

# ICPC Notebook

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template	
0settings.sh	
export CXXFLAGS='-O3 -std=c++2a -D_GLIBCXX_DEBUG -D_GLIBCXX_DEBUG_PEDANTIC -Wfatal-errors'	
1template.hpp	md5: f368a0
<pre>#include &lt;bits/stdc++.h&gt; using namespace std; #define ll long long #define pii pair&lt;int, int&gt; #define pll pair&lt;ll, ll&gt; #define vi vector&lt;int&gt; #define vl vector&lt;ll&gt; #define ov4(a, b, c, d, name, ...) name #define rep3(i, a, b, c) for(ll i = (a); i &lt; (b); i += (c)) #define rep2(i, a, b) rep3(i, a, b, 1) #define rep1(i, n) rep2(i, 0, n) #define rep0(n) rep1(aaaaa, n) #define rep(...) ov4(__VA_ARGS__, rep3, rep2, rep1, rep0) (__VA_ARGS__) #define per(i, a, b) for(ll i = (a)-1; i &gt;= (b); i--) #define fore(e, v) for(auto&amp;&amp; e : v) #define all(a) begin(a), end(a) #define si(a) (int)(size(a)) #define lb(v, x) (lower_bound(all(v), x) - begin(v)) #define eb emplace_back  template&lt;typename T, typename S&gt; bool chmin(T&amp; a, const S&amp; b) { return a &gt; b ? a = b, 1 : 0; } template&lt;typename T, typename S&gt; bool chmax(T&amp; a, const S&amp; b) { return a &lt; b ? a = b, 1 : 0; }  const int INF = 1e9 + 100; const ll INFL = 3e18 + 100;  #define i128 __int128_t  struct _ { _() { cin.tie(0)-&gt;sync_with_stdio(0), cout.tie(0); } } _;</pre>	
hash.sh	
# 使い方: sh hash.sh -> コピー -> Ctrl + D # コメント・空白・改行を削除して md5 でハッシュする g++ -dD -E -P -fpreprocessed -   tr -d '[:space:]'   md5sum   cut -c-6	
random_test.sh	
# correct wrong generate make \$1 make \$2 make \$3 while true;do ./\$3 > input.txt c=\$(./\$1 < input.txt) w=\$(./\$2 < input.txt) if [[ \$c = \$w ]]; then echo "pass" else echo "WA" echo "\$(cat input.txt)" echo "o:" echo "\$c" echo "x:" echo "\$w" exit fi done	
rnd.hpp	md5: a81b0a
<pre>ll rnd(ll l, ll r) { // [l, r) static mt19937_64</pre>	

```
gen(chrono::steady_clock::now().time_since_epoch().count());
return uniform_int_distribution<ll>(l, r - 1)(gen);
}

template<typename T> void rndshuf(vector<T>& v) { rep(i, 1,
si(v)) swap(v[i], v[rnd(0, i)]); }
template<class T> vector<T> rvi(int n, T l, T r, bool unique =
false) {
if(unique) {
assert(r - l >= n);
vector<T> res;
rep(i, n) res.eb(rnd(l, r - n + 1));
sort(all(res));
rep(i, n) res[i] += i;
rndshuf(res);
return res;
}
vector<T> v(n);
fore(e, v) e = rnd(l, r);
return v;
}
```

data-structure	
BIT.hpp	md5: 5f098b
<pre>struct BIT { vl a; BIT(ll n) : a(n + 1) {} void add(ll i, ll x) { i++; while(i &lt; si(a)) a[i] += x, i += i &amp; -i; } ll sum(ll r) { ll s = 0; while(r) s += a[r], r -= r &amp; -r; return s; } ll sum(ll l, ll r) { return sum(r) - sum(l); } // minimize i s.t. sum(i) &gt;= w int lower_bound(ll w) { if(w &lt;= 0) return 0; int x = 0, N = si(a) + 1; for(int k = 1 &lt;&lt; __lg(N); k; k &gt;= 1) { if(x + k &lt;= N - 1 &amp;&amp; a[x + k] &lt; w) { w -= a[x + k]; x += k; } } return x; } };</pre>	
FastSet.hpp	md5: 9dd1e2
<pre>using U = uint64_t; const U B = 64; struct FS { U n; vector&lt;vector&lt;U&gt;&gt; a; FS(U n) : n(n) { do a.eb(n = (n + B - 1) / B); while(n &gt; 1); } bool operator[](ll i) const { return a[0][i / B] &gt;&gt; (i % B) &amp; 1; } void set(ll i) { for(auto&amp; v : a) { v[i / B]  = 1ULL &lt;&lt; (i % B); i /= B; } } void erase(ll i) { for(auto&amp; v : a) { v[i / B] &amp;= ~(1ULL &lt;&lt; (i % B)); if(v[i / B]) break; i /= B; } } ll next(ll i) { rep(h, si(a)) {</pre>	

```
        i++;
        if(i / B >= si(a[h])) break;
        U d = a[h][i / B] >> (i % B);
        if(d) {
            i += countr_zero(d);
            while(h--) i = i * B + countr_zero(a[h][i]);
            return i;
        }
        i /= B;
    }
    return n;
}
ll prev(ll i) {
    rep(h, si(a)) {
        i--;
        if(i < 0) break;
        U d = a[h][i / B] << (~i % B);
        if(d) {
            i -= countl_zero(d);
            while(h--) i = i * B + __lg(a[h][i]);
            return i;
        }
        i /= B;
    }
    return -1;
}
};
```

Skew-Heap.hpp

md5: 38dad3

```
template<typename T, bool isMin = true> struct SkewHeap {
    struct Node {
        T key, laz;
        Node *l, *r;
        int idx;
        Node() = default;
        Node(const T& k, int i = -1) : key(k), laz(0), l(nullptr),
r(nullptr), idx(i) {}
    };
    using P = Node*;
    static void propagate(P x) {
        if(x->laz == 0) return;
        if(x->l) x->l->laz += x->laz;
        if(x->r) x->r->laz += x->laz;
        x->key += x->laz;
        x->laz = 0;
    }
    static P meld(P x, P y) {
        if(!x || !y) return x ? x : y;
        if(!comp(x, y)) swap(x, y);
        propagate(x);
        x->r = meld(x->r, y);
        swap(x->l, x->r);
        return x;
    }
    static P alloc(const T& key, int idx = -1) { return new
Node(key, idx); }
    static P pop(P x) {
        propagate(x);
        return meld(x->l, x->r);
    }
    static P push(P x, const T& key, int idx = -1) { return
meld(x, alloc(key, idx)); }
    static void apply(P x, const T& laz) {
        x->laz += laz;
        propagate(x);
    }

private:
    static inline bool comp(P x, P y) {
        if constexpr(isMin) {
            return x->key + x->laz < y->key + y->laz;
        } else {
            return x->key + x->laz > y->key + y->laz;
        }
    }
};
```

cht.hpp

md5: a05621

```
template<bool isMin = true> struct CHT {
#define x first
```

```
#define y second
    CHT() = default;
    deque<pll> v;
    bool empty() { return v.empty(); }
    void clear() { return v.clear(); }
    inline int sgn(ll x) { return !x ? 0 : (x < 0 ? -1 : 1); }
    using D = long double;
    inline bool check(const pll& a, const pll& b, const pll& c) {
        if(b.y == a.y or c.y == b.y) return sgn(b.x - a.x) *
sgn(c.y - b.y) >= sgn(c.x - b.x) * sgn(b.y - a.y);
        return D(b.x - a.x) * sgn(c.y - b.y) / D(abs(b.y - a.y))
>= D(c.x - b.x) * sgn(b.y - a.y) / D(abs(c.y - b.y));
    }
    void add(ll a, ll b) {
        if(!isMin) a *= -1, b *= -1;
        pll line(a, b);
        if(empty()) v.emplace_front(line);
        else {
            if(ll c = v[0].x; c <= a) {
                if(c == a) {
                    if(v[0].y <= b) return;
                    v.pop_front();
                }
                while(si(v) >= 2 and check(line, v[0], v[1]))
v.pop_front();
                v.emplace_front(line);
            } else {
                assert(a <= v.back().x);
                if(v.back().x == a) {
                    if(v.back().y <= b) return;
                    v.pop_back();
                }
                while(si(v) >= 2 and check(v[si(v) - 2], v.back(),
line)) v.pop_back();
                v.emplace_back(line);
            }
        }
        ll get_y(const pll& a, const ll& x) { return a.x * x + a.y; }
        ll query(ll x) {
            assert(!empty());
            int l = -1, r = si(v) - 1;
            while(l + 1 < r) {
                int m = (l + r) >> 1;
                if(get_y(v[m], x) >= get_y(v[m + 1], x)) l = m;
                else r = m;
            }
            return get_y(v[r], x) * (isMin ? 1 : -1);
        }
        ll query_monotone_inc(ll x) {
            assert(!empty());
            while(si(v) >= 2 and get_y(v[0], x) >= get_y(v[1], x))
v.pop_front();
            return get_y(v[0], x) * (isMin ? 1 : -1);
        }
        ll query_monotone_dec(ll x) {
            assert(!empty());
            while(si(v) >= 2 and get_y(v.back(), x) >= get_y(v.end()
[-2], x)) v.pop_back();
            return get_y(v.back(), x) * (isMin ? 1 : -1);
        }
    };
#undef x
#undef y
};
```

hash\_map.hpp

md5: 1893ff

```
#include <bits/extc++.h>
struct chash {
    const uint64_t C = (ll)(4e18 * acos(0)) | 71;
    ll operator()(ll x) const { return __builtin_bswap64(x * C);
}
};
using namespace __gnu_pbds;
template<class T, class S> using hash_map = gp_hash_table<T, S,
chash>;
```

lazy-segtree.hpp

md5: e79596

```
using U = uint64_t;
template<class S, S (*op)(S, S), S (*e)(), class F, S (*mpp)(F,
S), F (*cmpo)(F, F), F (*id)(> struct lazy_segtree {
```

```

    lazy_segtree() : lazy_segtree(0) {}
    explicit lazy_segtree(int n) : lazy_segtree(vector<S>(n,
e())) {}
    explicit lazy_segtree(const vector<S>& v) : n(si(v)) {
        s = bit_ceil(U(n));
        log = countr_zero(U(s));
        d = vector<S>(2 * s, e());
        lz = vector<F>(s, id());
        rep(i, n) d[s + i] = v[i];
        per(i, s, 1) update(i);
    }
    void set(int p, S x) {
        p += s;
        PUSH(p);
        d[p] = x;
        rep(i, 1, log + 1) update(p >> i);
    }
    S get(int p) {
        p += s;
        PUSH(p);
        return d[p];
    }
    S prod(int l, int r) {
        if(l == r) return e();
        l += s, r += s;
        per(i, log + 1, 1) {
            if(((l >> i) << i) != l) push(l >> i);
            if(((r >> i) << i) != r) push((r - 1) >> i);
        }
        S sm_l = e(), sm_r = e();
        while(l < r) {
            if(l & 1) sm_l = op(sm_l, d[l++]);
            if(r & 1) sm_r = op(d[--r], sm_r);
            l >>= 1, r >>= 1;
        }
        return op(sm_l, sm_r);
    }
    S all_prod() { return d[1]; }
    void apply(int p, F f) {
        // assert(0 <= p && p < n);
        p += s;
        PUSH(p);
        d[p] = mpp(f, d[p]);
        rep(i, 1, log + 1) update(p >> i);
    }
    void apply(int l, int r, F f) {
        // assert(0 <= l && l <= r && r <= _n);
        if(l == r) return;
        l += s, r += s;

        per(i, log + 1, 1) {
            if(((l >> i) << i) != l) push(l >> i);
            if(((r >> i) << i) != r) push((r - 1) >> i);
        }
        int m_l = l, m_r = r;
        while(l < r) {
            if(l & 1) all_apply(l++, f);
            if(r & 1) all_apply(--r, f);
            l >>= 1, r >>= 1;
        }
        l = m_l, r = m_r;
        rep(i, 1, log + 1) {
            if(((l >> i) << i) != l) update(l >> i);
            if(((r >> i) << i) != r) update((r - 1) >> i);
        }
    }
    template<class G> int max_right(int l, G g) {
        assert(g(e()));
        if(l == n) return n;
        l += s;
        PUSH(l);
        S sm = e();
        do {
            while(~l & 1) l >>= 1;
            if(!g(op(sm, d[l]))) {
                while(l < s) {
                    push(l);
                    l <<= 1;
                }
                if(g(op(sm, d[l]))) {
                    sm = op(sm, d[l]);
                    l++;
                }
            }
        }
    }

```

```

    }
    return l - s;
}
sm = op(sm, d[l]);
l++;
} while((l & -l) != l);
return n;
}
template<class G> int min_left(int r, G g) {
    assert(g(e()));
    if(r == 0) return 0;
    r += s;
    PUSH(r - 1);
    S sm = e();
    do {
        r--;
        while(r > 1 && r & 1) r >>= 1;
        if(!g(op(d[r], sm))) {
            while(r < s) {
                push(r);
                r = (2 * r + 1);
                if(g(op(d[r], sm))) {
                    sm = op(d[r], sm);
                    r--;
                }
            }
            return r + 1 - s;
        }
        sm = op(d[r], sm);
    } while((r & -r) != r);
    return 0;
}
S operator[](int k) { return get(k); }
int len() { return n; }

private:
int n, s, log;
vector<S> d;
vector<F> lz;
void update(int k) { d[k] = op(d[2 * k], d[2 * k + 1]); }
void all_apply(int k, F f) {
    d[k] = mpp(f, d[k]);
    if(k < s) lz[k] = cmpo(f, lz[k]);
}
void push(int k) {
    all_apply(2 * k, lz[k]);
    all_apply(2 * k + 1, lz[k]);
    lz[k] = id();
}
void PUSH(int k) { per(i, log + 1, 1) push(k >> i); }
};

```

## li-chao.hpp

md5: ca57d5

```

struct lctree {
    struct line {
        ll a, b;
        line() : a(0), b(INFL) {}
        line(ll a, ll b) : a(a), b(b) {}
        ll get(ll x) { return a * x + b; }
        inline bool over(line r, ll x) { return get(x) < r.get(x); }
    }
};
int n;

vector<ll> x;
vector<line> seg;
lctree() {}
lctree(const vector<ll>& _x) : x(_x) {
    sort(all(x));
    int n2 = si(x);
    n = 1;
    while(n < n2) n <<= 1;
    x.resize(n);
    rep(i, n2, n) x[i] = x[n2 - 1];
    seg = vector<line>(n * 2);
}
void upd(line L, int i, int l, int r) {
    while(true) {
        int mid = l + r >> 1;
        bool lov = L.over(seg[i], x[l]);
    }
}

```

```

        bool rov = L.over(seg[i], x[r - 1]);
        if(lov == rov) {
            if(lov) swap(seg[i], L);
            return;
        }
        bool mov = L.over(seg[i], x[mid]);
        if(mov) swap(seg[i], L);
        if(lov != mov) {
            i = (i << 1), r = mid;
        } else {
            i = (i << 1) + 1, l = mid;
        }
    }
}

void upd(line L, unsigned i) {
    int ub = bit_width(i) - 1;
    int l = (n >> ub) * (i - (1 << ub));
    int r = l + (n >> ub);
    upd(L, i, l, r);
}

void update(ll a, ll b) { upd(line(a, b), 1, 0, n); }
void update_segment(ll l, ll r, ll a, ll b) {
    l = lb(x, l) + n, r = lb(x, r) + n;
    line L(a, b);
    for(; l < r; l >=> 1, r >=> 1) {
        if(l & 1) upd(L, l++);
        if(r & 1) upd(L, --r);
    }
}

ll query(ll t) {
    ll k = lb(x, t);
    k += n;
    ll res = seg[k].get(t);
    while(k > 1) {
        k >>= 1;
        chmin(res, seg[k].get(t));
    }
    return res;
}
};

```

## line\_container.hpp

md5: b018d9

```

struct Line {
    mutable ll k, m, p;
    bool operator<(const Line& o) const { return k < o.k; }
    bool operator<(ll x) const { return p < x; }
};

template<bool ismin = true> struct LineContainer :
multiset<Line, less<>> {
    // (for doubles, use inf = 1/.0, div(a,b) = a/b)
    const ll inf = LLONG_MAX / 2;
    ll div(ll a, ll b) { // floored division
        return a / b - ((a ^ b) < 0 && a % b);
    }
    bool isect(iterator x, iterator y) {
        if(y == end()) {
            x->p = inf;
            return false;
        }
        if(x->k == y->k) x->p = x->m > y->m ? inf : -inf;
        else x->p = div(y->m - x->m, x->k - y->k);
        return x->p >= y->p;
    }
    void add(ll k, ll m) {
        if(ismin) k = -k, m = -m;
        auto z = insert({k, m, 0}), y = z++, x = y;
        while(isect(y, z)) z = erase(z);
        if(x != begin() && isect(--x, y)) isect(x, y = erase(y));
        while((y = x) != begin() && (--x->p >= y->p) isect(x,
erase(y)));
    }
    ll query(ll x) {
        auto l = *lower_bound(x);
        ll s = 1;
        if(ismin) s = -1;
        return s * (l.k * x + l.m);
    }
};

