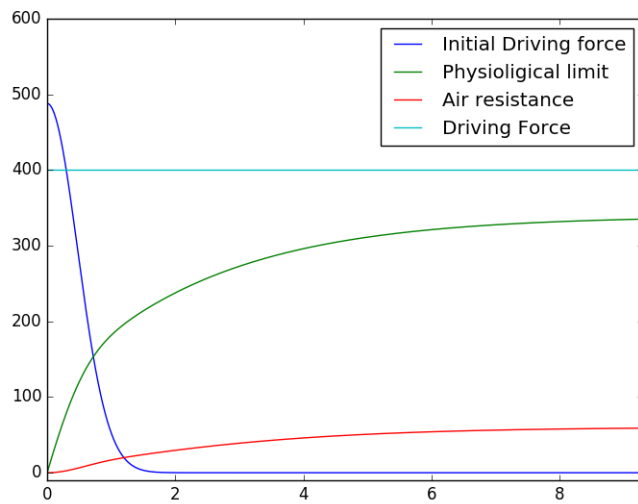
k)

As we can see at figure 4 on the following page the air resistance is slightly getting stronger as the runner is going faster, and the initial driving force is fast canceled out as anticipated. We can see the physiological limit is increasing as time goes by and this is an individual force.

The importance of these forces are great in it's own way. The physiological limit/force is important, because the air resistance is getting stronger the faster



Figur 3: Graphs of $x(t)$, $v(t)$ og $a(t)$



Figur 4: Graphs of the various forces

the person runs, and the person is getting exhausted. So the person needs to be in great shape.

Air resistance in this case is not so important as for instance aviation, or car

paces.

Do not forget the driving force; this is important for the person to move!

1)

If we change $w = \pm 1$ we can see that the result changes with approximately ± 0.1 seconds