Wide-scope distributivity

Keny Chatain (MIT)

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NELS

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plurals

paradox about dependent

A puzzle about scope and a

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 - a. collective: one salad overall
 - b. distributive: one salad per woman

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$$[\![D]\!]$$
 (predicate) = $\lambda X. \forall x \in X$, **atom**(x) \rightarrow predicate(x)

(2) John gave a pumpkin pie to the two girls

(Roberts, 1987)

- a. collective: one pumpkin pie overall
- b. distributive: one pumpkin pie per girl



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(Other analysis of (3): generalizing the operator (Lasersohn, 1998), thematic-role based account of distributivity (Champollion, 2016))

 $^{^{1}}$ Assuming Roberts (1987) and QR clause-boundedness. *A minima*, one can say that its scope is local to the **DP**, where the notion of *locality* depends on the theory of distributive readings.

(3) John gave a pumpkin pie to the two girls.

(Other analysis of (3): generalizing the operator (Lasersohn, 1998), thematic-role based account of distributivity (Champollion, 2016))

Locality conditions on distributivity

The universal force associated with the distributive reading of a **DP** has its scope within the same clause as the **DP** itself¹.

 $^{^{1}}$ Assuming Roberts (1987) and QR clause-boundedness. *A minima*, one can say that its scope is local to the **DP**, where the notion of *locality* depends on the theory of distributive readings.

- (4) a. **Context:** we're experimenting a new drug; Anna just came back with the results of the experiment.
 - b. Well, either the drug made the subjects sick or it made them sleepy; none of them was cured.

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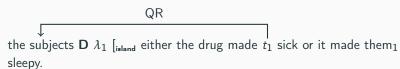
> WSD reading: every participant was either made sick or sleepy.

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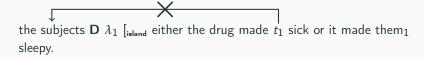
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- Other reading: either the drug made all of the subjects sick or it made all of them sleepy

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- > Other reading: either the drug made all of the subjects sick or it made all of them sleepy



_



(5) ?? Either the drug made every participant sick or it made him sleepy.

More examples

- (6) a. **Context:** Ten 3D printers are currently running; they're not expected to finish their prints at the same time.
 - b. When the printers are done with their prints, they will emit a long high-pitched noise.

More examples

- (6) a. **Context:** Ten 3D printers are currently running; they're not expected to finish their prints at the same time.
 - b. When the printers are done with their prints, they will emit a long high-pitched noise.

- ➤ WSD reading: for each printer p, when p will be done with p's print, p will emit a long high-pitched noise.
- ➤ Other reading: when all the printers are done with their prints, they will emit a long high-pitched noise

More examples

Some previously known cases may be subsumed under this paradigm.

(7) a. The people who voted for the rightwing candidates thought that they would win the election.

(Dimitriadis (2000), adapted)

b. **Reading:** for each of the rightwing candidates *x*, the people who voted for *x* thought *x* would win.

Data summary

➤ In a wide range of environments, a plural definite description may be interpreted distributively with an arbitrary wide-scope.

→ let's call these readings wide-scope distributivity readings

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Data summary

- ➤ In a wide range of environments, a plural definite description may be interpreted distributively with an arbitrary wide-scope.
 - → let's call these readings wide-scope distributivity readings
- Standard approaches to Q-distributivity predict local distributive readings.
- ➤ What's happening?

Idea

Let's restrict ourselves to pronominal examples for now. This will reveal a second challenge raised by these sentences.

- (8) a. Either it made them sick or it made them sleepy.
 - b. When they are done, they will emit a long high-pitched sounds.
 - c. The people who voted for them thought they would win.

Remarks

- ➤ Remark #1: pronouns in WSD sentences are plural pronouns with singular reference.
- ▶ Remark #2:
- > Remark #3:

(9) a. Either they were all sick or they were all sleepy.

- (9) a. Either they were all sick or they were all sleepy.
 - b. Reading: every subject was either made sick or sleepy.
 - Other reading: either all of the subjects were sick or all of them were sleepy.

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- (10) a. When they are all done, they will emit a long high-pitched sound.
 - b. **Reading:** for each printer p, when p will be done with p's print, p will emit a long high-pitched noise.
 - Other reading: when all the printers are done with their prints, they will emit a long high-pitched noise

This behaviour is familiar: bound plural pronouns.

- (11) a. All the children thought they would win. $\rightsquigarrow \checkmark$ one winner.
 - b. All the children thought they would all win.→# one winner.

