

# EE2000 Logic Circuit Design

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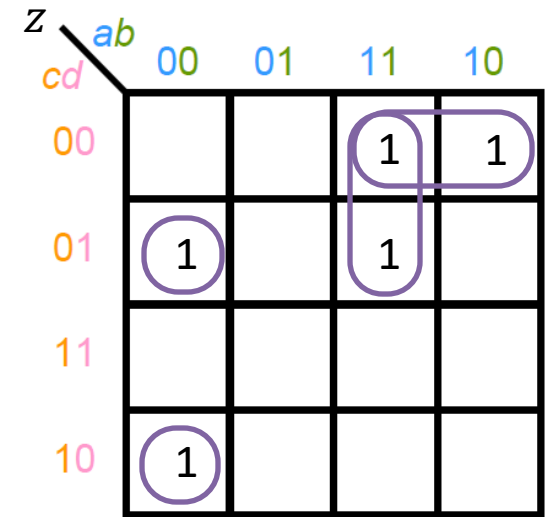
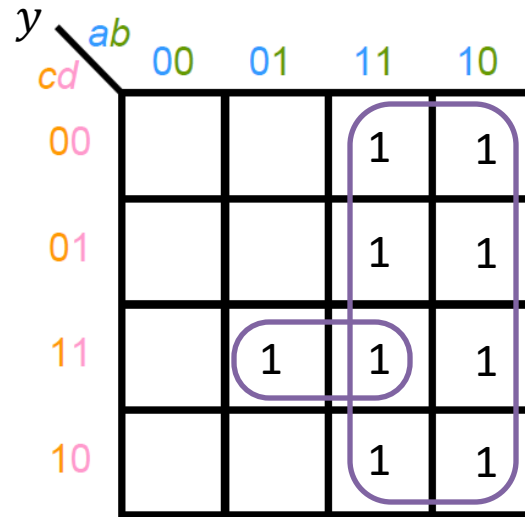
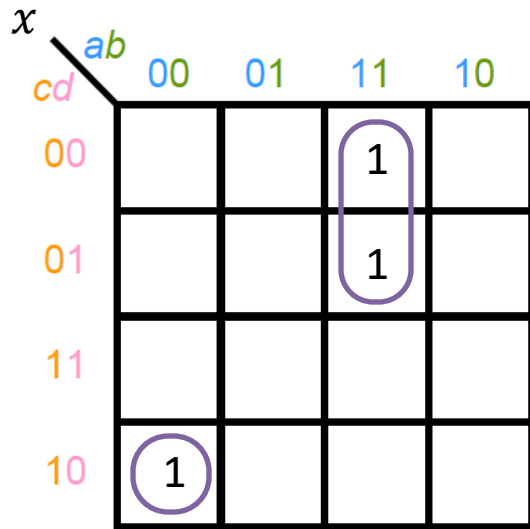
## Lecture 6 – Programmable Logic Devices



[mouser.com](https://www.mouser.com)

