

Q1)

for (i=0; i<n; i++)
 for (j=1; j<=i; j*=2)
 statement block;

	1st for	2nd for
n=0	1	0
n=1	2	0+1
n=2	3	0+1+2
n=3	4	0+1+2+2
n=4	5	0+1+2+2+3 - - -

0+1+2+2+3+3+3+4

$$\sum_{k=1}^n (\lfloor \log_2 k \rfloor + 1)$$

Q2)

Calculate the approximate value of the variable `sum` after the following code fragment, in terms of variable `n`. Use summation notation to compute a closed-form solution (ignore small errors caused by `i` not being evenly divisible by 2). Then use this value to give a tightly bounded Big-Oh analysis of the runtime of the code fragment.

```
int sum = 0;
for (int i = 1; i <= 10; i++) {
    for (int j = n; j <= n + i + 2; j++) {
        sum++;
        sum++;
    }
}

for (int i = 0; i < n; i += 2) {
    sum++;
}
```

$$\begin{aligned}
 & \left(\sum_{i=1}^{10} \sum_{j=n}^{n+i+2} 2 \right) + \sum_{i=0}^{\frac{n}{2}} 1 \\
 & \left(\sum_{i=1}^{10} 2(n + i + 2 - n + 1) \right) + \frac{n}{2} \\
 & \left(\sum_{i=1}^{10} 2 \cdot (i + 3) \right) + \frac{n}{2} \\
 & \sum_{i=1}^{10} (2 \cdot i + 6) + \frac{n}{2} \\
 & \sum_{i=1}^{10} 2 \cdot i + \sum_{i=1}^{10} 6 + \frac{n}{2} \\
 & 2 \sum_{i=1}^{10} i + 60 + \frac{n}{2} \\
 & 2 \frac{10(11)}{2} + 60 + \frac{n}{2} \\
 & 110 + 60 + \frac{n}{2} \\
 & 170 + \frac{n}{2}
 \end{aligned}$$

Q3)

```
int count = 0;
for (int i = 0; i < n * n; i++) {
    for (int j = 0; j < n; j++) {
        count++;
    }
}
```

0, 1, 2, 3

<u>n</u>	<u>1st for</u>	<u>2nd for</u>
0	0	0
1	1	1
2	4	2
3	9	3
⋮		
n	n^2	n

$n^2 \times n = n^3 = O(n^3)$

Q4)

for (i=1; i<=n ; i+=3)
for (j=1; j<=n ; j+=2)
stop and

<u>n</u>	<u>1st loop</u>	<u>2nd loop</u>
0	0	0
1	1	1
2	1	2
3	2	2
4	2	3
5	2	3
6	2	4
7	2	4
8	2	4
9	3	4

$\left(\lfloor \log_3 n \rfloor + 1 \right) \times \left(\lfloor \log_2 n \rfloor + 1 \right)$

Q5)

```

1 count = 0 ; i = 1;
do {
    for (j = 1; j <= n; j += 2)
        count += j;
    i++;
} while (i <= n);
print ("count = %d", count);

```

Big Oh $O \rightarrow$

n	while	for
1	1	1
2	2	2
3	3	2
4	4	
	:	
	:	

$n \times (\lfloor \log_2 n \rfloor + 1)$