

Recursion → function call

↓      ↓  
itself

1) Factorial

↓  
2) Base case condition

↓  
terminate

2) Recursive calls

fact(m)

$0! = 1$

if( $m == 0$  or  $m == -1$ )  
 $!! = 1$

return 1;

)

return  $m * \underline{\underline{\text{fact}(n-1)}}$

$n=5$

$$5! = \cancel{5} \times \cancel{4} \times \cancel{3} \times \cancel{2} \times 1$$

$$\text{fact}(5) = \cancel{5} \times \underline{\underline{\text{fact}(4)}} = 120$$

$$6 = 24$$

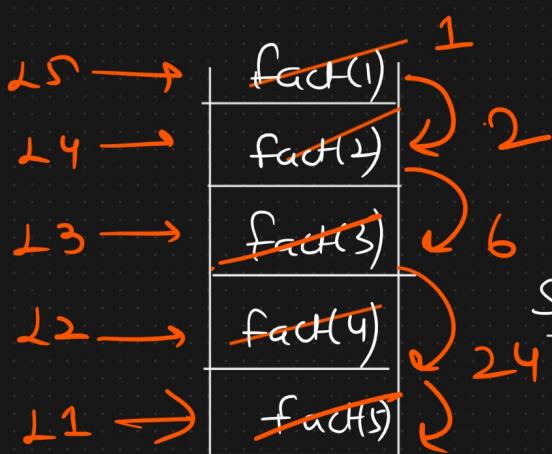
$$4 \times \underline{\underline{\text{fact}(3)}} = 24$$

$$6 = 6$$

$$3 \times \underline{\underline{\text{fact}(2)}} = 6$$

$$2 \times \underline{\underline{\text{fact}(1)}} = 2$$

1



↑  
Store  
function

Stack

LIFO

Call

120

$\mathcal{O}(n)$  - space complexity

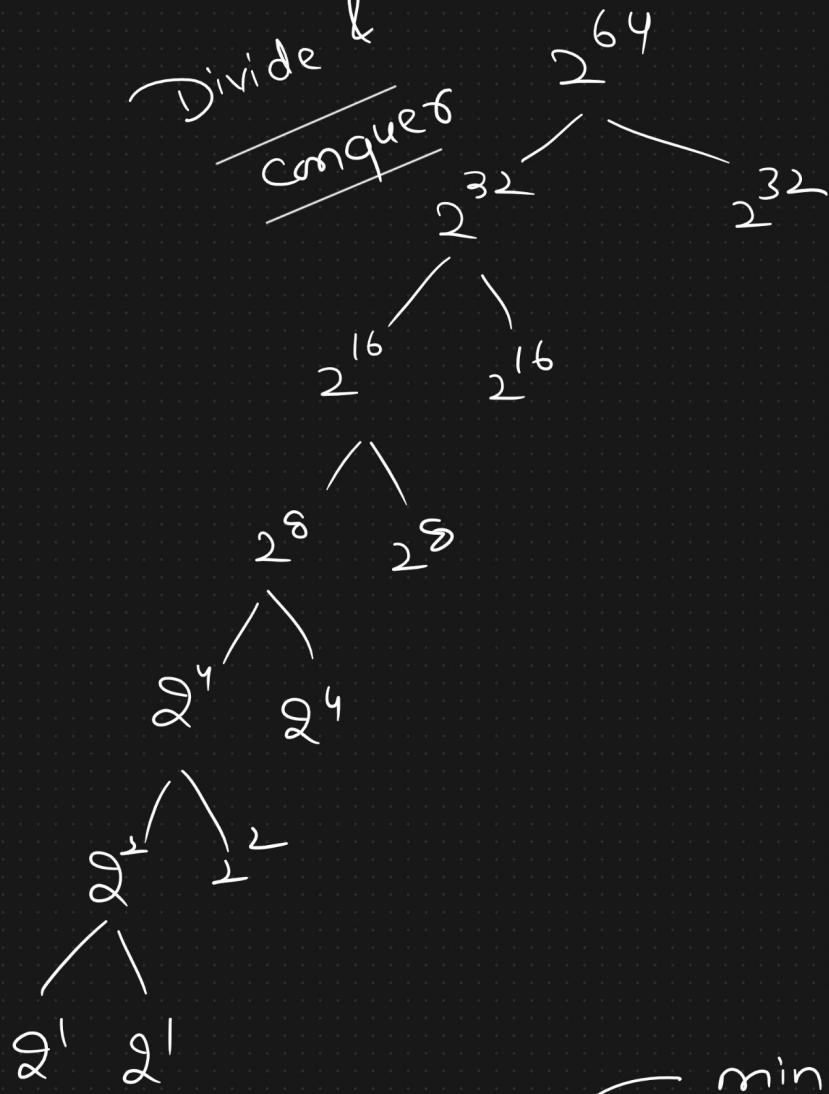
# Recursion (Real-time usage)

