

ICPC Notebook

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template

hash.sh

使い方: sh hash.sh -> コピペ -> Ctrl + D
コメント・空白・改行を削除して md5 でハッシュする
g++ -dD -E -P -fpreprocessed - | tr -d '[:space:]' | md5sum | cut -c-6

settings.sh

Clion の設定
Settings → Build → CMake → Reload CMake Project
add_compile_options(-D_GLIBCXX_DEBUG)
Caps Lock を Ctrl に変更
setxkbmap -option ctrl:nocaps

template.hpp

md5: 136d85

#include <bits/stdc++.h>
using namespace std;
using ll = long long;
const ll INF = LLONG_MAX / 4;
#define rep(i, a, b) for(ll i = a; i < (b); i++)
#define all(a) begin(a), end(a)
#define sz(a) ssize(a)
bool chmin(auto& a, auto b) { return a > b ? a = b, 1 : 0; }
bool chmax(auto& a, auto b) { return a < b ? a = b, 1 : 0; }

int main() {
cin.tie(0)->sync_with_stdio(0);
// your code here...
}

data-structure

BIT.hpp

md5: 8133c8

struct BIT {
vector<ll> a;
BIT(ll n) : a(n + 1) {}
void add(ll i, ll x) { // A[i] += x
i++;
while(i < sz(a)) {
a[i] += x;
i += i & -i;
}
}
ll sum(ll r) {
ll s = 0;
while(r) {
s += a[r];
r -= r & -r;
}
return s;
}
ll sum(ll l, ll r) { // sum of A[l, r)
return sum(r) - sum(l);
}
};

FastSet.hpp

md5: 2cb8c9

// using u64 = uint64_t;
const u64 B = 64;
struct FastSet {
u64 n;
vector<vector<u64>> a;
FastSet(u64 n_) : n(n_) {
do a.emplace_back(n_ = (n_ + B - 1) / B);
while(n_ > 1);
}
// bool operator[](ll i) const { return a[0][i / B] >> (i % B) & 1; }
void set(ll i) {
for(auto& v : a) {
v[i / B] |= 1ULL << (i % B);
i /= B;
}
}

```

    }
    void reset(ll i) {
        for(auto& v : a) {
            v[i / B] &= ~(1ULL << (i % B));
            if(v[i / B]) break;
            i /= B;
        }
    }
    ll next(ll i) { // i を超える最小の要素
        rep(h, 0, sz(a)) {
            i++;
            if(i / B >= sz(a[h])) break;
            u64 d = a[h][i / B] >> (i % B);
            if(d) {
                i += countr_zero(d);
                while(h--) i = i * B + countr_zero(a[h][i]);
                return i;
            }
            i /= B;
        }
        return n;
    }
    ll prev(ll i) { // i より小さい最大の要素
        rep(h, 0, sz(a)) {
            i--;
            if(i < 0) break;
            u64 d = a[h][i / B] << (~i % B);
            if(d) {
                i -= countl_zero(d);
                while(h--) i = i * B + __lg(a[h][i]);
                return i;
            }
            i /= B;
        }
        return -1;
    }
};

```

SortedSet.py

```

# https://github.com/tatyam-
prime/SortedSet/blob/main/SortedSet.py
import math
from bisect import bisect_left, bisect_right
from typing import Generic, Iterable, Iterator, List, Tuple,
TypeVar, Optional
T = TypeVar('T')

class SortedSet(Generic[T]):
    BUCKET_RATIO = 16
    SPLIT_RATIO = 24

    def __init__(self, a: Iterable[T] = []) -> None:
        "Make a new SortedSet from iterable. / O(N) if sorted
        and unique / O(N log N)"
        a = list(a)
        n = len(a)
        if any(a[i] > a[i + 1] for i in range(n - 1)):
            a.sort()
        if any(a[i] >= a[i + 1] for i in range(n - 1)):
            a, b = [], a
            for x in b:
                if not a or a[-1] != x:
                    a.append(x)
            n = self.size = len(a)
            num_bucket = int(math.ceil(math.sqrt(n /
self.BUCKET_RATIO)))
            self.a = [a[n * i // num_bucket : n * (i + 1) //
num_bucket] for i in range(num_bucket)]

    def __iter__(self) -> Iterator[T]:
        for i in self.a:
            for j in i: yield j

    def __reversed__(self) -> Iterator[T]:
        for i in reversed(self.a):
            for j in reversed(i): yield j

    def __eq__(self, other) -> bool:
        return list(self) == list(other)

    def __len__(self) -> int:

