Team notebook

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1 Data Structures

1.1 2D Segment Tree

```
struct Segtree2D {
   struct segtree {
       struct node {
        int 1, r, val;
        node *lc, *rc;
        node(int _l, int _r, int _val = INF) : l(_l), r(_r), val(_val),
        lc(NULL), rc(NULL) {}
   };
   typedef node* pnode;
   pnode root;
```

```
Segtree(int 1, int r) { root = new node(1, r); }
    void update(pnode &nw. int x. int val) {
       int 1 = nw - > 1, r = nw - > r, mid = (1+r)/2;
       if(1 == r) {
           nw->val = val;
       } else {
           assert(1 <= x && x <= r):
           pnode &child = x <= mid ? nw->lc : nw->rc;
           if(!child) {
              child = new node(x, x, val);
           else if(child->1 \le x \&\& x \le child->r)
               update(child, x, val):
           else {
              do {
                  if(x \le mid) r = mid;
                  else 1 = mid+1;
                  mid = (1+r)/2:
              } while((x <= mid) == (child->1 <= mid));</pre>
               pnode nxt = new node(1, r);
               if(child->l <= mid) nxt->lc = child;
               else nxt->rc = child;
               child = nxt:
              update(nxt, x, val);
           nw->val = min(nw->lc ? nw->lc->val : INF,
                  nw->rc ? nw->rc->val : INF);
    int query(pnode &nw, int x1, int x2) {
       if(!nw) return INF;
       int &1 = nw->1, &r = nw->r;
       if(r < x1 || x2 < 1) return INF;</pre>
       if(x1 <= 1 && r <= x2) {</pre>
           return nw->val;
       int ret = min(query(nw->lc, x1, x2),
              query(nw->rc, x1, x2));
       return ret;
   void update(int x, int val) {
       assert(root->1 <= x && x <= root->r);
       update(root, x, val);
   }
    int query(int 1, int r) {
       return query(root, 1, r);
};
struct node {
   int 1, r;
    Segtree v;
   node *lc, *rc;
   node(int _1, int _r) : 1(_1), r(_r), y(0, MAX),
   lc(NULL), rc(NULL) {}
};
```

```
typedef node* pnode;
   pnode root:
   Segtree2D(int 1, int r) { root = new node(1, r); }
   void update(pnode &nw, int x, int y, int val) {
       int &1 = nw - >1, &r = nw - >r, mid = (1+r)/2;
       if(1 == r) nw->y.update(y, val);
      else {
          if(x \le mid) \{
              if(!nw->lc) nw->lc = new node(1, mid);
              update(nw->lc, x, y, val);
          } else {
              if(!nw->rc) nw->rc = new node(mid+1, r);
              update(nw->rc, x, y, val);
          val = min(nw->lc ? nw->lc->y.query(y, y) : INF,
                 nw->rc ? nw->rc->y.query(y, y) : INF);
          nw->y.update(y, val);
   int query(pnode &nw, int x1, int x2, int y1, int y2) {
       if(!nw) return INF;
       int &1 = nw->1, &r = nw->r;
       if(r < x1 || x2 < 1) return INF;</pre>
       if(x1 <= 1 && r <= x2) return nw->y.query(y1, y2);
       int ret = min(query(nw->lc, x1, x2, y1, y2),
              query(nw->rc, x1, x2, y1, y2));
       return ret;
   void update(int x, int y, int val) {
      assert(root->1 <= x && x <= root->r);
       update(root, x, y, val);
   }
   int query(int x1, int x2, int y1, int y2) {
      return query(root, x1, x2, y1, y2);
};
```

