

In [6]:

```
import pandas as pd
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import quandl
import scipy.optimize as sco
from scipy.optimize import minimize
from pandas_datareader import data as wb
plt.style.use('fivethirtyeight')
np.random.seed(777)
%matplotlib inline
%config InlineBackend.figure_format = 'retina'
```

In [14]:

```
num_stocks = int(input("Number of stocks in the portfolio?"))

number = ['first', 'second', 'third', 'fourth', 'fifth', 'sixth', 'seventh', 'eighth', 'ninth', 'tenth']
stocks = []

for num in range (num_stocks):
    stocks.append(input("Name of the " + number[num] + " stock?"))
print(stocks)
```

```
Number of stocks in the portfolio?10
Name of the first stock?AA
Name of the second stock?AAPL
Name of the third stock?CSCO
Name of the fourth stock?CVS
Name of the fifth stock?DIS
Name of the sixth stock?GOOGL
Name of the seventh stock?JPM
Name of the eighth stock?MSFT
Name of the ninth stock?V
Name of the tenth stock?WFC
['AA', 'AAPL', 'CSCO', 'CVS', 'DIS', 'GOOGL', 'JPM', 'MSFT', 'V', 'WFC']
```

In [15]:

```
investment_duration = float(input('How many years would this portfolio investment hold? (can be fraction)'))
expected_daily_returns = []
for num in range(num_stocks):
    expected_daily_returns.append(float(input("The expected return of " + number[num] + " stock?")))

return_target = float(input("What is the target return in the investment period?"))
expected_annual_returns = [i*252 for i in expected_daily_returns]
print("Expected annual return: " + str(expected_annual_returns))
```

```
How many years would this portfolio investment hold? (can be fraction)
0.5
The expected return of AA in the investment period?0.23
The expected return of AAPL in the investment period?0.10
The expected return of CSCO in the investment period?0.07
The expected return of CVS in the investment period?0.15
The expected return of DIS in the investment period?0.044
The expected return of GOOGL in the investment period?0.055
The expected return of JPM in the investment period?0.13
The expected return of MSFT in the investment period?0.06
The expected return of V in the investment period?0.037
```

The expected return of WFC in the investment period?0.14  
 What is the target return in the investment period?0.11  
 Expected annual return: [0.46, 0.2, 0.14, 0.3, 0.088, 0.11, 0.26, 0.12, 0.074, 0.28]

```
In [16]: rf = float(input('What is the term risk-free rate for the investment p

What is the term risk-free rate for the investment period?0.03
```

```
In [70]: table = pd.DataFrame()
# Get data from yahoo source:
for i in stocks:
    stock_temp =wb.DataReader(i, data_source='yahoo',start='2019-3-1',
    table[i] = stock_temp['Adj Close']

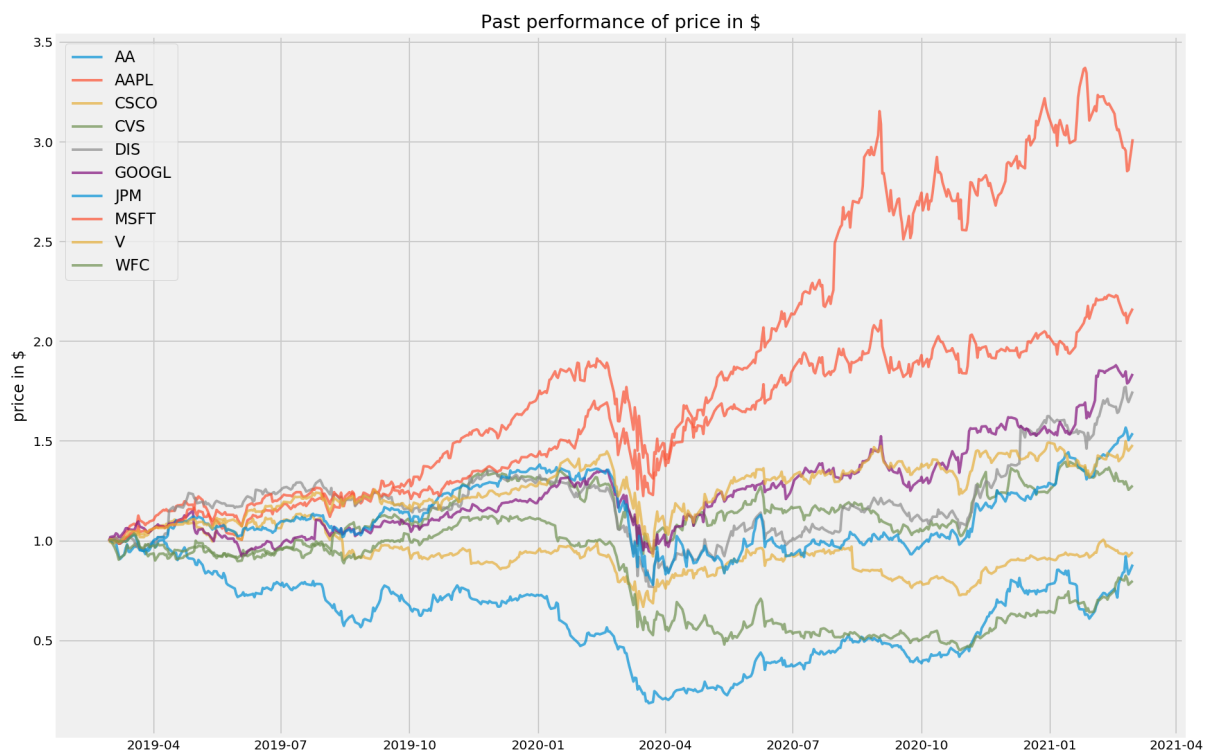
table_rf = table.copy()
table_rf['rf'] = rf
table.head()
```

```
Out[70]:
```

	AA	AAPL	CSCO	CVS	DIS	GOOGL	
<b>Date</b>							
<b>2019-02-28</b>	29.500000	42.399570	48.310696	54.246674	111.477608	1126.550049	97.17
<b>2019-03-01</b>	29.660000	42.845234	47.974754	54.528080	112.633484	1148.520020	97.23
<b>2019-03-04</b>	29.160000	43.060719	47.741455	52.492531	112.949623	1153.420044	97.0
<b>2019-03-05</b>	29.200001	42.982357	47.872097	51.554497	112.623604	1169.189941	96.93
<b>2019-03-06</b>	28.250000	42.735043	48.217377	50.653980	113.463341	1164.939941	96.57