```

## Link-cut.hpp

md5: e9b023

```

struct Node {
    typedef Node* NP;
    NP l, r, p;
    bool rev;
    int v, mx, lz;
    Node() : l(NULL), r(NULL), p(NULL), rev(false), v(-inf), mx(-
inf), lz(-inf) {}
    void Propagate() {
        if(rev) {
            swap(l, r);
            if(l) l->rev ^= true;
            if(r) r->rev ^= true;
            rev = false;
        }
        if(l) chmax(l->lz, lz);
        if(r) chmax(r->lz, lz);
        chmax(v, lz);
        chmax(mx, lz);
        lz = -inf;
    }
    int GetMax() { return max(mx, lz); }
    int GetVert() { return max(v, lz); }
    void Update() {
        assert(lz == -inf);
        mx = v;
        if(l) { chmax(mx, l->GetMax()); }
        if(r) { chmax(mx, r->GetMax()); }
    }
    int Pos() {
        if(p && p->l == this) return -1;
        if(p && p->r == this) return 1;
        return 0;
    }
    void Prepare() {
        if(Pos()) p->Prepare();
        Propagate();
    }
    void Rotate() {
        NP q = p, c;
        if(Pos() == 1) {
            c = l;
            l = p;
            p->r = c;
        } else {
            c = r;
            r = p;
            p->l = c;
        }
        if(c) c->p = p;
        p = p->p;
        q->p = this;
        if(p && p->l == q) p->l = this;
        if(p && p->r == q) p->r = this;
        q->Update();
    }
    void Splay() {
        Prepare();
        while(Pos()) {
            int a = Pos(), b = p->Pos();
            if(b && a == b) p->Rotate();
            if(b && a != b) Rotate();
            Rotate();
        }
        Update();
    }
    void Expose() {
        for(NP x = this; x; x = x->p) x->Splay();
        for(NP x = this; x->p; x = x->p) {
            x->p->r = x;
            x->p->Update();
        }
        Splay();
    }
    void Evert() {
        Expose();
        if(l) {
            l->rev ^= true;
            l = NULL;
            Update();
        }
    }
};

```

```
    }
}
void Link(NP x) {
    Evert();
    p = x;
}
void Set(int q) {
    Expose();
    r = NULL;
    chmax(lz, q);
}
void Cut() {
    Expose();
    assert(l);
    l->p = NULL;
    l = NULL;
    Update();
}
int Get() {
    Expose();
    r = NULL;
    Update();
    return GetMax();
}
};
Node* LCA(Node* a, Node* b) {
    a->Expose();
    b->Expose();
    if(!a->p) { return NULL; }
    Node* d = a;
    while(a->p != b) {
        if(a->Pos() == 0) { d = a->p; }
        a = a->p;
    }
    if(a == b->l) {
        return d;
    } else {
        return b;
    }
}
}
```

pbds.hpp

md5: a38245

```
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
#include <ext/pb_ds/tag_and_trait.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
// using namespace __gnu_pbds;
template<typename T> using PQ = __gnu_pbds::priority_queue<T,
greater<T>, __gnu_pbds::rc_binomial_heap_tag>;
using Trie = __gnu_pbds::trie<string,
__gnu_pbds::null_type,
__gnu_pbds::trie_string_access_traits<>,
__gnu_pbds::pat_trie_tag,
__gnu_pbds::trie_prefix_search_node_update>;
// not a multiset
// find_by_order(k) -> itr of k-th(0-based) element
// order_of_key(k) -> index of lower_bound(k)
using ordered_set = tree<int, null_type, less<int>, rb_tree_tag,
tree_order_statistics_node_update>;

#include <ext/rope>
using namespace __gnu_cxx;
```

rbst.hpp

md5: b392ca

```
template<typename T, T (*f)(T, T), T (*e)()> struct RBST {
    inline int rnd() {
        static int x = 123456789;
        static int y = 362436069;
        static int z = 521288629;
        static int w = 88675123;
        int t;

        t = x ^ (x << 11);
        x = y;
        y = z;
        z = w;
```

```
        return w = (w ^ (w >> 19)) ^ (t ^ (t >> 8));
    }
    struct node {
        node *l, *r;
        int cnt;
        T x, sum;
        node() = default;
        node(T x) : x(x), sum(x), l(0), r(0) { cnt = 1; }
    };
    RBST(int n) : pool(n) {}
    int cnt(const node* t) { return t ? t->cnt : 0; }
    T sum(const node* t) { return t ? t->sum : e(); }
    node* update(node* t) {
        t->cnt = cnt(t->l) + cnt(t->r) + 1;
        t->sum = f(sum(t->l), t->x, sum(t->r));
        return t;
    }
    vector<node> pool;
    int ptr = 0;
    inline node* alloc(const T& v) {
        if(si(pool) == ptr) pool.resize(si(pool) * 2);
        return &(pool[ptr++] = node(v));
    }
    node* merge(node* l, node* r) {
        if(!l or !r) return l ? l : r;
        if(rnd() % (cnt(l) + cnt(r)) < cnt(l)) {
            l->r = merge(l->r, r);
            return update(l);
        }
        r->l = merge(l, r->l);
        return update(r);
    }
}

pair<node*, node*> split(node* t, int k) {
    if(!t) return {t, t};
    if(k <= cnt(t->l)) {
        auto [l, r] = split(t->l, k);
        t->l = r;
        return {l, update(t)};
    }
    auto [l, r] = split(t->r, k - cnt(t->l) - 1);
    t->r = l;
    return {update(t), r};
}

void insert(node*& t, int k, const T& v) {
    auto [l, r] = split(t, k);
    t = merge(merge(l, alloc(v)), r);
}
};
```

segbeats.hpp

md5: 2fbe43

```
struct Segtree_beats {
    ll op(int type, ll x, ll y) { return type ? min(x, y) :
max(x, y); }
    bool cmp(int type, ll x, ll y) { return type ? x < y : x > y; }
}

    struct alignas(32) Node {
        ll sum = 0;
        ll a1[2] = {}, a2[2] = {-INFL, INFL}, ac[2] = {1, 1}, add
= 0;
    };

    vector<Node> v;
    ll n, log, e[3] = {-INFL, INFL, 0};

    Segtree_beats() {}
    Segtree_beats(int n) : Segtree_beats(vl(n)) {}
    Segtree_beats(const vl& a) {
        n = 1, log = 0;
        while(n < si(a)) n <= 1, log++;
        v.resize(2 * n);
        rep(i, si(a)) { v[i + n].sum = v[i + n].a1[0] = v[i +
n].a1[1] = a[i]; }
        per(i, n, 1) update(i);
    }

    // 0 : add, 1 : chmin, 2 : chmax, 3 : update
    template<int cmd> void apply(int l, int r, ll x) {
        if(l == r) return;
```

```

    l += n, r += n;
    per(i, log + 1, 1) {
        if(((l >> i) << i) != l) push(l >> i);
        if(((r >> i) << i) != r) push((r - 1) >> i);
    }
    {
        int l2 = l, r2 = r;
        while(l < r) {
            if(l & 1) _apply<cmd>(l++, x);
            if(r & 1) _apply<cmd>(--r, x);
            l >>= 1;
            r >>= 1;
        }
        l = l2;
        r = r2;
    }
    rep(i, 1, log + 1) {
        if(((l >> i) << i) != l) update(l >> i);
        if(((r >> i) << i) != r) update((r - 1) >> i);
    }
}
// 0 : max, 1 : min, 2 : sum
template<int cmd> ll fold(int l, int r) {
    if(l == r) return e[cmd];
    l += n, r += n;
    per(i, log + 1, 1) {
        if(((l >> i) << i) != l) push(l >> i);
        if(((r >> i) << i) != r) push((r - 1) >> i);
    }
    ll lx = e[cmd], rx = e[cmd];
    while(l < r) {
        if(l & 1) op<cmd>(lx, v[l++]);
        if(r & 1) op<cmd>(rx, v[--r]);
        l >>= 1;
        r >>= 1;
    }
    if constexpr(cmd <= 1) lx = op(cmd, lx, rx);
    if constexpr(cmd == 2) lx += rx;
    return lx;
}

private:
void update(int k) {
    Node& p = v[k];
    Node& l = v[k * 2 + 0];
    Node& r = v[k * 2 + 1];
    p.sum = l.sum + r.sum;
    rep(t, 2) {
        if(l.a1[t] == r.a1[t]) {
            p.a1[t] = l.a1[t];
            p.a2[t] = op(t, l.a2[t], r.a2[t]);
            p.ac[t] = l.ac[t] + r.ac[t];
        } else {
            bool f = cmp(t, l.a1[t], r.a1[t]);
            p.a1[t] = f ? l.a1[t] : r.a1[t];
            p.ac[t] = f ? l.ac[t] : r.ac[t];
            p.a2[t] = op(t, f ? r.a1[t] : l.a1[t], f ? l.a2[t] :
r.a2[t]);
        }
    }
}

void push_add(int k, ll x) {
    Node& p = v[k];
    p.sum += x << (log + __builtin_clz(k) - 31);
    rep(t, 2) {
        p.a1[t] += x;
        if(p.a2[t] != e[t]) p.a2[t] += x;
    }
    p.add += x;
}

void push(int cmd, int k, ll x) {
    Node& p = v[k];
    p.sum += (x - p.a1[cmd]) * p.ac[cmd];
    if(p.a1[cmd ^ 1] == p.a1[cmd]) p.a1[cmd ^ 1] = x;
    if(p.a2[cmd ^ 1] == p.a1[cmd]) p.a2[cmd ^ 1] = x;
    p.a1[cmd] = x;
}

void push(int k) {
    Node& p = v[k];
    if(p.add) {

```

```

        rep(t, 2) push_add(k * 2 + t, p.add);
        p.add = 0;
    }
    rep(t, 2) rep(s, 2) if(cmp(t, v[k * 2 + s].a1[t],
p.a1[t])) push(t, k * 2 + s, p.a1[t]);
}

void subtree_ch(int cmd, int k, ll x) {
    if(!cmp(cmd, v[k].a1[cmd], x)) return;
    if(cmp(cmd, x, v[k].a2[cmd])) { return push(cmd, k, x); }
    push(k);
    rep(t, 2) subtree_ch(cmd, k * 2 + t, x);
    update(k);
}

template<int cmd> inline void _apply(int k, ll x) {
    rep(i, 2) if(cmd >> i & 1) subtree_ch(i, k, x);
    if constexpr(cmd == 0) push_add(k, x);
}

template<int cmd> inline void op(ll& a, const Node& b) {
    if constexpr(cmd <= 1) a = op(cmd, a, b.a1[cmd]);
    if constexpr(cmd == 2) a += b.sum;
}
};

```

## segtree-2d.hpp

md5: 1301f7

```

template<typename T, T (*op)(T, T), T (*e)()> class RangeTree {
private:
    int n, sz;
    vector<segtree<T, op, e>> seg;
    vector<vector<pll>> yx;
    vector<pll> sorted;

    void update_(int id, ll x, ll y, T val) {
        id += n - 1;
        int yid = lb(yx[id], pll(y, x));
        seg[id].set(yid, val);
        while(id > 0) {
            id = (id - 1) / 2;
            int yid = lb(yx[id], pll(y, x));
            seg[id].set(yid, val);
        }
    }

    T query(int lxid, int rxid, ll ly, ll ry, int k, int l, int
r) {
        if(r <= lxid || rxid <= l) return e();
        if(lxid <= l && r <= rxid) {
            int lyid = lb(yx[k], pll(ly, -INFL));
            int ryid = lb(yx[k], pll(ry, -INFL));
            return (lyid >= ryid) ? e() : seg[k].prod(lyid, ryid);
        } else {
            return op(query(lxid, rxid, ly, ry, 2 * k + 1, l, (l +
r) / 2),
                    query(lxid, rxid, ly, ry, 2 * k + 2, (l + r)
/ 2, r));
        }
    }

public:
    // 座標, 点の値
    RangeTree(vector<pll>& cand, vector<T>& val) : n(1),
sz(si(cand)), sorted(sz) {
        while(n < sz) n *= 2;
        rep(i, sz) sorted[i] = {cand[i].first, i};
        sort(all(sorted), [&](pll& a, pll& b) {
            return (a.first == b.first) ? (cand[a.second].second <
cand[b.second].second) : (a.first < b.first);
        });
        yx.resize(2 * n - 1), seg.resize(2 * n - 1);
        rep(i, sz) {
            yx[i + n - 1] = {{sorted[i].second, sorted[i].first}};
            vector<T> arg = {val[sorted[i].second]};
            seg[i + n - 1] = segtree<T, op, e>(arg);
            sorted[i].second = cand[sorted[i].second].second;
        }
        per(i, n - 1, 0) {
            yx[i].resize(si(yx[2 * i + 1]) + si(yx[2 * i + 2]));
            if(yx[i].empty()) continue;
            merge(all(yx[2 * i + 1]), all(yx[2 * i + 2]),

```



```
yx[i].begin(), [&](pll& a, pll& b) {
    return (cand[a.first].second ==
cand[b.first].second) ? (a.second < b.second)

: (cand[a.first].second < cand[b.first].second);
});
vector<T> arg((int)yx[i].size());
rep(j, si(yx[i])) arg[j] = val[yx[i][j].first];
seg[i] = segtree<T, op, e>(arg);
}
rep(i, 2 * n - 1) {
    for(auto& [a, b] : yx[i]) a = cand[a].second;
}
}
void update(ll x, ll y, T val) {
    int id = lb(sorted, pll(x, y));
    return update_(id, x, y, val);
}
T query(ll lx, ll ly, ll rx, ll ry) {
    int lxid = lb(sorted, pll(lx, -INFL));
    int rxid = lb(sorted, pll(rx, -INFL));
    return (lxid >= rxid) ? e() : query(lxid, rxid, ly, ry, 0,
n);
}
};
```

segtree.hpp

md5: f8e201

```
template<class S, S (*op)(S, S), S (*e)()> struct segtree {
    segtree(int n) : segtree(vector<S>(n, e())) {}
    segtree(const vector<S>& v) : n(si(v)) {
        s = bit_ceil(unsigned(n));
        log = countr_zero(unsigned(s));
        d = vector<S>(2 * s, e());
        rep(i, n) d[s + i] = v[i];
        per(i, s, 1) update(i);
    }
    void set(int p, S x) {
        d[p += s] = x;
        rep(i, 1, log + 1) update(p >> i);
    }
    S prod(int l, int r) const {
        S sml = e(), smr = e();
        l += s, r += s;
        while(l < r) {
            if(l & 1) sml = op(sml, d[l++]);
            if(r & 1) smr = op(d[--r], smr);
            l >>= 1, r >>= 1;
        }
        return op(sml, smr);
    }
    S all_prod() const { return d[1]; }
    template<typename F> int max_right(int l, F f) const {
        if(l == n) return n;
        l += s;
        S sm = e();
        do {
            while(~l & 1) l >>= 1;
            if(!f(op(sm, d[l]))) {
                while(l < s) {
                    l <<= 1;
                    if(f(op(sm, d[l]))) sm = op(sm, d[l++]);
                }
                return l - s;
            }
            sm = op(sm, d[l++]);
        } while((l & -l) != l);
        return n;
    }
    template<typename F> int min_left(int r, F f) const {
        if(!r) return 0;
        r += s;
        S sm = e();
        do {
            r--;
            while(r > 1 and r & 1) r >>= 1;
            if(!f(op(d[r], sm))) {
                while(r < s) {
                    r = (2 * r + 1);
                    if(f(op(d[r], sm))) sm = op(d[r--], sm);
                }
                return r + 1 - s;
            }
        }
```

```
    }
    sm = op(d[r], sm);
    } while((r & -r) != r);
    return 0;
}

private:
int n, s, log;
vector<S> d;
void update(int k) { d[k] = op(d[k * 2], d[k * 2 + 1]); }
};
```

sparse-table-disjoint.hpp

md5: 198e80

```
template<typename T, typename F> struct sptable {
    const F f;
    vector<vector<T>> a;
    vi l;

    sptable(const vector<T>& v, F f) : f(f) {
        int m = 0;
        while((1 << m) <= si(v)) ++m;
        a.resize(m, vector<T>(si(v), T()));
        rep(i, si(v)) a[0][i] = v[i];
        rep(i, 1, m) {
            int s = 1 << i;
            for(int j = 0; j < si(v); j += s * 2) {
                int t = min(j + s, si(v));
                a[i][t - 1] = v[t - 1];
                per(k, t - 1, j) a[i][k] = f(v[k], a[i][k + 1]);
                if(si(v) <= t) break;
                a[i][t] = v[t];
                int r = min(t + s, si(v));
                rep(k, t + 1, r) a[i][k] = f(a[i][k - 1], v[k]);
            }
        }
        l.resize(1 << m);
        rep(i, 2, si(l)) l[i] = l[i >> 1] + 1;
    }

    T query(int x, int y) {
        if(x >= --y) return a[0][x];
        int p = l[x ^ y];
        return f(a[p][x], a[p][y]);
    }
};
```