# Exercise

Implement the following functions with a PAL



$$x(a, b, c, d) = abc' + a'b'cd'$$

$$y(a, b, c, d) = a + bcd$$

$$z(a, b, c, d) = abc' + a'b'cd' + a'b'c'd + ac'd'$$

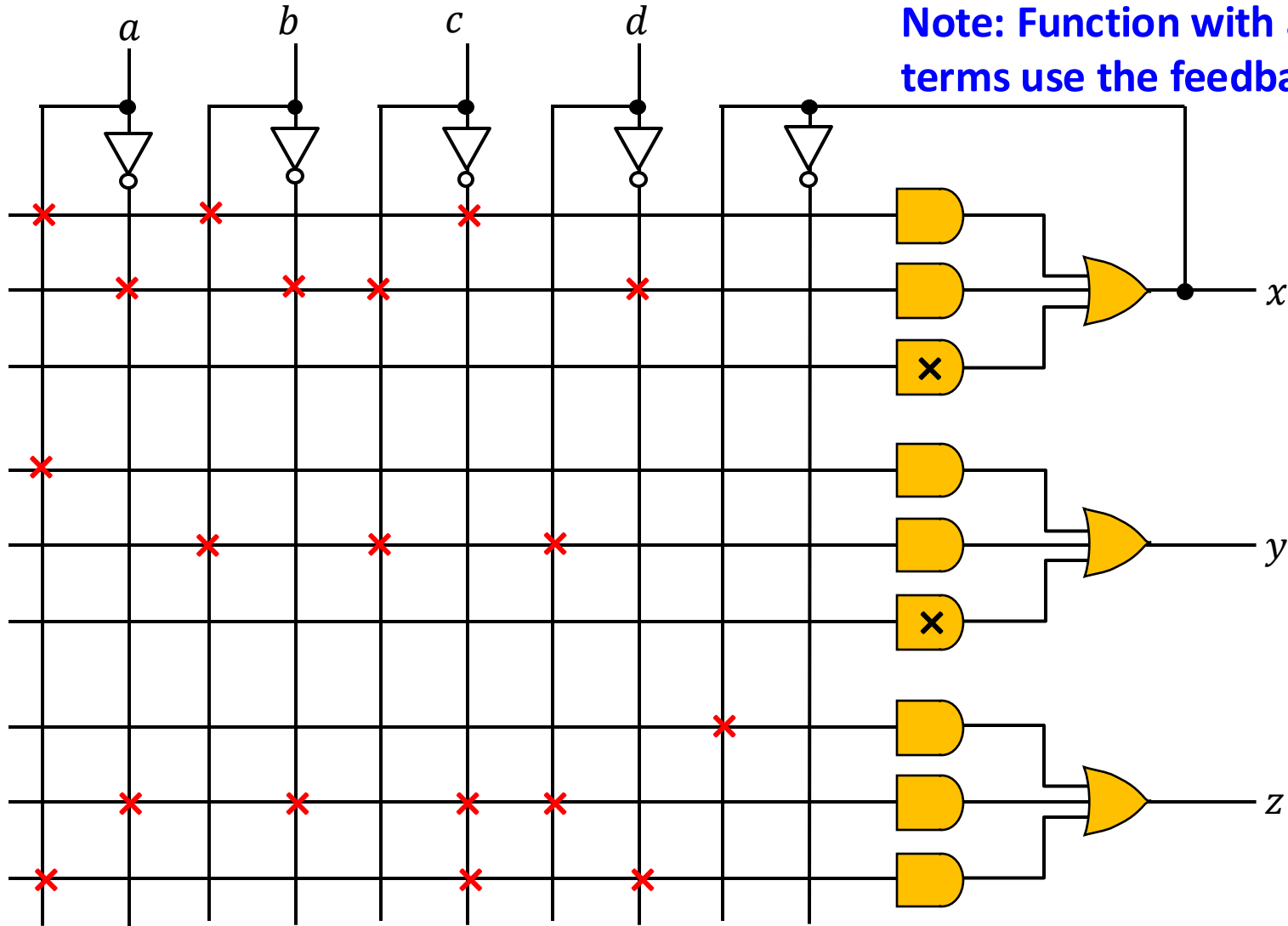