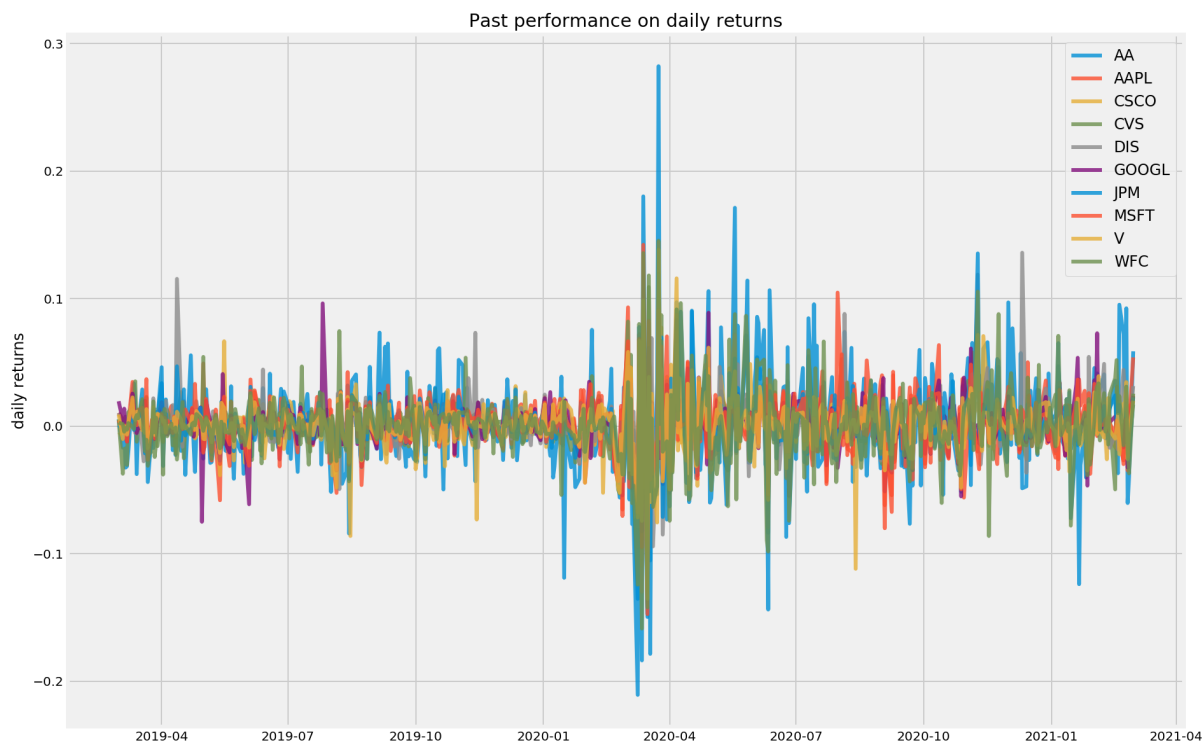
```
In [71]: plt.figure(figsize=(14, num_stocks))
for c in table.columns.values:
    plt.plot(table.index, table[c]/table.loc[table.index[0],c], lw=2,
plt.legend(loc='upper left', fontsize=12)
plt.ylabel('price in $')
plt.title('Past performance of price in $')
```

```
Out[71]: Text(0.5, 1.0, 'Past performance of price in $')
```



```
In [72]:
returns = table.pct_change()
plt.figure(figsize=(14, num_stocks))
for c in returns.columns.values:
    plt.plot(returns.index, returns[c], lw=3, alpha=0.8, label=c)
plt.legend(loc='upper right', fontsize=12)
plt.ylabel('daily returns')
plt.title('Past performance on daily returns')
```

```
Out[72]: Text(0.5, 1.0, 'Past performance on daily returns')
```



```
In [73]:
def portfolio_annualised_performance(weights, mean_returns, cov_matrix):
    returns = np.sum(mean_returns*weights ) *252
    std = np.sqrt(np.dot(weights.T, np.dot(cov_matrix, weights))) * np
```

```

    return std, returns

def random_portfolios(num_portfolios, mean_returns, cov_matrix, risk_free_rate):
    results = np.zeros((3, num_portfolios))
    weights_record = []
    for i in range(num_portfolios):
        weights = np.random.random(num_stocks)
        weights /= np.sum(weights)
        weights_record.append(weights)
        portfolio_std_dev, portfolio_return = portfolio_annualised_performance(
            mean_returns, cov_matrix, weights, num_stocks, risk_free_rate)
        results[0,i] = portfolio_std_dev
        results[1,i] = portfolio_return
        results[2,i] = (portfolio_return - risk_free_rate) / portfolio_std_dev
    return results, weights_record

```

In [74]:

```

returns = table.pct_change()
mean_returns = returns.mean()
cov_matrix = returns.cov()
expected_returns = pd.Series(expected_daily_returns, index = stocks)

returns_rf = returns.copy()
returns_rf['rf'] = rf/252
mean_returns_rf = returns_rf.mean()
cov_matrix_rf = returns_rf.cov()

expected_returns_rf = expected_returns.copy()
expected_returns_rf['rf'] = rf/252

num_portfolios = 100000
risk_free_rate = rf

print("mean_return(daily) in the past 2 years:")
print(mean_returns)
print('\n')
print("expected_returns(daily) in the investment period:")
print(expected_returns)
type(mean_returns)

```

mean\_return(daily) in the past 2 years:

```

AA      0.000606
AAPL    0.002471
CSCO    0.000118
CVS     0.000699
DIS     0.001408
GOOGL   0.001418
JPM     0.001189
MSFT    0.001763
V       0.000996
WFC     -0.000005
dtype: float64

```

expected\_returns(daily) in the investment period:

```

AA      0.001825
AAPL    0.000794
CSCO    0.000556
CVS     0.001190
DIS     0.000349
GOOGL   0.000437

```

```
JPM      0.001032
MSFT     0.000476
V        0.000294
WFC      0.001111
dtype: float64
```

Out[74]: pandas.core.series.Series

```
In [75]: def neg_sharpe_ratio(weights, mean_returns, cov_matrix, risk_free_rate,
    p_var, p_ret = portfolio_anualised_performance(weights, mean_returns, cov_matrix, risk_free_rate, p_var, p_ret)
    return -(p_ret - risk_free_rate) / p_var

def max_sharpe_ratio(mean_returns, cov_matrix, risk_free_rate):
    num_assets = len(mean_returns)
    args = (mean_returns, cov_matrix, risk_free_rate)
    constraints = ({'type': 'eq', 'fun': lambda x: np.sum(x) - 1})
    bound = (0.0, 2.0)
    bounds = tuple(bound for asset in range(num_assets))
    result = sco.minimize(neg_sharpe_ratio, num_assets*[1./num_assets], method='SLSQP', bounds=bounds, constraints=constraints)
    return result
```

```
In [76]: def portfolio_volatility(weights, mean_returns, cov_matrix):
    return portfolio_anualised_performance(weights, mean_returns, cov_matrix, risk_free_rate, p_var, p_ret)

def min_variance(mean_returns, cov_matrix):
    num_assets = len(mean_returns)
    args = (mean_returns, cov_matrix)
    constraints = ({'type': 'eq', 'fun': lambda x: np.sum(x) - 1})
    bound = (0.0, 2.0)
    bounds = tuple(bound for asset in range(num_assets))

    result = sco.minimize(portfolio_volatility, num_assets*[1./num_assets], method='SLSQP', bounds=bounds, constraints=constraints)
    return result
```

```
In [77]: def efficient_return(mean_returns, cov_matrix, target, rf = False):
    num_assets = len(mean_returns)
    args = (mean_returns, cov_matrix)

    def portfolio_return(weights):
        return portfolio_anualised_performance(weights, mean_returns, cov_matrix, risk_free_rate, p_var, p_ret)

    constraints = ({'type': 'eq', 'fun': lambda x: portfolio_return(x) - target},
                   {'type': 'eq', 'fun': lambda x: np.sum(x) - 1})

    if rf == True:
        bounds = tuple((0, 2) for asset in range(num_assets-1)) + tuple((0, 1) for asset in range(num_assets-1, num_assets))
    else:
        bounds = tuple((0, 2) for asset in range(num_assets))

    result = sco.minimize(portfolio_volatility, num_assets*[1./num_assets], method='SLSQP', bounds=bounds, constraints=constraints)
    return result
```

```
def efficient_frontier(mean_returns, cov_matrix, returns_range, rf = 0.01):
    efficient_returns = []
    for ret in returns_range:
        efficient_returns.append(efficient_return(mean_returns, cov_matrix, rf, ret))
    return efficient_returns
```

