Full Name: KEY



Math 104 – 2<sup>nd</sup> Midterm Exam (26 November 2018, Time: 17:00-18:00)

## **IMPORTANT**

1. Write down your name and surname on top of each page. 2. The exam consists of 4 questions, some of which have multiple parts. 3. Read each question carefully and put your answers neatly on the answer sheets. Simplify your answers. 4. Show all your work. Correct answers without justification will not get credit. 5. Unless otherwise specified, you may use any method from classwork to solve the problems. 6. Calculators are not allowed. 7. All cell phones, smart watches and electronic devices are to be kept shut and out of sight. All cell phones and smart watches are to be left on the instructor's desk prior to the

Q1	Q2	Q3	Q4	TOT
6 pts	6 pts	6 pts	6 pts	24 pts

Evaluate the following limit  $\lim_{x\to 0} (1-\sin x)^{\frac{1}{\sin x}} = 1^{\infty}$ , indeterminate power Q1. y = (1- Sinx) sinx lug = lu (1-sinx)  $\lim_{x\to 0} \lim_{x\to 0} = \lim_{x\to 0} \frac{\ln(1-\sin x)}{\sin x} = \frac{0}{0}$ , indeterminate form. = light - losx 1-Ginx , 2'Hospital Rule x+0 losx L' luy = - L' - 1-sinx =-1 ling y = e' = 1/e (1-5,mx) Tinx = 1/e

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Q2. Evaluate the following integral

$$\int_{0}^{2} \frac{dx}{\sqrt{4-x^2}}$$

$$x = 25 \text{ int}$$
,  $dx = 2600 do$ 

$$4 \text{ int} = x/2$$

$$\int \frac{dn}{\sqrt{4-x^2}} = \int \frac{2610}{2\sqrt{1-5in^20}} d\theta = \int \frac{2690}{2\sqrt{650}} d\theta = \int d\theta = \theta = \sin(\frac{x}{2}) \Big|_{0}^{2}$$

$$= \frac{x}{2}$$

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Q3. Evaluate the following integral  $\int \frac{dx}{x^2 - 3x + 2}$ 

$$\frac{1}{\chi^{2}-3\chi+2} = \frac{A}{\chi-1} + \frac{B}{\chi-2}$$

$$= \frac{1}{\chi^{2}-3\chi+2} = \frac{\chi-1}{\chi-2} + \frac{\chi}{\chi-2} = \frac{\chi}{\chi-2}$$

$$1 = (x-2)A + (x-1)B$$

$$\chi=1: 1=-A \Rightarrow A=-1$$

$$\chi = 1$$
:  $\chi = 2$ :  $\chi = 2$ :  $\chi = 3$  =  $\chi = 1$ 

$$\int \frac{dn}{x^{2}-3x+2} = -\int \frac{dx}{x-1} + \int \frac{dx}{x-2}$$

$$= -\ln|x-1| + \ln|x-2| + G$$

$$= -\ln\left|\frac{x-2}{x-1}\right| + G$$

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Q4. (a) Evaluate the following integral

the following integral 
$$\int e^x \ln x \, dx = \int u \, dv = uv - \int v \, du$$
  
 $u = lux$ ,  $du = dx/x$ ,  $dv = e^x dx$ ,  $v = e^x$ 

$$\int e^{x} \ln x \, dx = e^{x} \ln x - \int \frac{e^{x}}{x} dx$$

$$u' = e^{x} \int e^{x} dx$$

$$du' = e^{x} dx \quad e' = \ln x$$

$$= e^{x \ln x} - \left[e^{x \ln x} - \int e^{x \ln x} dx\right]$$

$$\int e^{x \ln x} dx = e^{x \ln x} - e^{x \ln x} + \int e^{x \ln x} dx$$

0 = 0 No slus 1

(b) Evaluate the following integral  $\int \cos^3 x \sin^4 x \, dx$ 

$$\int G_{3}^{2} \times S_{1}^{2} u^{2} \times G_{2} \times G_{3} \times G_{4} \times G_{4} \times G_{5} \times G_{5$$