# Exercise

$$x(a, b, c, d) = abc' + a'b'cd'$$

$$y(a, b, c, d) = a + bcd$$

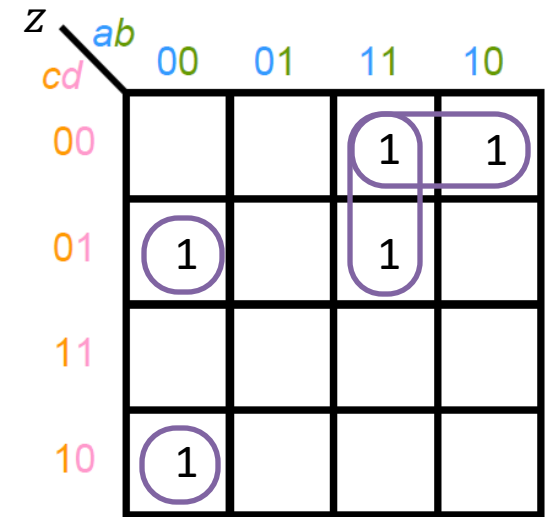
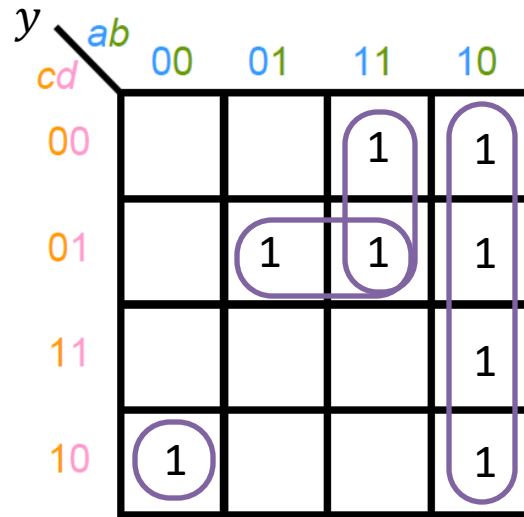
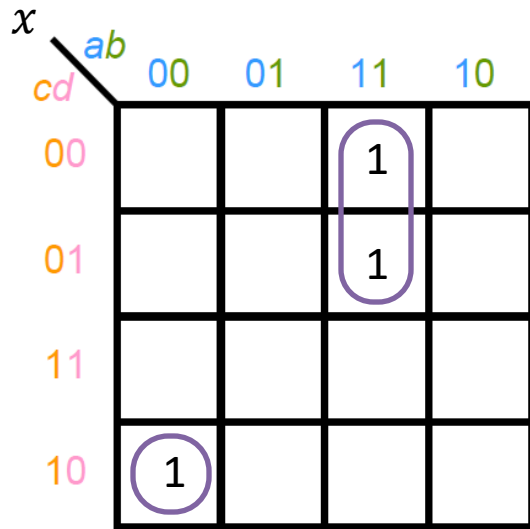
$$z(a, b, c, d) = abc' + a'b'cd' + a'b'c'd + ac'd'$$