In [78]:

```
def display_simulated_ef_with_random(mean_returns, cov_matrix, num_portfolios, rf, return_target):
    results, weights = random_portfolios(num_portfolios, mean_returns, cov_matrix, rf)

    max_sharpe_idx = np.argmax(results[2])
    sdp, rp = results[0, max_sharpe_idx], results[1, max_sharpe_idx]
    max_sharpe_allocation = pd.DataFrame(weights[max_sharpe_idx], index=table.index, columns=table.columns)
    max_sharpe_allocation.allocation = [round(i*100, 2) for i in max_sharpe_allocation.allocation]
    max_sharpe_allocation = max_sharpe_allocation.T

    min_vol_idx = np.argmin(results[0])
    sdp_min, rp_min = results[0, min_vol_idx], results[1, min_vol_idx]
    min_vol_allocation = pd.DataFrame(weights[min_vol_idx], index=table.index, columns=table.columns)
    min_vol_allocation.allocation = [round(i*100, 2) for i in min_vol_allocation.allocation]
    min_vol_allocation = min_vol_allocation.T

    if return_target != 0:
        target_min_vol = efficient_return(expected_returns, cov_matrix, rf, return_target)
        target_sdp_min, target_rp_min = portfolio_annualised_performance(target_min_vol, expected_returns, cov_matrix, rf)
        target_min_vol_allocation = pd.DataFrame(target_min_vol.x, index=table.index, columns=table.columns)
        target_min_vol_allocation.allocation = [round(i*100, 2) for i in target_min_vol_allocation.allocation]
        target_min_vol_allocation = target_min_vol_allocation.T

    print("-"*80)
    print("Maximum Sharpe Ratio Portfolio Allocation\n")
    print("Annualised Return:", round(rp, 2))
    print("Annualised Volatility:", round(sdp, 2))
    print("\n")
    print(max_sharpe_allocation)
    print("-"*80)
    print("Global Minimum Volatility Portfolio Allocation\n")
    print("Annualised Return:", round(rp_min, 2))
    print("Annualised Volatility:", round(sdp_min, 2))
    print("\n")
    print(min_vol_allocation)

    if return_target != 0:
        print("-"*80)
        print("Optimal Portfolio for Target Return Allocation\n")
        print("Annualised Return:", round(target_rp_min, 2))
        print("Annualised Volatility:", round(target_sdp_min, 2))
        print("\n")
        print(target_min_vol_allocation)

    plt.figure(figsize=(10, num_stocks))
    plt.scatter(results[0, :], results[1, :], c=results[2, :], cmap='YlGnBu')
    plt.colorbar()
    plt.scatter(sdp, rp, marker='*', color='r', s=500, label='Maximum Sharpe Ratio Portfolio')
    plt.scatter(sdp_min, rp_min, marker='*', color='g', s=500, label='Global Minimum Volatility Portfolio')
    if return_target != 0:
        plt.scatter(efficient_return(expected_returns, cov_matrix, rf, return_target), target_sdp_min, target_rp_min, marker='*', color='b', s=500, label='Optimal Portfolio for Target Return')
    plt.title('Portfolio Optimization based on Simulation')
    plt.xlabel('annualised volatility')
```

```
plt.ylabel('annualised returns')
plt.legend(labelspace=0.8)
```

In [79]:

```
def display_calculated_ef_with_random(mean_returns, cov_matrix, num_p
    results, _ = random_portfolios(num_portfolios, mean_returns, cov_ma

    max_sharpe = max_sharpe_ratio(mean_returns, cov_matrix, risk_free_
    sdp, rp = portfolio_annualised_performance(max_sharpe['x'], mean_r
    max_sharpe_allocation = pd.DataFrame(max_sharpe.x, index=table.colu
    max_sharpe_allocation.allocation = [round(i*100,2) for i in max_sh
    max_sharpe_allocation = max_sharpe_allocation.T

    min_vol = min_variance(mean_returns, cov_matrix)
    sdp_min, rp_min = portfolio_annualised_performance(min_vol['x'], r
    min_vol_allocation = pd.DataFrame(min_vol.x, index=table.columns, co
    min_vol_allocation.allocation = [round(i*100,2) for i in min_vol_al
    min_vol_allocation = min_vol_allocation.T

    if return_target!=0:
        if expected_return == True:
            target_min_vol = efficient_return(expected_returns_rf, cov
            target_sdp_min, target_rp_min = portfolio_annualised_perfo
            target_min_vol_allocation = pd.DataFrame(target_min_vol.x,
            target_min_vol_allocation.allocation = [round(i*100,2) for
            target_min_vol_allocation = target_min_vol_allocation.T
        else:
            target_min_vol = efficient_return(mean_returns_rf, cov_mat
            target_sdp_min, target_rp_min = portfolio_annualised_perfo
            target_min_vol_allocation = pd.DataFrame(target_min_vol.x,
            target_min_vol_allocation.allocation = [round(i*100,2) for
            target_min_vol_allocation = target_min_vol_allocation.T

    print ("-"*80)
    print ("Maximum Sharpe Ratio Portfolio Allocation\n")
    print ("Annualised Return:", round(rp,2))
    print ("Annualised Volatility:", round(sdp,2))
    print ("\n")
    print (max_sharpe_allocation)
    print ("-"*80)
    print ("Global Minimum Volatility Portfolio Allocation\n")
    print ("Annualised Return:", round(rp_min,2))
    print ("Annualised Volatility:", round(sdp_min,2))
    print ("\n")
    print (min_vol_allocation)

    if return_target!=0:
        print ("-"*80)
        print ("Optimal Portfolio for Target Return Allocation\n")
        print ("Annualised Return:", round(target_rp_min,2))
        print ("Annualised Volatility:", round(target_sdp_min,2))
        print ("\n")
        print (target_min_vol_allocation)

    plt.figure(figsize=(10, num_stocks))
    plt.scatter(results[0,:], results[1:], c=results[2:], cmap='YlGnBu')
    plt.colorbar()
    plt.scatter(sdp, rp, marker='*', color='r', s=500, label='Maximum Shar
```



```

plt.scatter(sdp_min, rp_min, marker='*', color='g', s=500, label='Global Minimum Variance Portfolio')

if return_target!=0:
    plt.scatter(target_sdp_min, return_target, marker='*', color='b', s=500, label='Target Portfolio')

target = np.linspace(rp_min, max(mean_returns)*252, 50)
target_rf = np.linspace(risk_free_rate, rp * 2)

efficient_portfolios = efficient_frontier(mean_returns, cov_matrix)
plt.plot([p['fun'] for p in efficient_portfolios], target, linestyle='solid', color='r', label='Efficient Frontier')

if expected_return == True:
    capital_allocation_line = efficient_frontier(expected_returns_rf, cov_matrix)
    plt.plot([p['fun'] for p in capital_allocation_line], target_rf, linestyle='solid', color='b', label='Capital Allocation Line')
else:
    capital_allocation_line = efficient_frontier(mean_returns_rf, cov_matrix)
    plt.plot([p['fun'] for p in capital_allocation_line], target_rf, linestyle='solid', color='b', label='Capital Allocation Line')

plt.title('Portfolio Optimization based on Efficient Frontier and Capital Allocation Line')
plt.xlabel('annualised volatility')
plt.ylabel('annualised returns')
plt.legend(labelspace=0.8)

