

# Chapter 2. Signals and Signal Space

Communication Theory - 2026

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# Definition: Signal and System

## Signal

A signal is a set of information or data.

The signals are functions of the independent variable **time  $t$** .

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- Examples: Audio signals, video signals, sensor data, etc.

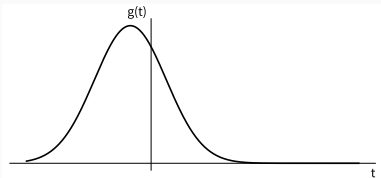
## System

Signals may be processed further by systems, which may modify them or extract additional information from them.

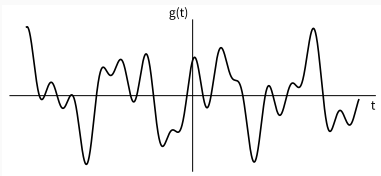
Thus, a system is an entity that processes signals (**inputs**) to yield another set of signals (**outputs**).

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- For example, an anti-aircraft radar system processes the received signals (inputs) to determine the position and velocity of an aircraft (outputs).
  - More examples: Amplifiers, filters, modulators, demodulators, etc.

# Energy vs Power Signals



(a) Signal with finite energy



(b) Signal with finite power

**Figure 2.1:** Examples of signals

## Energy Signal

A signal is said to be an energy signal if its energy is finite and its average power approaches zero.

$$E = \int_{-\infty}^{\infty} |g(t)|^2 dt < \infty, \quad P \rightarrow 0$$

## Power Signal

A signal is said to be a power signal if its average power is finite and its energy approaches infinite.

$$P = \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} |g(t)|^2 dt < \infty, \quad E \rightarrow \infty$$

# Units of Signal Power

- The standard units of signal energy and power are the "joule" and the "watt".
- However, in practice, it is often customary to use logarithmic scales to describe signal power.
- A signal with average power of  $P$  watts has power of either  $P_{dBW}$  or  $P_{dBm}$ .

$$P_{dBW} = [10 \cdot \log_{10} P] \text{ dBW}$$

$$P_{dBm} = [30 + 10 \cdot \log_{10} P] \text{ dBm}$$

- For example,  
 $P_{dBm} = -30 \text{ dBm} = 10^{-6} \text{ W}.$

## Example 2.1

Determine the suitable measures of the signals in the left Figure.

### (a) Energy signal

Energy signal. Power approaches 0 as  $|t| \rightarrow \infty$ .

$$E_g = \int_{-\infty}^{\infty} |g(t)|^2 dt = \int_{-1}^0 (2)^2 dt + \int_0^{\infty} 4e^{-t} dt = 4 + 4 = 8$$

### (b) Power signal

Averaging  $g^2(t)$  over an infinitely large interval is equivalent to averaging it over one period (2 seconds).

$$\begin{aligned} P_g &= \lim_{T \rightarrow \infty} \frac{1}{T} \int_{-T/2}^{T/2} |g(t)|^2 dt = \frac{1}{T} \int_{-T/2}^{T/2} |g(t)|^2 dt \\ &= \frac{1}{2} \int_{-1}^1 t^2 dt = \frac{1}{3} \end{aligned}$$

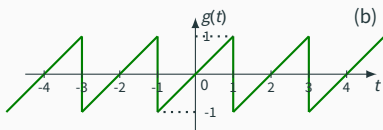
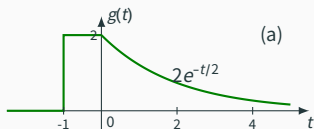
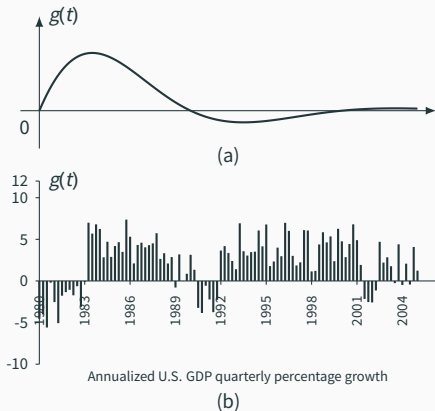


Figure 2.2: Signal for Example

# Classification of Signals

1. Continuous time and discrete time signals
2. Analog and digital signals
3. Periodic and aperiodic signals
4. Energy and power signals
5. Deterministic and probabilistic signals

## Figure 2.3 Continuous vs Discrete Time Signals



### (a) Continuous Time Signal

Continuous time signals are specified for every value of time  $t$ . Many examples including:

- Audio recordings in analog media like LP, magnetic cassette, or reel-to-reel tapes.
- Signals received through AM/FM radio channel.

### (b) Discrete Time Signal

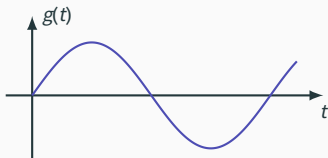
Discrete time signals are specified only at discrete points of  $t = nT$ . Many examples including:

- The quarterly gross domestic product (GDP), stock market daily averages, and monthly sales of a corporation.
- Audio signals formatted by MP3, HE-AAC, FLAC, or ALAC.

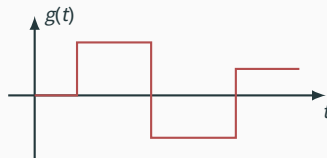
**Figure 2.3:** *Continuous vs Discrete Time Signals*



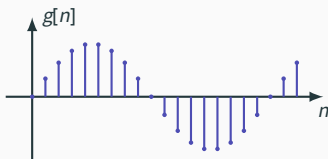
## Figure 2.4 Classification of Signals



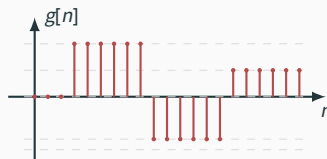
(a) Analog, Continuous-time



(b) Digital, Continuous-time



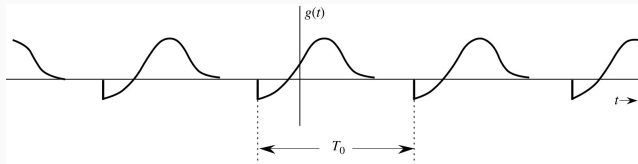
(c) Analog, Discrete-time



(d) Digital, Discrete-time

**Figure 2.4:** Classification of signals based on amplitude and time domains

# Periodic and Aperiodic Signals



**Figure 2.5:** Periodic signal of period  $T_0$

A signal  $g(t)$  is **periodic** if there exists a positive constant  $T_0$ .

$$g(t) = g(t + T_0) \quad \text{for all } t \quad (2.5)$$

The smallest value of  $T_0$  in Eq. (2.5) is the **period** of  $g(t)$ .

- **Unit Step**  $u(t)$ : 인과성(Causality) 표현의 핵심
- **Operations**:  $x(at - b)$  꼴의 변환을 자유자재로 다뤄야 함
- **Correlation**: 통신 시스템에서 수신 신호를 검출(Detection)하는 기본 원리