Remarks

- ➤ Remark #1: pronouns in WSD sentences are plural pronouns with singular reference.
- > Remark #2: WSD sentences license dependent plurals
- ➤ Remark #3:

Remark #2: WSD sentences license dependent plurals

Dependent plurals are expressions that seem equivalent to their singular counterparts².

- (12) a. All the boys flew their kites/kites.
 - \rightsquigarrow \checkmark one kite per boy
 - b. All the boys flew their 10 kites/several kites/ten kites.
 - → *one kite per boy.

²Mise en abyme.

Descriptive generalizations about dependent plurals

- > They need to be "licensed".
- ➤ They are licensed by all, plural definite descriptions, etc.
- ➤ The licensing is subject to intervention effects by e.g. singular indefinites

(Roberts, 1987; Spector, 2003; Zweig, 2008; Ivlieva, 2013; Minor, 2017, a.o.)

Remark #2: WSD sentences license dependent plurals

- (13) a. **Pretext:** The participants of our survival game are in critical conditions.
 - b. Either they have finished their ration boxes or they lost them to mountain lions.
 - → ✓ one ration box per participant

Remarks

- ➤ Remark #1: pronouns in WSD sentences are plural pronouns with singular reference.
- ▶ Remark #2: WSD sentences license dependent plurals
- ▶ Remark #3: Pronouns with singular reference do not license dependent plurals

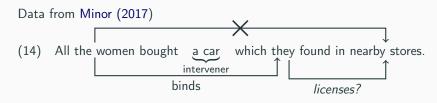
Remark #3: Pronouns with singular reference do not license dependent plurals

Data from Minor (2017)

(14) All the women bought a car which they found in nearby stores.

 \sim * all \gg a and one car per woman and one store per car

Remark #3: Pronouns with singular reference do not license dependent plurals



 \rightarrow * all \gg a and one car per woman and one store per car

Remarks

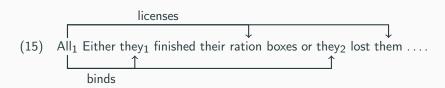
- ➤ Remark #1: pronouns in WSD sentences are plural pronouns with singular reference.
- > Remark #2: WSD sentences license dependent plurals
- ➤ **Remark** #3: Pronouns with singular reference do not license dependent plurals

[→] What licenses dependent plurals in WSD sentences?

Solution

Pronouns in WSD sentences are bound by a covert All operator; it is this operator that licenses the dependent plurals.

Solution



The pronominals do not need to move to get a distributive reading. They are simply bound.

The pronominals do not need to move to get a distributive reading. They are simply bound.

 \checkmark ALL₁ ... [island ... they₁

What about sentences with definite descriptions?

What about sentences with definite descriptions? licenses (16) All₁ Either the participants₁ finished their ration boxes or binds? To extend this account to the case of definite descriptions, we have to assume that these definite decriptions can be interpreted anaphorically.

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** ✓

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** ✓
 - c. Coordination of proper names:

 \checkmark When Printer 1 and Printer 2 are done with their prints, they will emit a high-pitched noise.

- (17) a. Definite descriptions: \checkmark
 - b. **Pronouns:** √
 - c. Coordination of proper names: \checkmark
 - d. Numerals:

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** √
 - c. Coordination of proper names: √
 - d. Numerals:

When two printers are done with their prints, they will emit a high-pitched noise.

 \checkmark when there are two printers that are done with their prints,

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** ✓
 - c. Coordination of proper names: √
 - d. Numerals:

. . .

When two printers are done with their prints, they will emit a high-pitched noise.

- \checkmark when there are two printers that are done with their prints,
- \checkmark there are two printers such that when both of them are done with their prints, . . .

(17) a. **Definite descriptions:** ✓

- b. **Pronouns:** √
- c. Coordination of proper names: √
- d. Numerals:

When two printers are done with their prints, they will emit a high-pitched noise.

- \checkmark when there are two printers that are done with their prints,
- \checkmark there are two printers such that when both of them are done with their prints, . . .
- * for each of two printers x, when x is done with its print, ...

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** ✓
 - c. Coordination of proper names: $\sqrt{}$
 - d. Numerals:

When two printers are done with their prints, they will emit a high-pitched noise.

 \checkmark when there are two printers that are done with their prints,

. . .

 \checkmark there are two printers such that when both of them are done with their prints, . . .

* for each of two printers x, when x is done with its print, . . .