```

In [80]:

```

def display_ef_with_selected(mean_returns, cov_matrix, risk_free_rate, expected_return):

    max_sharpe = max_sharpe_ratio(mean_returns, cov_matrix, risk_free_rate)
    sdp, rp = portfolio_annualised_performance(max_sharpe['x'], mean_returns, cov_matrix)
    max_sharpe_allocation = pd.DataFrame(max_sharpe.x, index=table.columns, columns=table.columns)
    max_sharpe_allocation.allocation = [round(i*100,2) for i in max_sharpe_allocation.allocation]
    max_sharpe_allocation = max_sharpe_allocation.T

    min_vol = min_variance(mean_returns, cov_matrix)
    sdp_min, rp_min = portfolio_annualised_performance(min_vol['x'], mean_returns, cov_matrix)
    min_vol_allocation = pd.DataFrame(min_vol.x, index=table.columns, columns=table.columns)
    min_vol_allocation.allocation = [round(i*100,2) for i in min_vol_allocation.allocation]
    min_vol_allocation = min_vol_allocation.T

    if return_target!=0:
        if expected_return == True:
            target_min_vol = efficient_return(expected_returns_rf, cov_matrix)
            target_sdp_min, target_rp_min = portfolio_annualised_performance(target_min_vol['x'], mean_returns, cov_matrix)
            target_min_vol_allocation = pd.DataFrame(target_min_vol.x, index=table.columns, columns=table.columns)
            target_min_vol_allocation.allocation = [round(i*100,2) for i in target_min_vol_allocation.allocation]
            target_min_vol_allocation = target_min_vol_allocation.T
        else:
            target_min_vol = efficient_return(mean_returns_rf, cov_matrix)
            target_sdp_min, target_rp_min = portfolio_annualised_performance(target_min_vol['x'], mean_returns, cov_matrix)
            target_min_vol_allocation = pd.DataFrame(target_min_vol.x, index=table.columns, columns=table.columns)
            target_min_vol_allocation.allocation = [round(i*100,2) for i in target_min_vol_allocation.allocation]
            target_min_vol_allocation = target_min_vol_allocation.T

    an_vol = np.std(returns) * np.sqrt(252)
    an_rt = mean_returns * 252

    print ("-"*80)
    print ("Maximum Sharpe Ratio Portfolio Allocation\n")
    print ("Annualised Return:", round(rp,2))

```



```

print ("Annualised Volatility:", round(sdp,2))
print ("\n")
print (max_sharpe_allocation)
print ("-"*80)
print ("Global Minimum Volatility Portfolio Allocation\n")
print ("Annualised Return:", round(rp_min,2))
print ("Annualised Volatility:", round(sdp_min,2))
print ("\n")
print (min_vol_allocation)

if return_target!=0:
    print ("-"*80)
    print ("Optimal Portfolio for Target Return Allocation\n")
    print ("Annualised Return:", round(target_rp_min,2))
    print ("Annualised Volatility:", round(target_sdp_min,2))
    print ("\n")
    print (target_min_vol_allocation)

print ("-"*80)
print ("Individual Stock Returns and Volatility\n")
for i, txt in enumerate(table.columns):
    print (txt,":","annualised return",round(an_rt[i],2),", annuali
print ("-"*80)

fig, ax = plt.subplots(figsize=(10, num_stocks))
ax.scatter(an_vol,an_rt,marker='o',s=200)

for i, txt in enumerate(table.columns):
    ax.annotate(txt, (an_vol[i],an_rt[i]), xytext=(10,0), textcolor=
ax.scatter(sdp,rp,marker='*',color='r',s=500, label='Maximum Sharpe
ax.scatter(sdp_min,rp_min,marker='*',color='g',s=500, label='Global

if return_target!=0:
    plt.scatter(target_sdp_min, return_target, marker='*',color='k

target = np.linspace(rp_min, max(mean_returns)*252, 50)
target_rf = np.linspace(risk_free_rate, rp * 2)

efficient_portfolios = efficient_frontier(mean_returns, cov_matrix)
plt.plot([p['fun'] for p in efficient_portfolios], target, linestyle=

if expected_return == True:
    capital_allocation_line = efficient_frontier(expected_returns,
plt.plot([p['fun'] for p in capital_allocation_line], target, l
else:
    capital_allocation_line = efficient_frontier(mean_returns_rf,
plt.plot([p['fun'] for p in capital_allocation_line], target, l

ax.set_title('Portfolio Optimization based on Efficient Frontier &
ax.set_xlabel('annualised volatility')
ax.set_ylabel('annualised returns')
ax.legend(labelspace=0.8)

```

In [87]:

```

display_simulated_ef_with_random(mean_returns, cov_matrix, num_portfol
print ("-"*80)
print("\n\n***It is a optimization base on the past performance in ret

```

-----  
Maximum Sharpe Ratio Portfolio Allocation

Annualised Return: 0.44

Annualised Volatility: 0.31

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V
WFC									
allocation	5.15	34.14	0.25	7.96	0.88	20.8	7.47	23.07	0.12
	0.15								

