

**Student:** Huseyin Kerem Mican  
**Date:** 7/1/21

**Instructor:** Taylan Sengul  
**Course:** Linear Algebra

**Assignment:** Section 3.2 Homework

1. Find the determinant by row reduction to echelon form.

$$\begin{vmatrix} 1 & 5 & -7 \\ -1 & -4 & -5 \\ 2 & 8 & 7 \end{vmatrix}$$

Use row operations to reduce the matrix to echelon form.

$$\begin{bmatrix} 1 & 5 & -7 \\ -1 & -4 & -5 \\ 2 & 8 & 7 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

Find the determinant of the given matrix.

$$\begin{vmatrix} 1 & 5 & -7 \\ -1 & -4 & -5 \\ 2 & 8 & 7 \end{vmatrix} = \underline{-3} \quad (\text{Simplify your answer.})$$

2. Find the determinant by row reduction to echelon form.

$$\begin{vmatrix} 1 & -1 & -3 & 0 \\ 7 & -6 & 3 & 2 \\ 1 & 3 & -2 & 3 \\ -3 & 7 & 10 & 3 \end{vmatrix}$$

Use row operations to reduce the matrix to echelon form.

$$\begin{bmatrix} 1 & -1 & -3 & 0 \\ 7 & -6 & 3 & 2 \\ 1 & 3 & -2 & 3 \\ -3 & 7 & 10 & 3 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 & 0 & \frac{17}{19} \\ 0 & 1 & 0 & \frac{14}{19} \\ 0 & 0 & 1 & \frac{1}{19} \\ 0 & 0 & 0 & 0 \end{bmatrix}$$

Find the determinant of the given matrix.

$$\begin{vmatrix} 1 & -1 & -3 & 0 \\ 7 & -6 & 3 & 2 \\ 1 & 3 & -2 & 3 \\ -3 & 7 & 10 & 3 \end{vmatrix} = \underline{0} \quad (\text{Simplify your answer.})$$

3. Find the determinant by row reduction to echelon form.

$$\begin{vmatrix} 1 & -3 & 1 & 0 & -6 \\ 0 & 2 & -2 & 9 & 2 \\ -2 & 6 & -2 & 2 & 4 \\ 1 & -5 & 4 & 1 & 6 \\ 0 & 2 & -2 & 11 & 4 \end{vmatrix}$$

Use row operations to reduce the matrix to echelon form.

$$\begin{bmatrix} 1 & -3 & 1 & 0 & -6 \\ 0 & 2 & -2 & 9 & 2 \\ -2 & 6 & -2 & 2 & 4 \\ 1 & -5 & 4 & 1 & 6 \\ 0 & 2 & -2 & 11 & 4 \end{bmatrix} \sim \begin{bmatrix} 1 & 0 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 0 & 1 \end{bmatrix}$$

Find the determinant of the given matrix.

$$\begin{vmatrix} 1 & -3 & 1 & 0 & -6 \\ 0 & 2 & -2 & 9 & 2 \\ -2 & 6 & -2 & 2 & 4 \\ 1 & -5 & 4 & 1 & 6 \\ 0 & 2 & -2 & 11 & 4 \end{vmatrix} = \underline{-40} \text{ (Simplify your answer.)}$$

4. Combine the methods of row reduction and cofactor expansion to compute the determinant.

$$\begin{vmatrix} -1 & 2 & 6 & 0 \\ 3 & 3 & 5 & 0 \\ 7 & 6 & 8 & 6 \\ 5 & 3 & 5 & 3 \end{vmatrix}$$

The determinant is 126.  
(Simplify your answer.)

5. Combine the methods of row reduction and cofactor expansion to compute the determinant.

$$\begin{vmatrix} 1 & 5 & 4 & 1 \\ 0 & -4 & -8 & 0 \\ 3 & 5 & 4 & 1 \\ -6 & 4 & 4 & 0 \end{vmatrix}$$

The determinant is 32.  
(Simplify your answer.)

6.

Find the determinant below, where  $\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = 8$ .

$$\begin{vmatrix} a & b & c \\ d & e & f \\ 7g & 7h & 7i \end{vmatrix}$$

$$\begin{vmatrix} a & b & c \\ d & e & f \\ 7g & 7h & 7i \end{vmatrix} = \underline{56} \quad (\text{Simplify your answer.})$$

7.

