

# Beliefs about Inflation and the Term Structure of Interest Rates

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- Gave us DSGE models used by central bankers & structural asset pricing/term structure models.
- We learned a lot from them including drawbacks/deficiencies.

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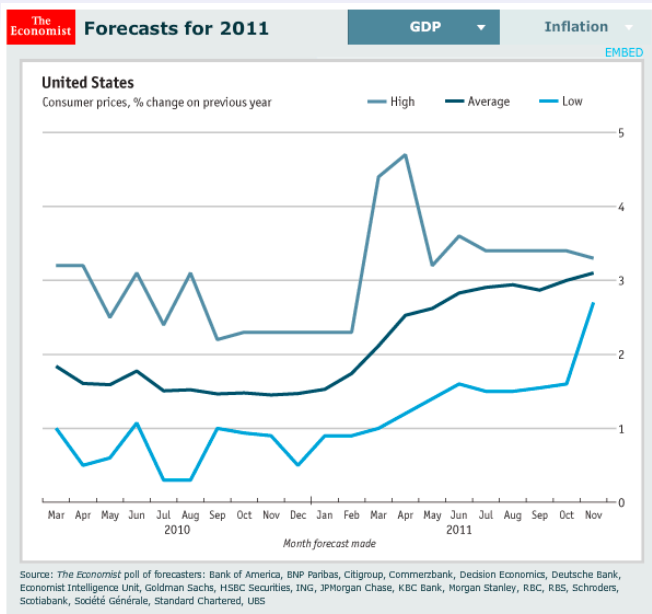
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# Opinions about Inflation



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- how do belief differences impact real & nominal yield curves?
- what belief structure is necessary to capture return predictability & real spillover effects?
- what is the impact of belief differences when quantitative properties of bonds are fit?
- empirically, do we find support for how belief differences impact the yield curve?

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- Expected inflation mean reversion disagreement captures dynamics/predictability.
- Disagreement alone cannot capture the slope of yield curves.

# Model - Key Features

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- Closed-form bond prices in the quadratic Gaussian class

# Model - Output & Inflation

- Uncertainty — a real shock  $z_{\epsilon}(t)$  & a nominal shock  $z_{\pi}(t)$
- Real output  $\epsilon(t)$  observed by all:

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- Expected inflation  $x(t)$  unobserved by all:

$$dx(t) = \kappa (\bar{x} - x(t)) dt + \sigma_{x, \epsilon} dz_{\epsilon}(t) + \sigma_{x, \$} dz_{\$}(t),$$

# Model - Heterogeneous Beliefs about Expected Inflation

- Two investors ( $i = 1, 2$ ) & an econometrician ( $i = 0$ )
- Have different beliefs or models about  $x(t)$  through
  - ① the long run mean of expected inflation  $\bar{x}$
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  - ① the long run mean of expected inflation  $\bar{x}$
  - ② the speed of mean reversion of expected inflation  $\kappa$
- Update beliefs via Bayes Rule:

$$x^i(t) = E^i[x(t) \mid \mathcal{F}_t^{\epsilon, \pi}], \quad i \in \{0, 1, 2\}$$

- Disagreement about expected inflation implies:

$$dz_{\$}^i(t) = dz_{\$}^0(t) + \frac{x^0(t) - x^i(t)}{\sigma_{\pi, \$}} dt$$

# Model - How Each Agent Views the World

- Price level under each agent's beliefs:

$$\frac{d\pi(t)}{\pi(t)} = x^i(t) dt + \sigma_{\pi,\epsilon} dz_\epsilon(t) + \sigma_{\pi,\$} dz_\$^i(t)$$

- Unobserved expected inflation under each agent's beliefs:

$$dx^i(t) = \kappa^i (\bar{x}^i - x^i(t)) dt + \sigma_x \rho_{x\epsilon} dz_\epsilon(t) + \sigma_{x,\$}^i dz_\$^i(t)$$

- Volatility  $\sigma_{x,\$}^i$

- Driven by agent  $i$ 's steady state estimation error which is driven by  $\kappa^i$

# Model - Disagreement Processes

- $\Delta^i(t)$  — disagreement across the econometrician & investor  $i$ :

$$\Delta^i(t) = \frac{x^0(t) - x^i(t)}{\sigma_{\pi, \$}}$$

- $\Delta(t)$  — disagreement across investors:

$$\Delta(t) = \Delta^1(t) - \Delta^2(t) = \frac{x^2(t) - x^1(t)}{\sigma_{\pi, \$}}.$$

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- No  $\kappa$  disagreement  $\Rightarrow \Delta^i(t)$  &  $\Delta(t)$  deterministic