-----  
Global Minimum Volatility Portfolio Allocation

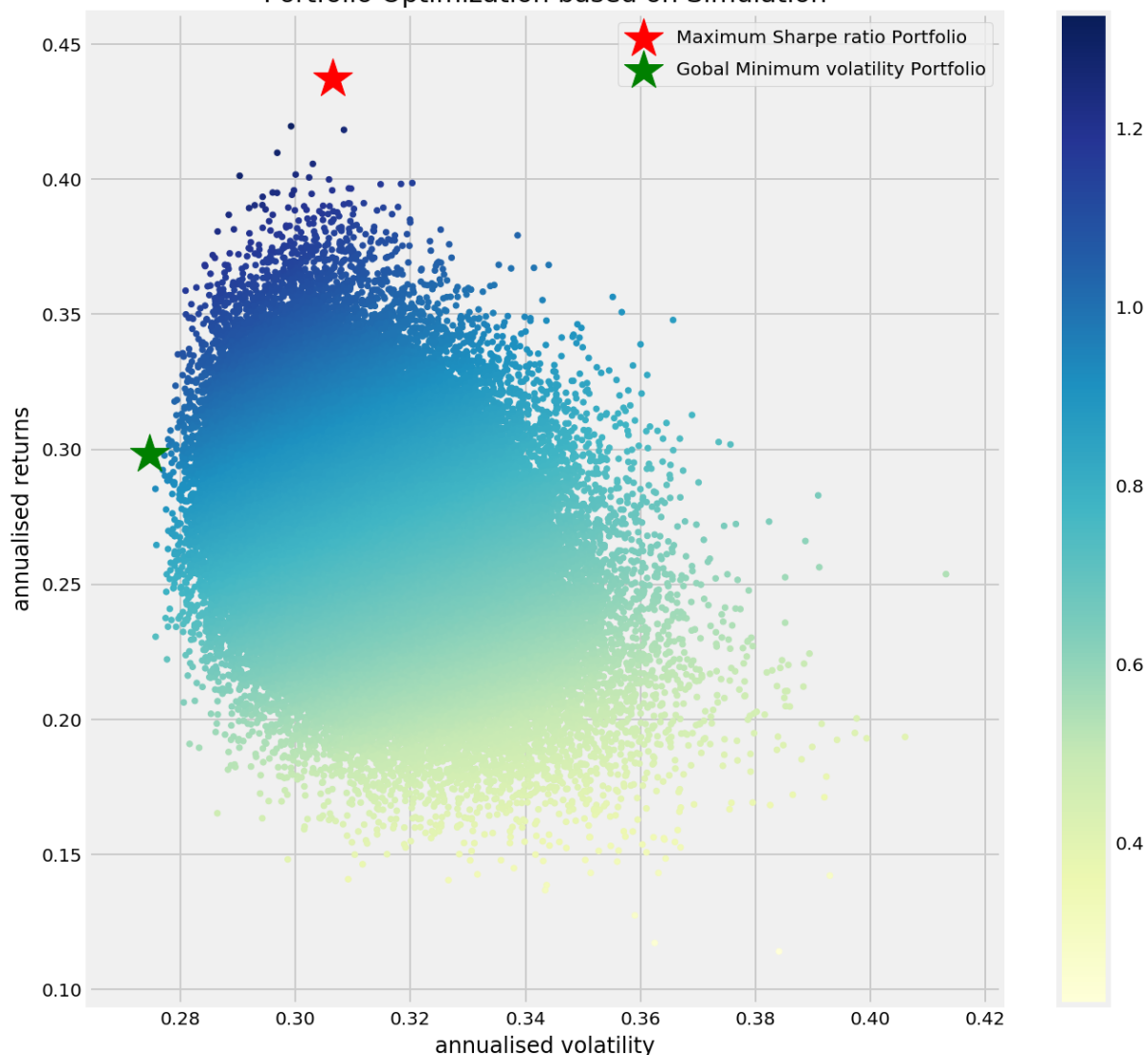
Annualised Return: 0.3

Annualised Volatility: 0.27

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V
WFC									
allocation	0.38	4.24	9.42	23.5	15.36	23.76	0.57	16.46	5.07
	1.25								

\*\*\*It is a optimization base on the past performance in return\*\*\*

Portfolio Optimization based on Simulation



```
In [82]: display_calculated_ef_with_random(mean_returns, cov_matrix, num_portfo
print ("-"*80)
print("\n\n***It is a optimization base on the past performance in ret
```

-----  
 -----  
 Maximum Sharpe Ratio Portfolio Allocation

Annualised Return: 0.6

Annualised Volatility: 0.36

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	92.33	0.0	0.0	7.67	0.0	0.0	0.0	0.0	0.0

-----  
 -----  
 Global Minimum Volatility Portfolio Allocation

Annualised Return: 0.25

Annualised Volatility: 0.27

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	3.36	13.07	36.84	10.26	28.98	0.0	0.0	7.5	0.0

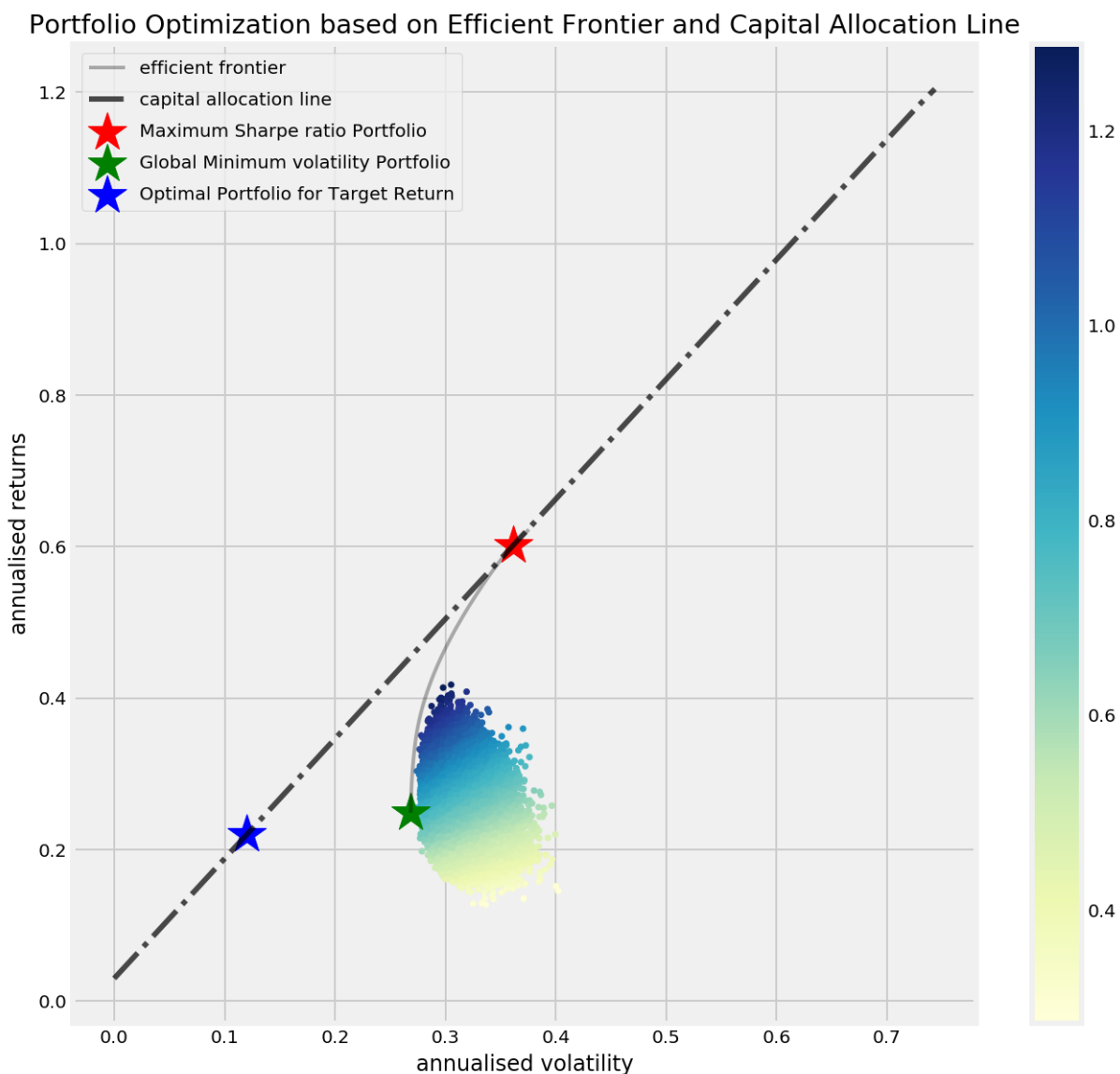
-----  
 -----  
 Optimal Portfolio for Target Return Allocation