If  $\begin{vmatrix} a & b & c \\ d & e & f \\ g & h & i \end{vmatrix} = 3$ , find  $\begin{vmatrix} a & b & c \\ 6d+g & 6e+h & 6f+i \\ g & h & i \end{vmatrix}$ .

$$\begin{vmatrix} a & b & c \\ 6d+g & 6e+h & 6f+i \\ g & h & i \end{vmatrix} = \underline{18} \quad (\text{Simplify your answer.})$$

8. Use determinants to find out if the matrix is invertible.

$$\begin{bmatrix} -5 & 0 & 1 \\ 1 & -3 & -2 \\ 0 & -5 & -3 \end{bmatrix}$$

The determinant of the matrix is 0. (Simplify your answer.)

Is the matrix invertible? Choose the correct answer below.

- ☐ The matrix is invertible.
- ☒ The matrix is not invertible.

9. Use determinants to find out if the matrix is invertible.

$$\begin{bmatrix} 1 & -1 & -2 & 0 \\ 0 & 1 & 5 & 4 \\ 3 & -1 & -3 & 4 \\ -1 & 2 & 7 & 5 \end{bmatrix}$$

The determinant of the matrix is -7. (Simplify your answer.)

Is the matrix invertible? Choose the correct answer below.

- ☒ **A.** The matrix is invertible.
- ☐ **B.** The matrix is not invertible.

10. Use determinants to decide if the set of vectors is linearly independent.

$$\begin{bmatrix} 4 \\ -7 \\ 1 \end{bmatrix}, \begin{bmatrix} -5 \\ 8 \\ 4 \end{bmatrix}, \begin{bmatrix} 4 \\ 0 \\ -8 \end{bmatrix}$$

The determinant of the matrix whose columns are the given vectors is -120.  
(Simplify your answer.)

Is the set of vectors linearly independent? Choose the correct answer below.

- ☐ A. The set of vectors is linearly dependent, because the determinant is not zero.
- ☒ B. The set of vectors is linearly independent, because the determinant is not zero.
- ☐ C. The set of vectors is linearly dependent, because the determinant exists.
- ☐ D. The set of vectors is linearly independent, because the determinant exists.

11.

Compute  $\det B^4$  where  $B = \begin{bmatrix} 1 & 0 & 2 \\ 2 & 2 & 3 \\ 2 & 2 & 2 \end{bmatrix}$ .

$\det B^4 =$  16 (Simplify your answer.)

12. Verify that  $\det AB = (\det A)(\det B)$ , where the matrices A and B are given below.

$$A = \begin{bmatrix} 5 & 0 \\ 10 & 1 \end{bmatrix}, B = \begin{bmatrix} 3 & 0 \\ 5 & 6 \end{bmatrix}$$

Calculate  $\det A$  and  $\det B$ .

$\det A =$  5,  $\det B =$  18 (Simplify your answers.)

Now calculate the product  $(\det A)(\det B)$ .

$(\det A)(\det B) =$  90 (Simplify your answer.)

Calculate the product of matrices AB.

$AB =$   $\begin{bmatrix} 15 & 0 \\ 35 & 6 \end{bmatrix}$  (Type an integer or decimal for each matrix element.)

Now calculate the determinant of the product of matrices A and B.

$\det (AB) =$  90 (Simplify your answer.)

13. Let  $A$  and  $B$  be  $3 \times 3$  matrices, with  $\det A = 4$  and  $\det B = 3$ . Use properties of determinants to complete parts (a) through (e) below.
- 

a. Compute  $\det AB$ .

$\det AB =$  12 (Type an integer or a fraction.)

b. Compute  $\det 5A$ .

$\det 5A =$  500 (Type an integer or a fraction.)

c. Compute  $\det B^T$ .

$\det B^T =$  3 (Type an integer or a fraction.)

d. Compute  $\det A^{-1}$ .

$\det A^{-1} =$   $\frac{1}{4}$  (Type an integer or a simplified fraction.)

e. Compute  $\det A^3$ .

$\det A^3 =$  64 (Type an integer or a fraction.)