**Note: Function with all common terms use the feedback loop**



# Exercise

Implement the following functions with a PAL



$$x(a, b, c, d) = a'b'cd' + abc'$$

$$y(a, b, c, d) = a'b'cd' + abc' + bc'd + ab'$$

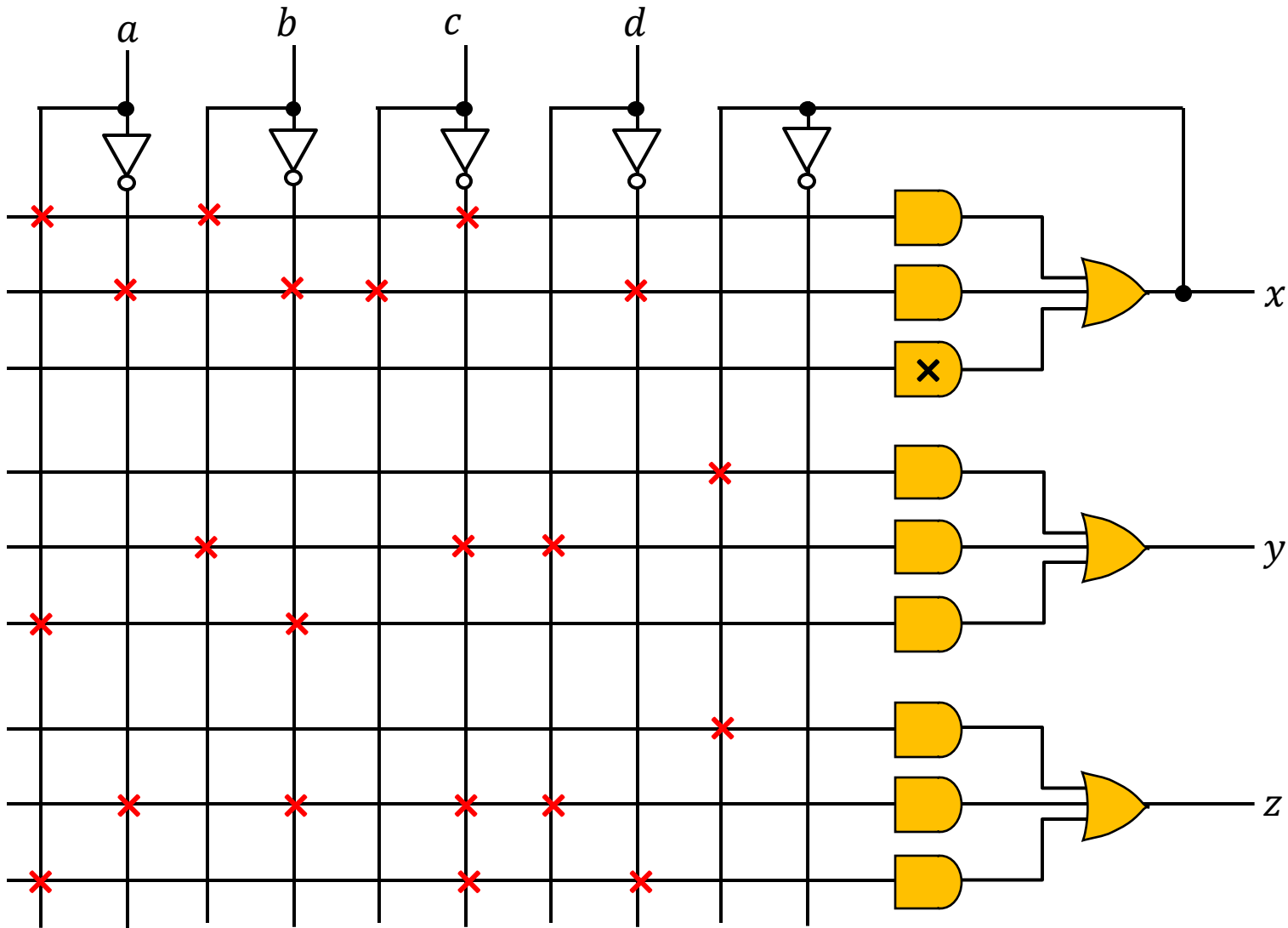
$$z(a, b, c, d) = a'b'cd' + abc' + a'b'c'd + ac'd'$$

# Exercise

$$x(a, b, c, d) = a'b'cd' + abc'$$

$$y(a, b, c, d) = a'b'cd' + abc' + bc'd + ab'$$

$$z(a, b, c, d) = a'b'cd' + abc' + a'b'c'd + bc'd'$$



# Exercise

$$f_1(a, b, c) = \sum m(0, 2, 3, 6)$$

$$f_2(a, b, c) = \sum m(3, 6, 7)$$

$c \backslash ab$		00	01	11	10
0	$m_0$	$m_2$	$m_6$	$m_4$	
1	$m_1$	$m_3$	$m_7$	$m_5$	

$f_1$

$c \backslash ab$		00	01	11	10
0	1	1	1		
1		1			

$f_2$

$c \backslash ab$		00	01	11	10
0				1	
1		1	1		

$$f_1(a, b, c) = a'c' + bc' + a'bc$$

$$f_2(a, b, c) = ab + a'bc$$

Four distinct  
product term

# Exercise

$$f_1(a, b, c) = \sum m(0, 2, 3, 6)$$

$$f_2(a, b, c) = \sum m(3, 6, 7)$$

$c \backslash ab$		00	01	11	10
0		$m_0$	$m_2$	$m_6$	$m_4$
1		$m_1$	$m_3$	$m_7$	$m_5$