Annualised Return: 0.22

Annualised Volatility: 0.12

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
rf										
allocation	0.0	30.7	0.0	0.0	2.47	0.0	0.0	0.0	0.0	0.0
6.83										6

-----  
 -----  
 \*\*\*It is a optimization base on the past performance in return\*\*\*



```
In [83]: display_ef_with_selected(mean_returns, cov_matrix, risk_free_rate, exp
print("-"*80)
print("\n\n***It is a optimization base on the past performance in ret
```

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Maximum Sharpe Ratio Portfolio Allocation

Annualised Return: 0.6

Annualised Volatility: 0.36

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	92.33	0.0	0.0	7.67	0.0	0.0	0.0	0.0	0.0

-----

Global Minimum Volatility Portfolio Allocation

Annualised Return: 0.25

Annualised Volatility: 0.27

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	3.36	13.07	36.84	10.26	28.98	0.0	0.0	7.5	0.0

-----

## Optimal Portfolio for Target Return Allocation

Annualised Return: 0.22

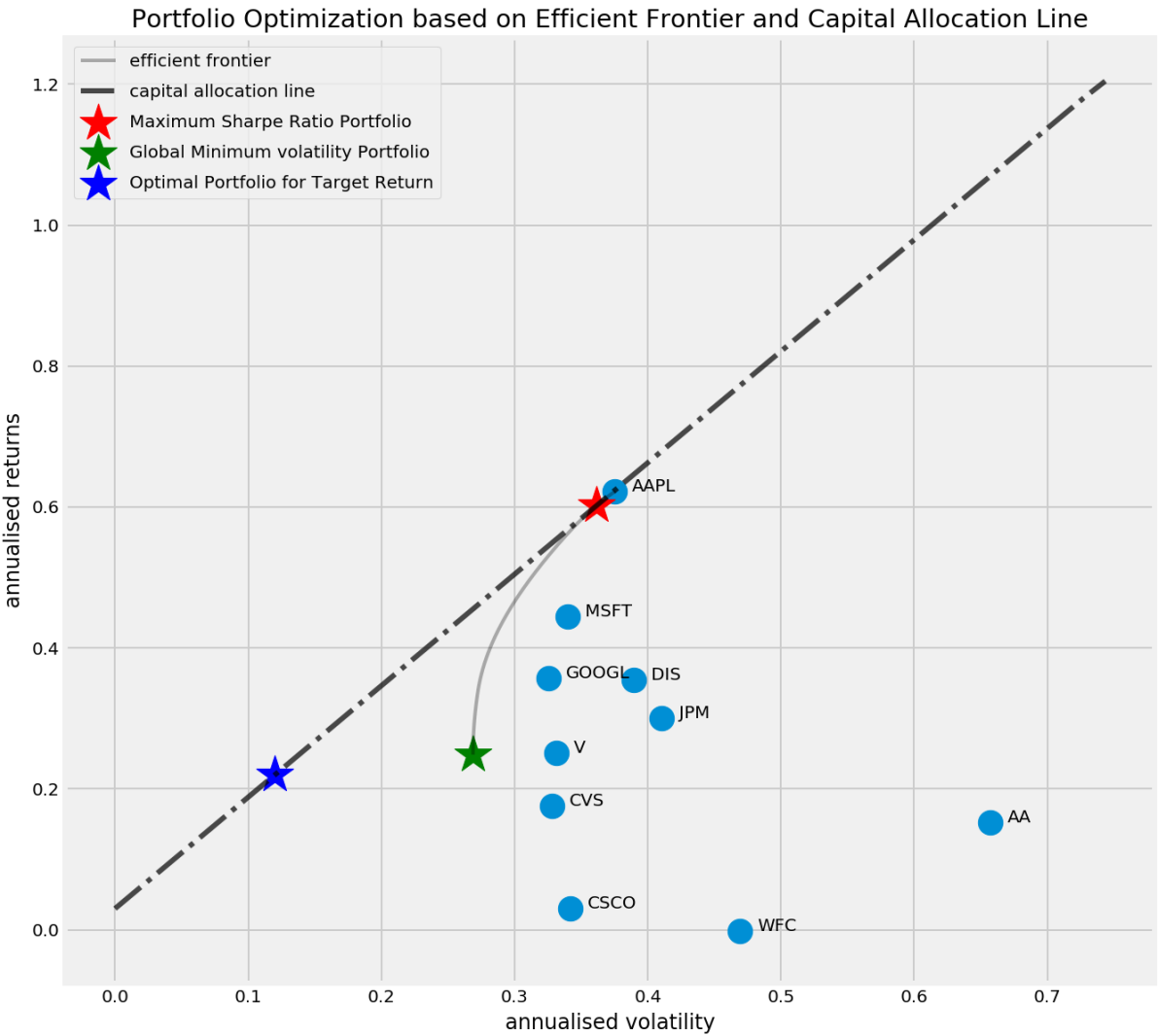
Annualised Volatility: 0.12

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC	
rf											
allocation	0.0	30.7	0.0	0.0	2.47	0.0	0.0	0.0	0.0	0.0	6.83

-----  
Individual Stock Returns and Volatility

AA : annuaised return 0.15 , annualised volatility: 0.66  
 AAPL : annuaised return 0.62 , annualised volatility: 0.38  
 CSCO : annuaised return 0.03 , annualised volatility: 0.34  
 CVS : annuaised return 0.18 , annualised volatility: 0.33  
 DIS : annuaised return 0.35 , annualised volatility: 0.39  
 GOOGL : annuaised return 0.36 , annualised volatility: 0.33  
 JPM : annuaised return 0.3 , annualised volatility: 0.41  
 MSFT : annuaised return 0.44 , annualised volatility: 0.34  
 V : annuaised return 0.25 , annualised volatility: 0.33  
 WFC : annuaised return -0.0 , annualised volatility: 0.47

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 \*\*\*It is a optimization base on the past performance in return\*\*\*



```
In [88]: display_simulated_ef_with_random(expected_returns, cov_matrix, num_por
```