1.2 Heavy-Light Decomposition

```
#define N 300020
vector<int> adj[N];
int memo[25][N], lvl[N], subsize[N], col[N]; //col=array input
int chainHead[N], chainInd[N], baseArray[N], posInBase[N];
int chainNo, p, n;//chainHead=nodeHead,baseArray=array tree, int st[N*4]; //posInBase=convert input
    to tree indelax
void buildtree(int v, int l, int r){
    if (1 == r){
        st[v] = baseArray[l];
        return;
}
```

```
int m = (1+r) >> 1;
   buildtree(v<<1.1.m):
   buildtree(v<<1|1,m+1,r);
   st[v] = st[v << 1] + st[v << 1|1];
void updatetree(int v, int 1, int r, int x){
   if(1 == r){
       st[v] = baseArray[x]; return;
   int m = (1+r) >> 1;
   if(x <= m) updatetree(v<<1,1,m,x);</pre>
   else updatetree(v<<1|1.m+1.r.x):</pre>
   st[v] = st[v << 1] + st[v << 1|1];
int querytree(int v, int 1, int r, int ss, int se){
   if(ss > se) return 0;
   if (1 == ss && r == se) return st[v]:
   int m = (1+r) >> 1;
   int ans = querytree(v << 1, 1, m, ss, min(se,m)) + querytree(v << 1|1, m+1, r, max(m+1,ss), se);
   return ans:
void dfs(int cur. int par){
   lvl[cur] = lvl[par]+1;
   memo[0][cur] = par;
   subsize[cur] = 1;
   for(int to : adj[cur]){
       if (to == par) continue;
       dfs(to,cur);
       subsize[cur] += subsize[to];
   }
void HLD(int cur, int par){
   if(chainHead[chainNo] == -1) chainHead[chainNo] = cur;
   chainInd[cur] = chainNo;
   baseArray[p] = col[cur];
   posInBase[cur] = p++;
   int maksto = -1;
   for(int to : adj[cur]){
       if (to == par) continue;
       if (maksto == -1 || subsize[maksto] < subsize[to]){</pre>
           maksto = to;
   if (maksto != -1) HLD(maksto,cur);
   for(int to : adj[cur]){
       if (to == par || to == maksto) continue;
       chainNo++:
       HLD(to,cur);
}
int queryup(int u, int v){
   int ans = 0;
   while(u != v){
       if (chainInd[u] == chainInd[v]){
           ans += querytree(1,0,n-1,posInBase[v]+1,posInBase[u]);
       } else {
           ans += guervtree(1.0.n-1. posInBase[chainHead[chainInd[u]]] .posInBase[u]):
```

```
u = chainHead[chainInd[u]];
u = memo[0][u];
}

return ans;
}

int main()
{
    rep(i,0,n-1){ //init
        col[i] = s[i]-'0';
        chainHead[i] = -1;
        adj[i].clear();
}
    chainNo = p = 0;
    // add edge here
    dfs(0,0); // 0-based
    sparsing();
    HLD(0,0);
    buildtree(1,0,n-1);
    return 0;
}
```

1.3 Li Chao Tree

```
typedef long long int TD;
const TD INF = 10000000000000;
namespace LICHAO {
   struct Node {
       TD m, c;
       Node *1. *r:
   Node *newNode(Node *x = NULL) {
       Node *ret = (Node*)malloc(sizeof(Node));
       if (x) ret->m = x->m, ret->c = x->c;
       ret->1 = ret->r = NULL:
       return ret;
   void update(Node *k, TD 1, TD r, TD m, TD c) {
       TD mid = 1 + r >> 1;
       bool le = m*l + c < k->m*l + k->c:
       bool ri = m*mid + c < k->m*mid + k->c;
       if (ri) swap(k\rightarrow m, m), swap(k\rightarrow c, c);
       if (r - 1 <= 1) return;</pre>
       else if (le != ri) update((k->1)?(k->1):(k->1=newNode(k)), 1, mid, m, c);
       else update((k->r)?(k->r):(k->r=newNode(k)), mid, r, m, c);
   TD query(Node *k, TD 1, TD r, TD p) {
       if (!k) return INF;
       if (r - 1 <= 1) return p*k->m + k->c;
       if (p < (1+r >> 1)) return min(p*k->m + k->c, query(k->1, 1, 1+r>>1, p));
       else return min(p*k->m + k->c, query(k->r, 1+r>>1, r, p));
}
```

3

1.4 Persistent Segment Tree

```
class PersistentSegtree {
   private:
       int n, ptr, sz;
       struct P {
           int val = 0, 1, r;
       };
       vector<P> node;
       vector<int> root;
       int newNode() { return ptr++; }
       int copyNode(int idx) {
           node[ptr] = node[idx];
           return ptr++;
       int build(int 1, int r) {
           int idx = newNode();
           if(1 == r) return idx;
           node[idx].1 = build(1, (1+r)/2);
           node[idx].r = build((1+r)/2+1, r);
           return idx;
       int update(int idx, int 1, int r, int x, int val) {
           idx = copyNode(idx);
           if(1 == r) {
              node[idx].val += val;
              return idx;
          }
           int mid = (1+r)/2;
           if(x <= mid) node[idx].1 = update(node[idx].1, 1, mid, x, val);</pre>
           else node[idx].r = update(node[idx].r, mid+1, r, x, val);
           node[idx].val = node[node[idx].1].val + node[node[idx].r].val;
           return idx;
       int query(int idxl, int idxr, int l, int r, int x, int y) {
           if(y < 1 \mid | r < x) return 0;
           if(x <= 1 && r <= y) return node[idxr].val - node[idxl].val;</pre>
           int mid = (1+r)/2;
           return query(node[idxl].1, node[idxr].1, 1, mid, x, y)
              + query(node[idxl].r, node[idxr].r, mid+1, r, x, y);
   public:
       PersistentSegtree(int _n) : n(_n), ptr(0) {
           sz = 30 * n;
           node.resize(sz);
           root.push_back(build(1, n));
       void update(int x, int val) {
           root.push_back(update(root.back(), 1, n, x, val));
       int query(int 1, int r, int x, int y) {
           return query(root[1-1], root[r], 1, n, x, y);
};
```