$f_1$

$c \backslash ab$		00	01	11	10
0		1	1	1	
1			1		

$f_2$

$c \backslash ab$		00	01	11	10
0				1	
1			1	1	

$$f_1(a, b, c) = a'c' + a'b + abc'$$

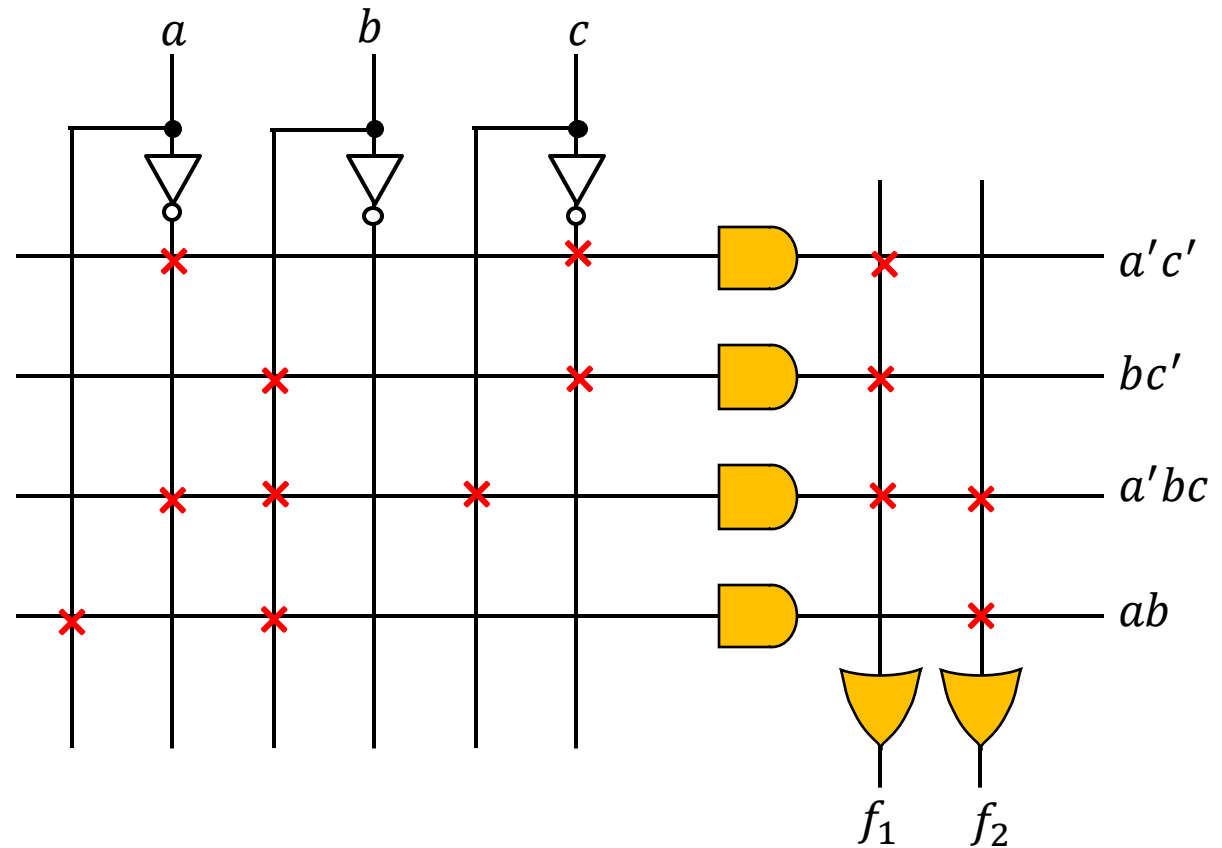
$$f_2(a, b, c) = bc + abc'$$

Four distinct  
product term

# Exercise

$$f_1(a, b, c) = a'c' + bc' + a'bc$$

$$f_2(a, b, c) = ab + a'bc$$



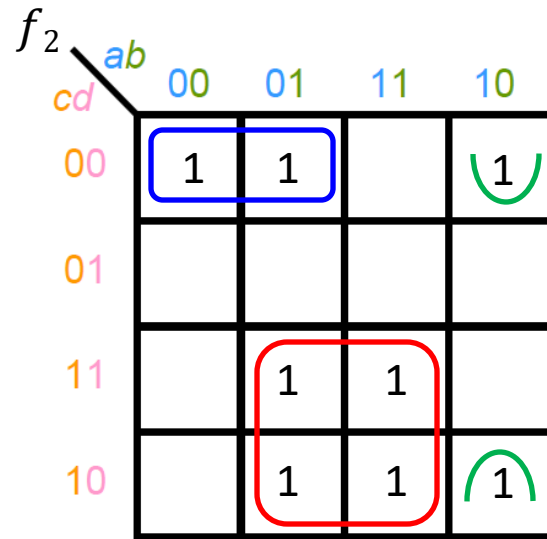
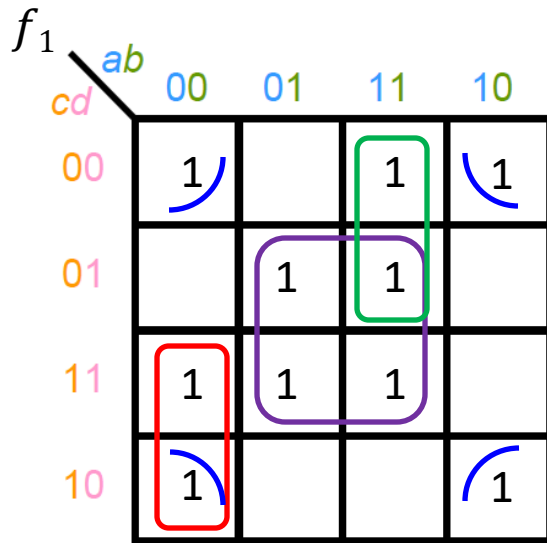


# Exercise

Simplify the following functions and their complements.

$$f_1(a, b, c, d) = \sum m(0, 2, 3, 5, 7, 8, 10, 12, 13, 15)$$

$$f_2(a, b, c, d) = \sum m(0, 4, 6, 7, 8, 10, 14, 15)$$



$$f_1(a, b, c, d) = a'b'c + abc' + bd + b'd'$$

$$f_2(a, b, c, d) = a'c'd' + bc + ab'd'$$

# Exercise

Simplify the following functions and their complements.

$$f_1(a, b, c, d) = \sum m(0, 2, 3, 5, 7, 8, 10, 12, 13, 15)$$

$$f_2(a, b, c, d) = \sum m(0, 4, 6, 7, 8, 10, 14, 15)$$