Advantages

- 1) Complex tasks  $\xrightarrow{\text{split}}$  simpler task

## Power function

Divide & Conquer



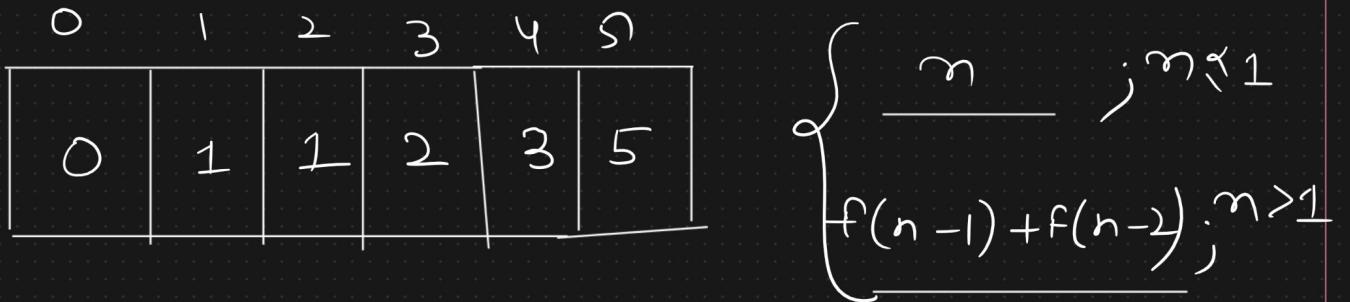
- 2) Short & Efficient

min time complexity  
for space

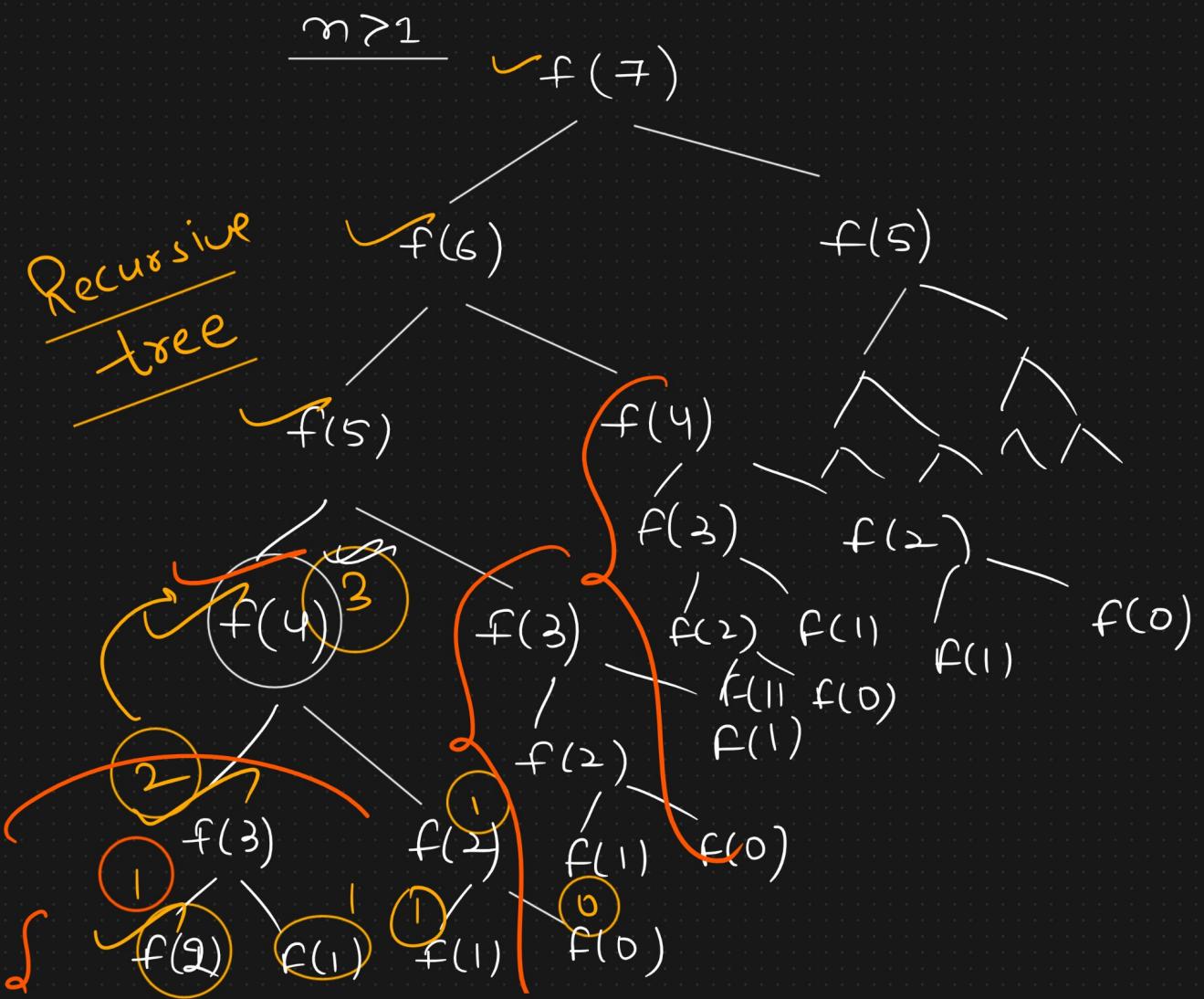
- 3) Interview  $\frac{50:00 \text{ min}}{2 \text{ Problems}}$