1.5 STL PBDS

1.6 Treap

```
// Complexity: O(log N) for split and merge
// empty treap: Treap* tr = nullptr;
// insert v at x: [1, r] = split(tr, x), m = Treap(v), merge lmr
// delete at x: [l, r] = split(tr, x), [m, r] = split(r, 1), merge lr
// lazy prop: propagate every time a node is accessed
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
using Key = int;
struct Treap
   Key val;
   Treap* left;
   Treap* right;
   int prio, sz;
   Treap() {}
   Treap(int _val);
int size(Treap* tr)
   return tr ? tr->sz : 0;
void update(Treap* tr)
   tr->sz = 1 + size(tr->left) + size(tr->right);
Treap::Treap(Key _val) :
   val(_val), left(nullptr), right(nullptr), prio(rng())
   update(this);
pair<Treap*, Treap*> split(Treap* tr, int sz)
```

```
if(!tr) return {nullptr, nullptr};
   int left_sz = size(tr->left);
   if(sz <= left_sz)</pre>
       auto [left, mid] = split(tr->left, sz);
       tr->left = mid;
       update(tr):
       return {left, tr};
   else
       auto [mid, right] = split(tr->right, sz - left_sz - 1);
       tr->right = mid:
       update(tr);
       return {tr, right};
}
Treap* merge(Treap* 1, Treap* r)
   if(!1) return r;
   if(!r) return 1;
   if(l->prio < r->prio)
       1->right = merge(1->right, r);
       update(1);
       return 1;
   else
       r->left = merge(1, r->left);
       update(r);
       return r;
   }
}
```

1.7 Unordered Map Custom Hash

```
struct custom_hash {
    static uint64_t splitmix64(uint64_t x) {
        x += 0x9e3779b97f4a7c15;
        x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
        x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
        return x ^ (x >> 31);
    }
    size_t operator()(uint64_t x) const {
        static const uint64_t FIXED_RANDOM = chrono::steady_clock::now().time_since_epoch().count();
        return splitmix64(x + FIXED_RANDOM);
    }
};
unordered_map<int, int, custom_hash> umap;
```

2 Dynamic Programming

2.1 DP Convex Hull

```
/* dp[i] = min k<i {dp[k] + x[i]*m[k]}
   Make sure gradient (m[i]) is either non-increasing if min,
   or non-decreasing if max. x[i] must be non-decreasing. just sort */
int y[N], m[N];
// while this is true, pop back from dq. a=new line, b=last, c=2nd last
bool cekx(int a, int b, int c){
   // if not enough, change to cross mul
   // if cross mul, beware of negative denominator, and overflow
   return (double)(y[b]-y[a])/(m[a]-m[b])<=(double)(y[c]-y[b])/(m[b]-m[c]);
}</pre>
```

5

2.2 DP DNC

```
void f(int rem,int 1,int r,int opt1,int optr){
    if(1>r)return;
    int mid = 1+r>>1;
    int opt = MOD, optid = mid;
    for(int i = opt1; i<=mid && i<=optr; ++i){
        if(dp[rem-1][i] + c[i][mid] < opt){
            opt = dp[rem-1][i] + c[i][mid];
            optid = i;
        }
    }
    dp[rem][mid] = opt;
    f(rem, 1, mid-1, opt1, optid);
    f(rem, mid+1, r, optid, optr); return;
}
rep(i,1,n)dp[1][i] = c[0][i];
rep(i,2,k)f(i,i,n,i,n);</pre>
```

2.3 Knuth-Yao

.

3 Geometry

3.1 Closest Pair of Points

```
#define fi first
#define se second
typedef pair<int, int> pii;
struct Point{
   int x, y, id;
int compareX(const void* a, const void* b){
   Point *p1 = (Point *)a, *p2 = (Point *)b;
   return (p1->x - p2->x);
int compareY(const void* a, const void* b){
   Point *p1 = (Point *)a, *p2 = (Point *)b;
   return (p1->y - p2->y);
double dist(Point p1, Point p2) {
   return sqrt( (double)(p1.x - p2.x)*(p1.x - p2.x) +
               (double)(p1.y - p2.y)*(p1.y - p2.y)
pair<pii, double> bruteForce(Point P[], int n){
   double min = 1e8:
   pii ret=pii(-1, -1);
   for (int i = 0; i < n; ++i)
       for (int j = i+1; j < n; ++j)
           if (dist(P[i], P[j]) < min){</pre>
              ret=pii(P[i].id, P[j].id);
              min = dist(P[i], P[j]);
   return pair<pii, double> (ret, min);
pair<pii, double> getmin(pair<pii, double> x, pair<pii, double> y){
   if(x.fi.fi==-1 && x.fi.se==-1) return y;
   if(v.fi.fi==-1 && v.fi.se==-1) return x;
   return (x.se < y.se)? x : y;
pair<pii, double> stripClosest(Point strip[], int size, double d){
   double min = d:
   pii ret=pii(-1, -1);
   gsort(strip, size, sizeof(Point), compareY);
   for (int i = 0; i < size; ++i)</pre>
       for (int j = i+1; j < size && (strip[j].y - strip[i].y) < min; ++j)
           if (dist(strip[i],strip[j]) < min){</pre>
              ret=pii(strip[i].id, strip[j].id);
              min = dist(strip[i], strip[j]);
   return pair<pii, double>(ret, min);
pair<pii, double> closestUtil(Point P[], int n){
   if (n <= 3) return bruteForce(P, n);</pre>
   int mid = n/2;
```

```
Point midPoint = P[mid];
   pair<pii, double> dl = closestUtil(P, mid);
   pair<pii, double> dr = closestUtil(P + mid, n-mid);
   pair<pii, double> d = getmin(dl, dr);
   Point strip[n];
   int j = 0;
   for (int i = 0; i < n; i++)</pre>
       if (abs(P[i].x - midPoint.x) < d.second)</pre>
          strip[j] = P[i], j++;
   return getmin(d, stripClosest(strip, j, d.second));
pair<pii, double> closest(Point P[], int n){
   qsort(P, n, sizeof(Point), compareX);
   return closestUtil(P, n);
Point P[50005];
int main(){
   int n;
   scanf("%d", &n);
   for(int a=0;a<n;a++){</pre>
       scanf("%d%d", &P[a].x, &P[a].y);
       P[a].id=a;
   pair<pii, double> hasil=closest(P, n);
   if(hasil.fi.fi > hasil.fi.se) swap(hasil.fi.fi, hasil.fi.se);
   printf("%d %d %.6lf\n", hasil.fi.fi, hasil.fi.se, hasil.se);
   return 0;
```

