

Chapter 5 - MEMORY

Memory Hierarchy = A structure that uses multiple levels of memory.

(Distance from processor \uparrow \rightarrow

Size of memories &
access time \uparrow

Cost per bit \downarrow

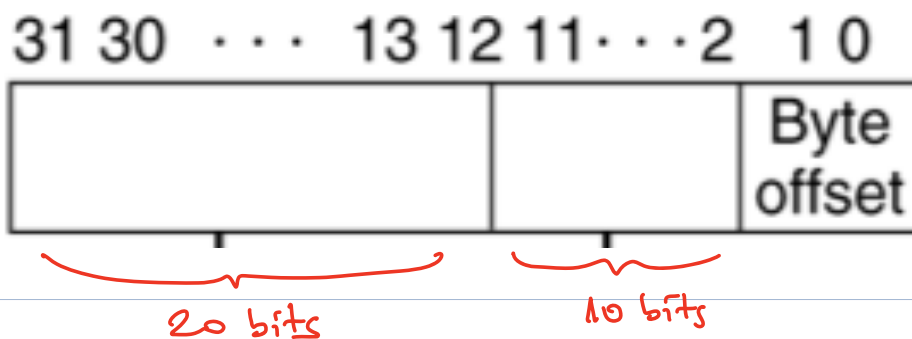
Block (or line) = minimum unit of information that can be present or not present in cache.

Hit Rate = Fraction of memory accesses found in a level of the memory hierarchy.

Direct-Mapped Cache = A cache structure in which each memory location is mapped to exactly one location in the cache.

Tag = A field in a table used for a memory hierarchy that contains the address info. required to identify whether the associated block in the hierarchy corresponds to a requested word.

Decimal address of reference	Binary address of reference	Hit or miss in cache	Assigned cache block (where found or placed)
22	10110_{two}	miss (5.9b)	$(10110_{\text{two}} \bmod 8) = 110_{\text{two}}$
26	11010_{two}	miss (5.9c)	$(11010_{\text{two}} \bmod 8) = 010_{\text{two}}$
22	10110_{two}	hit	$(10110_{\text{two}} \bmod 8) = 110_{\text{two}}$
26	11010_{two}	hit	$(11010_{\text{two}} \bmod 8) = 010_{\text{two}}$
16	10000_{two}	miss (5.9d)	$(10000_{\text{two}} \bmod 8) = 000_{\text{two}}$
3	00011_{two}	miss (5.9e)	$(00011_{\text{two}} \bmod 8) = 011_{\text{two}}$
16	10000_{two}	hit	$(10000_{\text{two}} \bmod 8) = 000_{\text{two}}$
18	10010_{two}	miss (5.9f)	$(10010_{\text{two}} \bmod 8) = 010_{\text{two}}$
16	10000_{two}	hit	$(10000_{\text{two}} \bmod 8) = 000_{\text{two}}$



The cache holds $1024 \text{ words} = 4 \text{ KiB}$

Block size = 1 word & cache has $1024 = 2^{10}$ words
 (10-Bit for index $32 - 10 - 2 = 20$ bit for TAG)

$$\text{Block} = (\text{Block Addr}) \bmod (\text{\# of blocks in Cache})$$

$$\text{Block Addr} = \text{Byte Addr} \div \text{Bytes per block}$$

(Block Addr) is the block containing all addresses between

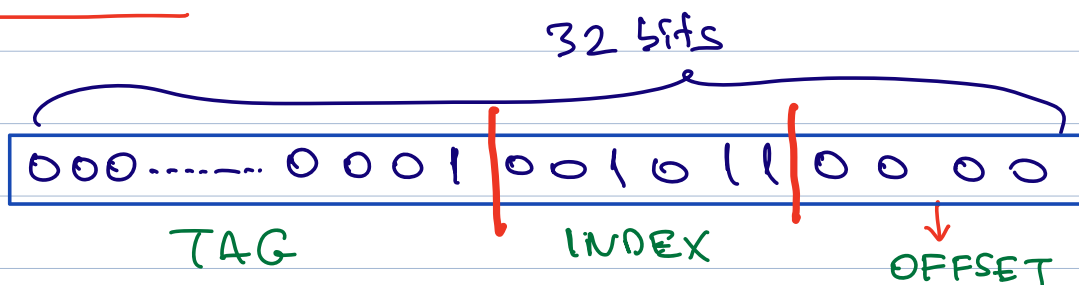
$$\left[\frac{\text{byte addr}}{\text{bytes per block}} \right] \times \text{Bytes per block}$$

$$\left[\frac{\text{byte addr}}{\text{bytes per block}} \right] \times \text{Bytes per block} + (\text{Bytes per block} - 1)$$

Question: Address $\rightarrow 1200$ mapped to which block?

Assume 64 blocks & 1 block = 16 bytes given

Answer



(Block offset +
byte offset)

Index = 11
(Block number)

That block maps all addresses between
1200 and 1245

Total # of Bits for a Cache

Total # of bits needed for a cache is a function of cache size & address size

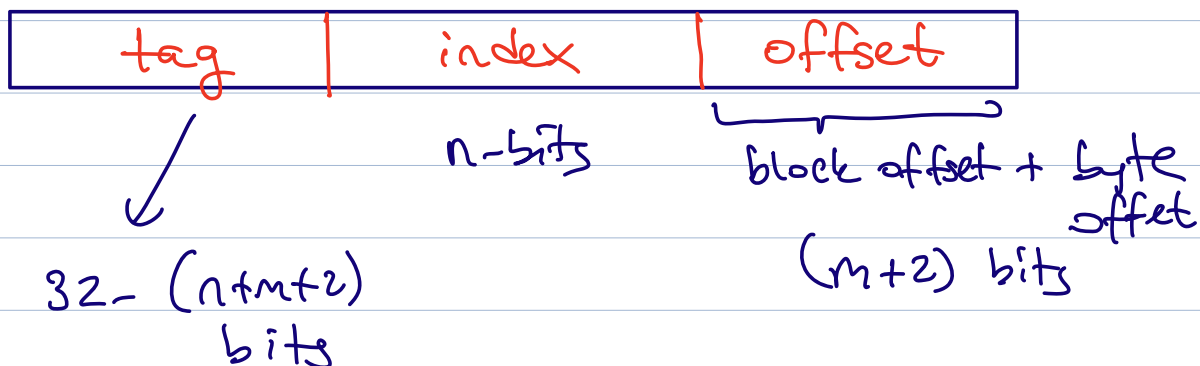
* 32-bit address

* Direct-mapped cache

* Cache size is 2^n blocks (n -bit for index)

* Block size is 2^m words (2^{m+2} bytes)
(m -bits word within block,
2 bits byte part of the addr)

Size of tag field: $32 - (n + m + 2)$



Total # of bits in a direct-mapped cache

$$= 2^n \times (\text{block size} + \text{tag size} + \text{valid field size})$$

$$= 2^n \times (2^m \times 32 + (32 - n - m - 2) + 1)$$

$$= 2^n \times (2^m \times 32 + 31 - n - m)$$