```

```

        return self.size

    def __repr__(self) -> str:
        return "SortedSet" + str(self.a)

    def __str__(self) -> str:
        s = str(list(self))
        return "{" + s[1 : len(s) - 1] + "}"

    def _position(self, x: T) -> Tuple[List[T], int, int]:
        "return the bucket, index of the bucket and position in
        which x should be. self must not be empty."
        for i, a in enumerate(self.a):
            if x <= a[-1]: break
        return (a, i, bisect_left(a, x))

    def __contains__(self, x: T) -> bool:
        if self.size == 0: return False
        a, _, i = self._position(x)
        return i != len(a) and a[i] == x

    def add(self, x: T) -> bool:
        "Add an element and return True if added. / O(VN)"
        if self.size == 0:
            self.a = [[x]]
            self.size = 1
            return True
        a, b, i = self._position(x)
        if i != len(a) and a[i] == x: return False
        a.insert(i, x)
        self.size += 1
        if len(a) > len(self.a) * self.SPLIT_RATIO:
            mid = len(a) >> 1
            self.a[b:b+1] = [a[:mid], a[mid:]]
        return True

    def _pop(self, self, a: List[T], b: int, i: int) -> T:
        ans = a.pop(i)
        self.size -= 1
        if not a: del self.a[b]
        return ans

    def discard(self, x: T) -> bool:
        "Remove an element and return True if removed. / O(VN)"
        if self.size == 0: return False
        a, b, i = self._position(x)
        if i == len(a) or a[i] != x: return False
        self._pop(a, b, i)
        return True

    def lt(self, self, x: T) -> Optional[T]:
        "Find the largest element < x, or None if it doesn't
        exist."
        for a in reversed(self.a):
            if a[0] < x:
                return a[bisect_left(a, x) - 1]

    def le(self, self, x: T) -> Optional[T]:
        "Find the largest element <= x, or None if it doesn't
        exist."
        for a in reversed(self.a):
            if a[0] <= x:
                return a[bisect_right(a, x) - 1]

    def gt(self, self, x: T) -> Optional[T]:
        "Find the smallest element > x, or None if it doesn't
        exist."
        for a in self.a:
            if a[-1] > x:
                return a[bisect_right(a, x)]

    def ge(self, self, x: T) -> Optional[T]:
        "Find the smallest element >= x, or None if it doesn't
        exist."
        for a in self.a:
            if a[-1] >= x:
                return a[bisect_left(a, x)]

    def __getitem__(self, i: int) -> T:
        "Return the i-th element."
        if i < 0:
            for a in reversed(self.a):
                i += len(a)

```

```
        if i >= 0: return a[i]
    else:
        for a in self.a:
            if i < len(a): return a[i]
            i -= len(a)
        raise IndexError

def pop(self, i: int = -1) -> T:
    "Pop and return the i-th element."
    if i < 0:
        for b, a in enumerate(reversed(self.a)):
            i += len(a)
            if i >= 0: return self._pop(a, ~b, i)
    else:
        for b, a in enumerate(self.a):
            if i < len(a): return self._pop(a, b, i)
            i -= len(a)
        raise IndexError

def index(self, x: T) -> int:
    "Count the number of elements < x."
    ans = 0
    for a in self.a:
        if a[-1] >= x:
            return ans + bisect_left(a, x)
        ans += len(a)
    return ans

def index_right(self, x: T) -> int:
    "Count the number of elements <= x."
    ans = 0
    for a in self.a:
        if a[-1] > x:
            return ans + bisect_right(a, x)
        ans += len(a)
    return ans
```

math

BinaryGCD.hpp

md5: f3ab31

```
u64 ctz(u64 x) { return countr_zero(x); }
u64 binary_gcd(u64 x, u64 y) {
    if(!x || !y) return x | y;
    u64 n = ctz(x), m = ctz(y);
    x >>= n, y >>= m;
    while(x != y) {
        if(x > y) x = (x - y) >> ctz(x - y);
        else y = (y - x) >> ctz(y - x);
    }
    return x << min(n, m);
}
```