3.2 Convex Hull

```
typedef double TD;
                              // for precision shits
namespace GEOM {
   typedef pair<TD,TD> Pt;
                                // vector and points
   const TD EPS = 1e-9;
   const TD maxD = 1e9:
   TD cross(Pt a, Pt b, Pt c) { // right hand rule
      TD v1 = a.first - c.first; // (a-c) X (b-c)
      TD v2 = a.second - c.second;
      TD u1 = b.first - c.first;
      TD u2 = b.second - c.second:
      return v1 * u2 - v2 * u1;
   TD cross(Pt a, Pt b) {
                              // a X b
      return a.first*b.second - a.second*b.first;
   TD dot(Pt a, Pt b, Pt c) { // (a-c) . (b-c)
      TD v1 = a.first - c.first:
      TD v2 = a.second - c.second:
      TD u1 = b.first - c.first;
      TD u2 = b.second - c.second:
      return v1 * u1 + v2 * u2:
   TD dot(Pt a, Pt b) {
       return a.first*b.first + a.second*b.second;
```

```
7
```

```
TD dist(Pt a, Pt b) {
    return sqrt((a.first-b.first)*(a.first-b.first) + (a.second-b.second)*(a.second-b.second));
TD shoelaceX2(vector<Pt> &convHull) {
    TD ret = 0:
   for (int i = 0, n = convHull.size(); i < n; i++)</pre>
       ret += cross(convHull[i], convHull[(i+1)%n]);
vector<Pt> createConvexHull(vector<Pt> &points) {
    sort(points.begin(), points.end());
    vector<Pt> ret;
   for (int i = 0; i < points.size(); i++) {</pre>
       while (ret.size() > 1 &&
              cross(points[i], ret[ret.size()-1], ret[ret.size()-2]) < -EPS)</pre>
           ret.pop_back();
       ret.push_back(points[i]);
   for (int i = points.size() - 2, sz = ret.size(); i >= 0; i--) {
       while (ret.size() > sz &&
              cross(points[i], ret[ret.size()-1], ret[ret.size()-2]) < -EPS)</pre>
           ret.pop_back();
       if (i == 0) break;
       ret.push_back(points[i]);
   return ret:
    bool isInside(Pt pv, vector<Pt> &x){//using winding number
       int n = x.size(), wn = 0;
       x.push_back(x[0]);
       for(int i = 0; i<n; ++i){</pre>
           if(((x[i+1].first<=pv.first&&x[i].first>=pv.first)||
                      (x[i+1].first>=pv.first&&x[i].first<=pv.first)) &&</pre>
                   ((x[i+1].second<=pv.second&&x[i].second>=pv.second)||
                    (x[i+1].second>=pv.second&&x[i].second<=pv.second)) ){</pre>
               if(cross(x[i],x[i+1],pv) == 0){
                  x.pop_back();
                  return true;
              }
          }
       for(int i = 0; i<n; ++i){</pre>
           if(x[i].second <= pv.second) {</pre>
              if(x[i+1].second>pv.second && cross(x[i],x[i+1],pv)>0)++wn;
           else if(x[i+1].second<=pv.second && cross(x[i],x[i+1],pv)<0)--wn;</pre>
       x.pop_back();
       return wn!=0:
bool isInside(Pt pv, vector<Pt> &x){//using winding number
   int n = x.size(), wn = 0;
   x.push_back(x[0]);
    for(int i = 0; i<n; ++i){</pre>
       if(((x[i+1].first<=pv.first&&x[i].first>=pv.first)||
                   (x[i+1].first>=pv.first&&x[i].first<=pv.first)) &&
               ((x[i+1].second<=pv.second&&x[i].second>=pv.second)||
                (x[i+1].second>=pv.second&&x[i].second<=pv.second)) ){
```