swag.hpp

md5: 85c3df

```
template<typename T, typename F> struct SWAG {
    using vp = vector<pair<T, T>>;
    vp a, b;
    F f;
    T I;
    SWAG(F f, T i) : f(f), I(i) {}

    private:
    T get(vp& v) { return empty(v) ? I : v.back().second; }
    void pusha(T x) { a.eb(x, f(x, get(a))); }
    void pushb(T x) { b.eb(x, f(get(b), x)); } // reversed!!
    void rebalance() {
        int n = si(a) + si(b);
        int s0 = n / 2 + (empty(a) ? n & 1 : 0);
        vp v{a};
        reverse(all(v));
        copy(all(b), back_inserter(v));
        a.clear(), b.clear();
        per(i, s0, 0) pusha(v[i].first);
        rep(i, s0, n) pushb(v[i].first);
    }

    public:
    T front() { return (a.empty() ? b.front() : a.back()).first; }
    T back() { return (b.empty() ? a.front() : b.back()).first; }
    void pop_front() {
        if(empty(a)) rebalance();
        a.pop_back();
    }
    void pop_back() {
        if(empty(b)) rebalance();
        b.pop_back();
    }
};
```



```

}
T query() { return f(get(a), get(b)); }
};

wavelet_matrix.hpp
md5: dec827

#define U uint32_t
#define L uint64_t
struct bit_vector {
    static constexpr U w = 64;
    vector<L> block;
    vector<U> count;
    int n, zeros;

    inline U get(U i) const { return U(block[i / w] >> (i % w)) &
1; }
    inline void set(U i) { block[i / w] |= 1LL << (i % w); }

    bit_vector() {}
    bit_vector(int n) { init(n); }
    void init(int _n) {
        n = zeros = _n;
        block.resize(n / w + 1, 0);
        count.resize(si(block), 0);
    }

    void build() {
        rep(i, 1, si(block)) count[i] = count[i - 1] +
popcount(block[i - 1]);
        zeros = rank0(n);
    }

    inline U rank0(U i) const { return i - rank1(i); }
    inline U rank1(U i) const { return count[i / w] +
popcount(block[i / w] & ((1ULL << i % w) - 1)); }
};

template<typename T, const int lg = 31> struct WaveletMatrix {
    int n;
    vector<T> a;
    array<bit_vector, lg> bv;
    WaveletMatrix(const vector<T>& _a) : n(_a.size()), a(_a) {
build2(); }

    void build() {
        rep(i, lg) bv[i] = bit_vector(n);
        vector<T> cur = a, nxt(n);
        per(h, lg, 0) {
            rep(i, n) if(cur[i] >> h & 1) bv[h].set(i);
            bv[h].build();
            array<decltype(begin(nxt)), 2> it{begin(nxt),
begin(nxt) + bv[h].zeros};
            rep(i, n) * it[bv[h].get(i)]++ = cur[i];
            swap(cur, nxt);
        }
        return;
    }

    inline pair<U, U> succ0(int l, int r, int h) const { return
make_pair(bv[h].rank0(l), bv[h].rank0(r)); }

    inline pair<U, U> succ1(int l, int r, int h) const {
        U l0 = bv[h].rank0(l);
        U r0 = bv[h].rank0(r);
        U zeros = bv[h].zeros;
        return make_pair(l + zeros - l0, r + zeros - r0);
    }

    T access(U k) const {
        T ret = 0;
        per(h, lg, 0) {
            U f = bv[h].get(k);
            ret |= f ? T(1) << h : 0;
            k = f ? bv[h].rank1(k) + bv[h].zeros : bv[h].rank0(k);
        }
        return ret;
    }

    T kth_smallest(U l, U r, U k) const {
        T res = 0;
        for(int h = lg - 1; h >= 0; --h) {
            U l0 = bv[h].rank0(l), r0 = bv[h].rank0(r);

```

```

            if(k < r0 - l0) l = l0, r = r0;
            else {
                k -= r0 - l0;
                res |= (T)1 << h;
                l += bv[h].zeros - l0, r += bv[h].zeros - r0;
            }
        }
        return res;
    }

    T kth_largest(int l, int r, int k) { return kth_smallest(l,
r, r - l - k - 1); }

    int range_freq(int l, int r, T upper) {
        if(upper >= (T)1 << lg) return r - l;
        int ret = 0;
        per(h, lg, 0) {
            bool f = (upper >> h) & 1;
            U l0 = bv[h].rank0(l), r0 = bv[h].rank0(r);
            if(f) {
                ret += r0 - l0;
                l += bv[h].zeros - l0;
                r += bv[h].zeros - r0;
            } else {
                l = l0;
                r = r0;
            }
        }
        return ret;
    }

    int range_freq(int l, int r, T lower, T upper) { return
range_freq(l, r, upper) - range_freq(l, r, lower); }

    array<vector<ll>, lg> sums;
    vector<ll> acc;
    void build2() {
        rep(i, lg) bv[i] = bit_vector(n), sums[i].assign(n + 1,
0);
        acc.resize(si(a) + 1);
        vector<T> cur = a, nxt(n);
        per(h, lg, 0) {
            rep(i, n) if((cur[i] >> h) & 1) bv[h].set(i);
            bv[h].build();
            array<decltype(begin(nxt)), 2> it{begin(nxt),
begin(nxt) + bv[h].zeros};
            rep(i, n) * it[bv[h].get(i)]++ = cur[i];
            swap(cur, nxt);
            rep(i, n) sums[h][i + 1] = sums[h][i] + cur[i];
        }
        rep(i, n) acc[i + 1] = acc[i] + a[i];
    }

    ll bottom_k_sum(int l, int r, int k) {
        ll res = 0;
        per(h, lg, 0) {
            U l0 = bv[h].rank0(l), r0 = bv[h].rank0(r);
            if(k < r0 - l0) {
                l = l0, r = r0;
            } else {
                res += sums[h][r0] - sums[h][l0];
                k -= r0 - l0;
                l += bv[h].zeros - l0;
                r += bv[h].zeros - r0;
            }
        }
        res += sums[0][l + k] - sums[0][l];
        return res;
    }

    ll top_k_sum(int l, int r, int k) { return acc[r] - acc[l] -
bottom_k_sum(l, r, r - l - k); }
};
#undef U
#undef L

```

dp

d-edge-monge.hppmd5: 4ab7ee

template<class C, class T = decltype(std::declval<C>().get())> T incremental\_monge\_shortest\_path(const int n, C init) { class env {

```

public:
    C mid;
    C last;
    int prev;
};
std::vector<env> nodes;
{
    int n_ = n;
    int d = 0;
    while(n_ != 0) {
        n_ /= 2;
        d += 1;
    }
    nodes.assign(d, {init, init, 0});
}
std::vector<T> dp(n + 1, static_cast<T>(0));

const auto f = [&](const auto& f, const int d, const int r) -
> int {
    auto& [mid, last, prev] = nodes[d];
    const int w = 1 << d;
    if((r >> d) % 2 == 1) {
        for(int i = std::max(0, r - 2 * w); i != r; i += 1) {
            mid.push_back(i);
        }
        const int next = r + w <= n ? f(f, d + 1, r + w) : r -
w;

        int argmin = prev;
        dp[r] = dp[argmin] + mid.get();
        for(int i = prev; i != next; i++) {
            mid.pop_front(i);
            i += 1;
            const T t = dp[i] + mid.get();
            if(dp[r] > t) {
                dp[r] = t;
                argmin = i;
            }
        }
        prev = next;
        return argmin;
    } else {
        for(int i = std::max(0, r - 2 * w); i != r; i += 1) {
            last.push_back(i);
        }
        for(int i = std::max(0, r - 3 * w); i != r - 2 * w; i
+= 1) { last.pop_front(i); }
        int argmin = prev;
        for(int i = r - 2 * w; i != r - w; i++) {
            last.pop_front(i);
            i += 1;
            const T t = dp[i] + last.get();
            if(dp[r] > t) {
                dp[r] = t;
                argmin = i;
            }
        }
        return argmin;
    }
};

for(int i = 1; i != n + 1; i += 1) { f(f, 0, i); }

return dp[n];
}

namespace golden_section_search_impl {

using i64 = std::int64_t;

template<class F, class T = decltype(std::declval<F>()
(std::declval<i64>()))>, class Compare = std::less<T>>
std::pair<i64, T> golden_section_search(F f, i64 min, i64 max,
Compare comp = Compare()) {
    assert(min <= max);

    i64 a = min - 1, x, b;
    {
        i64 s = 1, t = 2;
        while(t < max - min + 2) { std::swap(s += t, t); }
        x = a + t - s;
        b = a + t;
    }
    T fx = f(x), fy;
    while(a + b != 2 * x) {

```

```

const i64 y = a + b - x;
    if(max < y || comp(fx, (fy = f(y)))) {
        b = a;
        a = y;
    } else {
        a = x;
        x = y;
        fx = fy;
    }
}
return {x, fx};
}

// namespace golden_section_search_impl

using golden_section_search_impl::golden_section_search;

struct cost {
    const vector<ll>* a;
    ll lambda;
    ll cost;
    void pop_front(int l) {}
    void push_back(int r) {}
    ll get() { return lambda + c } // 最小化なら -
};

// k : 使う辺の本数
const auto f = [&](ll l) -> ll {
    auto res = incremental_monge_shortest_path(n + 1, cost{l, 0,
0}) - l * (k + 1);
    return res;
};
// L = - max(|e|) * 3, R = max(|e|) * 3
OUT(golden_section_search(f, L, R, greater<ll>()).se);

```

## mo-rollback.hpp

md5: 5737bf

```

struct MoRollBack {
    using ADD = function<void(int)>;
    using REM = function<void(int)>;
    using RESET = function<void()>;
    using SNAP = function<void()>;
    using ROLLBACK = function<void()>;
    int w;
    vector<int> l, r, ord;
    MoRollBack(int n, int q) : w((int)sqrt(n)), ord(q) {
iota(all(ord), 0); }
    void add(int a, int b) { /* [l, r) */
        l.emplace_back(a);
        r.emplace_back(b);
    }
    void run(const ADD& add, const REM& rem, const RESET& reset,
const SNAP& snap, const ROLLBACK& rollback) {
        sort(begin(ord), end(ord), [&](int a, int b) {
            int ab = l[a] / w, bb = l[b] / w;
            if(ab != bb) return ab < bb;
            return r[a] < r[b];
        });
        reset();
        for(auto idx : ord) {
            if(r[idx] - l[idx] < w) {
                rep(i, l[idx], r[idx]) add(i);
                rem(idx);
                rollback();
            }
        }
        int nr = 0, lb = -1;
        for(auto idx : ord) {
            if(r[idx] - l[idx] < w) continue;
            int b = l[idx] / w;
            if(lb != b) {
                reset();
                lb = b;
                nr = (b + 1) * w;
            }
            while(nr < r[idx]) add(nr++);
            snap();
            per(j, (b + 1) * w, l[idx]) add(j);
            rem(idx);
            rollback();
        }
    }
}

```

```
    }  
};
```

mo.hpp

md5: 6ff6db

```
struct Mo {  
    int n;  
    vector<pii> lr;  
    Mo(int n) : n(n) {}  
    void add(int l, int r) { lr.pb(l, r); }  
    template<typename AL, typename AR, typename EL, typename ER,  
typename O>  
    void build(const AL& add_left, const AR& add_right, const EL&  
erase_left, const ER& erase_right, const O& out) {  
        int q = (int)lr.size();  
        int bs = n / min<int>(n, sqrt(q));  
        vector<int> ord(q);  
        iota(all(ord), 0);  
        sort(all(ord), [&](int a, int b) {  
            int ab = lr[a].first / bs, bb = lr[b].first / bs;  
            if(ab != bb) return ab < bb;  
            return (ab & 1) ? lr[a].second > lr[b].second :  
lr[a].second < lr[b].second;  
        });  
        int l = 0, r = 0;  
        for(auto idx : ord) {  
            while(l > lr[idx].first) add_left(--l);  
            while(r < lr[idx].second) add_right(r++);  
            while(l < lr[idx].first) erase_left(l++);  
            while(r > lr[idx].second) erase_right(--r);  
            out(idx);  
        }  
    }  
    template<typename A, typename E, typename O> void build(const  
A& add, const E& erase, const O& out) {  
        build(add, add, erase, erase, out);  
    }  
};
```

monge-incremental-rowmin.hpp

md5: 2cff0f

```
// A[N + 1][N + 1]: Monge が i > j のみ存在しているとき、i (= 0,  
..., N)行目の最小値を返す  
// f(i, j, v) で、j 行目の最小値が求まっている v を用いて、A[i][j] にア  
クセス  
template<typename T, typename F> vector<T> monge_rowmin(int n,  
const F& f) {  
    vector<T> mi(n + 1, numeric_limits<T>::max());  
    mi[0] = 0;  
    vector<int> amin(n + 1);  
    auto check = [&](int i, int j) {  
        if(chmin(mi[i], f(i, j, mi))) { amin[i] = j; }  
    };  
    check(n, 0);  
    auto solve = [&](auto&& self, int l, int r) {  
        if(r - l == 1) return;  
        int mid = l + r >> 1;  
        rep(k, amin[l], amin[r] + 1) check(mid, k);  
        self(self, l, mid);  
        rep(k, l + 1, mid + 1) check(r, k);  
        self(self, mid, r);  
    };  
    solve(solve, 0, n);  
    return mi;  
}
```

monotone-minima.hpp

md5: 187a2d

```
// monotone 行列の各行について、最小値を取る場所とその値を返す  
template<typename T, typename F> vector<pair<int, T>>  
monotone_minima(int h, int w, const F& f) {  
    vector<pair<int, T>> dp(h, pair(-1, T()));  
    auto rec = [&](auto&& rec, int u, int d, int l, int r) {  
        if(u > d) return;  
        int mid = u + d >> 1;  
        auto& [idx, mi] = dp[mid];  
        idx = l, mi = f(mid, l);  
        rep(i, l + 1, r + 1) if(chmin(mi, f(mid, i))) idx = i;  
        rec(rec, u, mid - 1, l, idx);  
    };
```

```
        rec(rec, mid + 1, d, idx, r);  
    };  
    rec(rec, 0, h - 1, 0, w - 1);  
    return dp;  
}
```

math

ExtGCD.hpp

md5: 88cb1c

```
// returns gcd(a, b) and assign x, y to integers  
// s.t. ax + by = gcd(a, b) and |x| + |y| is minimized  
ll extgcd(ll a, ll b, ll& x, ll& y) {  
    // assert(a >= 0 && b >= 0);  
    if(!b) return x = 1, y = 0, a;  
    ll d = extgcd(b, a % b, y, x);  
    y -= a / b * x;  
    return d;  
}  
ll inv_mod(ll x, ll md) {  
    ll y, z;  
    extgcd(x, md, y, z);  
    return (y % md + md) % md;  
}
```

and-or-convolution.hpp

md5: da6157

```
// and / or convolution  
template<bool isOR, typename T> void fzt(vector<T>& a, bool inv  
= false) {  
    int n = si(a);  
    int m = __lg(n);  
    rep(i, m) {  
        rep(b, n) {  
            if((b >> i & 1) == isOR) a[b] += a[b ^ 1 << i] * (inv ?  
-1 : 1);  
        }  
    }  
}
```

binom.hpp

md5: db2821

```
constexpr int N = 1e6 + 100;  
mint fact[N], ifact[N];  
void pre() {  
    fact[0] = 1;  
    rep(i, 1, N) fact[i] = i * fact[i - 1];  
    ifact[N - 1] = fact[N - 1].inv();  
    per(i, N - 1, 0) ifact[i] = ifact[i + 1] * (i + 1);  
}  
mint C(int n, int m) { return (n < m or m < 0 ? 0 : fact[n] *  
ifact[m] * ifact[n - m]); }
```

crt.hpp

md5: 0e9c10

```
// (rem, mod)  
pll crt(const vl& b, const vl& c) {  
    int n = si(b);  
    ll r = 0, m = 1;  
    rep(i, n) {  
        ll g, im, x;  
        g = extgcd(m, c[i], im, x);  
        if((b[i] - r) % g) return {0, -1};  
        ll tmp = (b[i] - r) / g * im % (c[i] / g);  
        r += m * tmp;  
        m *= c[i] / g;  
    }  
    return {(r % m + m) % m, m};  
}
```

floor\_sum.hpp

md5: 930ca0

```
// x_i=floor((a*i+b)/c), i=0,1,..n-1  
// a,c>0, b>=0  
ll floor_sum(ll n, ll a, ll b, ll c) {  
    if(n == 0) return 0;  
    ll res = 0;  
    res += n * (n - 1) / 2 * (a / c);  
    a %= c;  
    res += n * (b / c);
```

```
    b %= c;
    if(a == 0) return res;
    ll top = (a * (n - 1) + b) / c;
    res += top * n;
    ll h = (b + 1 + c - 1) / c;
    if(h <= top) res -= floor_sum(top - h + 1, c, c * h - (b +
1), a) + top - h + 1;
    return res;
}
```

lagrange-hokan.hpp

md5: 22b9e3

```
template<typename T> T lagrange_polynomial(const vector<T>& y,
ll t) {
    int n = si(y) - 1;
    if(t <= n) return y[t];
    T ret(0);
    vector<T> dp(n + 1, 1), pd(n + 1, 1);
    rep(i, n) dp[i + 1] = dp[i] * (t - i);
    per(i, n + 1, 1) pd[i - 1] = pd[i] * (t - i);
    rep(i, n + 1) {
        T tmp = y[i] * dp[i] * pd[i] * ifact[i] * ifact[n - i];
        ret -= ((n - i) & 1 ? tmp : -tmp);
    }
    return ret;
}
```