## Disadvantage

↳ Time Limit Exceeded



$$\begin{aligned}
 f(6) &= f(5) + f(4) \\
 &= 5 + 3 \\
 &= 8
 \end{aligned}$$



f(1) f(0)

→ Count of number of stairs

→ Binary search Recursion

→ Multiples

$$k = 5, \text{num} = 4$$

$$\underline{4, 8, 12, 16, 20}$$

→ Sum of Digits

$$\text{num} = 12345$$

$$\text{sum} = 1 + 2 + 3 + 4 + 5$$

Bal<sup>k</sup>      call      num = 0        = 15

  0

Recursive      call      num % 10 + sum (num / 10)

$$-1 + 3 - 4 - 1 \\ 1 - 2 + 3 - 4 + 5 - 6 = -3$$

n      m = 6

$m = 5$

(1)      Alternate sign  
pattern

$$1 - \cancel{2} + 3 - \cancel{4} + 5 = \underline{\underline{3}}$$

+ sign  
Odd num

```

alternateSign(Even m)
if(m==0) return 0; - sign
if(m%2 == 0) even

```

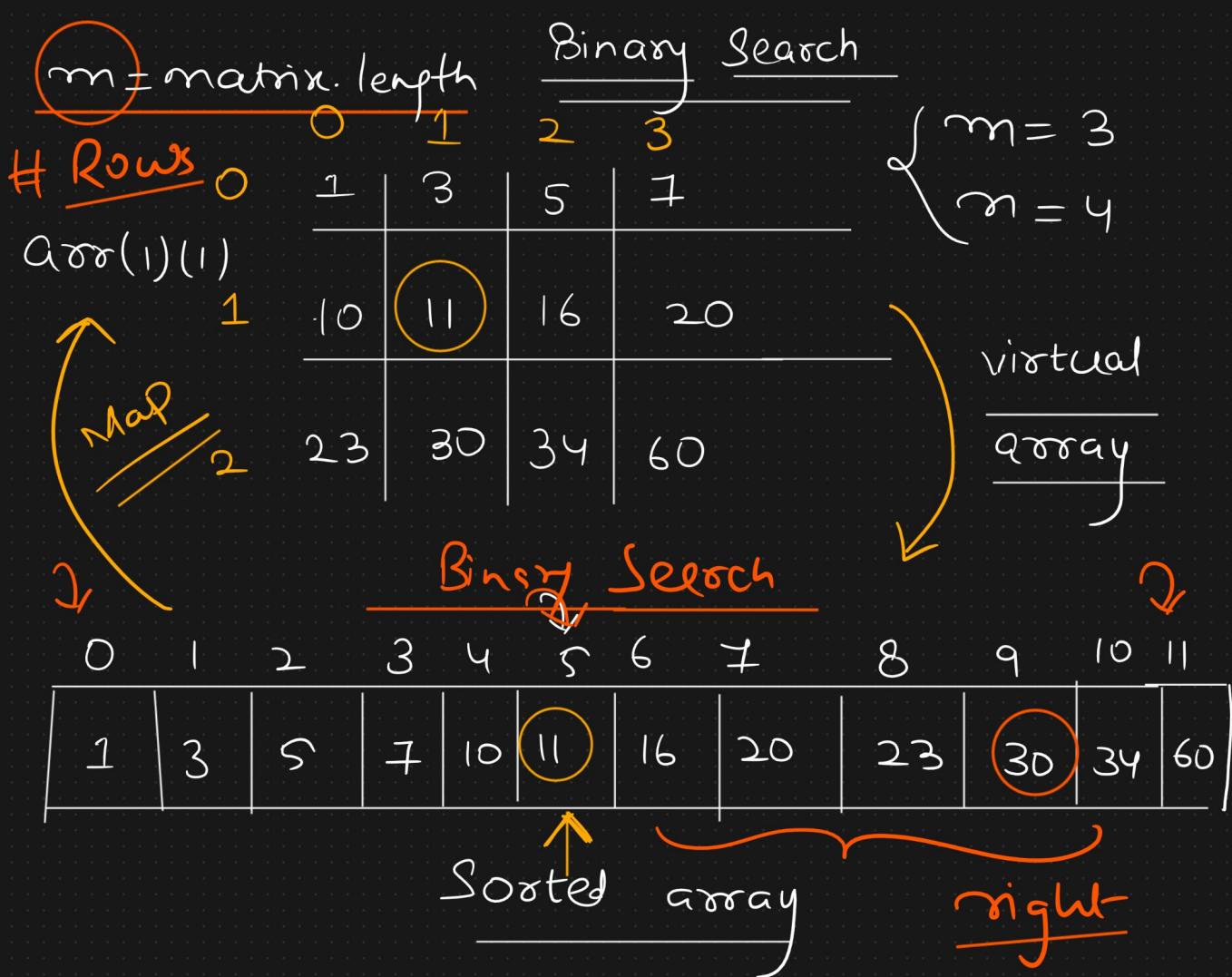
Recursive call

$$\left\{ \begin{array}{l} \text{if } m-1 \text{ is odd num} \\ \quad \text{alternateSign}(m-1) - m \\ \text{else } m \text{ is odd num} \\ \quad \text{alternateSign}(m-1) + m \end{array} \right.$$

$$\begin{array}{r}