3.3 Geometry Template

```
TABLE OF CONTENT
O. Basic Rule
   0.1. Everything is in double
   0.2. Every comparison use EPS
   0.3. Every degree in rad
1. General Double Operation
   1.1. const double EPS=1E-9
   1.2. const double PI=acos(-1.0)
   1.3. const double INFD=1E9
   1.3. between_d(double x,double 1,double r)
       check whether x is between 1 and r inclusive with EPS
   1.4. same_d(double x,double y)
       check whether x=y with EPS
   1.5. dabs(double x)
       absolute value of x
2. Point
   2.1. struct point
       2.1.1. double x, y
           cartesian coordinate of the point
       2.1.2. point()
           default constructor
       2.1.3. point(double x.double v)
           constructor, set the point to (_x,_y)
       2.1.4. bool operator< (point other)
           regular pair < double, double > operator < with EPS
       2.1.5. bool operator == (point other)
           regular pair < double, double > operator == with EPS
   2.2. hypot(point P)
       length of hypotenuse of point P to (0,0)
   2.3. e_dist(point P1,point P2)
       euclidean distance from P1 to P2
   2.4. m_dist(point P1,point P2)
       manhattan distance from P1 to P2
   2.5. point rotate(point P,point O,double angle)
       rotate point P from the origin O by angle ccw
3. Vector
   3.1. struct vec
```

```
8
```

```
3.1.1. double x,y
           x and y magnitude of the vector
       3.1.2. vec()
           default constructor
       3.1.3. vec(double _x,double _y)
           constructor, set the vector to (_x,_y)
       3.1.4. vec(point A, point B)
           constructor, set the vector to vector AB (A->B)
/*General Double Operation*/
const double PI=acos(-1.0);
const double INFD=1E9:
double between_d(double x,double 1,double r) {
   return (min(1,r) \le x + EPS \&\& x \le max(1,r) + EPS);
double same_d(double x,double y) {
   return between_d(x,y,y);
double dabs(double x) {
   if (x<EPS) return -x; return x;</pre>
/*Point*/
struct point {
   double x,y;
   point() {
       x=y=0.0;
   point(double _x,double _y) {
       x=_x; y=_y;
   bool operator< (point other) {</pre>
       if (x<other.x+EPS) return true;</pre>
       if (x+EPS>other.x) return false;
       return y<other.y+EPS;</pre>
   bool operator== (point other) {
       return same_d(x,other.x)&&same_d(y,other.y);
};
double e_dist(point P1,point P2) {
   return hypot(P1.x-P2.x,P1.y-P2.y);
double m_dist(point P1,point P2) {
   return dabs(P1.x-P2.x)+dabs(P1.y-P2.y);
double pointBetween(point P,point L,point R) {
   return (e_dist(L,P)+e_dist(P,R)==e_dist(L,R));
bool collinear(point P, point L, point R) { //newly added(luis), cek 3 poin segaris
   return P.x*(L.y-R.y)+L.x*(R.y-P.y)+R.x*(P.y-L.y)==0; // bole gnti dabs(x)<EPS
}
/*Vector*/
struct vec {
   double x, y;
   vec() {
       x=y=0.0;
   vec(double _x,double _y) {
```

```
x=_x; y=_y;
   vec(point A) {
       x=A.x; y=A.y;
   vec(point A,point B) {
       x=B.x-A.x; y=B.y-A.y;
};
vec scale(vec v,double s) {
   return vec(v.x*s,v.y*s);
vec flip(vec v) {
   return vec(-v.x,-v.y);
double dot(vec u,vec v) {
   return (u.x*v.x+u.y*v.y);
double cross(vec u.vec v) {
   return (u.x*v.y-u.y*v.x);
double norm_sq(vec v) {
   return (v.x*v.x+v.y*v.y);
point translate(point P,vec v) {
   return point(P.x+v.x,P.y+v.y);
point rotate(point P,point O,double angle) {
   vec v(0); P=translate(P,flip(v));
   return translate(point(P.x*cos(angle)-P.y*sin(angle),P.x*sin(angle)+P.y*cos(angle)),v);
point mid(point P,point Q) {
   return point((P.x+Q.x)/2,(P.y+Q.y)/2);
double angle(point A,point O,point B) {
   vec OA(O,A), OB(O,B);
   return acos(dot(OA,OB)/sqrt(norm_sq(OA)*norm_sq(OB)));
int orientation(point P,point Q,point R) {
   vec PQ(P,Q), PR(P,R);
   double c=cross(PQ,PR);
   if (c<-EPS) return -1;</pre>
   if (c>EPS) return 1;
   return 0;
/*Line*/
struct line {
   double a,b,c;
   line() {
       a=b=c=0.0;
   line(double _a,double _b,double _c) {
       a=_a; b=_b; c=_c;
   line(point P1, point P2) {
       if (P1<P2) swap(P1,P2);</pre>
       if (same_d(P1.x,P2.x)) a=1.0, b=0.0, c=-P1.x;
       else a=-(P1.y-P2.y)/(P1.x-P2.x), b=1.0, c=-(a*P1.x)-P1.y;
   line (point P,double slope) {
```

```
q
```

```
if (same_d(slope,INFD)) a=1.0, b=0.0, c=-P.x;
       else a=-slope, b=1.0, c=-(a*P.x)-P.y;