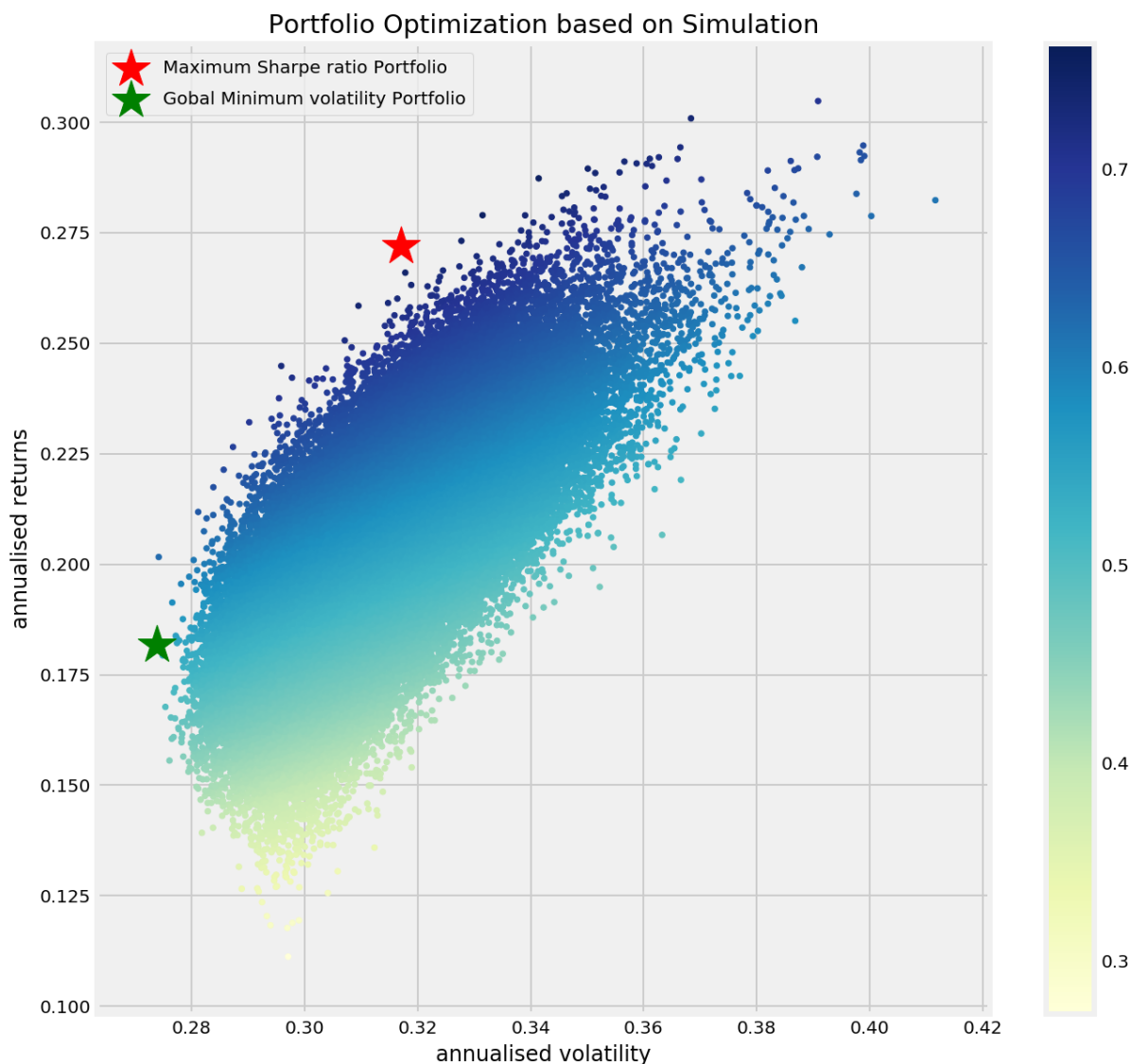
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-----  
Maximum Sharpe Ratio Portfolio Allocation  
  
Annualised Return: 0.27  
Annualised Volatility: 0.32  
  

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V
WFC									
allocation	14.5	17.77	0.8	33.13	5.47	3.66	18.26	0.36	2.19

  
-----  
-----  
Global Minimum Volatility Portfolio Allocation  
  
Annualised Return: 0.18  
Annualised Volatility: 0.27  
  

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WF
C										
allocation	1.1	2.68	8.86	32.46	18.06	20.83	3.57	5.23	6.3	0.9

  
1



```
In [85]: display_calculated_ef_with_random(expected_returns, cov_matrix, num_p
```

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 -----  
 Maximum Sharpe Ratio Portfolio Allocation

Annualised Return: 0.33  
 Annualised Volatility: 0.34

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	22.07	0.95	0.0	76.97	0.0	0.0	0.0	0.0	0.0	0.0

-----  
 -----  
 Global Minimum Volatility Portfolio Allocation

Annualised Return: 0.18  
 Annualised Volatility: 0.27

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	3.36	13.07	36.84	10.26	28.98	0.0	0.0	7.5	0.0

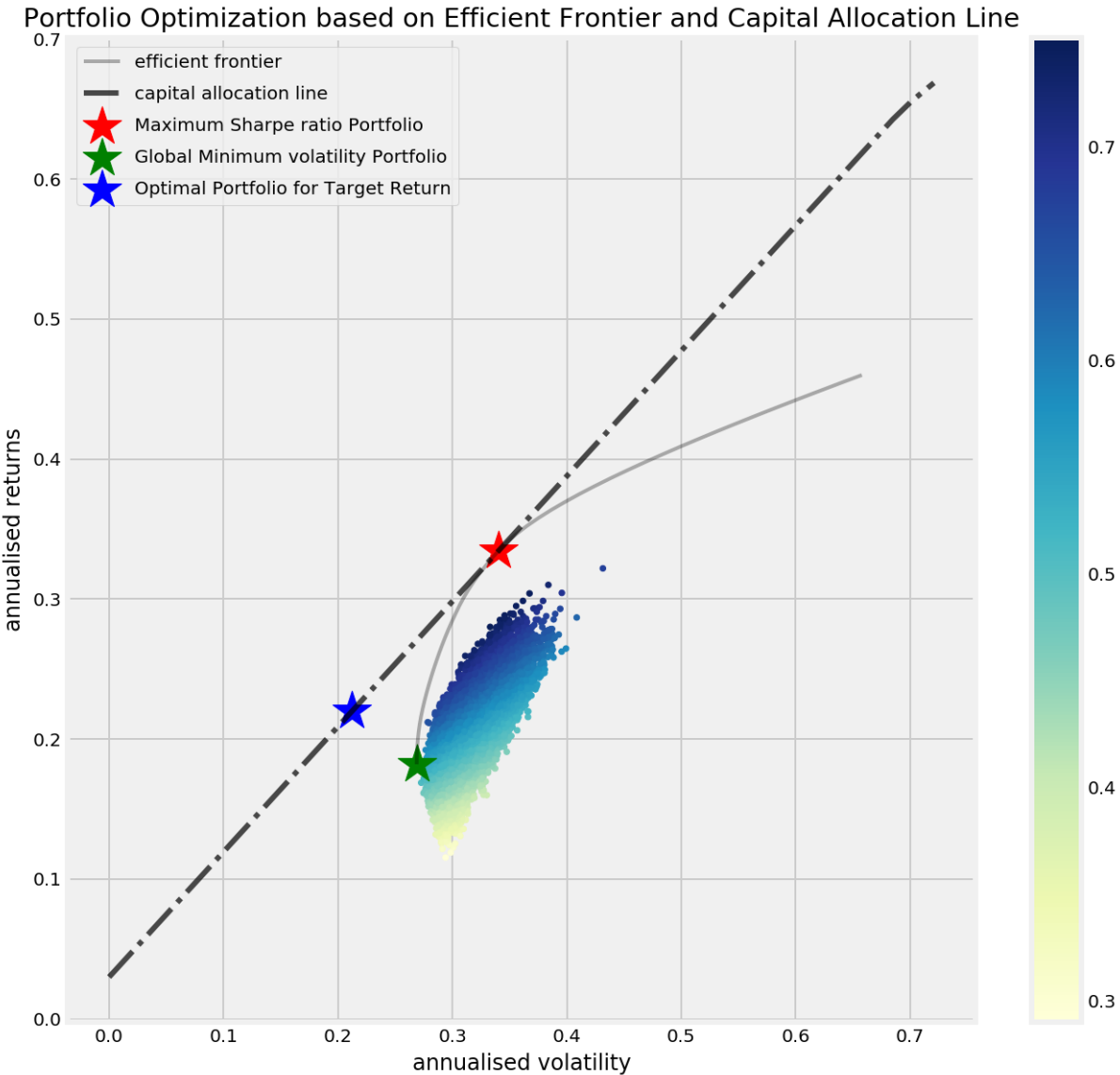
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 -----  
 Optimal Portfolio for Target Return Allocation