- (17) a. **Definite descriptions:** ✓
 - b. **Pronouns:** √
 - c. Coordination of proper names: $\sqrt{}$
 - d. Numerals: *
 - e. Plural quantifiers:
 - * When all/most (of the) printers are done with their prints, they will emit a high-pitched noise.

Generalization

Only referential expressions (i.e. type e) can receive WSD readings.

The plot

- ➤ Adopt an already existing analysis of dependent plurals and bound plurals under a quantifier like *all*.
 - → plural assignment approach from Minor (2017) and also Champollion et al. (2017), Nouwen (2003)
- > Adapt it so that referential expressions may act as anaphors.
 - → referential expressions contribute their descriptive content as a presupposition.

bird's-eye view

Formal implementation:

Standard picture

Sentences are evaluated against a single assignment function

van den Berg (1996)'s proposal

Sentences are evaluated against multiple assignment functions

- (18) a. Every boy₁ picked a flower₂ ...
 - b. ... They $_1$ gave them $_2$ to Bill.

Output assignment of the first sentence:

- (18) a. Every boy₁ picked a flower₂ . . .
 - b. ... They₁ gave them₂ to Bill.

Output assignment of the first sentence:

G	1	2	 Evaluating (18b)
g1 g2	_	$\begin{array}{c} \texttt{flower}_1' \\ \texttt{flower}_2' \end{array}$	$g_1(1)$ gave $g_1(2)$ to B. $g_2(1)$ gave $g_2(2)$ to B.
g 47	boy ₄₇	flower' ₄₇	 $g_{47}(1)$ gave $g_{47}(2)$ to B.

- (18) a. Every boy₁ picked a flower₂ ...
 - b. ... They₁ gave them₂ to Bill.

Output assignment of the first sentence:

 \leadsto (18b) is true iff [boy 1 gave flower 1 to Bill] and [boy 2 gave flower 2 to Bill] and \ldots

Principle of interpretation

A sentence is evaluated for every assignment function. The sentence comes out true if true under all evaluations. In other words, evaluation is row-wise³.

 $^{^3}$ In the more fleshed-out version of this semantics, this principle comes out as a consequence of the way we define operators. Thus, different choices of implementation of the plural assignment semantics may fail to vindicate this principle.

Another ingredient is needed for bound plurals and dependent plurals: column-wise evaluation of number features.

(19) The students all₁ λ_1 t_1 thought they₁ would win.

The students introduces a plurality in the assignment at index 1.

$$\emptyset \longrightarrow \frac{G}{g_1 \quad \text{student}_1' \oplus ... \oplus \text{student}_{35}'}$$

(19) The students all₁ λ_1 t_1 thought they₁ would win. all₁ "splits" the singular assignment into a plural one.

			G	1
G	1	,	g ₁	$\mathtt{student}_1'$
g	$\mathtt{student}_1' \oplus \ldots \oplus \mathtt{student}_{35}'$		g 2	$\mathtt{student}_2'$
	_ 30		<i>g</i> 35	student' ₃₅

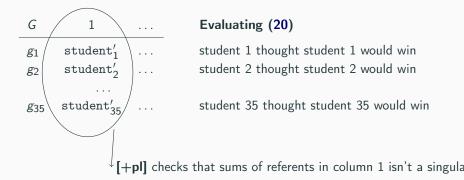
(19) The students all₁ λ_1 t_1 thought pro₁[+pl] would win.

G	1	 Evaluating (21)
g ₁ g ₂	1	 student 1 thought student 1 would win student 2 thought student 2 would win
<i>g</i> 35	student'	 student 35 thought student 35 would win

 \rightsquigarrow for all students s, s thought s would win. (singular reference reading)

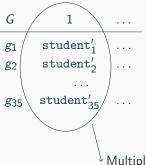
What does [+pl] do?

(20) The students all₁ λ_1 t_1 thought pro₁[+pl] would win.



⁴I am assuming that plural means "*more than one*"; whether the multiplicity inference should be derived as an implicature is, as far as I can tell, orthogonal to my concerns.

(21) # The students all₁ thought he₁ would win.



Evaluating (21)

student 1 thought student 1 would win student 2 thought student 2 would win student 35 thought student 35 would win

 $^{\downarrow}$ Multiple students: the presupposition of <code>[+sg]</code> is not satisfie

Dichotomy

- ➤ Content is evaluated row-wise.
- > Number feature presuppositions is evaluated column-wise.