   bool operator== (line other) {
       return same_d(a,other.a)&&same_d(b,other.b)&&same_d(c,other.c);
   double slope() {
       if (same d(b,0.0)) return INFD:
       return -(a/b);
};
bool paralel(line L1,line L2) {
   return same_d(L1.a,L2.a)&&same_d(L1.b,L2.b);
bool intersection(line L1,line L2,point &P) {
   if (paralel(L1,L2)) return false;
   P.x=(L2.b*L1.c-L1.b*L2.c)/(L2.a*L1.b-L1.a*L2.b);
   if (same_d(L1.b,0.0)) P.y=-(L2.a*P.x+L2.c);
   else P.y=-(L1.a*P.x+L1.c);
   return true;
double pointToLine(point P,point A,point B,point &C) {
   vec AP(A,P), AB(A,B);
   double u=dot(AP,AB)/norm_sq(AB);
   C=translate(A,scale(AB,u));
   return e_dist(P,C);
double lineToLine(line L1,line L2) {
   if (!paralel(L1,L2)) return 0.0;
   return dabs(L2.c-L1.c)/sqrt(L1.a*L1.a+L1.b*L1.b);
/*Line Segment*/
struct segment {
   point P,Q;
   line L:
   segment() {
       point T1; P=Q=T1;
       line T2; L=T2;
    segment(point _P,point _Q) {
       P=_P; Q=_Q;
       if (Q<P) swap(P,Q);</pre>
       line T(P,Q); L=T;
   bool operator== (segment other) {
       return P==other.P&&Q==other.Q;
};
bool onSegment(point P,segment S) {
   if (orientation(S.P,S.Q,P)!=0) return false;
   return between_d(P.x,S.P.x,S.Q.x) && between_d(P.y,S.P.y,S.Q.y);
bool s_intersection(segment S1, segment S2) {
   double o1=orientation(S1.P,S1.Q,S2.P);
   double o2=orientation(S1.P,S1.Q,S2.Q);
   double o3=orientation(S2.P,S2.Q,S1.P);
   double o4=orientation(S2.P,S2.Q,S1.Q);
   if (o1!=o2 && o3!=o4) return true;
   if (o1==0 && onSegment(S2.P,S1)) return true;
   if (o2==0 && onSegment(S2.Q.S1)) return true:
```

```
if (o3==0 && onSegment(S1.P,S2)) return true;
   if (o4==0 && onSegment(S1.Q,S2)) return true;
   return false:
double pointToSegment(point P,point A,point B,point &C) {
   vec AP(A,P), AB(A,B);
   double u=dot(AP,AB)/norm_sq(AB);
   if (u<EPS) {
      C=A; return e_dist(P,A);
   if (u+EPS>1.0) {
      C=B; return e_dist(P,B);
   return pointToLine(P.A.B.C):
double segmentToSegment(segment S1,segment S2) {
   if (s_intersection(S1,S2)) return 0.0;
   double ret=INFD; point dummy;
   ret=min(ret,pointToSegment(S1.P,S2.P,S2.Q,dummy));
   ret=min(ret,pointToSegment(S1.Q,S2.P,S2.Q,dummy));
   ret=min(ret,pointToSegment(S2.P,S1.P,S1.Q,dummy));
   ret=min(ret,pointToSegment(S2.Q,S1.P,S1.Q,dummy));
   return ret;
/*Circle*/
struct circle {
   point P;
   double r;
   circle() {
       point P1; P=P1;
       r=0.0:
   circle(point _P,double _r) {
      P=_P; r=_r;
   circle(point P1,point P2) {
      P=mid(P1,P2); r=e_dist(P,P1);
   circle(point P1,point P2,point P3) {
      vector<point> T; T.clear(); T.pb(P1); T.pb(P2); T.pb(P3);
       sort(T.begin(),T.end());
      P1=T[0]; P2=T[1]; P3=T[2];
      point M1,M2; M1=mid(P1,P2); M2=mid(P2,P3);
      point Q2,Q3; Q2=rotate(P2,P1,PI/2); Q3=rotate(P3,P2,PI/2);
       vec P1Q2(P1,Q2), P2Q3(P2,Q3);
      point M3,M4; M3=translate(M1,P1Q2); M4=translate(M2,P2Q3);
      line L1(M1,M3), L2(M2,M4);
       intersection(L1,L2,P); r=e_dist(P,P1);
   bool operator==(circle other) {
       return (P==other.P && same d(r.other.r)):
bool insideCircle(point P,circle C) {
   return e_dist(P,C.P) <= C.r + EPS;</pre>
bool c_intersection(circle C1, circle C2, point &P1, point &P2) {
   double d=e_dist(C1.P,C2.P);
   if (d>C1.r+C2.r) return false;//d+EPS kalo butuh
   if (d<dabs(C1.r-C2.r)+EPS) return false:
```

```
double x1=C1.P.x, y1=C1.P.y, r1=C1.r, x2=C2.P.x, y2=C2.P.y, r2=C2.r;
   double a=(r1*r1-r2*r2+d*d)/(2*d), h=sqrt(r1*r1-a*a);
   point T(x1+a*(x2-x1)/d.v1+a*(v2-v1)/d):
   P1=point(T.x-h*(y2-y1)/d,T.y+h*(x2-x1)/d);
   P2=point(T.x+h*(y2-y1)/d,T.y-h*(x2-x1)/d);
bool lc intersection(line L.circle O.point &P1.point &P2) {
   double a=L.a, b=L.b, c=L.c, x=0.P.x, y=0.P.y, r=0.r;
   double A=a*a+b*b, B=2*a*b*y-2*a*c-2*b*b*x, C=b*b*x*x+b*b*y*y-2*b*c*y+c*c-b*b*r*r;
   double D=B*B-4*A*C; point T1,T2;
   if (same_d(b,0.0)) {
       T1.x=c/a:
       if (dabs(x-T1.x)+EPS>r) return false:
       if (same_d(T1.x-r-x,0.0) | | same_d(T1.x+r-x,0.0)) {
          P1=P2=point(T1.x,y); return true;
       double dx=dabs(T1.x-x), dy=sqrt(r*r-dx*dx);
       P1=point(T1.x,y-dy); P2=point(T1.x,y+dy); return true;
   if (same d(D,0.0)) {
       T1.x=-B/(2*A); T1.y=(c-a*T1.x)/b; P1=P2=T1; return true;