ExtGCD.hpp

md5: c3fa9b

```
// returns gcd(a, b) and assign x, y to integers
// s.t. ax + by = gcd(a, b) and |x| + |y| is minimized
ll extgcd(ll a, ll b, ll& x, ll& y) {
    // assert(a >= 0 && b >= 0);
    if(!b) return x = 1, y = 0, a;
    ll d = extgcd(b, a % b, y, x);
    y -= a / b * x;
    return d;
}
```

modint

BarrettReduction.hpp

md5: 2ca7f3

```
// using u64 = uint64_t;
struct Barrett { // mod < 2^32
    u64 m, im;
    Barrett(u64 mod) : m(mod), im((-1ULL / m + 1) {}
    // input: a * b < 2^64, output: a * b % mod
    u64 mul(u64 a, u64 b) const {
        a *= b;
        u64 x = ((__uint128_t)a * im) >> 64;
        a -= x * m;
        if((ll)a < 0) a += m;
        return a;
    }
};
```

```
    }
};

modint.hpp
md5: 81b530

const ll mod = 998244353;
struct mm {
    ll x;
    mm(ll x_ = 0) : x(x_ % mod) {
        if(x < 0) x += mod;
    }
    friend mm operator+(mm a, mm b) { return a.x + b.x; }
    friend mm operator-(mm a, mm b) { return a.x - b.x; }
    friend mm operator*(mm a, mm b) { return a.x * b.x; }
    friend mm operator/(mm a, mm b) { return a * b.inv(); }
    // 4 行コピペ Alt + Shift + クリックで複数カーソル
    friend mm& operator+=(mm& a, mm b) { return a = a.x + b.x; }
    friend mm& operator-=(mm& a, mm b) { return a = a.x - b.x; }
    friend mm& operator*=(mm& a, mm b) { return a = a.x * b.x; }
    friend mm& operator/=(mm& a, mm b) { return a = a * b.inv(); }
}

mm inv() const { return pow(mod - 2); }
mm pow(ll b) const {
    mm a = *this, c = 1;
    while(b) {
        if(b & 1) c *= a;
        a *= a;
        b >>= 1;
    }
    return c;
}
};
```

FPS

FFT.hpp

md5: 3138c7

```
// {998244353, 3}, {1811939329, 13}, {2013265921, 31}
mm g = 3; // 原始根
void fft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    assert((1 << lg) == n);
    vector<mm> b(n);
    rep(l, 1, lg + 1) {
        ll w = n >> l;
        mm s = 1, r = g.pow(mod >> l);
        for(ll u = 0; u < n / 2; u += w) {
            rep(d, 0, w) {
                mm x = a[u << 1 | d], y = a[u << 1 | w | d] * s;
                b[u | d] = x + y;
                b[n >> 1 | u | d] = x - y;
            }
            s *= r;
        }
        swap(a, b);
    }
}

vector<mm> conv(vector<mm> a, vector<mm> b) {
    if(a.empty() || b.empty()) return {};
    size_t s = sz(a) + sz(b) - 1, n = bit_ceil(s);
    // if(min(sz(a), sz(b)) <= 60) 愚直に掛け算
    a.resize(n);
    b.resize(n);
    fft(a);
    fft(b);
    mm inv = mm(n).inv();
    rep(i, 0, n) a[i] *= b[i] * inv;
    reverse(1 + all(a));
    fft(a);
    a.resize(s);
    return a;
}
```