matrix.hpp

md5: 270f1c

```
template<typename T> struct M {
    vector<vector<T>>> a;
    int n, m;
    M(int n, int m) : n(n), m(m), a(n, vector<T>(m)) {}
    M(int n = 0) : M<T>(n, n) {}
    vector<T>& operator[](int k) { return a[k]; }
    const vector<T>& operator[](int k) const { return a[k]; }
    static M I(int n) {
        M mat(n);
        rep(i, n) mat[i][i] = 1;
        return mat;
    }
    M& operator+=(const M& b) {
        rep(i, n) rep(j, m) (*this)[i][j] += b[i][j];
        return *this;
    }
    M& operator-=(const M& b) {
        rep(i, n) rep(j, m) (*this)[i][j] -= b[i][j];
        return *this;
    }
    M& operator*=(const M& b) {
        int l = b.m;
        vector c(n, vector<T>(l));
        rep(i, n) rep(j, m) rep(k, l) c[i][k] += (*this)[i][j] *
b[j][k];
        a.swap(c);
        return *this;
    }
    M& operator^=(ll k) {
        M b = M::I(n);
        while(k) {
            if(k & 1) b *= *this;
            *this *= *this;
            k >>= 1;
        }
        a.swap(b.a);
        return *this;
    }
    M operator+(const M& b) const { return (M(*this) += b); }
    M operator-(const M& b) const { return (M(*this) -= b); }
    M operator*(const M& b) const { return (M(*this) *= b); }
    M operator^(const M& b) const { return (M(*this) ^= b); }
};
template<typename T> pair<int, T> GaussElimination(M<T>& a, bool
LE = false) {
    int n = a.n, m = a.m;
    int rank = 0, je = LE ? m - 1 : m;
    mint det = 1;
    rep(j, je) {
        int idx = -1;
        rep(i, rank, n) {
            if(a[i][j].x) {
```

```
                idx = i;
                break;
            }
        }
        if(idx == -1) {
            det = 0;
            continue;
        }
        if(rank != idx) {
            det = -det;
            swap(a[rank], a[idx]);
        }
        det *= a[rank][j];
        if(LE && a[rank][j].x != 1) {
            mint coeff = a[rank][j].inv();
            rep(k, j, m) a[rank][k] *= coeff;
        }
        int is = LE ? 0 : rank + 1;
        rep(i, is, n) {
            if(i == rank) continue;
            if(a[i][j].x) {
                mint coeff = a[i][j] / a[rank][j];
                rep(k, j, m) a[i][k] -= a[rank][k] * coeff;
            }
        }
        rank++;
    }
    return make_pair(rank, det);
}

template<typename T> vector<vector<T>>> LinearEquation(M<T> a,
vector<T> b) {
    int n = a.n, m = a.m;
    rep(i, n) a[i].eb(b[i]);
    a.m++;
    auto p = GaussElimination(a, true);
    int rank = p.first;
    rep(i, rank, n) {
        if(a[i][m].x != 0) return {};
    }
    vector<vector<T>>> res(1, vector<T>(m));
    vi piv(m, -1);
    int j = 0;
    rep(i, rank) {
        while(a[i][j].x == 0) ++j;
        res[0][j] = a[i][m], piv[j] = i;
    }
    rep(j, m) {
        if(piv[j] == -1) {
            vector<T> x(m);
            x[j] = 1;
            rep(k, j) {
                if(piv[k] != -1) x[k] = -a[piv[k]][j];
            }
            res.eb(x);
        }
    }
    return res;
}
```

prime.hpp

md5: 94a4a8

```
template<class T, class U> T pow_mod(T x, U n, T md) {
    T r = 1 % md;
    x %= md;
    while(n) {
        if(n & 1) r = (r * x) % md;
        x = (x * x) % md;
        n >>= 1;
    }
    return r;
}
bool is_prime(ll n) {
    if(n <= 1) return false;
    if(n == 2) return true;
    if(n % 2 == 0) return false;
    ll d = n - 1;
    while(d % 2 == 0) d /= 2;
    for(ll a : {2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37}) {
        if(n <= a) break;
        ll t = d;
        ll y = pow_mod<i128>(a, t, n); // over
```

```
while(t != n - 1 && y != 1 && y != n - 1) {
    y = i128(y) * y % n; // flow
    t <=< 1;
}
if(y != n - 1 && t % 2 == 0) { return false; }
}
return true;
}
ll pollard_single(ll n) {
    ll R;
    auto f = [&](ll x) { return (i128(x) * x + R) % n; };
    if(is_prime(n)) return n;
    if(n % 2 == 0) return 2;
    ll st = 0;
    while(true) {
        R = rnd(1, n);
        st++;
        ll x = st, y = f(x);
        while(true) {
            ll p = gcd((y - x + n), n);
            if(p == 0 || p == n) break;
            if(p != 1) return p;
            x = f(x);
            y = f(f(y));
        }
    }
}
vl factor(ll n) {
    if(n == 1) return {};
    ll x = pollard_single(n);
    if(x == n) return {x};
    vl l = factor(x), r = factor(n / x);
    return l.insert(end(l), all(r)), l;
}
```

primitive-root.hpp

md5: 4088f5

```
ll primitive_root(ll p) {
    auto v = factor(p - 1);
    sort(all(v)), v.erase(unique(all(v)), end(v));
    while(true) {
        ll g = rnd(1, p);
        bool ok = true;
        for(auto d : v) {
            ll f = (p - 1) / d;
            if(pow_mod<i128>(g, f, p) == 1) {
                ok = false;
                break;
            }
        }
        if(ok) return g;
    }
}
```

xor-convolution.hpp

md5: f5168d

```
template<typename T> void fwt(vector<T>& f, bool inv = false) {
    int n = si(f), m = __lg(n);
    rep(i, m) {
        rep(b, n) {
            rep(~b >> i & 1) {
                T x = f[b], y = f[b ^ 1 << i];
                f[b] = x + y, f[b ^ 1 << i] = x - y;
            }
        }
    }
    if(inv) {
        T iz = T(1) / T(si(f));
        fore(e, f) e *= iz;
    }
}
```

graph

bcc.hpp

md5: 3df588

```
template<typename G> struct BCC : LL<G> {
    vi used;
    vector<vector<pii>> bc;
    vector<pii> tmp;
    using L = LL<G>;
```

```
using L::g;
using L::low;
using L::ord;

BCC(G g) : L(g) { build(); }

void build() {
    used.assign(si(g), 0);
    rep(i, si(used)) if(!used[i]) dfs(i, -1);
}

void dfs(int x, int p) {
    used[x] = true;
    fore(e, g[x]) {
        if(e == p) continue;
        if(!used[e] || ord[e] < ord[x]) tmp.eb(minmax(x, e));
        if(!used[e]) {
            dfs(e, x);
            if(low[e] >= ord[x]) {
                bc.eb();
                while(true) {
                    auto p = tmp.back();
                    bc.back().eb(p);
                    tmp.pop_back();
                    if(p.first == min(x, e) and p.second == max(x,
e)) break;
                }
            }
        }
    }
}
};
```

eulerian-trail.hpp

md5: 5d421d

```
struct edge {
    int x, y, idx;
};
vector<edge> eulerian_path(vector<edge> es, int s, bool directed
= false) {
    if(es.empty()) return {};
    int n = 0;
    fore(e, es) chmax(n, max(e.x, e.y) + 1);
    vector<vector<pair<edge, int>>> g(n);
    for(auto& e : es) {
        int p = si(g[e.y]);
        g[e.x].emplace_back(e, p);
        if(!directed) {
            int q = si(g[e.x]) - 1;
            swap(e.x, e.y);
            g[e.x].emplace_back(e, q);
        }
    }
    vector<edge> ord;
    stack<pair<int, edge>> st;
    st.emplace(s, edge{-1, -1, -1});
    while(st.size()) {
        int x = st.top().first;
        if(empty(g[x])) {
            ord.eb(st.top().second);
            st.pop();
        } else {
            auto e = g[x].back();
            g[x].pop_back();
            if(e.second == -1) continue;
            if(!directed) g[e.first.y][e.second].second = -1;
            st.emplace(e.first.y, e.first);
        }
    }
    ord.pop_back();
    reverse(begin(ord), end(ord));
    if(si(ord) != si(es)) return {};
    return ord;
}
```

lowlink.hpp

md5: e3987c

```
template<typename G> struct LL {
    int n;
    const G g;
    vi ord, low, arti;
```

```
LL(G g) : n(si(g)), g(g), ord(si(g), -1), low(si(g), -1) {
    int k = 0;
    rep(i, n) {
        if(ord[i] == -1) k = dfs(i, k, -1);
    }
}

int dfs(int x, int k, int p) {
    low[x] = (ord[x] = k++);
    int cnt = 0;
    bool is_arti = false, second = false;
    fore(e, g[x]) {
        if(ord[e] == -1) {
            cnt++;
            k = dfs(e, k, x);
            chmin(low[x], low[e]);
            is_arti |= (p != -1) && (low[e] >= ord[x]);
            if(ord[x] < low[e]) bridge.eb(minmax(x, e));
        } else if(e != p or second) {
            chmin(low[x], ord[e]);
        } else {
            second = true;
        }
    }
    is_arti |= p == -1 && cnt > 1;
    if(is_arti) arti.eb(x);
    return k;
}
};
```

max\_matching.hpp md5: 2ece25

```
struct Matching {
    int n;
    vector<vi> g;
    vi mt;
    vi is_ev, gr_buf;
    vector<pii> nx;
    int st;
    int group(int x) {
        if(gr_buf[x] == -1 || is_ev[gr_buf[x]] != st) return
gr_buf[x];
        return gr_buf[x] = group(gr_buf[x]);
    }
    void match(int p, int b) {
        int d = mt[p];
        mt[p] = b;
        if(d == -1 || mt[d] != p) return;
        if(nx[p].second == -1) {
            mt[d] = nx[p].first;
            match(nx[p].first, d);
        } else {
            match(nx[p].first, nx[p].second);
            match(nx[p].second, nx[p].first);
        }
    }
    bool arg() {
        is_ev[st] = st;
        gr_buf[st] = -1;
        nx[st] = pii(-1, -1);
        queue<int> q;
        q.push(st);
        while(q.size()) {
            int a = q.front();
            q.pop();
            for(auto b : g[a]) {
                if(b == st) continue;
                if(mt[b] == -1) {
                    mt[b] = a;
                    match(a, b);
                    return true;
                }
            }
            if(is_ev[b] == st) {
                int x = group(a), y = group(b);
                if(x == y) continue;
                int z = -1;
                while(x != -1 || y != -1) {
                    if(y != -1) swap(x, y);
                    if(nx[x] == pii(a, b)) {
                        z = x;
                        break;
                    }
                }
            }
        }
    }
};
```

```
nx[x] = pii(a, b);
x = group(nx[mt[x]].first);
}
for(int v : {group(a), group(b)}) {
    while(v != z) {
        q.push(v);
        is_ev[v] = st;
        gr_buf[v] = z;
        v = group(nx[mt[v]].first);
    }
}
} else if(is_ev[mt[b]] != st) {
    is_ev[mt[b]] = st;
    nx[b] = pii(-1, -1);
    nx[mt[b]] = pii(a, -1);
    gr_buf[mt[b]] = b;
    q.push(mt[b]);
}
}
return false;
}
Matching(const vector<vi>& _g) : n(int(_g.size())), g(_g),
mt(n, -1), is_ev(n, -1), gr_buf(n), nx(n) {
    for(st = 0; st < n; st++)
        if(mt[st] == -1) arg();
}
vector<pii> max_match() {
    vector<pii> res;
    rep(i, n) if(i < mt[i]) res.eb(i, mt[i]);
    return res;
}
};
```

maximum-independent-set.hpp md5: ac1384

```
unsigned ll maximum_independent_set(vector<vi> g) {
    using U = unsigned long long;
    int n = si(g);
    vector<U> nbd(n);
    rep(i, n) fore(e, g[i]) nbd[i] |= 1ULL << e;
    int best = 0;
    U res = 0;
    auto dfs = [&](auto&& dfs, U now, U rest) -> void {
        pii p(-1, -1);
        while(true) {
            bool upd = 0;
            rep(v, n) {
                if(rest >> v & 1) {
                    int d = popcount(nbd[v] & rest);
                    if(chmax(p.second, d)) p.first = v;
                    if(d <= 1) rest ^= 1ULL << v, rest &= ~nbd[v],
now |= 1ULL << v, upd = 1;
                }
            }
            if(!upd) break;
            p = {-1, -1};
        }
        int a = popcount(now), b = popcount(rest);
        if(chmax(best, a)) res = now;
        if(!b or a + b <= best) return;
        int v = p.first;
        rest &= ~(1ULL << v);
        if(p.second >= 3) dfs(dfs, now, rest);
        now |= 1ULL << v;
        dfs(dfs, now, rest & ~(nbd[v]));
    };
    U now = 0, rest = (1ULL << n) - 1;
    dfs(dfs, now, rest);
    return res;
}
};
```

scc.hpp md5: 73554b

```
template<typename G> struct SCC {
    G g;
    vector<vi> rg;
    vi comp, ord, used;
    int num; // 連結成分の数

    SCC(G g) : g(g), rg(si(g)), comp(si(g), -1), ord(si(g)),
```

tecc.hpp md5: 17c69f

modint

```

mint operator-() { return mint(-x); }
mint& operator+=(const mint& r) { return s(x + r.x); }
mint& operator-=(const mint& r) { return s(x + mod - r.x); }
mint& operator*=(const mint& r) { return x = b.mul(x, r.x),
*this; }
mint& operator/=(const mint& r) { return *this *= r.inv(); }
friend mint operator+(mint l, mint r) { return l += r; }
friend mint operator-(mint l, mint r) { return l -= r; }
friend mint operator*(mint l, mint r) { return l *= r; }
friend mint operator/(mint l, mint r) { return l /= r; }
mint inv() const { return pow(mod - 2); }
mint pow(ll b) const {
    mint a = *this, c = 1;
    while(b) {
        if(b & 1) c *= a;
        a *= a;
        b >>= 1;
    }
    return c;
}
};

using vm = vector<mint>;