 \frac{\text{alternateSign}(5)}{|} = 3 \\
 -2 + 5 = 3 \\
 \frac{\text{alternateSign}(4) + 5}{|} \\
 2 - 4 = -2 \\
 \frac{\text{alternateSign}(3) - 4}{|} \\
 -1 + 3 = 2 \\
 \frac{\text{alternateSign}(2) + 3}{|} \\
 1 = -1 \\
 \frac{\text{alternateSign}(1) - 2}{|} \\
 1 \\
 \frac{\text{alternateSign}(0) + 1}{|} \\
 0
 \end{array}$$

H col.

$m = \underline{\text{matrix}[0].length}$



$$\text{low} = 0, \underline{\text{high}} = 11$$

$\text{while}(\text{low} <= \text{high})$        $m \times m - 1$

$$\text{midIdx} = \text{low} + (\text{high} - \text{low}) / 2;$$

$$\text{midEle} = \text{arr} \left( \frac{\text{midIdx}/n}{\text{low}} \right) \left( \frac{\text{midIdx \% n}}{\text{col.}} \right)$$

$n = \# \text{columns}$

$$\text{RowNum} = 5 / 4 = 1$$

$$\text{ColNum} = 5 \% 4 = 1$$

if ( $\text{midEle} == \text{target}$ )  
    return true;

}

else if ( $\text{midEle} < \text{target}$ )  
    right —

        low = mid + 1;

}

else  $\alpha$

    left —

        high = mid - 1;

}

}

return false

}

