

<u>Binomial Probability Distribution</u> $P(x = k) = C_k^n p^k q^{n-k} = \frac{n!}{k!(n-k)!} p^k q^{n-k}$ Mean : $\mu = np$ Variance : $\sigma^2 = npq$ Standard deviation : $\sigma = \sqrt{npq}$	<u>Hypergeometric Probability Distribution</u> $P(x = k) = \frac{C_k^M C_{n-k}^{N-M}}{C_n^N}$ $M \rightarrow$ successes, $N-M \rightarrow$ failures, $n \rightarrow$ size of the random sample space Mean : $\mu = n \left(\frac{M}{N} \right)$ Variance : $\sigma^2 = n \left(\frac{M}{N} \right) \left(\frac{N-M}{N} \right) \left(\frac{N-n}{N-1} \right)$
<u>Poisson Probability Distribution</u> $P(x = k) = \frac{\mu^k e^{-\mu}}{k!}$ Mean: $E(x) = \mu$ Variance : $\sigma^2 = \mu$ Standard deviation: $\sigma = \sqrt{\mu}$	Variance of a Sample $s^2 = \frac{\sum (x_i - \bar{x})^2}{n-1} = \frac{\sum x_i^2 - \frac{(\sum x_i)^2}{n}}{n-1}$ Variance of Population: $\sigma^2 = \frac{\sum (x_i - \mu)^2}{N}$
Correlation coefficient, $r = \frac{S_{xy}}{S_x S_y}$	<u>Normal Distribution, $N(\mu, \sigma^2)$</u>

<u>Standardizing the value of \bar{x} :</u> $z = \frac{\bar{x} - \mu}{\sigma / \sqrt{n}}$	<u>Standardizing the value \hat{p} :</u> $z = \frac{\hat{p} - p}{\sqrt{\frac{pq}{n}}}$
<u>Statistical Process Control</u> LCL : $\bar{\bar{x}} - 3 \frac{s}{\sqrt{n}}$ UCL : $\bar{\bar{x}} + 3 \frac{s}{\sqrt{n}}$ LCL : $\bar{p} - 3 \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$ UCL : $\bar{p} + 3 \sqrt{\frac{\bar{p}(1-\bar{p})}{n}}$	Confidence interval for a population mean μ : $\bar{x} \pm z_{\alpha/2} \frac{s}{\sqrt{n}}$ Confidence interval for a population proportion p : $\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}\hat{q}}{n}}$
Point estimator of population mean μ : \bar{x} The 95% margin of error ($n \geq 30$) : $\pm 1.96 \frac{s}{\sqrt{n}}$	Point estimator of population proportion p : $\hat{p} = x/n$ The 95% margin of error ($n \geq 30$) : $\pm 1.96 \sqrt{\frac{\hat{p}\hat{q}}{n}}$

<p>Standardizing the value of a test statistic :</p> $\{Z_t\} = \frac{(test_statistic) - (population\ parameter)}{SE}$ <p>Standard Error (SE)</p> $SE = \frac{\sigma}{\sqrt{n}}, \quad \text{or}$ $SE = \sqrt{\frac{\hat{p}\hat{q}}{n}}, \quad \text{or}$ $SE = \sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}, \quad \text{or}$ $SE = \sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}, \quad \text{or}$ $SE = \sqrt{s^2 \left(\frac{1}{n_1} + \frac{1}{n_2} \right)} \quad (\text{for two small samples with common variance})$	<table> <tr> <th>Parameter</th><th>Test Statistic</th></tr> <tr> <td>μ</td><td>$z = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$</td></tr> <tr> <td>$p$</td><td>$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$</td></tr> <tr> <td>$\mu_1 - \mu_2$</td><td>$z = \frac{(\bar{x}_1 - \bar{x}_2) - D_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$</td></tr> <tr> <td>$p_1 - p_2$</td><td>$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad \text{or} \quad z = \frac{(\hat{p}_1 - \hat{p}_2) - D_0}{\sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}}$</td></tr> </table> <p>Bound, B</p> $z_{\alpha/2} \left(\frac{\sigma}{\sqrt{n}} \right) < B, \quad \text{or}$ $z_{\alpha} \left(\frac{\sigma}{\sqrt{n}} \right) < B, \quad \text{or}$ $z_{\alpha/2} \left(\sqrt{\frac{pq}{n}} \right) < B, \quad \text{or}$ $z_{\alpha} \left(\sqrt{\frac{pq}{n}} \right) < B$	Parameter	Test Statistic	μ	$z = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$	p	$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$	$\mu_1 - \mu_2$	$z = \frac{(\bar{x}_1 - \bar{x}_2) - D_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$	$p_1 - p_2$	$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad \text{or} \quad z = \frac{(\hat{p}_1 - \hat{p}_2) - D_0}{\sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}}$
Parameter	Test Statistic										
μ	$z = \frac{\bar{x} - \mu_0}{s/\sqrt{n}}$										
p	$z = \frac{\hat{p} - p_0}{\sqrt{\frac{p_0 q_0}{n}}}$										
$\mu_1 - \mu_2$	$z = \frac{(\bar{x}_1 - \bar{x}_2) - D_0}{\sqrt{\frac{s_1^2}{n_1} + \frac{s_2^2}{n_2}}}$										
$p_1 - p_2$	$z = \frac{\hat{p}_1 - \hat{p}_2}{\sqrt{\hat{p}\hat{q}\left(\frac{1}{n_1} + \frac{1}{n_2}\right)}} \quad \text{or} \quad z = \frac{(\hat{p}_1 - \hat{p}_2) - D_0}{\sqrt{\frac{\hat{p}_1\hat{q}_1}{n_1} + \frac{\hat{p}_2\hat{q}_2}{n_2}}}$										
<p>pooled estimate for the common value of p (large samples)</p> $\hat{p} = \frac{x_1 + x_2}{n_1 + n_2}$	<p>Common variance for two samples (small samples)</p> $s^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2}$										
$\chi^2 = \frac{(n - 1)s^2}{\sigma^2}$	$F = \frac{s_1^2}{s_2^2}$										
<p>Variance of a Sample</p> $s^2 = \frac{\sum (x_i - \bar{x})^2}{n - 1} = \frac{\sum x_i^2 - \frac{(\sum x_i)^2}{n}}{n - 1}$	<p>Variance of Population:</p> $\sigma^2 = \frac{\sum (x_i - \mu)^2}{N}$										
<p>Confidence Interval for σ^2</p> $\frac{(n - 1)s^2}{\chi_{\alpha/2}^2} < \sigma^2 < \frac{(n - 1)s^2}{\chi_{(1-\alpha/2)}^2}$	<p>Confidence Interval for σ_1^2 / σ_2^2</p> $\left(\frac{s_1^2}{s_2^2} \right) \frac{1}{F_{df_1, df_2}} < \frac{\sigma_1^2}{\sigma_2^2} < \left(\frac{s_1^2}{s_2^2} \right) F_{df_2, df_1}$										