

tonosama Library

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template

hash.sh

```
# 使い方: sh hash.sh -> コピーペ -> Ctrl + D
# コメント・空白・改行を削除して md5 でハッシュする
g++ -dD -E -fpreprocessed - | tr -d '[:space:]' | md5sum | cut -c-6
```

settings.sh

```
# CLion の設定
Settings → Build → CMake → Reload CMake Project
add_compile_options(-D_GLIBCXX_DEBUG)
# Caps Lock を Ctrl に変更
setxkbmap -option ctrl:nocaps
```

template.hpp

md5: 365d7f

```
#include <bits/stdc++.h>
using namespace std;
using ll = long long;
const ll INF = LLONG_MAX / 4;
#define rep(i, a, b) for (ll i = a; i < (b); i++)
#define all(a) begin(a), end(a)
ll sz(const auto& a) { return size(a); }
bool chmin(auto& a, auto b) {
    if (a <= b) return 0;
    a = b;
    return 1;
}
bool chmax(auto& a, auto b) {
    if (a >= b) return 0;
    a = b;
    return 1;
}

int main() {
    cin.tie(0)->sync_with_stdio(0);
    // your code here...
}
```

data-structure

BIT.hpp

md5: d8ec49

```
struct BIT {
    vector<ll> a;
    BIT(ll n) : a(n + 1) {}
    void add(ll p, ll x) { // A[p] += x
        p++;
        while (p < sz(a)) {
            a[p] += x;
            p += p & -p;
        }
    }
    ll sum(ll r) {
        ll s = 0;
```

```
        while (r > 0) {
            s += a[r];
            r -= r & -r;
        }
        return s;
    }
    ll sum(ll l, ll r) { // sum of A[l, r)
        return sum(r) - sum(l);
    }
};
```

math

modint

BarrettReduction.hpp

md5: b4bd2c

```
using u64 = uint64_t;
struct Barrett { // mod < 2^32
    u64 m, im;
    Barrett(u64 mod) : m(mod), im(-1ULL / m + 1) {}
    // input: a * b < 2^64, output: a * b % mod
    u64 mul(u64 a, u64 b) const {
        a *= b;
        u64 x = ((__uint128_t)a * im) >> 64;
        a -= x * m;
        if ((ll)a < 0) a += m;
        return a;
    }
};
```

modint.hpp

md5: 1dcff5

```
const ll mod = 998244353;
struct mm {
    ll x;
    mm(ll x_ = 0) : x(x_ % mod) {
        if (x < 0) x += mod;
    }
    friend mm operator+(mm a, mm b) { return a.x + b.x; }
    friend mm operator-(mm a, mm b) { return a.x - b.x; }
    friend mm operator*(mm a, mm b) { return a.x * b.x; }
    friend mm operator/(mm a, mm b) { return a * b.inv(); }
    // 4 行コピー Alt + Shift + クリックで複数カーソル
    friend mm& operator+=(mm& a, mm b) { return a = a.x + b.x; }
    friend mm& operator-=(mm& a, mm b) { return a = a.x - b.x; }
    friend mm& operator*=(mm& a, mm b) { return a = a.x * b.x; }
    friend mm& operator/=(mm& a, mm b) { return a = a * b.inv(); }
}

mm inv() const { return pow(*this, mod - 2); }
friend mm pow(mm a, ll b) {
    mm c = 1;
    while (b) {
        if (b & 1) c *= a;
        a *= a;
        b >>= 1;
    }
    return c;
}
};
```