$f_1$

	$ab$	00	01	11	10
$cd$	00	1	0	1	1
	01	0	1	1	0
	11	1	1	1	0
	10	1	0	0	1

$f_2$

	$ab$	00	01	11	10
$cd$	00	1	1	0	1
	01	0	0	0	0
	11	0	1	1	0
	10	0	1	1	1

$$f'_1(a, b, c, d) = bcd' + b'c'd + ab'd + a'bd'$$

$$f'_2(a, b, c, d) = a'b'c + abc' + ab'd + c'd$$

# Exercise

Simplify the following functions and their complements.

$$f_1(a, b, c, d) = \sum m(0, 2, 3, 5, 7, 8, 10, 12, 13, 15)$$

$$f_2(a, b, c, d) = \sum m(0, 4, 6, 7, 8, 10, 14, 15)$$

$f_1$

	$ab$	00	01	11	10
$cd$	00	1		1	1
	01		1	1	
	11	1	1	1	
	10	1			1

$f_2$

	$ab$	00	01	11	10
$cd$	00	1	1	0	1
	01	0	0	0	0
	11	0	1	1	0
	10	0	1	1	1

$$f_1(a, b, c, d) = a'b'c + abc' + bd + b'd'$$

$$f_2'(a, b, c, d) = a'b'c + abc' + ab'd + c'd$$

**Look for  
common  
terms!!!**

# Exercise

$$f_1(a, b, c, d) = a'b'c + abc' + bd + b'd'$$

$$f_2'(a, b, c, d) = a'b'c + abc' + ab'd + c'd$$