(22) The boys all λ_1 [t_1 flew kites[+pl]] $_{\alpha}$

 α is evaluated against the following plural assignment:

G	1	2
g ₁	$boy_1'\\boy_2'$	
g 47	 boy ₄₇	

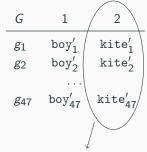
(22) The boys all λ_1 [t_1 flew kites[+pl]] $_{\alpha}$

 α is evaluated against the following plural assignment:

G	1	2
g ₁	$\mathtt{boy}_1'\\\mathtt{boy}_2'$	$\begin{array}{c} \mathtt{kite}_{11}' \oplus \mathtt{kite}_{12}' \\ \mathtt{kite}_{21}' \end{array}$
g 47	boy' ₄₇	kite ₄₇

(22) The boys all λ_1 [t_1 flew kites[+pl]] α

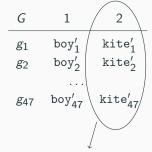
 α is evaluated against the following plural assignment:



[+pl] checks if sum of referents in column 1 isn't a singularity

(23) The boys all λ_1 [t_1 flew ten kites[+pl]] α

 α is evaluated against the following plural assignment:



[+pl] checks if column forms a plurality

(23) The boys all λ_1 [t_1 flew ten kites[+pl]] α

 α is evaluated against the following plural assignment:

G	1	2	Evaluation
g ₁ g ₂	$\begin{array}{c} \mathtt{boy}_1' \\ \mathtt{boy}_2' \end{array}$	kite' ₁ kite' ₂	$#g_1(2) = 10$ $#g_2(2) = 10$
g 47	 boy ₄₇	\mathtt{kite}_{47}'	$\#g_{47}(47) = 10$

ALL has the same meaning as \emph{all} . It splits the assignment function

(24) ALL₁ [either it made them₁ sick or it made them₁ sleepy.]_{α} Input assignment to the sentence:

$$G \qquad 1$$

$$g_1 \qquad p_1 \oplus \ldots \oplus p_{12}$$

(24) ALL₁ [either it made them₁ sick or it made them₁ sleepy.]_{α} Input assignment to α :

$$\begin{array}{c|cc}
G & 1 \\
\hline
g_1 & p_1 \\
g_2 & p_2 \\
& \cdots \\
g_{12} & p_{12}
\end{array}$$

 \rightsquigarrow presupposition of [+pl] on pronouns is satisfied, presupposition of [+sg] isn't.

 $^{^5}$ Compositionally, for this analysis to go through, we need to treat a special version of plural logic disjunction, called "splitjunction". Ask me or cf Champollion (2016) for more details

(24) ALL₁ [either it made them₁ sick or it made them₁ sleepy.]_{α} Input assignment to α :

G	1	Evaluation ⁵
g ₁ g ₂	<i>p</i> ₁ <i>p</i> ₂	it made $g_1(1)$ sick or it made $g_1(1)$ sleepy it made $g_2(1)$ sick or it made $g_2(1)$ sleepy
<i>g</i> 12	 p ₁₂	it made $g_{12}(1)$ sick or it made $g_{12}(1)$ sleepy

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(24) ALL₁ [either it made them₁ sick or it made them₁ sleepy.]_{α} Input assignment to α :

G	1	Evaluation ⁵
g ₁	p_1	it made p_1 sick or it made p_1 sleepy
g ₂	p_2	it made p_2 sick or it made p_2 sleepy
g 12	p_{12}	it made p_{12} sick or it made p_{12} sleepy

 \iff for each p_i , either it made p_i sick or it made p_i sleepy.

 $^{^5}$ Compositionally, for this analysis to go through, we need to treat a special version of plural logic disjunction, called "splitjunction". Ask me or cf Champollion (2016) for more details

(25) ALL1 [either they1 have finished their1 ration boxes2 or they1 lost them2 to mountain lions] $_{\alpha}$

G	1	2
g ₁ g ₂	$\begin{array}{c} \mathtt{participant}_1' \\ \mathtt{participant}_2' \end{array}$	$\begin{array}{c} \texttt{ration-box}_1' \\ \texttt{ration-box}_2' \end{array}$
<i>g</i> 12	$\begin{array}{c} \dots \\ \text{participant}_{12}' \end{array}$	$\mathtt{ration\text{-}box}_{12}'$

(25) ALL₁ [either they₁ have finished their₁ ration boxes₂ or they₁ lost them₂ to mountain lions] $_{\alpha}$