Annualised Return: 0.22



Annualised Volatility: 0.21

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
rf										
allocation	13.68	0.7	0.0	48.14	0.0	0.0	0.0	0.0	0.0	0.0
37.48										



```
In [86]: display_ef_with_selected(expected_returns, cov_matrix, risk_free_rate,
```

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Maximum Sharpe Ratio Portfolio Allocation

Annualised Return: 0.33

Annualised Volatility: 0.34

AA AAPL CSCO CVS DIS GOOGL JPM MSFT V WFC

allocation 22.07 0.95 0.0 76.97 0.0 0.0 0.0 0.0 0.0 0.0

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Global Minimum Volatility Portfolio Allocation

Annualised Return: 0.18

Annualised Volatility: 0.27

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
allocation	0.0	3.36	13.07	36.84	10.26	28.98	0.0	0.0	7.5	0.0

-----  
 Optimal Portfolio for Target Return Allocation

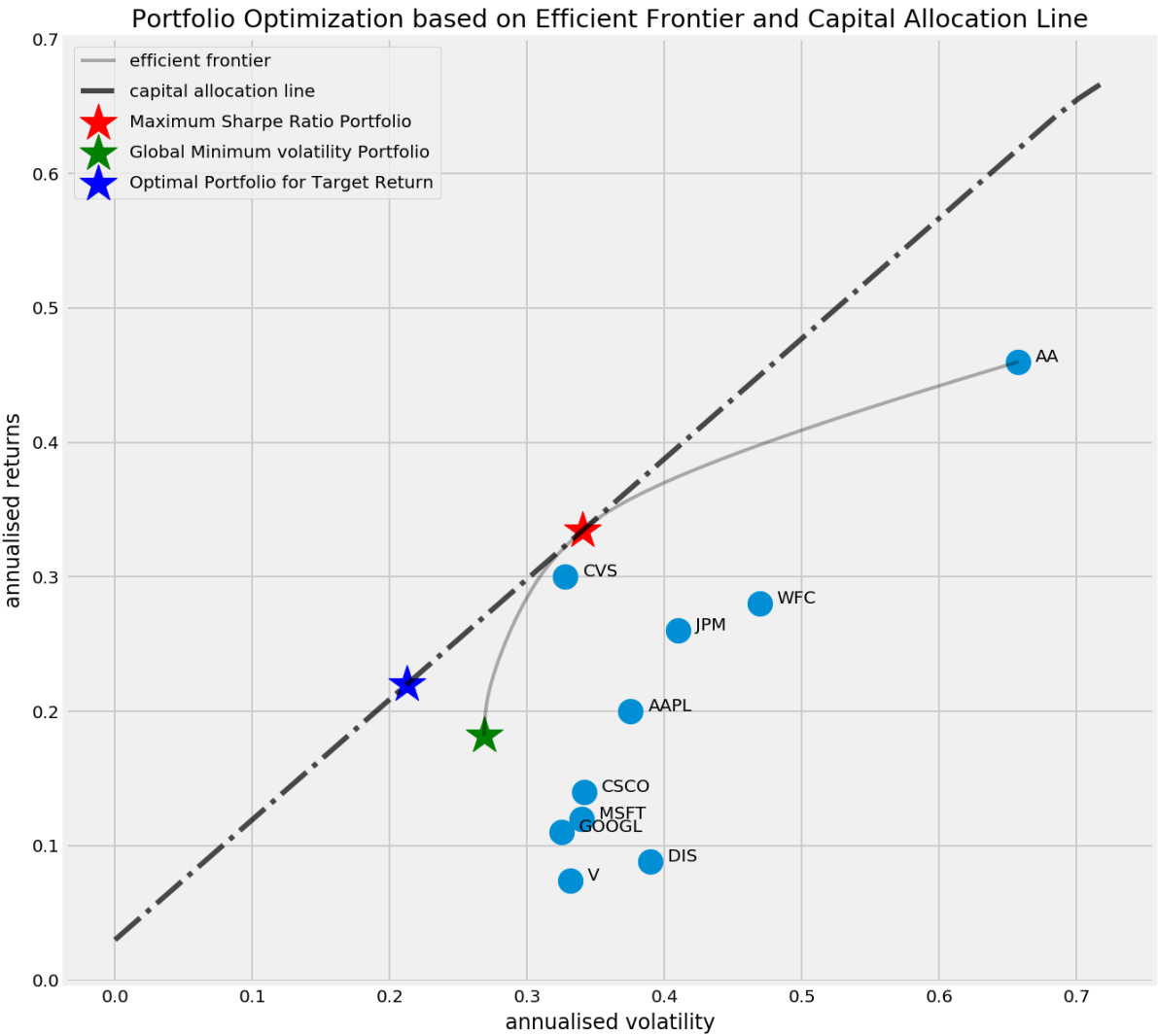
Annualised Return: 0.22

Annualised Volatility: 0.21

	AA	AAPL	CSCO	CVS	DIS	GOOGL	JPM	MSFT	V	WFC
rf										
allocation	13.68	0.7	0.0	48.14	0.0	0.0	0.0	0.0	0.0	0.0

-----  
 Individual Stock Returns and Volatility

AA : annuaised return 0.46 , annualised volatility: 0.66  
 AAPL : annuaised return 0.2 , annualised volatility: 0.38  
 CSCO : annuaised return 0.14 , annualised volatility: 0.34  
 CVS : annuaised return 0.3 , annualised volatility: 0.33  
 DIS : annuaised return 0.09 , annualised volatility: 0.39  
 GOOGL : annuaised return 0.11 , annualised volatility: 0.33  
 JPM : annuaised return 0.26 , annualised volatility: 0.41  
 MSFT : annuaised return 0.12 , annualised volatility: 0.34  
 V : annuaised return 0.07 , annualised volatility: 0.33  
 WFC : annuaised return 0.28 , annualised volatility: 0.47



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In [ ]:
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In [ ]:
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