```

**modint.hpp** md5: 3db9f2

modint.hpp.gch

```
gpcWritey-=-/A|@x86-  
64generic__SSP_STRONG_  
300__DBL_MIN_EXP__ (-1021)__cpp_attributes 200809L-  
%__cctype__ __cstdarg__ __cstddef__ __cplusplus__  
201606L__UINT_LEAST16_MAX__ 0xffff__FLT16_HAS_QUIET_NAN__  
100__ATOMIC_ACQUIRE 200__FLT128_MAX_10_EXP__ 493260__FLT_MIN__  
1.17549435082228750796873653722224568e-  
38F00__GCC_IEC_559_COMPLEX 200__cpp_aggregate_nsdmi  
201304L'__UINT_LEAST8_TYPE__ unsigned char__SIZEOF_FLOAT80__  
16'0__cpp_impl_three_way_comparison 201907L0  
__INTMAX_C(c) c ## L0__CHAR_BIT__  
8%__cpp_designated_initializers 201707L0  
__UINT8_MAX__ 0xff__SCHAR_WIDTH__ 8__WINT_MAX__  
0xffffffffU0__FLT32_MIN_EXP__ (-125)__cpp_static_assert
```



```
201411L00__ORDER_LITTLE_ENDIAN__ 1234!__SIZE_MAX__
0xffffffffffffffffFUL0
__WCHAR_MAX__ 0x7fffffff$__GCC_HAVE_SYNC_COMPARE_AND_SWAP_2
1$__GCC_HAVE_SYNC_COMPARE_AND_SWAP_4
1$__GCC_HAVE_SYNC_COMPARE_AND_SWAP_8
100__GCC_ATOMIC_CHAR_LOCK_FREE 20
__GCC_IEC_559 200__FLT32X_DECIMAL_DIG__ 1700__FLT_EVAL_METHOD__
000__cpp_binary_literals 201304L00__FLT64_DECIMAL_DIG__ 17
0__CET__ 300__cpp_noexcept_function_type
201510L!0__GCC_ATOMIC_CHAR32_T_LOCK_FREE 2
0__cpp_variadic_templates 200704L(0__UINT_FAST64_MAX__
0xffffffffffffffffFUL00__SIG_ATOMIC_TYPE__
int00__DBL_MIN_10_EXP__ (-307)00__FINITE_MATH_ONLY__ 0
__cpp_variable_templates 201304L00__FLT32X_MAX_EXP__
1024$__GCC_HAVE_SYNC_COMPARE_AND_SWAP_1 100__FLT32_HAS_DENORM__
100__UINT_FAST8_MAX__ 0xff00__cpp_rvalue_reference
200610L*__cpp_nested_namespace_definitions
201411L00__DEC64_MAX_EXP__ 385
0__INT8_C(c) c00__INT_LEAST8_WIDTH__ 800__cpp_variadic_using
201611L)0__UINT_LEAST64_MAX__
0xffffffffffffffffFUL00__INT_LEAST8_MAX__
0x7f00__cpp_capture_star_this 201603L0__SHRT_MAX__
0x7fff9__LDBL_MAX__
1.18973149535723176502126385303097021e+4932L00__cpp_impl_coroutine
201902L00__FLT64X_MAX_10_EXP__ 493200__cpp_if_constexpr
201606L00__LDBL_IS_IEC_60559__ 200__FLT64X_HAS_QUIET_NAN__
100__UINT_LEAST8_MAX__ 0xff00__GCC_ATOMIC_BOOL_LOCK_FREE
2E0__FLT128_DENORM_MIN__ 6.47517511943802511092443895822764655e-
4966F128"0__UINTMAX_TYPE__ long unsigned int 0__linux
100__DEC32_EPSILON__ 1E-60F 0__FLT_EVAL_METHOD_TS_18661_3__
00__OPTIMIZE__ 100__unix 100__UINT32_MAX__
0xffffffffF000__GXX_EXPERIMENTAL_CXX0X__ 1F0__DBL_DENORM_MIN__
double(4.94065645841246544176568792868221372e-
324L)00__FLT128_MIN_EXP__ (-16381)0__WINT_MIN__
0000__FLT128_MIN_10_EXP__ (-4931)00__FLT32X_IS_IEC_60559__
200__INT_LEAST16_WIDTH__ 160
__SCHAR_MAX__ 0x7f00__FLT128_MANT_DIG__ 113"
__WCHAR_MIN__ (-__WCHAR_MAX__ - 1)0 __INT64_C(c) c ##
L$0__cpp_impl_destroying_delete 201806L
0__GCC_ATOMIC_POINTER_LOCK_FREE 200__FORTIFY_SOURCE
200__FLT32X_MANT_DIG__ 53!0__GCC_ATOMIC_CHAR16_T_LOCK_FREE
200__cpp_aligned_new 201606L00__FLT32_MAX_10_EXP__
3800__FLT64X_EPSILON__ 1.08420217248550443400745280086994171e-
19F64x00__STDC_HOSTED__ 100__DEC64_MIN_EXP__
(-382)00__cpp_decltype_auto 201304L00__DBL_DIG__ 150
__FLT32_DIG__ 690__FLT_EPSILON__
1.19209289550781250000000000000000000e-7F0
__cpp_char8_t 201811L0__GXX_WEAK__ 100__SHRT_WIDTH__
1600__FLT32_IS_IEC_60559__ 29__LDBL_MIN__
3.36210314311209350626267781732175260e-
4932L00__DBL_IS_IEC_60559__ 20
__DEC32_MAX__ 9.999999E96DF00__CHAR8_TYPE__ unsigned
char$0__cpp_threadsafe_static_init
200806L#00__cpp_enumerator_attributes
201411LE0__FLT64X_DENORM_MIN__
3.64519953188247460252840593361941982e-
4951F64x00__FLT32X_HAS_INFINITY__ 10
__INT32_MAX__ 0x7fffffff00__GLIBCXX_DEBUG 10
__FLT16_DIG__ 3
0__unix__ 10
__INT_WIDTH__ 3200__SIZEOF_LONG__ 800__STDC_IEC_559__
100__STDC_ISO_10646__ 201706L0
__UINT16_C(c) c00__DECIMAL_DIG__ 2100__STDC_IEC_559_COMPLEX__
10__FLT64_EPSILON__ 2.22044604925031308084726333618164062e-
16F640
__gnu_linux__ 10
__INT16_MAX__ 0x7fff00__FLT64_MIN_EXP__
(-1021)00__cpp_using_enum 201907L00__FLT64X_MIN_10_EXP__
(-4931)00__LDBL_HAS_QUIET_NAN__ 100__FLT16_MIN_EXP__
(-13)00__FLT64_MANT_DIG__ 5300__cpp_consteval
201811L00__FLT64X_MANT_DIG__ 6400__GNUC__ 12
__GXX_RTTI 1 0__pie__ 2 0__MMX__ 100noimi
100__FLT_HAS_DENORM__ 100__SIZEOF_LONG_DOUBLE__
1600__BIGGEST_ALIGNMENT__ 1600__STDC_UTF_16__
100__FLT64_MAX_10_EXP__ 30800__FLT16_MAX_10_EXP__
4%0__cpp_delegating_constructors 200604L00__FLT32_HAS_INFINITY__
1?0__DBL_MAX__
double(1.79769313486231570814527423731704357e+308L)00__cpp_raw_string
200710L&00__INT_FAST32_MAX__
0x7fffffffffffffffL00__DBL_HAS_INFINITY__ 100__SIZEOF_FLOAT__
400__HAVE_SPECULATION_SAFE_VALUE 100__cpp_fold_expressions
201603L00__DEC32_MIN_EXP__ (-94)00__INTPTR_WIDTH__
6400__FLT64X_HAS_INFINITY__ 1 0__UINT_LEAST32_MAX__
0xffffffffF000__FLT32X_HAS_DENORM__ 100__INT_FAST16_TYPE__ long
int00__STRICT_ANSI__ 100__MMX_WITH_SSE__ 100__LDBL_HAS_DENORM__
1
0__SEG_6S 100__cplusplus 202002L00__cpp_ref_qualifiers 200710L0
__DEC32_MIN__ 1E-95DF0__DEPRECATED 100__cpp_rvalue_references
200610L00__DBL_MAX_EXP__ 102400__WCHAR_WIDTH__ 32:
__FLT32_MAX__
3.40282346638528859811704183484516925e+38F3200__DEC128_EPSILON__
1E-33DL00__FLT16_DECIMAL_DIG__ 50
__SSE2_MATH__ 100__ATOMIC_HLE_RELEASE 131072#0__PTRDIFF_MAX__
0x7fffffffffffffffL 0__amd64 100__ATOMIC_HLE_ACQUIRE
6553600__GNUC__ 12&0__LONG_LONG_MAX__
0x7fffffffffffffffL00__SIZEOF_SIZE_T__ 800__cpp_nsdmi
200809L00__FLT64X_MIN_EXP__ (-16381)00__SIZEOF_WINT_T__
400__LONG_LONG_WIDTH__ 6400__cpp_initializer_lists
200806L00__FLT32_MAX_EXP__ 12800__cpp_hex_float
201603L00__GXX_ABI_VERSION 101700__FLT128_HAS_INFINITY__
100__FLT_MIN_EXP__ (-125)00__GCC_HAVE_DWARF2_CFI_ASM 1
0__x86_64 10
__cpp_lambdas 200907L00__INT_FAST64_TYPE__ long
int00__FLT64_DENORM_MIN__
4.94065645841246544176568792868221372e-
324F6400__cpp_template_auto 201606L?0__DBL_MIN__
double(2.22507385850720138309023271733240406e-
308L)00__FLT16_DENORM_MIN__
5.96046447753906250000000000000000000e-8F1600__FLT128_EPSILON__
1.92592994438723585305597794258492732e-
34F128C0__FLT64X_NORM_MAX__
1.18973149535723176502126385303097021e+4932F64x00__SIZEOF_POINTER
8
0__LP64__ 100__DBL_HAS_QUIET_NAN__ 100__FLT32X_EPSILON__
2.22044604925031308084726333618164062e-
16F32x00__DECIMAL_BID_FORMAT__ 100__FLT64_MIN_10_EXP__
(-307)00__FLT16_MIN_10_EXP__ (-4)00__FLT64X_DECIMAL_DIG__
2100__DEC128_MIN__ 1E-6143DL00__REGISTER_PREFIX__
00__UINT16_MAX__ 0xffffffff00__LDBL_HAS_INFINITY__ 1:
__FLT32_MIN__ 1.1754943508222875079687365372224568e-
38F3200__UINT8_TYPE__ unsigned char
0__FLT_DIG__ 600__DEC_EVAL_METHOD__ 290__DEC128_MAX__
9.999999999999999999999999999999999999E6144DL00__FLT_MANT_DIG__
2400__LDBL_DECIMAL_DIG__ 2100__VERSION__ "12.3.0"0
__UINT64_C(c) c ## UL 0__cpp_unicode_characters
201411L00__STDC_PREDEF_H 100__INT_LEAST32_MAX__
0x7ffffffff00__GCC_ATOMIC_INT_LOCK_FREE 200__FLT128_MAX_EXP__
16384"0__cpp_conditional_explicit 201806L00__FLT32_MANT_DIG__
24,0__FLOAT_WORD_ORDER__
__ORDER_LITTLE_ENDIAN__00__FLT32X_MIN_EXP__
(-1021)"0__cpp_aggregate_paren_init
201902L&0__UINT_FAST64_TYPE__ long unsigned
int*0__STDC_IEC_60559_COMPLEX__ 201404L00__cpp_aggregate_bases
201603L00__FLT128_HAS_DENORM__ 100__FLT32_DECIMAL_DIG__
900__FLT128_DIG__ 330 __INT32_C(c) c00__DEC64_EPSILON__ 1E-
15DD00__ORDER_PDP_ENDIAN__ 341200__DEC128_MIN_EXP__
(-6142)00__cpp_constinit 201907L00__INT_FAST32_TYPE__ long
int(0__UINT_LEAST16_TYPE__ short unsigned
int00__DBL_HAS_DENORM__ 10
__cpp_rtti 199711L0
__SIZE_TYPE__ long unsigned int#0__UINT64_MAX__
0xffffffffffffffffFUL00__FLT_IS_IEC_60559__ 2-
"__GNUC_WIDE_EXECUTION_CHARSET_NAME "UTF-32LE"00__FLT64X_DIG__
180
__INT8_TYPE__ signed char00__cpp_digit_separators 201309L
0__ELF__ 100__GCC_ASM_FLAG_OUTPUTS__ 100__UINT32_TYPE__ unsigned
int0
__FLT_RADIX__ 200__INT_LEAST16_TYPE__ short
int;0__LDBL_EPSILON__ 1.08420217248550443400745280086994171e-
19L00__UINTMAX_C(c) c ## UL00__k8 1=0__FLT32X_MIN__
2.22507385850720138309023271733240406e-
308F32x00__SIG_ATOMIC_MAX__ 0x7fffffff
0__GCC_ATOMIC_WCHAR_T_LOCK_FREE 200__USER_LABEL_PREFIX__
00__STDC_IEC_60559_BFP__ 201404L00__SIZEOF_PTRDIFF_T__
80__LDBL_DIG__ 1800__FLT64_IS_IEC_60559__ 2
__x86_64__ 100__FLT16_IS_IEC_60559__ 200__FLT16_MAX_EXP__
16&0__DEC32_SUBNORMAL_MIN__ 0.000001E-95DF&0__INT_FAST16_MAX__
0x7fffffffffffffffL00__GCC_CONSTRUCTIVE_SIZE 640
__FLT64_DIG__ 15(0__UINT_FAST32_MAX__
0xffffffffffffffffFUL'0__UINT_LEAST64_TYPE__ long unsigned
int=0__FLT16_EPSILON__ 9.76562500000000000000000000000000000e-
4F1600__FLT_HAS_QUIET_NAN__ 100__FLT_MAX_10_EXP__ 38
__LONG_MAX__ 0x7fffffffffffffffL00__FLT64X_HAS_DENORM__
1D0__DEC128_SUBNORMAL_MIN__
```

[illegible]

```

45F00__FLT128_IS_IEC_60559__ 20__INT8_MAX__ 0x7f00__LONG_WIDTH__
64 __PIC__ 2&0__UINT_FAST32_TYPE__ long unsigned
int00__FLT16_MANT_DIG__ 1180__FLT32X_NORM_MAX__
1.79769313486231570814527432731704357e+308F32x00__CHAR32_TYPE__
unsigned int60__FLT_MAX__
3.40282346638528859811704183484516925e+38F00__cpp_constexpr
202002L00__GLIBCXX_DEBUG_PEDANTIC 1
0__SSE2__ 100__cpp_deduction_guides 201907L00__INT32_TYPE__
int00__SIZEOF_DOUBLE__ 800__cpp_exceptions
199711L00__FLT_MIN_10_EXP__ (-37);
__FLT64_MIN__ 2.22507385850720138309023271733240406e-
308F6400__INT_LEAST32_WIDTH__ 3200__INTMAX_TYPE__ long
int00__DEC128_MAX_EXP__ 614500__FLT32X_HAS_QUIET_NAN__
100__ATOMIC_CONSUME 100__GNUC_MINOR__ 300__INT_FAST16_WIDTH__
64$0__UINTMAX_MAX__ 0xffffffffffffffffUL __PIE__
000__FLT32X_DENORM_MIN__ 4.94065645841246544176568792868221372e-
324F32x$0__cpp_template_template_args
201611L00__DBL_MAX_10_EXP__ 308@0__LDBL_DENORM_MIN__
3.64519953188247460252840593361941982e-4951L
0__GCC_ATOMIC_CHAR8_T_LOCK_FREE 20 __INT16_C(c) c
0__STDC__ 100__FLT32X_DIG__ 1500__PTRDIFF_TYPE__ long
int00__ATOMIC_SEQ_CST 500__FLT32X_MIN_10_EXP__
(-307)"0__UINTPTR_TYPE__ long unsigned
int00__DEC64_SUBNORMAL_MIN__ 0.0000000000000001E-
383DD00__DEC128_MANT_DIG__ 3400__LDBL_MIN_10_EXP__
(-4931)00__cpp_generic_lambdas 201707L0__SSE_MATH__
100__SIZEOF_LONG_LONG__ 8#0__cpp_user_defined_literals
200809L00__FLT128_DECIMAL_DIG__ 3600__GCC_ATOMIC_LLONG_LOCK_FREE
200__FLT32_HAS_QUIET_NAN__ 100__FLT_DECIMAL_DIG__
9(0__UINT_FAST16_MAX__ 0xffffffffffffffffUL>0__LDBL_NORM_MAX__
1.18973149535723176502126385303097021e+4932L00__GCC_ATOMIC_SHORT
2!0__UINT_FAST8_TYPE__ unsigned char
0__GNU_SOURCE 100__cpp_init_captures 201803L00__ATOMIC_ACQ_REL
400__ATOMIC_RELEASE 3

```

md5: f769b5

```

mint g = 3; // 原始根
void fft(vm& a, bool inv = false) {
    int n = si(a), s = __lg(n);
    static vm z, iz;
    while(si(z) <= s) {
        z.eb(g.pow(mint(-1).x / (1 << si(z))));
        iz.eb(z.back().inv());
    }
    vm b(n);
    rep(i, 1, s + 1) {
        int w = 1 << s - i;
        mint base = inv ? iz[i] : z[i], now = 1;
        for(int y = 0; y < n / 2; y += w) {
            rep(x, w) {
                auto l = a[y << 1 | x], r = now * a[y << 1 | x | w];
                b[y | x] = l + r, b[y | x | n >> 1] = l - r;
            }
            now *= base;
        }
        swap(a, b);
    }
}

vm mul(vm a, vm b) {
    int n = si(a), m = si(b);
    if(!n or !m) return {};
    if(min(n, m) <= 30) {
        vm ans(n + m - 1);
        rep(i, n) rep(j, m) ans[i + j] += a[i] * b[j];
        return ans;
    }
    int N = n + m - 1;
    int z = bit_ceil(unsigend(N));
    a.resize(z), b.resize(z);
    fft(a), fft(b);
    rep(i, z) a[i] *= b[i];
    fft(a, true);
    a.resize(n + m - 1);
    mint iz = mint(z).inv();
    fore(e, a) e *= iz;
    return a;
}

```

**linear-recurrence.hpp**

md5: 7ef16a

```
// [x ^ k] p / q
mint LinearRecurrence(ll k, fps q, fps p) {
    q.shrink();
    mint ret = 0;
    if(si(p) >= si(q)) {
        auto r = p / q;
        p -= r * q;
        p.shrink();
        if(k < r.size()) ret += r[k];
    }
    if(p.size() == 0) return ret;
    p.resize(q.size() - 1);
    while(k) {
        auto q2 = q;
        for(int i = 1; i < q2.size(); i += 2) q2[i] = -q2[i];
        auto s = p * q2, t = q * q2;
        for(int i = (k & 1); i < s.size(); i += 2) p[i >> 1] =
s[i];
        for(int i = 0; i < t.size(); i += 2) q[i >> 1] = t[i];
        k >>= 1;
    }
    return ret + p[0];
}
// a * q = 0
mint kitamasa(ll n, fps q, fps a) {
    if(n < si(a)) return a[n];
    auto p = a.pre(si(q) - 1) * q;
    p.resize(si(q) - 1);
    return LinearRecurrence(n, q, p);
}
```

