

Math 104 2nd Midterm Exam 8 April 2019, 19:00-20:00)

IMPORTANT

1. Write down your name and surname on top of each page. 2. The exam consists of 4 questions, some of which have multiple parts. 3. Read each question carefully and put your answers neatly on the answer sheets. Simplify your answers. 4. Show all your work. Correct answers without justification will not get credit. 5. Unless otherwise specified, you may use any method from classwork to solve the problems. 6. Calculators are not allowed. 7. All cell phones and electronic devices are to be kept shut and out of sight. All cell phones are to be left on the instructor's desk prior to the exam.

Q1	Q2	Q3	Q4	TOT
25 pts	25 pts	25 pts	25 pts	100 pts

Q1. Evaluate the following integral:

$$\int \sin^{3} 2\theta \cos^{3} 2\theta d\theta$$

$$\cos^{3} 2\theta \cdot \cos^{3} 2\theta$$

$$(1 - \sin^{3} 2\theta)$$

$$= \int \sin^{3} 2\theta (1 - \sin^{3} 2\theta) \cos^{3} 2\theta d\theta$$

$$= \int \sin^{3} 2\theta \cos^{3} 2\theta d\theta - \int \sin^{5} 2\theta \cos^{3} 2\theta d\theta$$

$$= \int \sin^{3} 2\theta \cos^{3} 2\theta d\theta - \int \sin^{5} 2\theta \cos^{3} 2\theta d\theta$$

$$= \int \sin^{4} 2\theta \cos^{3} 2\theta d\theta$$

$$= \int \sin^{4} 2\theta - \int \sin^{5} 2\theta + C$$

$$= \int \sin^{4} 2\theta - \int \sin^{5} 2\theta + C$$

$$= \int \sin^{4} 2\theta - \int \sin^{5} 2\theta + C$$



Q2. Evaluate the following limit, if it exists.

$$\lim_{x\to 1} (2-x)^{\tan(\frac{\pi x}{2})} \qquad y = (2-x)^{\frac{\pi x}{2}} \qquad \tan \frac{\pi x}{2} \qquad \ln (1-x)^{\frac{\pi x}{2}}$$

$$\lim_{x\to 1} \exp = \lim_{x\to 1} \tan \frac{\pi x}{2} \ln (1-x)^{\frac{\pi x}{2}}$$

$$\lim_{x\to 1} \exp = \lim_{x\to 1} \tan \frac{\pi x}{2} \ln (1-x)^{\frac{\pi x}{2}}$$

$$\lim_{x\to 1} \frac{\ln (1-x)}{2} \ln (1-x)^{\frac{\pi x}{2$$



Q3. Evaluate the following integral:

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$$\int \frac{dx}{(x^2-1)^{3/2}}$$

$$= \begin{cases}
Sec O = x \\
Sec O =$$



Q4. Evaluate the following integral: Integration by parts
$$\int x^2 Arctanx dx \qquad (U = Arctanx) \qquad dv = x^2$$

$$\int x^2 Arctanx dx$$

$$\begin{cases} u = Avctaux & du = x^3 \\ du = \frac{dx}{1+x^2} & v = x^3 \end{cases}$$

$$dv = x^{2}$$

$$v = x^{3}/3$$

=
$$\frac{x^3}{3}$$
 Avetan $\times -\frac{1}{3}$ $\left(\frac{x^3 dx}{1+x^2}\right)$

$$\begin{array}{c|c} \times^3 & \times^2 + 1 \\ \hline \times^3 + \times & \times \end{array}$$

$$= \frac{x^3}{3} \operatorname{Arctanx} - \frac{1}{3} \left(x - \frac{x}{x^2 H} \right) dx$$

$$= \frac{x^3}{3} Arctaux - \frac{x^2}{6} + \frac{1}{3} \cdot \frac{1}{2} \int \frac{2 \times dx}{x^2 + 1}$$

=
$$\frac{x^3}{3}$$
 Arctaux - $\frac{x^2}{6}$ + $\frac{1}{6}$ ln(x^2 +1)+C