# Model - Consumption-Portfolio Choice Problem

- Investors trade in complete markets. Differ in initial wealth & beliefs.
- External habit preferences,  $u(c) = \frac{c^{1-\gamma}}{1-\gamma}$ , and  $\gamma > 0$ :

$$\max_{\{c_i(t)\}} E^i \left[ \int_0^T e^{-\rho t} u \left( \frac{c^i(t)}{X(t)} \right) dt \right], \quad \text{s.t.} \quad E^i \left[ \int_0^T \xi^i(t) c^i(t) dt \right] \leq W^i(0)$$



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- Standard of living process  $X(t)$ , a weighted “geometric sum” of past consumption, where  $\delta$  captures the history dependence
- Define the business cycle variable  $\omega(t) = \log(\epsilon(t)/X(t))$ :

$$d\omega(t) = \delta(\bar{\omega} - \omega(t)) dt + \sigma_\epsilon dz_\epsilon(t)$$

# Equilibrium - Asset Prices

- Econometrician's real & nominal market prices of risk:

$$\theta_{\epsilon}(t) = \gamma \sigma_{\epsilon},$$

$$\theta_{\$}^0(t) = \Delta_1(t) - (1 - f(t)) \Delta(t),$$

$$\theta_{\$, \epsilon} = \gamma \sigma_{\epsilon} + \sigma_{\pi} \rho_{\epsilon \pi},$$

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- Real & nominal short rates:

$$\begin{aligned} r(t) = & \rho + \mu_{\epsilon} - \frac{1}{2}(\gamma^2 + 1)\sigma_{\epsilon}^2 + \delta(\gamma - 1)(\bar{\omega} - \omega(t)) \\ & + \frac{1}{2} \left( 1 - \frac{1}{\gamma} \right) f(t)(1 - f(t))(\Delta(t))^2, \end{aligned}$$

$$r_{\$}(t) = r(t) + f(t)x^1(t) + (1 - f(t))x^2(t) - \gamma \sigma_{\epsilon} \sigma_{\pi} \rho_{\epsilon \pi} - \sigma_{\pi}^2.$$

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- Spillover from nominal to real when  $\Delta \neq 0$

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- When  $\gamma > 1$ , the income effect dominates
  - Investors want to consume more today by borrowing against future consumption, but cannot as consumption today is fixed
  - Short rates rise to counterbalance
- When  $\gamma < 1$ , the substitution effect dominates and the short rates fall to counterbalance



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  - and  $\downarrow$  when  $\gamma < 1$ ,
- Real bond volatilities also rise with  $\uparrow$  disagreement.

# Equilibrium - Closed-Form Bond Prices

- When  $\gamma$  is an integer, real & nominal bond prices:

$$B(t; T') = \sum_{k=0}^{\gamma} \binom{\gamma}{k} (1 - f(t))^k f(t)^{\gamma-k} B_k(t; T')$$

$$P_{\$}(t; T') = \sum_{k=0}^{\gamma} \binom{\gamma}{k} (1 - f(t))^k f(t)^{\gamma-k} P_{k,\$}(t; T')$$

with  $B_k(t; T')$  &  $P_{k,\$}(t; T')$  fictitious economy  $k$  bond prices.

- In economy  $k$ ,  $B_k(t; T')$  &  $P_{k,\$}(t; T')$  follow
  - Completely affine Gaussian term structure when investors disagree about  $\bar{x}$
  - Quadratic Gaussian term structure when investors disagree about  $\kappa$

# Numerical Results - Parameters

Parameter	Description	Value
<i>Preferences</i>		
$\rho$	Time Preference Parameter	2.5%
$\gamma$	Risk Aversion	7
$\delta$	Habit Parameter	0.07
<i>Consumption</i> (Chan & Kogan)		
$\mu_\epsilon$	Expected Consumption Growth	1.72%
$\sigma_\epsilon$	Volatility of Consumption	3.32%
<i>Inflation</i> (Brennan & Xia)		
$\sigma_\pi$	Inflation Volatility	1.3%
$\bar{x}$	Long Run Mean of Expected Inflation	3%
$\kappa$	Mean Reversion of Expected Inflation	0.35
$\sigma_x$	Volatility of Expected Inflation	1.4%
$\rho_{\epsilon\pi}$	$\rho$ of Realized Inflation & Real Consumption Growth	-0.2
$\rho_{\pi x}$	$\rho$ of Realized and Expected Inflation	0
$\rho_{x\epsilon}$	$\rho$ of Expected Inflation & Real Consumption Growth	0