   if (D<EPS) return false:
   D=sqrt(D);
   T1.x=(-B-D)/(2*A); T1.y=(c-a*T1.x)/b; P1=T1;
   T2.x=(-B+D)/(2*A); T2.y=(c-a*T2.x)/b; P2=T2; return true;
bool sc_intersection(segment S,circle C,point &P1,point &P2) {
   bool cek=lc_intersection(S.L,C,P1,P2);
   if (!cek) return false;
   double x1=S.P.x, y1=S.P.y, x2=S.Q.x, y2=S.Q.y;
   bool b1=between_d(P1.x,x1,x2)&&between_d(P1.y,y1,y2);
   bool b2=between_d(P2.x,x1,x2)&&between_d(P2.y,y1,y2);
   if (P1==P2) return b1:
   if (b1||b2) {
       if (!b1) P1=P2; if (!b2) P2=P1; return true;
   return false;
/*Triangle*/
double t_perimeter(point A,point B,point C) {
   return e_dist(A,B)+e_dist(B,C)+e_dist(C,A);
double t_area(point A,point B,point C) {
   double s=t_perimeter(A,B,C)/2;
   double ab=e_dist(A,B), bc=e_dist(B,C), ac=e_dist(C,A);
   return sqrt(s*(s-ab)*(s-bc)*(s-ac));
circle t_inCircle(point A,point B,point C) {
   vector<point> T; T.clear(); T.pb(A); T.pb(B); T.pb(C); sort(T.begin(),T.end());
   A=T[0]; B=T[1]; C=T[2];
   double r=t_area(A,B,C)/(t_perimeter(A,B,C)/2);
   double ratio=e_dist(A,B)/e_dist(A,C);
   vec BC(B,C); BC=scale(BC,ratio/(1+ratio));
   point P; P=translate(B,BC); line AP1(A,P);
   ratio=e_dist(B,A)/e_dist(B,C);
   vec AC(A,C); AC=scale(AC,ratio/(1+ratio));
   P=translate(A,AC); line BP2(B,P);
   intersection(AP1.BP2.P): return circle(P.r):
```

```
circle t_outCircle(point A,point B,point C) {
   return circle(A.B.C);
/*Polygon*/
struct polygon {
   vector<point> P;
   polygon() {
      P.clear();
   polygon(vector<point> &_P) {
      P = P;
}:
bool rayCast(point P,polygon &A) {
   point Q(P.x,10000);
   line cast(P,Q);
   int cnt=0;
   FOR(i,(int)(A.P.size())-1){
      line temp(A.P[i],A.P[i+1]);
      point I;
       bool B=intersection(cast,temp,I);
       if (!B) continue;
       else if (I==A.P[i]||I==A.P[i+1]) continue;
       else if (pointBetween(I,A.P[i],A.P[i+1])&&pointBetween(I,P,Q)) cnt++;
   return cnt%2==1;
// line segment p-q intersect with line A-B.
point lineIntersectSeg(point p, point q, point A, point B) {
   double a = B.y - A.y;
   double b = A.x - B.x;
   double c = B.x * A.y - A.x * B.y;
   double u = fabs(a * p.x + b * p.y + c);
   double v = fabs(a * q.x + b * q.y + c);
   return point((p.x * v + q.x * u) / (u + v),(p.y * v + q.y * u) / (u + v));
// cuts polygon Q along the line formed by point a -> point b
// (note: the last point must be the same as the first point)
vector<point> cutPolygon(point a, point b, const vector<point> &Q) {
   vector<point> P;
   for (int i=0;i<(int)Q.size();i++) {</pre>
      double left1 = cross(toVec(a,b),toVec(a,Q[i]));
      double left2 = 0;
       if (i!=(int)Q.size()-1) left2 = cross(toVec(a,b),toVec(a,Q[i+1]));
       if (left1 > -EPS) P.push_back(Q[i]);
       if (left1*left2 < -EPS) {</pre>
          P.push_back(lineIntersectSeg(Q[i],Q[i+1],a,b));
      }
   if (!P.empty() && !(P.back()==P.front())) {
      P.push_back(P.front());
   }
   return P:
circle minCoverCircle(polygon &A) {
   vector<point> p=A.P;
   point c; circle ret;
   double cr = 0.0;
   int i. i. k:
```

```
c = p[0];
   for(i = 1; i < p.size(); i++) {</pre>
       if(e_dist(p[i], c) >= cr+EPS) {
           c = p[i], cr = 0;
          ret=circle(c,cr);
           for(j = 0; j < i; j++) {</pre>
              if(e_dist(p[j], c) >= cr+EPS) {
                  c=mid(p[i],p[j]);
                  cr = e_dist(p[i], c);
                  ret=circle(c,cr);
                  for(k = 0; k < j; k++) {
                      if(e_dist(p[k], c) >= cr+EPS) {
                         ret=circle(p[i],p[j],p[k]);
                          c=ret.P; cr=ret.r;
                 }
             }
          }
      }
   }
   return ret;
/*Geometry Algorithm*/
double DP[110][110];
double minCostPolygonTriangulation(polygon &A) {
   if (A.P.size()<3) return 0;</pre>
   FOR(i,A.P.size()) {
          for (int j=0,k=i;k<A.P.size();j++,k++) {</pre>
             if (k<j+2) DP[j][k]=0.0;</pre>
             else {
              DP[j][k]=INFD;
              REP(1,j+1,k-1) {
                  double cost=e_dist(A.P[j],A.P[k])+e_dist(A.P[k],A.P[1])+e_dist(A.P[1],A.P[j]);
                  DP[j][k]=min(DP[j][k],DP[j][1]+DP[1][k]+cost);
              }
          }
   return DP[0][A.P.size()-1];
```