FPS

FFT.hpp

md5: 10993d

```
constexpr ll pow_mod_constexpr(ll x, ll n, int m) {
    if (m == 1) return 0;
    uint _m = (uint)(m);
    ull r = 1;
    ull y = x % m;
    while (n) {
        if (n & 1) r = (r * y) % _m;
        y = (y * y) % _m;
        n >>= 1;
    }
    return r;
}

constexpr bool is_prime_constexpr(int n) {
    if (n <= 1) return false;
```

```

    if (n == 2 || n == 7 || n == 61) return true;
    if (n % 2 == 0) return false;
    ll d = n - 1;
    while (d % 2 == 0) d /= 2;
    constexpr ll bases[3] = {2, 7, 61};
    for (ll a : bases) {
        ll t = d;
        ll y = pow_mod_constexpr(a, t, n);
        while (t != n - 1 && y != 1 && y != n - 1) {
            y = y * y % n;
            t <<= 1;
        }
        if (y != n - 1 && t % 2 == 0) { return false; }
    }
    return true;
}

template<int n> constexpr bool is_prime =
is_prime_constexpr(n);

constexpr pair<ll, ll> inv_gcd(ll a, ll b) {
    a = safe_mod(a, b);
    if (a == 0) return {b, 0};

    ll s = b, t = a;
    ll m0 = 0, m1 = 1;

    while (t) {
        ll u = s / t;
        s -= t * u;
        m0 -= m1 * u; // |m1 * u| <= |m1| * s <= b

        auto tmp = s;
        s = t;
        t = tmp;
        tmp = m0;
        m0 = m1;
        m1 = tmp;
    }
    if (m0 < 0) m0 += b / s;
    return {s, m0};
}

ull floor_sum_unsigned(ull n, ull m, ull a, ull b) {
    ull ans = 0;
    while (true) {
        if (a >= m) {
            ans += n * (n - 1) / 2 * (a / m);
            a %= m;
        }
        if (b >= m) {
            ans += n * (b / m);
            b %= m;
        }

        ull y_max = a * n + b;
        if (y_max < m) break;
        n = (ull)(y_max / m);
        b = (ull)(y_max % m);
        swap(m, a);
    }
    return ans;
}

template<class mint, int g =
internal::primitive_root<mint::mod()>,
internal::is_static_modint_t<mint>* = nullptr>
struct fft_info {
    static constexpr int rank2 =
countr_zero_constexpr(mint::mod() - 1);
    array<mint, rank2 + 1> root; // root[i]^(2^i) == 1
    array<mint, rank2 + 1> iroot; // root[i] * iroot[i] == 1

    array<mint, max(0, rank2 - 2 + 1)> rate2;
    array<mint, max(0, rank2 - 2 + 1)> irate2;

    array<mint, max(0, rank2 - 3 + 1)> rate3;
    array<mint, max(0, rank2 - 3 + 1)> irate3;

    fft_info() {
        root[rank2] = mint(g).pow((mint::mod() - 1) >> rank2);
        iroot[rank2] = root[rank2].inv();
        for (int i = rank2 - 1; i >= 0; i--) {
            root[i] = root[i + 1] * root[i + 1];

