

# EE2000 Logic Circuit Design

---

## Lecture 5 – Combinational Functional Blocks



# Exercise

		<i>ab</i>			
<i>c</i>	<i>xy</i>	00	01	11	10
0	$m_0$	$m_2$	$m_6$	$m_4$	
1	$m_1$	$m_3$	$m_7$	$m_5$	

		<i>xy</i>			
<i>b<sub>o</sub></i>	<i>b<sub>in</sub></i>	00	01	11	10
0			1		
1	1	1	1	1	

$$\begin{aligned}
 b_o &= x'y + x'b_{in} + yb_{in} = x'y + b_{in}(x' + y) \\
 &= x'y + b_{in}(x'y' + x'y + xy) \\
 &= x'y(1 + b_{in}) + b_{in}(x'y' + xy) \\
 &= x'y + b_{in}(x \oplus y)'
 \end{aligned}$$

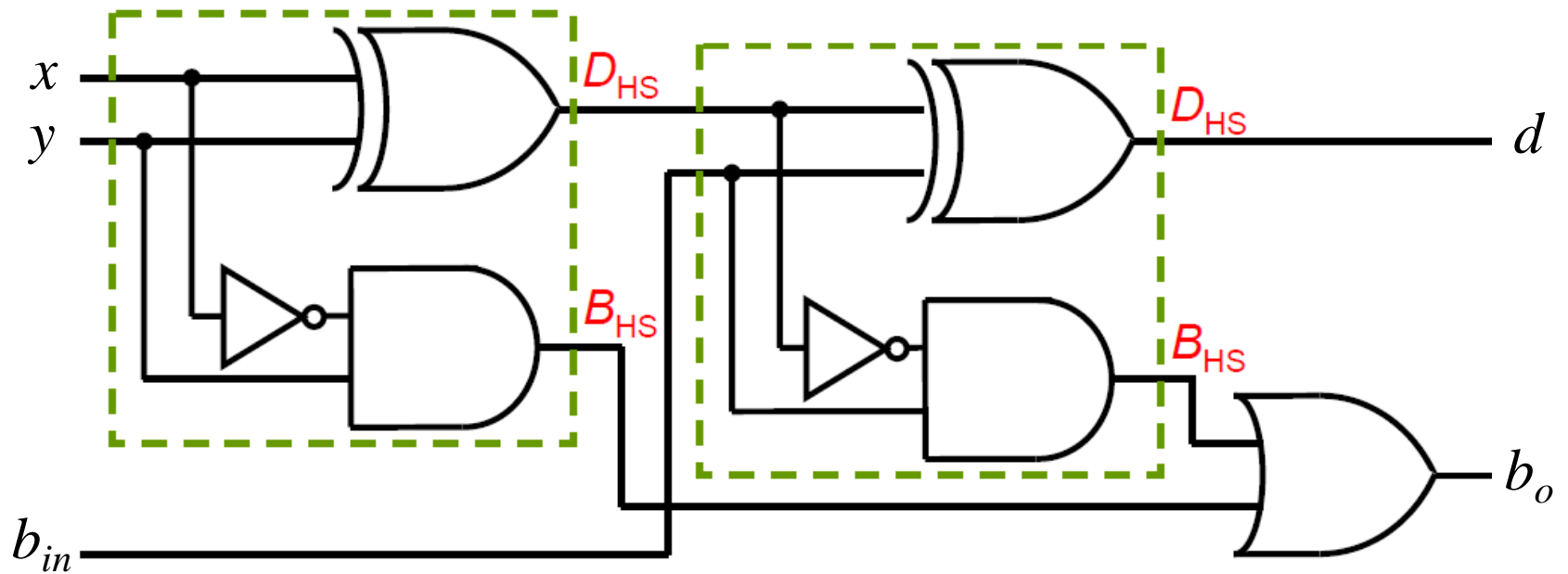
		<i>xy</i>			
<i>d</i>	<i>b<sub>in</sub></i>	00	01	11	10
0			1		1
1	1	1		1	

$$\begin{aligned}
 d &= x'y'b_{in} + xyb_{in} + x'yb'_{in} + xy'b'_{in} \\
 &= b_{in}(x'y' + xy) + b'_{in}(x'y + xy') \\
 &= b_{in}(x \oplus y)' + b'_{in}(x \oplus y) \\
 &= b_{in} \oplus (x \oplus y)
 \end{aligned}$$