# Numerical Results - Beliefs

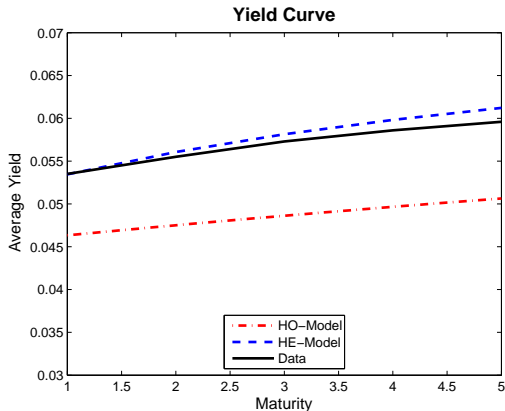
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## *Disagreement*

$\bar{x}_1$	Long run mean of first investor	$\bar{x} - \frac{1}{2}\Delta_{\bar{x}}$
$\bar{x}_2$	Long run mean of second investor	$\bar{x} + \frac{1}{2}\Delta_{\bar{x}}$
$\kappa_1$	Mean reversion of first investor	$\kappa - \frac{1}{2}\Delta_{\kappa}$
$\kappa_2$	Mean reversion of first investor	$\kappa + \frac{1}{2}\Delta_{\kappa}$

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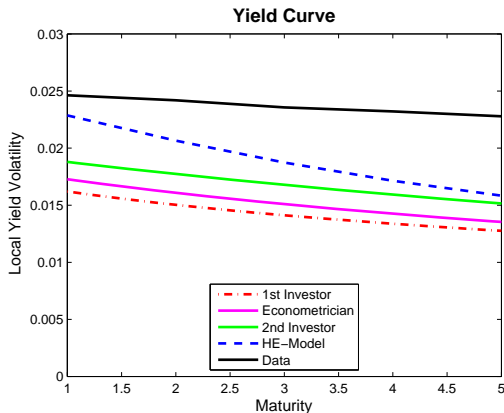
# Numerical Results - Nominal Yield Curve in Steady-State Disagreement



Parameters:  $f = 0.5$ ,  $\Delta_{\bar{x}} = 1\%$ , and  $\Delta_{\kappa} = -0.3$

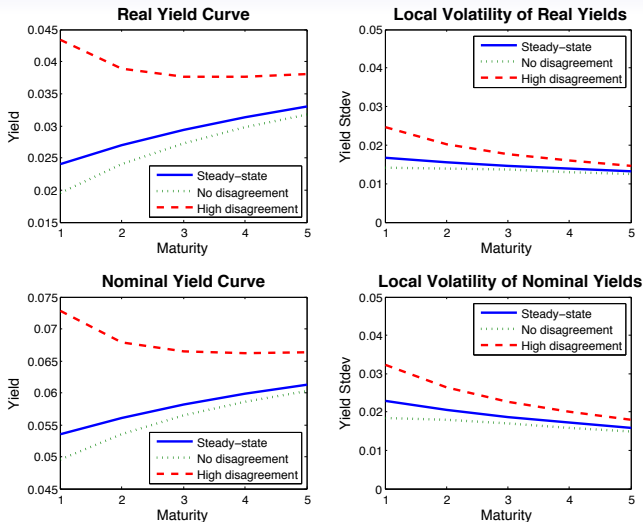


# Numerical Results - Yield Curve Volatility



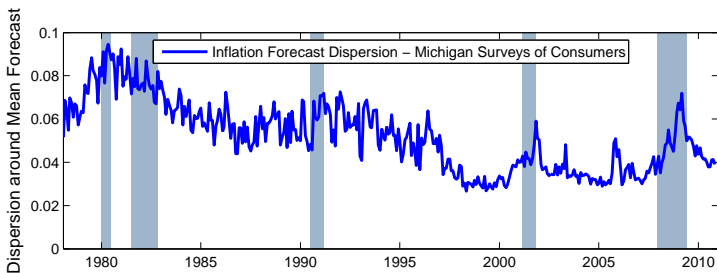
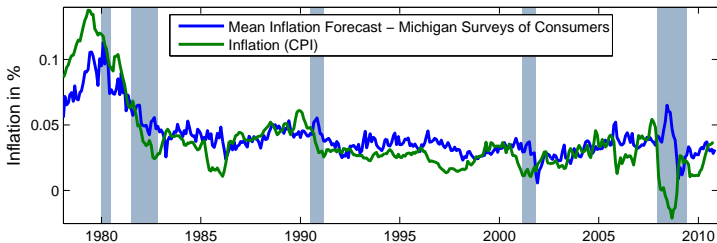
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# Numerical Results - Impact of Increased Disagreement



Parameters:  $f = 0.5$ ,  $\Delta_{\bar{x}} = 1\%$ , and  $\Delta_{\kappa} = -0.3$