**poly.hpp**

md5: 8da6ee

```
struct fps {
    vm v;
    fps(const vm& v = {}) : v(v) {}
    fps(int n) : v(n) {}
    void shrink() {
        while(v.size() && !v.back().x) v.pop_back();
    }
    void resize(int n) { v.resize(n); }
    int size() const { return int(v.size()); }
    mint freq(int p) const { return (p < size()) ? v[p] : 0; }
    mint& operator[](int k) { return v[k]; }
    void emplace_back(mint x) { v.eb(x); }
    fps pre(int le) const { return {{v.begin(), v.begin() +
min(size(), le)}}; }
    fps operator-() const {
        vm res{v};
        fore(e, res) e = -e;
        return res;
    }
    fps operator+(const fps& r) const {
        auto n = max(size(), r.size());
        vm res(n);
        rep(i, n) res[i] = freq(i) + r.freq(i);
        return res;
    }
    fps operator-(const fps& r) const { return (*this) + (-r); }
    fps operator*(const fps& r) const { return {mul(v, r.v)}; }
    fps operator*(const mint& r) const {
        int n = size();
        vm res(n);
        for(int i = 0; i < n; i++) res[i] = v[i] * r;
        return res;
    }
    fps operator/(const mint& r) const { return *this * r.inv(); }
}
fps operator/(const fps& r) const {
    if(size() < r.size()) return {};
    int n = size() - r.size() + 1;
    return (rev().pre(n) * r.rev().inv(n)).pre(n).rev();
}
fps operator%(const fps& r) const { return *this - *this / r
* r; }
fps operator<<(int s) const {
    vm res(size() + s);
    rep(i, size()) res[i + s] = v[i];
    return res;
}
```

```

}
fps operator>>(int s) const {
    if(size() <= s) return fps();
    vm res(size() - s);
    rep(i, size() - s) res[i] = v[i + s];
    return res;
}
fps& operator+=(const fps& r) { return *this = *this + r; }
fps& operator-=(const fps& r) { return *this = *this - r; }
fps& operator*=(const fps& r) { return *this = *this * r; }
fps& operator*=(const mint& r) { return *this = *this * r; }
fps& operator/=(const fps& r) { return *this = *this / r; }
fps& operator/=(const mint& r) { return *this = *this / r; }
fps& operator%=(const fps& r) { return *this = *this % r; }
fps& operator<<=(int n) { return *this = *this << n; }
fps& operator>>=(int n) { return *this = *this >> n; }
fps rev(int n = -1) const {
    vm res = v;
    if(n != -1) res.resize(n);
    reverse(res.begin(), res.end());
    return res;
}
fps diff() const {
    vm res(max(0, size() - 1));
    rep(i, 1, size()) res[i - 1] = freq(i) * i;
    return res;
}
fps integ() const {
    vm res(size() + 1);
    rep(i, size()) res[i + 1] = freq(i) / (i + 1);
    return res;
}
// f * f.inv() = 1 + g(x)x^m
fps inv(int m) const {
    fps res = fps(vm{mint(1) / freq(0)});
    for(int i = 1; i < m; i *= 2) { res = (res * mint(2) - res
* res * pre(2 * i)).pre(2 * i); }
    return res.pre(m);
}
fps exp(int n) const {
    assert(freq(0).x == 0);
    fps g = fps(vm{1});
    for(int i = 1; i < n; i *= 2) { g = (g * (pre(i * 2) +
fps(vm{1}) - g.log(i * 2))).pre(i * 2); }
    return g.pre(n);
}
fps log(int n) const {
    assert(freq(0).x == 1);
    auto f = pre(n);
    return (f.diff() * f.inv(n - 1)).pre(n - 1).integ();
}
fps sqrt(int n) const {
    assert(freq(0).x == 1);
    fps f = pre(n + 1);
    fps g{{1}};
    for(int i = 1; i < n; i *= 2) { g = (g + f.pre(2 * i) *
g.inv(2 * i)) * mint((mod + 1) / 2); }
    return g.pre(n + 1);
}
fps pow(ll k, ll n) {
    if(k == 0) {
        fps res(n);
        res[0] = 1;
        return res;
    }
    rep(i, size()) {
        if((*this)[i].x) {
            mint rev = mint(1) / (*this)[i];
            fps ret = (((*this * rev) >> i).log(n) *
mint(k)).exp(n);
            ret *= (*this)[i].pow(k);
            ret = (ret << (i * k)).pre(n);
            if(ret.size() < n) ret.resize(n);
            return ret;
        }
        if(i128(i + 1) * k >= n) return fps(n);
    }
    return fps(n);
}
fps pow_mod(ll n, const fps& mod) {
    fps x = *this, r = {{1}};
    while(n) {
```

```
        if(n & 1) r = r * x % mod;
        x = x * x % mod;
        n >>= 1;
    }
    return r;
};
```

relaxed-convolution.hpp

md5: f1c765

```
struct relaxed_multiplication {
    vector<mint> f, g, h;

    // fg_prefix_ntts[d] = (NTTs of first 2^d terms of f and g)
    vector<pair<vector<mint>, vector<mint>>> fg_prefix_ntts;

    const auto& get_fg_prefix_ntt(int d) {
        while(int(fg_prefix_ntts.size()) <= d) {
            int fftlen = 1 << fg_prefix_ntts.size();
            vector<mint> vf(f.begin(), f.begin() + fftlen);
            vector<mint> vg(g.begin(), g.begin() + fftlen);
            ntt(vf, false), ntt(vg, false);
            fg_prefix_ntts.emplace_back(vf, vg);
        }
        return fg_prefix_ntts[d];
    }

    relaxed_multiplication() {}

    mint add(const mint& f_i, const mint& g_i) {
        f.push_back(f_i), g.push_back(g_i);
        const int n = f.size(), d = __builtin_ctz(n), D = 1 << d;

        if(int gsz = n - 1 + D; h.size() < gsz) h.resize(gsz);

        if(n == D) {
            // Convolve f[0, D) * g[0, D) -> h[D - 1, D * 2 - 1)

            const auto& [nttf, ntth] = get_fg_prefix_ntt(d);
            vector<mint> tmp(nttf.size());
            for(int i = 0; i < ntth.size(); ++i) tmp[i] = ntth[i] *
nttg[i];
            ntt(tmp, true);

            for(int i = 0; i < n - 1; ++i) h[n + i] += tmp[i] -
h[i]; // 回り込みを削除
            h[n - 1] += tmp[n - 1];
        } else {
            // Convolve f[0, 2 * D) * g[n - D, n) -> h[n - 1, n - 1
+ D)

            if(d <= 4) { // Bruteforce threshold
                for(int i = n - D; i < n; ++i) {
                    for(int k = n - 1; k < n - 1 + D; ++k) { h[k] +=
f[i] * g[k - i] + f[k - i] * g[i]; }
                }
            } else {
                vector<mint> tmpf{f.end() - D, f.end()},
tmpg{g.end() - D, g.end()};
                tmpf.resize(D * 2), tmpg.resize(D * 2);
                ntt(tmpf, false), ntt(tmpg, false);

                const auto& [nttf, ntth] = get_fg_prefix_ntt(d + 1);
                for(int i = 0; i < tmpf.size(); ++i) { tmpf[i] =
tmpf[i] * ntth[i] + tmpg[i] * ntth[i]; }
                ntt(tmpf, true);
                for(int i = 0; i < D; ++i) h[n - 1 + i] += tmpf[D -
1 + i];
            }
        }

        return h[n - 1];
    }
};
```

tree

block-cut-tree.hpp

md5: bf0113

```
struct extended_block_cut_tree {
    int N, cnt;
```

```
vector<vector<int>> G;
extended_block_cut_tree(vector<vector<int>>& E) {
    N = E.size();
    vector<int> next(N, -1);
    vector<int> d(N, -1);
    vector<int> imos(N, 0);
    for(int i = 0; i < N; i++) {
        if(d[i] == -1) {
            d[i] = 0;
            dfs1(E, next, d, imos, i);
        }
    }
    cnt = 0;
    G.resize(N + 1);
    vector<bool> used(N, false);
    for(int i = 0; i < N; i++) {
        if(d[i] == 0) { dfs2(E, d, imos, used, cnt, i); }
        if(E[i].empty()) {
            G[i].push_back(N + cnt);
            G[N + cnt].push_back(i);
            cnt++;
            G.push_back({});
        }
    }
    G.pop_back();

    void dfs1(vector<vector<int>>& E, vector<int>& next,
vector<int>& d, vector<int>& imos, int v) {
        for(int w : E[v]) {
            if(d[w] == -1) {
                d[w] = d[v] + 1;
                next[w] = v;
                dfs1(E, next, d, imos, w);
                imos[v] += imos[w];
            } else if(d[w] < d[v] - 1) {
                imos[v]++;
                imos[next[w]]--;
            }
        }
    }

    void dfs2(vector<vector<int>>& E, vector<int>& d,
vector<int>& imos, vector<bool>& used, int b, int v) {
        used[v] = true;
        bool ok = false;
        for(int w : E[v]) {
            if(d[w] == d[v] + 1 && !used[w]) {
                if(imos[w] > 0) {
                    if(!ok) {
                        ok = true;
                        G[v].push_back(N + b);
                        G[N + b].push_back(v);
                    }
                    dfs2(E, d, imos, used, b, w);
                } else {
                    G[v].push_back(N + cnt);
                    G[N + cnt].push_back(v);
                    cnt++;
                    G.push_back({});
                    dfs2(E, d, imos, used, cnt - 1, w);
                }
            }
        }
        if(!ok && d[v] > 0) {
            G[v].push_back(N + b);
            G[N + b].push_back(v);
        }
    }

    int size() { return G.size(); }
    vector<int>& operator[](int v) { return G[v]; }
};
```

hld.hpp

md5: fa40a1

```
template<typename G> struct HLD {
    int n;
    G& g;
    vector<int> sub, in, out, head, rev, par, d;
    HLD(G& g) : n(si(g)), g(g), sub(n), in(n), out(n), head(n),
rev(n), par(n), d(n) {}
    void dfs1(int x, int p) {
        par[x] = p;
        sub[x] = 1;
```

```
if(g[x].size() and g[x][0] == p) swap(g[x][0],
g[x].back());
fore(e, g[x]) {
    if(e == p) continue;
    d[e] = d[x] + 1;
    dfs1(e, x);
    sub[x] += sub[e];
    if(sub[g[x][0]] < sub[e]) swap(g[x][0], e);
}
}
void dfs2(int x, int p, int& t) {
    in[x] = t++;
    rev[in[x]] = x;
    fore(e, g[x]) {
        if(e == p) continue;
        head[e] = (g[x][0] == e ? head[x] : e);
        dfs2(e, x, t);
    }
    out[x] = t;
}
void build() {
    int t = 0;
    head[0] = 0;
    dfs1(0, -1);
    dfs2(0, -1, t);
}
int la(int v, int k) {
    while(1) {
        int u = head[v];
        if(in[v] - k >= in[u]) return rev[in[v] - k];
        k -= in[v] - in[u] + 1;
        v = par[u];
    }
}
int lca(int u, int v) {
    for(;; v = par[head[v]]) {
        if(in[u] > in[v]) swap(u, v);
        if(head[u] == head[v]) return u;
    }
}
template<typename T, typename Q, typename F>
T query(int u, int v, const T& e, const Q& q, const F& f,
bool edge = false) {
    T l = e, r = e;
    for(;; v = par[head[v]]) {
        if(in[u] > in[v]) swap(u, v), swap(l, r);
        if(head[u] == head[v]) break;
        l = f(q(in[head[v]], in[v] + 1), l);
    }
    return f(f(q(in[u] + edge, in[v] + 1), l), r);
}
int dist(int u, int v) { return d[u] + d[v] - 2 * d[lca(u,
v)]; }
int jump(int s, int t, int i) {
    if(!i) return s;
    int l = lca(s, t);
    int dst = d[s] + d[t] - d[l] * 2;
    if(dst < i) return -1;
    if(d[s] - d[l] >= i) return la(s, i);
    i -= d[s] - d[l];
    return la(t, d[t] - d[l] - i);
}
};
```

flow

bipartite-matching.hpp

md5: 2ffb05

```
struct Bimatch {
    vector<vi> g;
    vi d, mc, used, vv;
    Bimatch(int n, int m) : g(n), mc(m, -1), used(n) {}
    void add(int u, int v) { g[u].eb(v); }
    void bfs() {
        d.assign(si(g), -1);
        queue<int> q;
        rep(i, si(g)) {
            if(!used[i]) {
                q.emplace(i);
                d[i] = 0;
            }
        }
    }
};
```

```

    }
    while(!q.empty()) {
        int x = q.front();
        q.pop();
        fore(e, g[x]) {
            int c = mc[e];
            if(c >= 0 and d[c] == -1) {
                d[c] = d[x] + 1;
                q.emplace(c);
            }
        }
    }
}
}
bool dfs(int x) {
    vv[x] = true;
    fore(e, g[x]) {
        int c = mc[e];
        if(c < 0 or (!vv[c] and d[c] == d[x] + 1 and dfs(c))) {
            mc[e] = x;
            used[x] = true;
            return true;
        }
    }
    return false;
}
int match() {
    int ret = 0;
    while(true) {
        bfs();
        vv.assign(si(g), false);
        int f = 0;
        rep(i, si(g)) if(!used[i] and dfs(i)) f++;
        if(!f) return ret;
        ret += f;
    }
}
};
```

flow.hpp

md5: e99393

```
template<typename T> struct Dinic {
    const T INF;

    struct edge {
        int to;
        T cap;
        int rev;
        bool isrev;
        int idx;
    };

    vector<vector<edge>> g;
    vector<int> c, iter;
    Dinic(int V) : INF(numeric_limits<T>::max()), g(V) {}
    void add_edge(int from, int to, T cap, int idx = -1) {
        g[from].emplace_back((edge){to, cap, si(g[to]), false,
idx});
        g[to].emplace_back((edge){from, 0, si(g[from]) - 1, true,
idx});
    }

    bool bfs(int s, int t) {
        c.assign(si(g), -1);
        queue<int> q;
        c[s] = 0;
        q.push(s);
        while(!q.empty() && c[t] == -1) {
            int x = q.front();
            q.pop();
            fore(e, g[x]) {
                if(e.cap > 0 && c[e.to] == -1) {
                    c[e.to] = c[x] + 1;
                    q.push(e.to);
                }
            }
        }
        return c[t] != -1;
    }

    T dfs(int x, int t, T flow) {
        if(x == t) return flow;
    }
};
```

```

    for(int& i = iter[x]; i < si(g[x]); i++) {
        edge& e = g[x][i];
        if(e.cap > 0 && c[x] < c[e.to]) {
            T d = dfs(e.to, t, min(flow, e.cap));
            if(d > 0) {
                e.cap -= d;
                g[e.to][e.rev].cap += d;
                return d;
            }
        }
    }
    return 0;
}

T max_flow(int s, int t) {
    T flow = 0;
    while(bfs(s, t)) {
        iter.assign(si(g), 0);
        T f = 0;
        while((f = dfs(s, t, INF)) > 0) flow += f;
    }
    return flow;
}

// void output() {
//     for(int i = 0; i < g.size(); i++) {
//         for(auto &e : g[i]) {
//             if(e.isrev) continue;
//             auto &rev_e = g[e.to][e.rev];
//             cout << i << "->" << e.to << " (flow: " <<
rev_e.cap << "/" << e.cap + rev_e.cap << ") " << endl;
//         }
//     }
// }
};

```

## Lower-upper-bound-flow.hpp

md5: 278a5a

```

template<typename T> struct lrFlow {
    Dinic<T> flow;
    vector<T> in, up;
    int X, Y, n;
    T sum;
    typename Dinic<T>::edge *p, *q;

    lrFlow(int n) : n(n), X(n), Y(n + 1), sum(0), in(n), flow(n +
2) {}

    void add_edge(int from, int to, T low, T high) {
        flow.add_edge(from, to, high - low, si(up));
        in[from] -= low, in[to] += low;
        up.eb(high);
    }

    void build() {
        rep(i, n) {
            if(in[i] > 0) {
                flow.add_edge(X, i, in[i]);
                sum += in[i];
            } else if(in[i] < 0) {
                flow.add_edge(i, Y, -in[i]);
            }
        }
    }

    bool can_flow(int s, int t) {
        flow.add_edge(t, s, flow.INF);
        p = &flow.g[t].back();
        q = &flow.g[s].back();
        return can_flow();
    }

    bool can_flow() {
        build();
        auto ret = flow.max_flow(X, Y);
        return ret >= sum;
    }

    T max_flow(int s, int t) {
        if(can_flow(s, t)) {
            return flow.max_flow(s, t);
        } else {

```

```

            return -1;
        }
    }

    T min_flow(int s, int t) {
        if(can_flow(s, t)) {
            auto ret = flow.INF - p->cap;
            p->cap = q->cap = 0;
            return ret - flow.max_flow(t, s);
        } else {
            return -1;
        }
    }

    // void output(int M) {
    //     vector<flow_t> ans(M);
    //     for(int i = 0; i < flow.graph.size(); i++) {
    //         for(auto &e : flow.graph[i]) {
    //             if(!e.isrev && ~e.idx) ans[e.idx] = up[e.idx]
- e.cap;
    //         }
    //     }
    //     for(auto &p : ans) cout << p << endl;
    // }
};

```

## mcf.hpp

md5: 96eeaa

```

struct MCF {
    struct edge {
        int to;
        ll cap, cost;
        int rev;
        bool isrev;
    };
    vector<vector<edge>> g;
    vl pot, cost;
    vi pv, pe;
    MCF(int n) : g(n) {}
    void add(int u, int v, ll cap, ll cost) {
        g[u].eb(v, cap, cost, si(g[v]), false);
        g[v].eb(u, 0, -cost, si(g[u]) - 1, true);
    }
    ll mcf(int s, int t, ll f) {
        int n = si(g);
        ll ret = 0;
        using P = pair<ll, int>;
        priority_queue<P, vector<P>, greater<P>> pq;
        pot.assign(n, 0), pe.assign(n, -1), pv.assign(n, -1);
        while(f) {
            cost.assign(n, INFL);
            pq.emplace(0, s);
            cost[s] = 0;
            while(!pq.empty()) {
                auto [c, x] = pq.top();
                pq.pop();
                if(cost[x] < c) continue;
                rep(i, si(g[x])) {
                    edge& e = g[x][i];
                    ll ncost = cost[x] + e.cost + pot[x] - pot[e.to];
                    if(e.cap and chmin(cost[e.to], ncost)) {
                        pv[e.to] = x, pe[e.to] = i;
                        pq.emplace(cost[e.to], e.to);
                    }
                }
            }
            if(cost[t] == INFL) return -1;
            rep(i, n) pot[i] += cost[i];
            ll addflow = f;
            for(int v = t; v != s; v = pv[v]) chmin(addflow,
g[pv[v]][pe[v]].cap);
            f -= addflow;
            ret += addflow * pot[t];
            for(int v = t; v != s; v = pv[v]) {
                auto& e = g[pv[v]][pe[v]];
                e.cap -= addflow;
                g[v][e.rev].cap += addflow;
            }
        }
        return ret;
    }
};