# Exercise

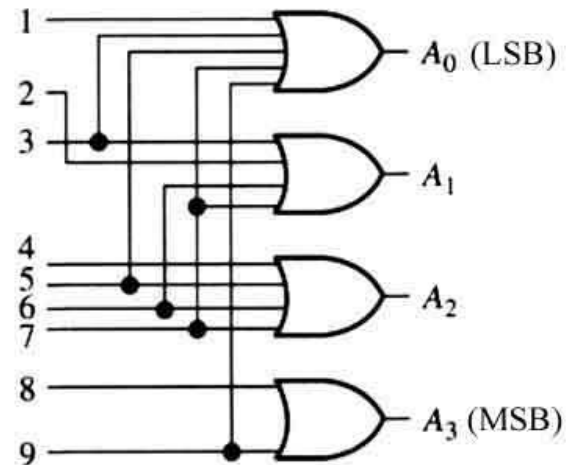
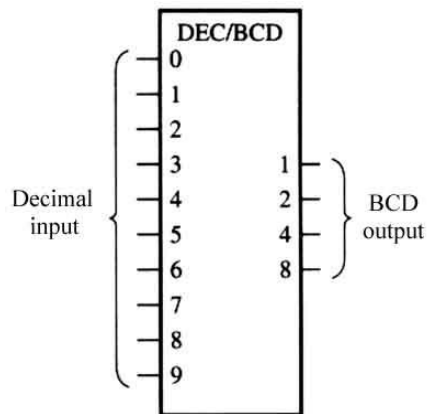
		<i>ab</i>			
<i>c</i>		00	01	11	10
	0	$m_0$	$m_2$	$m_6$	$m_4$
	1	$m_1$	$m_3$	$m_7$	$m_5$

$$b_o = x'y + b_{in}(x \oplus y)' \quad d = b_{in} \oplus (x \oplus y)$$



# Exercise (Decimal-to-Binary Encoder)

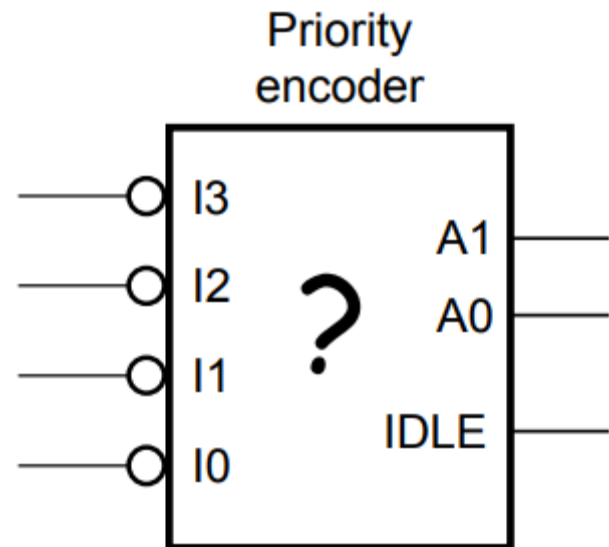
Inputs										Outputs			
0	1	2	3	4	5	6	7	8	9	$A_3$	$A_2$	$A_1$	$A_0$
1	0	0	0	0	0	0	0	0	0	0	0	0	0
0	1	0	0	0	0	0	0	0	0	0	0	0	1
0	0	1	0	0	0	0	0	0	0	0	0	1	0
0	0	0	1	0	0	0	0	0	0	0	0	1	1
0	0	0	0	1	0	0	0	0	0	0	1	0	0
0	0	0	0	0	1	0	0	0	0	0	1	0	1
0	0	0	0	0	0	1	0	0	0	0	1	1	0
0	0	0	0	0	0	0	1	0	0	0	1	1	1
0	0	0	0	0	0	0	0	1	0	1	0	0	0
0	0	0	0	0	0	0	0	0	1	1	0	0	1



# Exercise (Active Low)

- Design an Active Low 4-input priority encoder whereby inputs with higher subscript numbers has higher priority.
- Output IDLE is High when all inputs are high.

Input				Output		
$I_3$	$I_2$	$I_1$	$I_0$	$A_1$	$A_0$	IDLE
1	1	1	1	X	X	1
1	1	1	0	0	0	0
1	1	0	X	0	1	0
1	0	X	X	1	0	0
0	X	X	X	1	1	0



# Exercise (Active Low)

Input				Output		
$I_3$	$I_2$	$I_1$	$I_0$	$A_1$	$A_0$	IDLE
1	1	1	1	X	X	1
1	1	1	0	0	0	0
1	1	0	X	0	1	0
1	0	X	X	1	0	0
0	X	X	X	1	1	0