```

```

            iroot[i] = iroot[i + 1] * iroot[i + 1];
        }
    }

    mint prod = 1, iprod = 1;
    for (int i = 0; i <= rank2 - 2; i++) {
        rate2[i] = root[i + 2] * prod;
        irate2[i] = iroot[i + 2] * iprod;
        prod *= root[i + 2];
        iprod *= root[i + 2];
    }

    mint prod = 1, iprod = 1;
    for (int i = 0; i <= rank2 - 3; i++) {
        rate3[i] = root[i + 3] * prod;
        irate3[i] = iroot[i + 3] * iprod;
        prod *= iroot[i + 3];
        iprod *= root[i + 3];
    }
}

};

template<class mint, internal::is_static_modint_t<mint>* =
nullptr> void butterfly(vector<mint>& a) {
    int n = int(a.size());
    int h = internal::countr_zero((uint)n);

    static const fft_info<mint> info;

    int len = 0; // a[i, i+(n>>len), i+2*(n>>len), ..] is
transformed
    while (len < h) {
        if (h - len == 1) {
            int p = 1 << (h - len - 1);
            mint rot = 1;
            for (int s = 0; s < (1 << len); s++) {
                int offset = s << (h - len);
                for (int i = 0; i < p; i++) {
                    auto l = a[i + offset];
                    auto r = a[i + offset + p] * rot;
                    a[i + offset] = l + r;
                    a[i + offset + p] = l - r;
                }
                if (s + 1 != (1 << len)) rot *=
info.rate2[countr_zero(~(uint)(s))];
            }
            len++;
        } else {
            int p = 1 << (h - len - 2);
            mint rot = 1, imag = info.root[2];
            for (int s = 0; s < (1 << len); s++) {
                mint rot2 = rot * rot;
                mint rot3 = rot2 * rot;
                int offset = s << (h - len);
                for (int i = 0; i < p; i++) {
                    auto mod2 = 1ULL * mint::mod() * mint::mod();
                    auto a0 = 1ULL * a[i + offset].val();
                    auto a1 = 1ULL * a[i + offset + p].val() *
rot.val();
                    auto a2 = 1ULL * a[i + offset + 2 * p].val() *
rot2.val();
                    auto a3 = 1ULL * a[i + offset + 3 * p].val() *
rot3.val();
                    auto a1na3imag = 1ULL * mint(a1 + mod2 -
a3).val() * imag.val();
                    auto na2 = mod2 - a2;
                    a[i + offset] = a0 + a2 + a1 + a3;
                    a[i + offset + 1 * p] = a0 + a2 + (2 * mod2 -
(a1 + a3));
                    a[i + offset + 2 * p] = a0 + na2 + a1na3imag;
                    a[i + offset + 3 * p] = a0 + na2 + (mod2 -
a1na3imag);
                }
                if (s + 1 != (1 << len)) rot *=
info.rate3[countr_zero(~(uint)(s))];
            }
            len += 2;
        }
    }
}

```

```

template<class mint, internal::is_static_modint_t<mint>* =
nullptr> void butterfly_inv(vector<mint>& a) {
    int n = int(a.size());
    int h = internal::countr_zero((uint)n);

    static const fft_info<mint> info;

    int len = h; // a[i, i+(n>>len), i+2*(n>>len), ..] is
transformed
    while (len) {
        if (len == 1) {
            int p = 1 << (h - len);
            mint irot = 1;
            for (int s = 0; s < (1 << (len - 1)); s++) {
                int offset = s << (h - len + 1);
                for (int i = 0; i < p; i++) {
                    auto l = a[i + offset];
                    auto r = a[i + offset + p];
                    a[i + offset] = l + r;
                    a[i + offset + p] = (ull)(mint::mod() + l.val()
- r.val()) * irot.val();
                }
                if (s + 1 != (1 << (len - 1))) irot *=
info.irate2[countr_zero(~(uint)(s))];
            }
            len--;
        } else {
            int p = 1 << (h - len);
            mint irot = 1, iimag = info.iroot[2];
            for (int s = 0; s < (1 << (len - 2)); s++) {
                mint irot2 = irot * irot;
                mint irot3 = irot2 * irot;
                int offset = s << (h - len + 2);
                for (int i = 0; i < p; i++) {
                    auto a0 = 1ULL * a[i + offset + 0 * p].val();
                    auto a1 = 1ULL * a[i + offset + 1 * p].val();
                    auto a2 = 1ULL * a[i + offset + 2 * p].val();
                    auto a3 = 1ULL * a[i + offset + 3 * p].val();

                    auto a2na3iimag = 1ULL * mint((mint::mod() + a2
- a3) * iimag.val()).val();

                    a[i + offset] = a0 + a1 + a2 + a3;
                    a[i + offset + 1 * p] = (a0 + (mint::mod() - a1)
+ a2na3iimag) * irot.val();
                    a[i + offset + 2 * p] = (a0 + a1 + (mint::mod()
- a2) + (mint::mod() - a3)) * irot2.val();
                    a[i + offset + 3 * p] = (a0 + (mint::mod() - a1)
+ (mint::mod() - a2na3iimag)) * irot3.val();
                }
                if (s + 1 != (1 << (len - 2))) irot *=
info.irate3[countr_zero(~(uint)(s))];
            }
            len -= 2;
        }
    }
}

template<class mint, internal::is_static_modint_t<mint>* =
nullptr>
vector<mint> convolution_naive(const vector<mint>& a, const
vector<mint>& b) {
    int n = int(a.size()), m = int(b.size());
    vector<mint> ans(n + m - 1);
    if (n < m) {
        for (int j = 0; j < m; j++) {
            for (int i = 0; i < n; i++) { ans[i + j] += a[i] *
b[j]; }
        }
    } else {
        for (int i = 0; i < n; i++) {
            for (int j = 0; j < m; j++) { ans[i + j] += a[i] *
b[j]; }
        }
    }
    return ans;
}

template<class mint, internal::is_static_modint_t<mint>* =
nullptr>
vector<mint> convolution_fft(vector<mint> a, vector<mint> b) {
    int n = int(a.size()), m = int(b.size());