FFT_fast.hpp

md5: c8c567

```
// modint を u32 にして加減算を真面目にやると速い
mm g = 3; // 原始根
void fft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    static auto z = [] {
        vector<mm> z(30);
```

```
mm s = 1;
rep(i, 2, 32) {
    z[i - 2] = s * g.pow(mod >> i);
    s *= g.inv().pow(mod >> i);
}
return z;
}();
rep(l, 0, lg) {
    ll w = 1 << (lg - l - 1);
    mm s = 1;
    rep(k, 0, 1 << l) {
        ll o = k << (lg - l);
        rep(i, o, o + w) {
            mm x = a[i], y = a[i + w] * s;
            a[i] = x + y;
            a[i + w] = x - y;
        }
        s *= z[countr_zero<uint64_t>(~k)];
    }
}
// コピー
void ifft(vector<mm>& a) {
    ll n = sz(a), lg = __lg(n);
    static auto z = [] {
        vector<mm> z(30);
        mm s = 1;
        rep(i, 2, 32) { // g を逆数に
            z[i - 2] = s * g.inv().pow(mod >> i);
            s *= g.pow(mod >> i);
        }
        return z;
    }();
    for(ll l = lg; l--;) { // 逆順に
        ll w = 1 << (lg - l - 1);
        mm s = 1;
        rep(k, 0, 1 << l) {
            ll o = k << (lg - l);
            rep(i, o, o + w) {
                mm x = a[i], y = a[i + w]; // *s を下に移動
                a[i] = x + y;
                a[i + w] = (x - y) * s;
            }
            s *= z[countr_zero<uint64_t>(~k)];
        }
    }
}
vector<mm> conv(vector<mm> a, vector<mm> b) {
    if(a.empty() || b.empty()) return {};
    size_t s = sz(a) + sz(b) - 1, n = bit_ceil(s);
    // if(min(sz(a), sz(b)) <= 60) 愚直に掛け算
    a.resize(n);
    b.resize(n);
    fft(a);
    fft(b);
    mm inv = mm(n).inv();
    rep(i, 0, n) a[i] *= b[i] * inv;
    ifft(a);
    a.resize(s);
    return a;
}
```

- graph
- graph/tree
- flow

燃やす埋める.md

変形前の制約	変形後の制約
x が 0 のとき z 失う	(x, T, z)
x が 0 のとき z 得る	無条件で z 得る; (S, x, z)
x が 1 のとき z 失う	(S, x, z)
x が 1 のとき z 得る	無条件で z 得る; (x, T, z)

変形前の制約	変形後の制約
x, y, \dots がすべて 0 のとき z 得る	無条件で z 得る; $(S, w, z), (w, x, \infty), (w, y, \infty)$
x, y, \dots がすべて 1 のとき z 得る	無条件で z 得る; $(w, T, z), (x, w, \infty), (y, w, \infty)$

string

KMP.hpp

md5: 886c63

```
// kmp[i] := max{ l ≤ i | s[:l] == s[(i+1)-l:i+1] }
// abacaba -> 0010123
auto KMP(string s) {
    vector<ll> p(sz(s));
    rep(i, 1, sz(s)) {
        ll g = p[i - 1];
        while(g && s[i] != s[g]) g = p[g - 1];
        p[i] = g + (s[i] == s[g]);
    }
    return p;
}
```

Manacher.hpp

md5: 5882fb

```
// 各位置での回文半径を求める
// aaabaaa -> 1214121
// 偶数長の回文を含めて直径を知るには、N+1 個の $ を挿入して 1 を引く
// $a$a$a$b$a$a$a$ -> 123432181234321
auto manacher(string s) {
    ll n = sz(s), i = 0, j = 0;
    vector<ll> r(n);
    while(i < n) {
        while(i >= j && i + j < n && s[i - j] == s[i + j]) j++;
        r[i] = j;
        ll k = 1;
        while(i >= k && i + k < n && k + r[i - k] < j) {
            r[i + k] = r[i - k];
            k++;
        }
        i += k, j -= k;
    }
    return r;
}
```

