WonderMarket Section B – Client Report

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MATH3202 Assignment 3 Due 27/05/2019 1:00 pm

Abstract

In this report, we propose a solution to optimise your refridgerator logistics and maximise expected profit.

Solution

We have considered the customer-facing aspect of fridges put on display as well as the logistics of your fridge deliveries. We have arrived at the following optimal solutions for each communication.

Communication 1

In this communication, we know how much profit each fridge can be sold for and how expected sales vary with the types of fridges placed on display. Only 8 fridges can be displayed in total.

The maximum expected profit is \$1863.20. This is achieved by displaying 2 Alaska fridges, 3 Elsa fridges and 3 Lumi fridges. In this case, on average you will sell 3.1, 4.2 and 4.1 of Alaska, Elsa and Lumi fridges respectively, leading to the profit of

expected profit = $3.1 \times \$140 + 4.2 \times \$147 + 4.1 \times \$198 = \1863.20 .

Communication 2

In this communication, the focus moved from direct-to-customer sales to delivery processes. Because customer demand is not known in advance, we need to balance ordering and storing them with having enough fridges to meet future demand. We will consider a period of 4 weeks.

Using the demand distribution you provided us, the maximum expected profit over 4 weeks is \$5282.92 (assuming no fridges to start with). This is done by buying 4 Alaska fridges, 5 Elsa fridges and 5 Lumi fridges in the first week.

Moreover, in any week, your optimal strategy is to have 4, 5 and 5 fridges respectively of each type available. This means if you have less than this amount stored at the start of a week, buy exactly enough to make up this amount. We have verified that this is optimal for all feasible demand scenarios.

Insights

In general stochastic (uncertain) optimisation problems, the solution cannot be expressed so simply (see communication 3). However, in this case it is because each fridge does not affect the sales or deliveries of the other fridge types and demand remains constant through all weeks.

Moreover, because communication 2 (and 3) are stochastic problems, the value and actions we have calculated maximise the expected profit. During the course of the trial, your actual profit will vary above or below this value, depending on exactly how many fridges you sell each week.

Communication 3

In this communication, we need to consider the costs of transporting fridges to the storage warehouse where they are held before being sent to customers. Each truck costs \$150 and has a limited capacity of 7 fridges. At most 2 trucks will be ordered per week and at most 8 fridges of each type can be processed at the warehouse. A truck can hold any combination of fridge types so we need to consider all fridge types together.

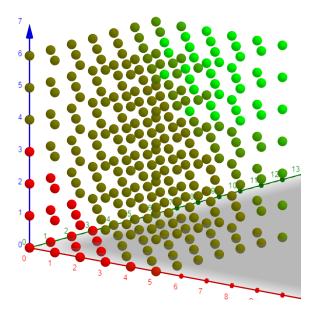
Assuming you currently have no fridges, the maximum expected profit is \$4229.46 and you should purchase 4, 5 and 5 respectively in week 1.

In this case, the solution is more complicated. Because each fridge affects other fridges and each fridge sells for a different amount, your buying strategy is more nuanced. With this in mind, we have developed an interactive solution explorer. You input the amount you sell each week and it recommends the optimal buying strategy for the next week. Please see the appendix.

Insights

By modifying the constraint that at most 8 fridges of each type are stored, we discovered that you can obtain the same expected profit with a maximum storage of 5 Alaska fridges and 6 Elsa/Lumi fridges. This means the optimal solution never recommends having more than 6 of any one fridge. This is because these are the maximum which can be sold per week. Buying any more than this amount will require excess stock to be stored to the next week, raising costs.

To try visualise this multi-dimensional situation, we have included a 3D plot below. This is at the beginning of the first week and the axes are number of each fridge type stored. Red is Alaska, green is Elsa and blue is Lumi. The colour of each dot represents how many fridges should be ordered in total (green being 0 and red being 14).



Here, you can see that there are approximately diagonal thresholds where transitions between truckloads ordered occur. However, these aren't exact; for example even if you have 5 Alaska fridges but no other fridges, you should still order 2 truckloads. This is because Alaska fridges have a small profit margin so it will be more profitable to have other fridge types as well.

Broadly, the optimal actions are grouped into 3 bunches—0, 1 and 2 truckloads. Most of the cases in each group will order the maximum possible but occasionally, you will want to order less due to the first paragraph in this section.

Observations

- The limit of 8 fridges per type stored is a significant factor in the runtime of the model.
- \bullet Because the solution to communication 2 is so simple, the maximum expected profit is actually linear as number of weeks increases. Profit can be calculated as number of weeks \times \$1320.73.
- However, comm 3 profit increases slightly faster than linear. This may be because
 in later weeks it is possible that fridges are left over from earlier weeks which can
 reduce later weeks' transport costs, increasing profit.

Appendix

We have included a file stochastic_explorer.py to interactively explore the solution week by week. Communications 2 and 3 are supported.

Usage

- 1. Place stochastic_explorer.py is in the same folder as assignment_dp.py.
- 2. Run stochastic_explorer.py.

- 3. Type "2" or "3" for the communication you wish to consider. Press Enter.
- 4. Once analysed, it will display the maximum expected profit and the fridges you should buy in the first week.
- 5. Type in how many of each fridge you sold in that week.
- 6. Your weekly and total profit will be displayed along with how many fridges you have stored for next week. Press Enter to continue.
- 7. Repeats from step 4 until you reach the end of the 4 weeks.