G	1	2	Evaluation
g ₁	$\mathtt{participant}_1'$	$\texttt{ration-box}_1'$	either $g_1(1)$ finished $g_1(2)$ or $g_1(1)$ lost $g_1(2)$
g ₂	participant' ₂	$ration-box_2'$	either $g_2(1)$ finished $g_2(2)$ or $g_2(1)$ lost $g_2(2)$
<i>g</i> 12	participant' ₁₂	$\mathtt{ration\text{-}box}_{12}'$	either $g_{12}(1)$ finished $g_{12}(2)$ or $g_{12}(1)$ lost $g_{12}(2)$

(25) ALL₁ [either they₁ have finished their₁ ration boxes₂ or they₁ lost them₂ to mountain lions] $_{\alpha}$

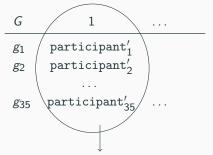
G	1	2	Evaluation
g ₁	$\mathtt{participant}_1'$	$\texttt{ration-box}_1'$	either participant 1 finished ration box 1 or
g ₂	participant' ₂	$ration-box_2'$	either participant 2 finished ration box 2 or
g 12	participant' ₁₂	$\mathtt{ration\text{-}box}_{12}'$	either participant 12 finished ration box 12 or

 \iff for each participant p_i , either p_i finished r_i or p_i lost r_i .

- (26) a. ALL_1 [they₁ were sick] or [they₁ were sleepy]
 - b. ALL₁ [the participants₁ were sick] or [they₁ were sleepy]
- (27) a. $pro[+pl]_1$ presupposes that the sum of referents in column 1 is a plurality
 - b. the participants₁ presupposes that the sum of referents in column 1 is the maximal sum of participants.

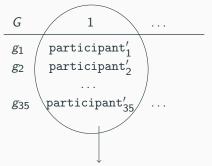
In some sense, referential expressions can act as "pronominal features".

(28) ALL_1 [they₁ were sick] or [they₁ were sleepy]



[+pl] presupposes that the sum of referents in column 1 is a plurality.

(29) ALL₁ [the participants₁ were sick] or [they₁ were sleepy]



"the participants" presupposes that the sum of referents in column 1 is the maximal sum of participants.

Recap

➤ **Initial puzzle:** non-clause-bound distributive readings of referential expressions

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Recap

- ➤ Initial puzzle: non-clause-bound distributive readings of referential expressions
- ➤ Illuminating paradox: pronouns in WSD sentences have singular reference but seem to license dependent plurals.
- > Suggested solution: covert index-based ALL operator
- > Extending to all referential expressions: referential expressions may act as pronouns, contributing their content as a presupposition.

Future questions

- ➤ How do we deal with cases of first-mention definite descriptions in WSD sentences?
- ➤ More complicated cases:
- (30) a. Context: This year at the G7 summit, all Japanese ministers met their French counterparts. The meetings happened in different rooms.
 - b. When the French ministers arrived, the Japanese ministers greeted them in French
 - c. **Reading:** for each specialty *s*, when the French minister of *s* arrived, the Japanese minister of *s* greeted him in French.

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Annex

Other WSD cases

- (31) a. **Context:** the employees have different work hours and do not all arrive at the same time.
 - b. When these employees arrived this morning, Alex smiled. (but she didn't smile when those ones did.)

(32) a. Pretext:

- _ Today was crazy; I had three classes and in each class, there was an arrogant mathematician in the back asking obnoxious technical questions.
- _ Well, how did you deal with them?
- b. I put on the board a problem that they could not solve. (In my experience, that's the most effective way to shut them up.)

- (33) a. **Context:** Speaker is organizing the presidential debate; she has to make sure that the candidates' every wish are granted; otherwise, she'll be accused of favoring one over the other
 - b. Unless Clinton and Trump ask me to, I won't give them water bottles.

Problematic singular cases for Sudo (2014)

Subject position

- (34) a. **Context:** I asked ten people to test my new video game. Because the first level is hard, they start the game with a randomly selected bonus in their inventory
 - b. \checkmark The items that the player started with helped them defeat the dragon
 - c. ✓ The item_ that the players started with helped them defeat the dragon in the first level.

Problematic cases

Object position

- (35) a. **Context:** I asked ten people to test my new video game. Because the first level is hard, they start the game with a randomly selected bonus in their inventory
 - b. The item that gave the players the most advantage wasn't the one that I placed in their inventory.

By contrast, functional RCs show a subject/object asymmetry (Sharvit, 1999).

(36)
$$[ALL_i](G)(G') =$$
true iff

a.
$$\bigoplus_{g \in G} g(i) = \bigoplus_{g \in G'} g'(i)$$

b. for all $g' \in G'$, there exists $g \in G$, g = g' and g'(i) is an atom.