RollingHash.hpp

md5: adb8d3

```
// using u64 = uint64_t;
const u64 mod = INF;
u64 add(u64 a, u64 b) {
    a += b;
    if(a >= mod) a -= mod;
    return a;
}
u64 mul(u64 a, u64 b) {
    auto c = (__uint128_t)a * b;
    return add(c >> 61, c & mod);
}
random_device rnd;
const u64 r = ((u64)rnd() << 32 | rnd()) % mod;
struct RH {
    ll n;
    vector<u64> hs, pw;
    RH(string s) : n(sz(s)), hs(n + 1), pw(n + 1, 1) {
        rep(i, 0, n) {
            pw[i + 1] = mul(pw[i], r);
            hs[i + 1] = add(mul(hs[i], r), s[i]);
        }
    }
    u64 get(ll l, ll r) const { return add(hs[r], mod - mul(hs[l], pw[r - l])); }
};
```

SuffixArray.hpp

md5: 1d70ce

```
// returns pair{sa, lcp}
// sa 長さ n : s[sa[0]:] < s[sa[1]:] < ... < s[sa[n-1]:]
// lcp 長さ n-1 : lcp[i] = LCP(s[sa[i]:], s[sa[i+1]:])
auto SA(string s) {
```

```
ll n = sz(s) + 1, lim = 256;
// assert(lim > ranges::max(s));
vector<ll> sa(n), lcp(n), x(all(s) + 1), y(n), ws(max(n,
lim)), rk(n);
iota(all(sa), 0);
for(ll j = 0, p = 0; p < n; j = max(1LL, j * 2), lim = p) {
    p = j;
    iota(all(y), n - j);
    rep(i, 0, n) if(sa[i] >= j) y[p++] = sa[i] - j;
    fill(all(ws), 0);
    rep(i, 0, n) ws[x[i]]++;
    rep(i, 1, lim) ws[i] += ws[i - 1];
    for(ll i = n; i--;) sa[--ws[x[y[i]]]] = y[i];
    swap(x, y);
    p = 1;
    x[sa[0]] = 0;
    rep(i, 1, n) {
        ll a = sa[i - 1], b = sa[i];
        x[b] = (y[a] == y[b] && y[a + j] == y[b + j]) ? p - 1
: p++;
    }
}
rep(i, 1, n) rk[sa[i]] = i;
for(ll i = 0, k = 0; i < n - 1; lcp[rk[i++]] = k) {
    if(k) k--;
    while(s[i + k] == s[sa[rk[i] - 1] + k]) k++;
}
sa.erase(begin(sa));
lcp.erase(begin(lcp));
return pair{sa, lcp};
}
```

Zalgorithm.hpp

md5: b20b04

```
// Z[i] := LCP(s, s[i:])
// abacaba -> 7010301
auto Z(string s) {
    ll n = sz(s), l = -1, r = -1;
    vector<ll> z(n, n);
    rep(i, 1, n) {
        ll& x = z[i] = i < r ? min(r - i, z[i - l]) : 0;
        while(i + x < n && s[i + x] == s[x]) x++;
        if(i + x > r) l = i, r = i + x;
    }
}
```

```
return z;
}
```

algorithm
geometry
memo

Primes.md

素数の個数

n	10^2	10^3	10^4	10^5	10^6	10^7	10^8	10^9
$\pi(n)$	25	168	1229	9592	78498	6.6×10^5	5.8×10^6	5.1×10^7

高度合成数

$\leq n$	10^3	10^4	10^5	10^6	10^7	10^8	10^9		
x	840	7560	83160	720720	8648640	73513440	735134400		
$d^0(x)$	32	64	128	240	448	768	1344		
$\leq n$	10^{10}	10^{11}	10^{12}	10^{13}	10^{14}	10^{15}	10^{16}	10^{17}	10^{18}
$d^0(x)$	2304	4032	6720	10752	17280	26880	41472	64512	103680

素数階乗

n	2	3	5	7	11	13	17	19	23	29
$n\#$	2	6	30	210	2310	30030	510510	9699690	2.2×10^8	6.5×10^9

階乗

5!	6!	7!	8!	9!	10!	11!	12!
120	720	5040	40320	362880	3628800	4.0×10^7	4.8×10^8