```

```

    int z = (int)internal::bit_ceil((uint)(n + m - 1));
    a.resize(z);
    internal::butterfly(a);
    b.resize(z);
    internal::butterfly(b);
    for (int i = 0; i < z; i++) { a[i] *= b[i]; }
    internal::butterfly_inv(a);
    a.resize(n + m - 1);
    mint iz = mint(z).inv();
    for (int i = 0; i < n + m - 1; i++) a[i] *= iz;
    return a;
}

template<class mint, internal::is_static_modint_t<mint>* =
nullptr>
vector<mint> convolution(const vector<mint>& a, const
vector<mint>& b) {
    int n = int(a.size()), m = int(b.size());
    if (!n || !m) return {};

    int z = (int)internal::bit_ceil((uint)(n + m - 1));
    assert((mint::mod() - 1) % z == 0);

    if (min(n, m) <= 60) return convolution_naive(a, b);
    return internal::convolution_fft(a, b);
}

vector<ll> convolution_ll(const vector<ll>& a, const
vector<ll>& b) {
    int n = int(a.size()), m = int(b.size());
    if (!n || !m) return {};

    static constexpr ull MOD1 = 754974721; // 2^24
    static constexpr ull MOD2 = 167772161; // 2^25
    static constexpr ull MOD3 = 469762049; // 2^26
    static constexpr ull M2M3 = MOD2 * MOD3;
    static constexpr ull M1M3 = MOD1 * MOD3;
    static constexpr ull M1M2 = MOD1 * MOD2;
    static constexpr ull M1M2M3 = MOD1 * MOD2 * MOD3;

    static constexpr ull i1 = internal::inv_gcd(MOD2 * MOD3,
MOD1).second;
    static constexpr ull i2 = internal::inv_gcd(MOD1 * MOD3,
MOD2).second;
    static constexpr ull i3 = internal::inv_gcd(MOD1 * MOD2,
MOD3).second;

    static constexpr int MAX_AB_BIT = 24;
    static_assert(MOD1 % (1ull << MAX_AB_BIT) == 1, "MOD1 isn't
enough to support an array length of 2^24.");
    static_assert(MOD2 % (1ull << MAX_AB_BIT) == 1, "MOD2 isn't
enough to support an array length of 2^24.");
    static_assert(MOD3 % (1ull << MAX_AB_BIT) == 1, "MOD3 isn't
enough to support an array length of 2^24.");
    assert(n + m - 1 <= (1 << MAX_AB_BIT));

    auto c1 = convolution<MOD1>(a, b);
    auto c2 = convolution<MOD2>(a, b);
    auto c3 = convolution<MOD3>(a, b);

    vector<ll> c(n + m - 1);
    for (int i = 0; i < n + m - 1; i++) {
        ull x = 0;
        x += (c1[i] * i1) % MOD1 * M2M3;
        x += (c2[i] * i2) % MOD2 * M1M3;
        x += (c3[i] * i3) % MOD3 * M1M2;
        ll diff = c1[i] - internal::safe_mod((ll)(x), (ll)
(MOD1));
        if (diff < 0) diff += MOD1;
        static constexpr ull offset[5] = {0, 0, M1M2M3, 2 *
M1M2M3, 3 * M1M2M3};
        x -= offset[diff % 5];
        c[i] = x;
    }

    return c;
}

```

graph
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memo