```



```
    }  
};
```

二部グラフ.md

||サイズ|構成||最大マッチング|| $M$ |||最小点被覆|| $M$ ||L到達不可能+R到達可能||最大安定集合|| $V$ |- $|M|$ ||上の補グラフ||最小辺被覆|孤立点がないなら $|V|-|M|$ ||最大マッチング+含まれない点 greedy|

燃やす埋める.md

変形前の制約	変形後の制約
$x$ が 0 のとき $z$ 失う	$(x, T, z)$
$x$ が 0 のとき $z$ 得る	無条件で $z$ 得る; $(S, x, z)$
$x$ が 1 のとき $z$ 失う	$(S, x, z)$
$x$ が 1 のとき $z$ 得る	無条件で $z$ 得る; $(x, T, z)$
$x, y, \dots$ がすべて 0 のとき $z$ 得る	無条件で $z$ 得る; $(S, w, z), (w, x, \infty), (w, y, \infty)$
$x, y, \dots$ がすべて 1 のとき $z$ 得る	無条件で $z$ 得る; $(w, T, z), (x, w, \infty), (y, w, \infty)$

string

KMP.hpp

md5: 886c63

```
// kmp[i] := max{ l ≤ i | s[:l] == s[(i+1)-l:i+1] }  
// abacaba -> 0010123  
auto KMP(string s) {  
    vector<ll> p(sz(s));  
    rep(i, 1, sz(s)) {  
        ll g = p[i - 1];  
        while(g && s[i] != s[g]) g = p[g - 1];  
        p[i] = g + (s[i] == s[g]);  
    }  
    return p;  
}
```

Manacher.hpp

md5: 5882fb

```
// 各位置での回文半径を求める  
// aaabaaa -> 1214121  
// 偶数長の回文を含めて直径を知るには、N+1 個の $ を挿入して 1 を引く  
// $a$a$a$b$a$a$a$ -> 123432181234321  
auto manacher(string s) {  
    ll n = sz(s), i = 0, j = 0;  
    vector<ll> r(n);  
    while(i < n) {  
        while(i >= j && i + j < n && s[i - j] == s[i + j]) j++;  
        r[i] = j;  
        ll k = 1;  
        while(i >= k && i + k < n && k + r[i - k] < j) {  
            r[i + k] = r[i - k];  
            k++;  
        }  
        i += k, j -= k;  
    }  
    return r;  
}
```

RollingHash.hpp

md5: b0e4a8

```
const ll mod = (1LL << 61) - 1;  
ll add(ll a, ll b) { return (a += b) >= mod ? a - mod : a; }  
ll mul(ll a, ll b) {  
    i128 c = (i128)a * b;  
    return add(c >> 61, c & mod);  
}  
ll r = 7954398468495;  
struct RH {  
    ll n;  
    vl hs, pw;  
    RH(string s) : n(si(s)), hs(n + 1), pw(n + 1, 1) {
```

```
        rep(i, n) {  
            pw[i + 1] = mul(pw[i], r);  
            hs[i + 1] = add(mul(hs[i], r), s[i]);  
        }  
    }  
    ll get(ll l, ll r) const { return add(hs[r], mod - mul(hs[l], pw[r - l])); }  
    int lcp(int i, int j) {  
        int ok = 0, ng = min(n - i, n - j) + 1;  
        while(ok < ng - 1) {  
            int mid = ok + ng >> 1;  
            (get(i, i + mid) == get(j, j + mid) ? ok : ng) = mid;  
        }  
        return ok;  
    }  
};
```

SuffixArray.hpp

md5: deae26

```
// returns pair{sa, lcp}  
// sa 長さ n : s[sa[0]:] < s[sa[1]:] < ... < s[sa[n-1]:]  
// lcp 長さ n-1 : lcp[i] = LCP(s[sa[i]:], s[sa[i+1]:])  
auto SA(string s) {  
    ll n = si(s) + 1, lim = 256;  
    // assert(lim > ranges::max(s));  
    vector<ll> sa(n), lcp(n), x(all(s) + 1), y(n), ws(max(n, lim)), rk(n);  
    iota(all(sa), 0);  
    for(ll j = 0, p = 0; p < n; j = max(1LL, j * 2), lim = p) {  
        p = j;  
        iota(all(y), n - j);  
        rep(i, 0, n) if(sa[i] >= j) y[p++] = sa[i] - j;  
        fill(all(ws), 0);  
        rep(i, 0, n) ws[x[i]]++;  
        rep(i, 1, lim) ws[i] += ws[i - 1];  
        for(ll i = n; i--;) sa[--ws[x[y[i]]]] = y[i];  
        swap(x, y);  
        p = 1;  
        x[sa[0]] = 0;  
        rep(i, 1, n) {  
            ll a = sa[i - 1], b = sa[i];  
            x[b] = (y[a] == y[b] && y[a + j] == y[b + j]) ? p - 1 : p++;  
        }  
        rep(i, 1, n) rk[sa[i]] = i;  
        for(ll i = 0, k = 0; i < n - 1; lcp[rk[i++]] = k) {  
            if(k) k--;  
            while(s[i + k] == s[sa[rk[i] - 1] + k]) k++;  
        }  
        sa.erase(begin(sa));  
        lcp.erase(begin(lcp));  
        return pair{sa, lcp};  
    }  
}
```

Zalgorithm.hpp

md5: d3bdba

```
template<typename T> vi z_algorithm(const vector<T>& s) {  
    int n = si(s), l = -1, r = -1;  
    vi z(n, n);  
    rep(i, 1, n) {  
        int& x = z[i] = i < r ? min<ll>(r - i, z[i - l]) : 0;  
        while(i + x < n and s[i + x] == s[x]) x++;  
        if(i + x > r) l = i, r = i + x;  
    }  
    return z;  
}
```

enumerate-runs.hpp

md5: aec96b

```
// (length, l, r)  
template<typename T> vector<array<int, 3>> enum_runs(const vector<T>& s) {  
    int n = si(s);  
    vector<array<int, 3>> res;  
    auto dfs = [&](auto&& f, int l, int r) -> void {  
        if(r - l <= 1) return;  
        int m = l + r >> 1;  
        f(f, l, m), f(f, m, r);  
        vector<T> sl(s.rbegin() + n - m, s.rbegin() + n - l);
```



```
sl.insert(sl.end(), s.rbegin() + n - r, s.rbegin() + n -
l);
vector<T> sr(s.begin() + m, s.begin() + r);
sr.insert(sr.end(), s.begin() + l, s.begin() + r);
auto zsl = z_algorithm(sl), zsr = z_algorithm(sr);
rep(t, 1, m - l + 1) {
    int ml = max<ll>(l, m - t - zsl[t]), mr = min(r, m +
zsr[r - l - t]);
    if(mr - ml >= 2 * t and (ml == 0 or s[ml - 1] != s[ml +
t - 1]) and (mr == n or s[mr] != s[mr - t]))
        res.push_back({ml, mr, t});
}
for(int t = 1; t <= r - m; t++) {
    int ml = max(l, m - zsl[r - l - t]), mr = min(r, m + t
+ zsr[t]);
    if(mr - ml >= 2 * t and (ml == 0 or s[ml - 1] != s[ml +
t - 1]) and (mr == n or s[mr] != s[mr - t]))
        res.push_back({ml, mr, t});
}
};
dfs(dfs, 0, n);
sort(all(res));
vector<array<int, 3>> nres;
int pl = -1, pr = -1;
for(auto [l, r, t] : res) {
    if(l == pl and r == pr) continue;
    pl = l, pr = r;
    nres.push_back({t, l, r});
}
return nres;
}
```

geometry

argument-sort.hpp

md5: 26b1fa

```
bool operator<(point P, point Q) {
    long long C = cross(P, Q);
    if(C == 0 && dot(P, Q) > 0) {
        return false;
    } else if(P.x < 0 && P.y == 0) {
        return true;
    } else if(Q.x < 0 && Q.y == 0) {
        return false;
    } else if(P.y * Q.y <= 0) {
        return P.y < Q.y;
    } else {
        return C > 0;
    }
}
```

circle.hpp

md5: 514ea6

```
struct circle {
    point C;
    double r;
    circle() {}
    circle(point C, double r) : C(C), r(r) {}
};
pair<point, point> line_circle_intersection(line L, circle C) {
    point P = projection(C.C, L);
    double d = point_line_distance(C.C, L);
    double h = sqrt(C.r * C.r - d * d);
    point A = P + vec(L) / abs(vec(L)) * h;
    point B = P - vec(L) / abs(vec(L)) * h;
    return make_pair(A, B);
}
pair<point, point> circle_intersection(circle C1, circle C2) {
    double d = dist(C1.C, C2.C);
    double m = (C1.r * C1.r - C2.r * C2.r + d * d) / (d * 2);
    point M = C1.C + (C2.C - C1.C) / d * m;
    double h = sqrt(C1.r * C1.r - m * m);
    point H = rotate90(C2.C - C1.C) / d * h;
    return make_pair(M - H, M + H);
}
pair<point, point> circle_tangent(point P, circle C) {
    double d = dist(P, C.C);
    double r = sqrt(d * d - C.r * C.r);
    return circle_intersection(C, circle(P, r));
}
vector<line> common_tangent(circle C1, circle C2) {
```

```
if(C1.r < C2.r) { swap(C1, C2); }
double d = dist(C1.C, C2.C);
vector<line> L;
if(C1.r - C2.r <= d + eps) {
    if(C1.r - C2.r <= eps) {
        point D = rotate90(C2.C - C1.C) / d * C1.r;
        L.push_back(line(C1.C + D, C2.C + D));
        L.push_back(line(C1.C - D, C2.C - D));
    } else {
        double m = (C1.r - C2.r) * (C1.r - C2.r) / d;
        point M = C1.C + (C2.C - C1.C) / d * m;
        double h = sqrt((C1.r - C2.r) * (C1.r - C2.r) - m * m);
        point H1 = M + rotate90(C2.C - C1.C) / d * h;
        point D1 = (H1 - C1.C) / dist(H1, C1.C) * C2.r;
        L.push_back(line(H1 + D1, C2.C + D1));
        point H2 = M - rotate90(C2.C - C1.C) / d * h;
        point D2 = (H2 - C1.C) / dist(H2, C1.C) * C2.r;
        L.push_back(line(H2 + D2, C2.C + D2));
    }
}
if(C1.r + C2.r <= d + eps) {
    double m = (C1.r + C2.r) * (C1.r + C2.r) / d;
    point M = C1.C + (C2.C - C1.C) / d * m;
    double h = sqrt((C1.r + C2.r) * (C1.r + C2.r) - m * m);
    point H1 = M + rotate90(C2.C - C1.C) / d * h;
    point D1 = (H1 - C1.C) / dist(H1, C1.C) * C2.r;
    L.push_back(line(H1 - D1, C2.C - D1));
    point H2 = M - rotate90(C2.C - C1.C) / d * h;
    point D2 = (H2 - C1.C) / dist(H2, C1.C) * C2.r;
    L.push_back(line(H2 - D2, C2.C - D2));
}
return L;
}
```

convex-hull.hpp

md5: 7b7e26

```
Points convex_hull(Points& p) {
    int n = p.size(), k = 0;
    if(n <= 2) return p;
    sort(begin(p), end(p), [](pt x, pt y) { return (x.x != y.x ?
x.x < y.x : x.y < y.y); });
    Points ch(2 * n);
    for(int i = 0; i < n; ch[k++] = p[i++]) {
        while(k >= 2 && cross(ch[k - 1] - ch[k - 2], p[i] - ch[k -
1]) <= 0) --k;
    }
    for(int i = n - 2, t = k + 1; i >= 0; ch[k++] = p[i--]) {
        while(k >= t && cross(ch[k - 1] - ch[k - 2], p[i] - ch[k -
1]) <= 0) --k;
    }
    ch.resize(k - 1);
    return ch;
}
```

funcs.hpp

md5: 19bea4

```
int contains(const Polygon& Q, const Point& p) {
    bool in = false;
    for(int i = 0; i < Q.size(); i++) {
        Point a = Q[i] - p, b = Q[(i + 1) % Q.size()] - p;
        if(a.y > b.y) swap(a, b);
        if(a.y <= 0 && 0 < b.y && cross(a, b) < 0) in = !in;
        if(cross(a, b) == 0 && dot(a, b) <= 0) return _ON;
    }
    return in ? _IN : _OUT;
}

Polygon Minkowski_sum(const Polygon& P, const Polygon& Q) {
    vector<Segment> e1(P.size()), e2(Q.size()), ed(P.size() +
Q.size());
    const auto cmp = [](const Segment& u, const Segment& v) {
return (u.b - u.a).arg_cmp(v.b - v.a); };
    rep(i, P.size()) e1[i] = {P[i], P[(i + 1) % P.size()]};
    rep(i, Q.size()) e2[i] = {Q[i], Q[(i + 1) % Q.size()]};
    rotate(begin(e1), min_element(all(e1), cmp), end(e1));
    rotate(begin(e2), min_element(all(e2), cmp), end(e2));
    merge(all(e1), all(e2), begin(ed), cmp);
    const auto check = [](const Points& res, const Point& u) {
        const auto back1 = res.back(), back2 = *prev(end(res), 2);
        return eq(cross(back1 - back2, u - back2), eps) and
dot(back1 - back2, u - back1) >= -eps;
    };
}
```

```

    auto u = e1[0].a + e2[0].a;
    Points res{u};
    res.reserve(P.size() + Q.size());
    for(const auto& v : ed) {
        u = u + v.b - v.a;
        while(si(res) >= 2 and check(res, u)) res.pop_back();
        res.eb(u);
    }
    if(res.size() and check(res, res[0])) res.pop_back();
    return res;
}

// -1 : on, 0 : out, 1 : in
// 0(log(n))
bool is_in(const Polygon& p, const Point& a) {
    if(p.size() == 1) return a == p[0] ? -1 : 0;
    if(p.size() == 2) return intersect(Segment(p[0], p[1]), a);
    if(a == p[0]) return -1;
    if((p[1] - p[0]).toleft(a - p[0]) == -1 || (p.back() - p[0]).toleft(a - p[0]) == 1) return 0;
    const auto cmp = [&](const Point& u, const Point& v) { return (u - p[0]).toleft(v - p[0]) == 1; };
    const size_t i = lower_bound(p.begin() + 1, p.end(), a, cmp) - p.begin();
    if(i == 1) return intersect(Segment(p[0], p[i]), a) ? -1 : 0;
    if(i == p.size() - 1 && intersect(Segment(p[0], p[i]), a)) return -1;
    return -1;
    if(intersect(Segment(p[i - 1], p[i]), a)) return -1;
    return (p[i] - p[i - 1]).toleft(a - p[i - 1]) > 0;
}

using speP = pair<ld, int>;
struct ccut {
private:
    set<speP> ags;
    vector<int> nexs;
    vector<int> pres;
    vector<Point> ps;

public:
    void init() {
        const ld sup = -100000;
        ps.push_back({-sup, -sup});
        ps.push_back({sup, -sup});
        ps.push_back({sup, sup});
        ps.push_back({-sup, sup});
        nexs.resize(4);
        pres.resize(4);
        rep(i, 4) {
            int ni = (i + 1) % 4;
            Point dif = ps[ni] - ps[i];
            ld t = arg(dif);
            ags.insert({t, i});
            nexs[i] = ni;
            pres[ni] = i;
        }
    }
    void convex_cut(Point a, Point b) {
        if(ags.empty()) return;
        Point dif = b - a;
        ld t = arg(dif);
        auto itr = ags.lower_bound({t, -1});
        if(itr == ags.end()) itr = ags.begin();
        int cur = (*itr).second;
        if(ccw(a, b, ps[cur]) != -1) return;
        int ricur = nexs[cur];
        while(ricur != cur && ccw(a, b, ps[ricur]) != 1) { ricur = nexs[ricur]; }
        if(ricur == cur) {
            ags.clear();
            return;
        }
        int lecur = pres[cur];
        while(ccw(a, b, ps[lecur]) != 1) { lecur = pres[lecur]; }
        // new point
        Line l = {a, b};
        Line l1 = {ps[lecur], ps[nexs[lecur]]};
        Line l2 = {ps[pres[ricur]], ps[ricur]};
        Point p1 = is_ll(l1, l);
        Point p2 = is_ll(l2, l);
        int id1 = ps.size();
        int id2 = ps.size() + 1;

```

```

        ps.push_back(p1), ps.push_back(p2);
        rep(2) nexs.push_back(-1), pres.push_back(-1);

        // erase(lecur,ricur)
        cur = lecur;
        int tmp = 0;
        while(cur != ricur || !tmp) {
            Point dif = ps[nexs[cur]] - ps[cur];
            ld t = arg(dif);
            ags.erase({t, cur});
            cur = nexs[cur];
            tmp++;
        }

        nexs[lecur] = id1, pres[id1] = lecur, nexs[id1] = id2;
        pres[id2] = id1, nexs[id2] = ricur, pres[ricur] = id2;
        cur = lecur, tmp = 0;
        while(cur != ricur || !tmp) {
            Point dif = ps[nexs[cur]] - ps[cur];
            ld t = arg(dif);
            ags.insert({t, cur});
            cur = nexs[cur];
            tmp++;
        }
    }
    polygon nw_poly() {
        polygon nw;
        for(auto p : ags) nw.push_back(ps[p.second]);
        return nw;
    }
    ld calc_area() {
        polygon nw;
        for(auto p : ags) nw.push_back(ps[p.second]);
        return area(nw);
    }
};