$$\text{IDLE} = I_3 I_2 I_1 I_0$$

$$A_0 = I_3' + I_3 I_2 I_1'$$

$$= I_3' + I_2 I_1'$$

$$A_1 = I_3 I_2' + I_3'$$

$$= I_2' + I_3'$$

Simplification  
 $a' + ab = a' + b$

# Exercise (Active Low)

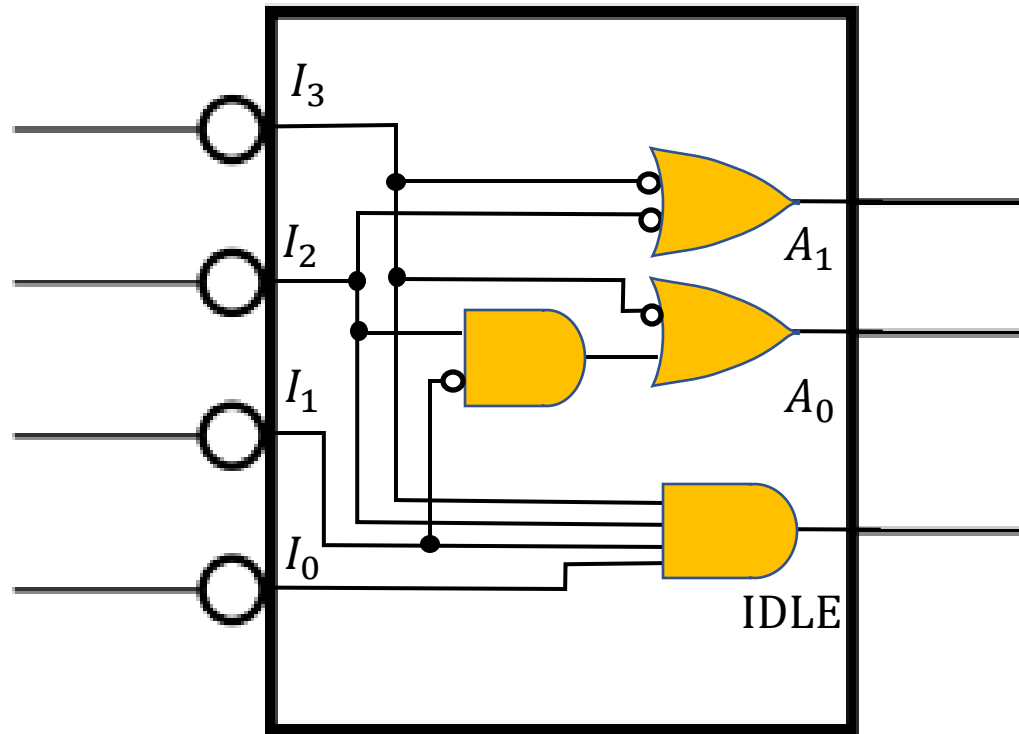
$$\text{IDLE} = I_3 I_2 I_1 I_0$$

$$A_0 = I_3' + I_3 I_2 I_1'$$

$$= I_3' + I_2 I_1'$$

$$A_1 = I_3 I_2' + I_3'$$

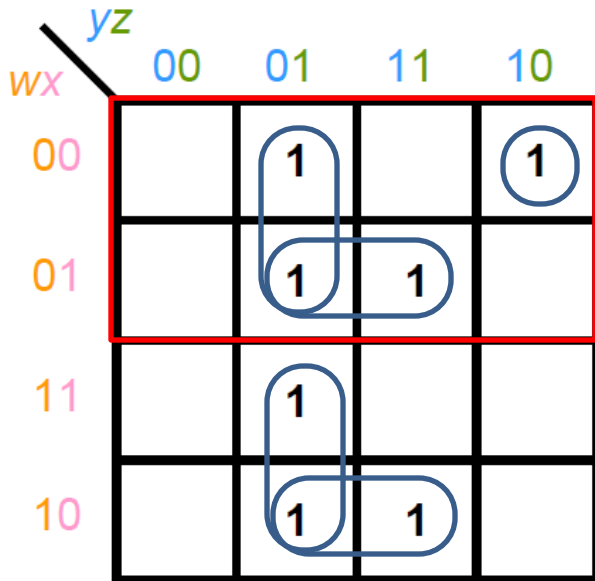
$$= I_2' + I_3'$$



# Exercise

Realize the function  $f(w, x, y, z) = \sum m(1, 2, 5, 7, 9, 11, 13)$  using a 2-to-1 MUX

$$w = S_0$$



$$f(w = 0) = y'z + xz + x'yz'$$

$$f(w = 1) = y'z + x'z$$



# Exercise

Realize the function  $f(w, x, y, z) = \sum m(1, 2, 5, 7, 9, 11, 13)$  using an 8-to-1 MUX

wxyz	F	$S_2=w, S_1=x, S_0=y$
0000	0	$I_0=z$
0001	1	
0010	1	$I_1=z'$
0011	0	
0100	0	$I_2=z$
0101	1	
0110	0	$I_3=z$
0111	1	

wxyz	F	$S_2=w, S_1=x, S_0=y$
1000	0	$I_4=z$
1001	1	
1010	0	$I_5=z$
1011	1	
1100	0	$I_6=z$
1101	1	
1110	0	$I_7=0$
1111	0	