

## CSE2023 - ASSIGNMENT #5

Solve the following questions from course book. (Discrete Mathematics and Discrete Mathematics and Its Applications, 7th Ed. by Kenneth Rosen)

Note that we may grade selected questions from HWs.

\* Show all your works.

- 1) Find the solution to  $a_n = 3a_{n-1} + a_{n-2} - 3a_{n-3}$  for  $n = 3, 4, 5, \dots$ , with  $a_0 = 4$ ,  $a_1 = 10$ , and  $a_2 = 12$ .
- 2) Find the solution of the recurrence relation  $a_n = 3a_{n-1} + 5 \cdot 3^n$ .
- 3) A new employee at an exciting new software company starts with a salary of \$2000 and is promised that at the end of each year her salary will be double her salary of the previous year, with an extra increment of \$150 for each year she has been with the company.
  - a) Construct a recurrence relation for her salary for her  $n$ th year of employment.
  - b) Solve this recurrence relation to find her salary for her  $n$ th year of employment
- 4) Let  $R$  be the relation on the set of people with doctorates such that  $(a, b) \in R$  if and only if  $a$  was the thesis advisor of  $b$ . When is an ordered pair  $(a, b)$  in  $R^2$ ? When is an ordered pair  $(a, b)$  in  $R^n$ , when  $n$  is a positive integer? (Assume that every person with a doctorate has a thesis advisor.)
- 5) How can the matrix for  $R^{-1}$ , the inverse of the relation  $R$ , be found from the matrix representing  $R$ , when  $R$  is a relation on a finite set  $A$ ?

### Submission Instruction (10p)

Please zip and submit all your files using filename YourNumberHW5.zip (ex: 150629573HW5.zip) to Canvas system (under Assignments tab).

Your zip file should contain the following:

1. Single PDF file for solutions (150629573HW5.pdf)

### Notes:

1. Write your name and student ID on each sheet.
2. No late submission will be accepted