# Empirical Work - Inflation Beliefs & Dispersion



# Empirical Work - Nominal Yields & Volatilities

Panel A: Yields										
	3 Month		1 Year		2 Year		3 Year		5 Year	
	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2
Intercept	-0.018	-0.022	-0.014	-0.018	-0.011	-0.014	-0.007	-0.009	-0.002	-0.004
t-statistics	-1.919	-2.431	-1.623	-2.020	-1.331	-1.627	-0.944	-1.175	-0.293	-0.497
Dispersion	1.423	0.787	1.429	0.855	1.415	0.956	1.385	1.029	1.342	1.095
t-statistics	7.778	3.458	8.370	3.666	8.881	4.086	9.169	4.465	9.809	5.013
Mean Inflation		0.901		0.812		0.650		0.504		0.351
t-statistics		4.212		3.719		2.887		2.227		1.586
Adj.R2	0.435	0.544	0.442	0.531	0.456	0.516	0.470	0.508	0.497	0.517
N	394	394	394	394	394	394	394	394	394	394
Panel B: Yield Volatilities										
Intercept	-0.016	-0.017	-0.012	-0.013	-0.016	-0.017	-0.015	-0.016	-0.019	-0.020
t-statistics	-2.051	-2.245	-1.712	-1.849	-2.732	-2.838	-2.572	-2.624	-3.976	-3.919
Dispersion	0.824	0.602	0.765	0.598	0.849	0.695	0.807	0.702	0.869	0.789
t-statistics	5.250	3.504	5.358	3.522	6.663	4.245	6.444	4.316	7.816	5.440
Mean Inflation		0.315		0.236		0.218		0.149		0.113
t-statistics		2.208		1.835		1.719		1.162		0.925
Adj.R2	0.313	0.341	0.296	0.312	0.377	0.391	0.361	0.367	0.439	0.442
N	394	394	394	394	394	394	394	394	394	394

Data: Monthly, January 1978 - October 2010

# Empirical Work - Real Yields & Volatilities

Panel A: Yields										
	3 Month		1 Year		2 Year		3 Year		5 Year	
	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2	Model 1	Model 2
Intercept	0.015	0.015	0.017	0.016	0.009	0.010	0.012	0.013	0.013	0.014
t-statistics	1.174	1.170	1.524	1.542	1.058	1.234	1.430	1.710	1.761	2.215
Dispersion	0.221	0.327	0.187	0.321	0.280	0.423	0.251	0.413	0.244	0.432
t-statistics	0.909	0.993	0.877	1.148	1.550	2.128	1.485	2.309	1.590	2.792
Mean Inflation		-0.126		-0.160		-0.198		-0.224		-0.259
t-statistics		-0.516		-0.766		-1.308		-1.577		-1.969
Adj.R2	0.019	0.015	0.019	0.022	0.074	0.093	0.071	0.106	0.088	0.149
N	100	100	100	100	127	127	127	127	131	131
Panel B: Yield Volatilities										
Intercept	0.002	0.002	0.001	0.001	0.002	0.002	0.001	0.001	-0.001	-0.001
t-statistics	0.417	0.370	0.270	0.205	0.535	0.635	0.223	0.280	-0.338	-0.338
Dispersion	0.268	0.400	0.242	0.347	0.202	0.247	0.198	0.223	0.191	0.194
t-statistics	2.698	3.216	2.956	3.256	3.356	3.080	3.909	3.142	4.713	3.139
Mean Inflation		-0.158		-0.126		-0.062		-0.034		-0.004
t-statistics		-1.805		-1.669		-1.169		-0.710		-0.082
Adj.R2	0.150	0.177	0.166	0.188	0.168	0.173	0.197	0.195	0.231	0.225
N	100	100	100	100	127	127	127	127	131	131

Data: Quarterly, Q3 1978 - Q3 2010

# Conclusion

## Key Results

- Inflation disagreement induces a real economy spillover effect.
- When common relative risk aversion  $\gamma > 1$  and disagreement increases,
  - an income effect dominates implying real & nominal short rates rise,
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## More Work ...

- Explore the risk/term premia
- Explore predictability (Wachter (2006), Xiong & Yan (2010))
  - Preliminary results - Tension between predictability & first two yield curve moments
- More complete calibration

# Related Work on Yield Curve Economics

## Reduced Form No Arbitrage Models

- Latent state variables
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# Related Work on Yield Curve Economics

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## Structural Models

- Exogenous inflation - Wachter (2006), Piazzesi & Schneider (2006)
- Endogenous Inflation - Gallmeyer, Hollifield, & Zin (2005), Buraschi & Jiltsov (2007), Gallmeyer, Hollifield, Palomino, & Zin (2007), Bekaert, Cho, & Moreno (2010), Palomino (2010)

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## Subjective Beliefs/Survey Data & Yield Curves

- Ang, Bekaert & Wei (2007), Buraschi & Whelan (2010), Chernov & Mueller (2008), Gürkaynak & Wright (2010), Xiong & Yan (2010)