```

## line.hpp

md5: 447fab

```

bool point_on_segment(point P, line L) { return dot(P - L.A, vec(L)) > -eps && dot(P - L.B, vec(L)) < eps; }
point projection(point P, line L) { return L.A + vec(L) / abs(vec(L)) * dot(P - L.A, vec(L)) / abs(vec(L)); }
point reflection(point P, line L) { return projection(P, L) * 2 - P; }
double point_line_distance(point P, line L) { return abs(cross(P - L.A, vec(L))) / abs(vec(L)); }
double point_segment_distance(point P, line L) {
    if(dot(P - L.A, vec(L)) < 0) {
        return dist(P, L.A);
    } else if(dot(P - L.B, vec(L)) > 0) {
        return dist(P, L.B);
    } else {
        return point_line_distance(P, L);
    }
}
bool is_parallel(line L1, line L2) { return abs(cross(vec(L1), vec(L2))) < eps; }
point line_intersection(line L1, line L2) {
    return L1.A + vec(L1) * cross(L2.A - L1.A, vec(L2)) / cross(vec(L1), vec(L2));
}
bool segment_intersect(line L1, line L2) {
    return cross(L1.A - L2.A, vec(L2)) * cross(L1.B - L2.A, vec(L2)) < eps
        && cross(L2.A - L1.A, vec(L1)) * cross(L2.B - L1.A, vec(L1)) < eps;
}
double segment_distance(line L1, line L2) {
    if(segment_intersect(L1, L2)) {
        return 0;
    } else {
        double ans = INF;
        ans = min(ans, point_segment_distance(L1.A, L2));
        ans = min(ans, point_segment_distance(L1.B, L2));
        ans = min(ans, point_segment_distance(L2.A, L1));
        ans = min(ans, point_segment_distance(L2.B, L1));
        return ans;
    }
}

```

## misc

## clock.hpp

md5: a1f32c

```

struct Timer {
    C::time_point c;
#define C chrono::high_resolution_clock
    Timer() : c(C::now()) {}
    long long elapsed() {
        auto d = C::now();
        return chrono::duration_cast<chrono::milliseconds>(d -
c).count();
    }
#undef C
};

```

## simplex.hpp

md5: 644ba1

```

template<typename F = double, int DEPS = 30, bool Randomize =
true> struct Simplex {
    const F EPS = F(1.0) / (1LL << DEPS);
    int n, m;
    vi shuffle_idx;
    vi idx;
    vector<vector<F>> mat;
    int i_ch, j_ch;

private:
    void _initialize(const vector<vector<F>>& A, const vector<F>&
b, const vector<F>& c) {
        n = c.size(), m = A.size();

        mat.assign(m + 2, vector<F>(n + 2));
        i_ch = m;
        rep(i, m) {
            rep(j, n) mat[i][j] = -A[i][j];
            mat[i][n] = 1, mat[i][n + 1] = b[i];
            if(mat[i_ch][n + 1] > mat[i][n + 1]) i_ch = i;
        }
        rep(j, n) mat[m][j] = c[j];
        mat[m + 1][n] = -1;

        idx.resize(n + m + 1);
        iota(idx.begin(), idx.end(), 0);
    }

    inline F abs_(F x) noexcept { return x > -x ? x : -x; }
    void _solve() {
        vi jupd;
        for(nb_iter = 0, j_ch = n;; nb_iter++) {
            if(i_ch < m) {
                swap(idx[j_ch], idx[i_ch + n + 1]);
                mat[i_ch][j_ch] = F(1) / mat[i_ch][j_ch];
                jupd.clear();
                rep(j, n + 2) {
                    if(j != j_ch) {
                        mat[i_ch][j] *= -mat[i_ch][j_ch];
                        if(abs_(mat[i_ch][j]) > EPS)
jupd.push_back(j);
                    }
                }
            }
            rep(i, m + 2) {
                if(abs_(mat[i][j_ch]) < EPS or i == i_ch)
continue;
                fore(j, jupd) mat[i][j] += mat[i][j_ch] *
mat[i][j_ch];
                mat[i][j_ch] *= mat[i_ch][j_ch];
            }

            j_ch = -1;
            rep(j, n + 1) {
                if(j_ch < 0 or idx[j_ch] > idx[j]) {
                    if(mat[m + 1][j] > EPS or (abs_(mat[m + 1][j]) <
EPS and mat[m][j] > EPS)) j_ch = j;
                }
            }
            if(j_ch < 0) break;

            i_ch = -1;

```

```

        rep(i, m) {
            if(mat[i][j_ch] < -EPS) {
                if(i_ch < 0) {
                    i_ch = i;
                } else if(mat[i_ch][n + 1] / mat[i_ch][j_ch] -
mat[i][n + 1] / mat[i][j_ch] < -EPS) {
                    i_ch = i;
                } else if(mat[i_ch][n + 1] / mat[i_ch][j_ch] -
mat[i][n + 1] / mat[i][j_ch] < EPS
and idx[i_ch] > idx[i]) {
                    i_ch = i;
                }
            }
        }
        if(i_ch < 0) {
            is_infty = true;
            break;
        }
    }
    if(mat[m + 1][n + 1] < -EPS) {
        infeasible = true;
        return;
    }
    x.assign(n, 0);
    rep(i, m) {
        if(idx[n + 1 + i] < n) x[idx[n + 1 + i]] = mat[i][n +
1];
    }
    ans = mat[m][n + 1];
}

public:
    Simplex(vector<vector<F>> A, vector<F> b, vector<F> c) {
        is_infty = infeasible = false;

        if(Randomize) {
            mt19937
rng(chrono::steady_clock::now().time_since_epoch().count());

            vector<pair<vector<F>, F>> Abs;
            rep(i, si(A)) Abs.emplace_back(A[i], b[i]);
            shuffle(Abs.begin(), Abs.end(), rng);
            A.clear(), b.clear();
            fore(Ab, Abs) A.emplace_back(Ab.first,
b.emplace_back(Ab.second);

            shuffle_idx.resize(c.size());
            iota(all(shuffle_idx), 0);
            shuffle(all(shuffle_idx), rng);
            auto Atmp = A;
            auto ctmp = c;
            rep(i, si(A)) rep(j, si(A[i])) A[i][j] = Atmp[i]
[shuffle_idx[j]];
            rep(j, si(c)) c[j] = ctmp[shuffle_idx[j]];
        }

        _initialize(A, b, c);
        _solve();

        if(Randomize and x.size() == c.size()) {
            auto xtmp = x;
            rep(j, si(c)) x[shuffle_idx[j]] = xtmp[j];
        }
    }
    unsigned nb_iter;
    bool is_infty;
    bool infeasible;
    vector<F> x;
    F ans;

    static void dual(vector<vector<F>>& A, vector<F>& b,
vector<F>& c) {
        const int n = b.size(), m = c.size();
        vector<vector<F>> At(m, vector<F>(n));
        rep(i, n) rep(j, m) At[j][i] = -A[i][j];
        A = At;
        rep(i, n) b[i] = -b[i];
        rep(j, m) c[j] = -c[j];
        b.swap(c);
    }
};

```

memo

Primes.md

素数の個数

<i>n</i>	10 <sup>2</sup>	10 <sup>3</sup>	10 <sup>4</sup>	10 <sup>5</sup>	10 <sup>6</sup>	10 <sup>7</sup>	10 <sup>8</sup>	10 <sup>9</sup>	10 <sup>10</sup>
<i>π</i> ( <i>n</i> )	25	168	1229	9592	78498	664579	5.76e+6	5.08e+7	4.55e+8

高度合成数

$\leq n$	$10^3$	$10^4$	$10^5$	$10^6$	$10^7$	$10^8$	$10^9$		
$x$	840	7560	83160	720720	8648640	73513440	735134400		
$d^0(x)$	32	64	128	240	448	768	1344		
$\leq n$	$10^{10}$	$10^{11}$	$10^{12}$	$10^{13}$	$10^{14}$	$10^{15}$	$10^{16}$	$10^{17}$	$10^{18}$
$d^0(x)$	2304	4032	6720	10752	17280	26880	41472	64512	103680

素数階乗

<i>n</i>	2	3	5	7	11	13	17	19	23	29
<i>n</i> #	2	6	30	210	2310	30030	510510	9.70e+6	2.23e+8	6.47e+9

階乗

4!	5!	6!	7!	8!	9!	10!	11!	12!	13!
24	120	720	5040	40320	362880	3.63e+6	3.99e+7	4.79e+8	6.23e+9

math.md

二項係数

n\k	0	1	2	3	4	5	6	7	8	9	10
0	1										
1	1	1									
2	1	2	1								
3	1	3	3	1							
4	1	4	6	4	1						
5	1	5	10	10	5	1					
6	1	6	15	20	15	6	1				
7	1	7	21	35	35	21	7	1			
8	1	8	28	56	70	56	28	8	1		
9	1	9	36	84	126	126	84	36	9	1	
10	1	10	45	120	210	252	210	120	45	10	1
11	1	11	55	165	330	462	462	330	165	55	11
12	1	12	66	220	495	792	924	792	495	220	66
13	1	13	78	286	715	1287	1a716	1716	1287	715	286
14	1	14	91	364	1001	2002	3003	3432	3003	2002	1001
15	1	15	105	455	1365	3003	5005	6435	6435	5005	3003
16	1	16	120	560	1820	4368	8008	11440	12870	11440	8008
17	1	17	136	680	2380	6188	12376	19448	24310	24310	19448
18	1	18	153	816	3060	8568	18564	31824	43758	48620	43758
19	1	19	171	969	3876	11628	27132	50388	75582	92378	92378
20	1	20	190	1140	4845	15504	38760	77520	125970	167960	184756

$$\binom{n}{k} = \binom{n-1}{k-1} + \binom{n-1}{k} \quad \binom{n}{k} = \frac{n}{k} \binom{n-1}{k-1} \quad \binom{L}{k} + \cdots + \binom{R-1}{k} = \binom{R}{k+1} - \binom{L}{k+1}$$

第一種スターリング数

*c*(*n*,*k*): 1, 2, ..., *n* の順列で巡回置換 *k* 個に分割できるものの個数

<i>n</i> \ <i>k</i>	0	1	2	3	4	5	6	7
0	1							
1	0	1						
2	0	1	1					
3	0	2	3	1				
4	0	6	11	6	1			
5	0	24	50	35	10	1		
6	0	120	274	225	85	15	1	
7	0	720	1764	1624	735	175	21	1

$$c(n,k) = c(n-1,k-1) + (n-1)c(n-1,k)$$
$$x(x+1)\ldots(x+n-1) = \sum_{k=0}^n c(n,k)x^k \quad \sum_{k=0}^n c(n,k) = n!$$
$$\sum_{k=0}^n 2^k c(n,k) = (n+1)! \quad \sum_{k=0}^n (-1)^k c(n,k) = 0$$

$\sum_{k=0}^n c(n,k)x^k = x(x+1)\ldots(x+n-1)$  を用いて分割統治し, 片方の計算を polynomial taylor shift で再利用すると,  $c(N,k)$  の *k* に関する列挙が *O*(*N* log *N*) 時間で行える。

第二種スターリング数

*S*(*n*,*k*): 1, 2, ..., *n* を *k* 個の区別しない集合に分割する方法の数

<i>n</i> \ <i>k</i>	0	1	2	3	4	5	6	7
0	1							
1	0	1						
2	0	1	1					
3	0	1	3	1				
4	0	1	7	6	1			
5	0	1	15	25	10	1		
6	0	1	31	90	65	15	1	
7	0	1	63	301	350	140	21	1

$$S(n,k) = S(n-1,k-1) + kS(n-1,k)$$
$$x^n = \sum_{k=0}^n S(n,k)x(x-1)\ldots(x-k+1)$$
$$S(n,k) = \frac{1}{k!} \sum_{m=1}^k (-1)^{k-m} \binom{k}{m} m^n$$

最後の式と畳み込みを使うと *S*(*N*,*k*) の *k* に関する列挙が *O*(*N* log *N*) 時間で行える。

ベル数

*B*<sub>*n*</sub>: 1, 2, ..., *n* をいくつかの集合に分割する方法の数

<i>n</i>	0	1	2	3	4	5	6	7	8	9	10
<i>B</i> <sub><i>n</i></sub>	1	1	2	5	15	52	203	877	4140	21147	115975

$$B_{n+1} = \sum_{k=0}^n \binom{n}{k} B_k \quad B_n = \frac{1}{e} \sum_{k=0}^{\infty} \frac{k^n}{k!}$$

指数型母関数 exp(exp *x* − 1) =  $\sum_{n=0}^{\infty} B_n \frac{x^n}{n!}$  を使うと *B*<sub>0</sub>, *B*<sub>1</sub>, ..., *B*<sub>*n*</sub> の計算が *O*(*N* log *N*) で行える。

カタラン数

*C*<sub>*n*</sub>: *n* 個の ( と ) を括弧列になるように並べる方法の数

<i>n</i>	0	1	2	3	4	5	6	7	8	9	10
<i>C</i> <sub><i>n</i></sub>	1	1	2	5	14	42	132	429	1430	4862	16796

$$C_n = \frac{1}{n+1} \binom{2n}{n} = \frac{(2n)!}{(n+1)!n!} \quad C_{n+1} = \frac{2(2n+1)}{n+2} C_n \quad C_{n+1} = \sum_{k=0}^n C_k C_{n-k}$$

モンモール数

*a*<sub>*n*</sub>: 1, 2, ..., *n* の順列 *P* で *P*<sub>*i*</sub> ≠ *i* となるものの個数

$a_n = (n-1)(a_{n-1} + a_{n-2}) \ a_n = na_{n-1} + (-1)^n$

分割数

$P_n$ :  $n$  を正の整数の和として表す方法の数

$n$	0	1	2	3	4	5	6	7	8	9	10
$P_n$	1	1	2	3	5	7	11	15	22	30	42

母関数は  $\prod_{n=1}^{\infty} \frac{1}{1-x^n} = \sum_{n=0}^{\infty} P_n x^n$  である. 五角数定理より  $\prod_{n=1}^{\infty} (1-x^n) = \sum_{n=-\infty}^{\infty} (-1)^n x^{n(3n+1)/2}$  なので,  $P_0, P_1, \dots, P_N$  を  $O(N \log N)$  時間で列挙できる.

母関数

$\frac{1}{1-x} = 1 + x + x^2 + x^3 + x^4 + \cdots = \sum_{n=0}^{\infty} x^n$

$\frac{1}{(1-x)^2} = 1 + 2x + 3x^2 + 4x^3 + 5x^4 + \cdots = \sum_{n=0}^{\infty} (n+1)x^n$

$\frac{1}{(1-x)^3} = 1 + 3x + 6x^2 + 10x^3 + 15x^4 + \cdots = \sum_{n=0}^{\infty} \frac{1}{2}(n+1)(n+2)x^n$

$\frac{1}{(1-x)^d} = \sum_{n=0}^{\infty} \binom{n+d-1}{n} x^n$

$\sqrt{1-x} = 1 - \frac{1}{2}x - \frac{1}{8}x^2 - \frac{1}{16}x^3 - \frac{5}{128}x^4 - \cdots = 1 - \sum_{n=1}^{\infty} \frac{(2n-2)!}{2^{2n-1}n!(n-1)!} x^n$

$\frac{1}{\sqrt{1-x}} = 1 + \frac{1}{2}x + \frac{3}{8}x^2 + \frac{5}{16}x^3 + \frac{35}{128}x^4 - \cdots = \sum_{n=0}^{\infty} \frac{(2n)!}{4^n n!} x^n$

$\frac{1-\sqrt{1-4x}}{2x} = 1 + x + 2x^2 + 5x^3 + 14x^4 + \cdots = \sum_{n=0}^{\infty} C_n x^n = \sum_{n=0}^{\infty} \frac{(2n)!}{(n+1)!n!} x^n$

(カタラン数)

$\frac{1}{\sqrt{1-4x}} = \sum_{n=0}^{\infty} \binom{2n}{n} x^n$

$\frac{1}{1-x-x^2} = 1 + x + 2x^2 + 3x^3 + 5x^4 + \cdots = \sum_{n=0}^{\infty} F_n x^n$  (フィボナッチ数)

$\log(1-x) = -x - \frac{1}{2}x^2 - \frac{1}{3}x^3 - \frac{1}{4}x^4 - \cdots = \sum_{n=1}^{\infty} \frac{1}{n} x^n$

$\exp(\exp x - 1) = \sum_{n=0}^{\infty} B_n \frac{x^n}{n!}$  (ベル数)

$\frac{1}{k} (\exp x - 1)^k = \sum_{n=0}^{\infty} S(n, k) \frac{x^n}{n!}$  (第二種スターリング数)

$\frac{\exp(-x)}{1-x} = 1 + \frac{1}{2}x^2 + \frac{1}{3}x^3 + \frac{3}{8}x^4 + \cdots = \sum_{n=0}^{\infty} a_n \frac{x^n}{n!}$  (モンモール数)

$C(x)^k = \left(\frac{1-\sqrt{1-4x}}{2x}\right)^k = \sum_{n=0}^{\infty} \frac{k}{n+k} \binom{2n+k-1}{n} \text{ (カタラン数の母関数の累乗)}$

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