3.4 Smallest Enclosing Circle

```
// Welzl's algorithm to find the smallest circle
// that encloses a group of poins in O(N * ITERS)
// returns {radius, x, y}
const int ITERS = 3e5;
const double INF = 1e12;

tuple<double, double, double> welzl(const vector<pair<int, int>>& points)
{
    double xt = 0, yt = 0;
    for(auto& [x, y] : points)
    {
        xt += x;
        yt += y;
    }
}
```

```
xt /= points.size();
yt /= points.size();
double p = 0.1;
double mx_d;
for(int i = 0; i < ITERS; ++i)</pre>
   mx d = -INF:
   int mx_idx = -1;
   for(int j = 0; j < (int) points.size(); ++j)</pre>
       double cx = xt - points[j].first;
       double cy = yt - points[j].second;
       double cur = cx * cx + cy * cy;
       if(cur > mx_d)
           mx_d = cur;
           mx_idx = j;
   xt += (points[mx_idx].first - xt) * p;
   yt += (points[mx_idx].second - yt) * p;
   p *= 0.999;
return {sqrt(mx_d), xt, yt};
```

3.5 Sutherland-Hodgman Algorithm

```
// Complexity: linear time
// Ada 2 poligon, cari poligon intersectionnya
// poly_point = hasilnya, clipper = pemotongnya
#include<bits/stdc++.h>
using namespace std;
const double EPS = 1e-9;
struct point{
   double x,y;
   point(double _x,double _y):x(_x),y(_y){}
struct vec {
   double x,y;
   vec(double _x, double _y):x(_x),y(_y){}
};
point pivot(0,0);
vec toVec(point a, point b){
   return vec(b.x-a.x,b.y-a.y);
double dist (point a, point b){
   return hypot(a.x-b.x,a.y-b.y);
double cross (vec a, vec b){
   return a.x*b.y-a.y*b.x;
bool ccw (point p, point q, point r){
```

```
return cross(toVec(p,q),toVec(p,r)) > 0;
bool collinear (point p, point q, point r){
   return fabs(cross(toVec(p,q),toVec(p,r))) < EPS;</pre>
bool lies(point a, point b, point c){
   if ((c.x \ge min(a.x,b.x) \&\& c.x \le max(a.x,b.x)) \&\&
           (c.y \ge min(a.y,b.y) \&\& c.y \le max(a.y,b.y))){
       return true;
   } else return false;
bool anglecmp(point a, point b){
   if (collinear(pivot,a,b)) return dist(pivot,a) < dist(pivot,b);</pre>
   double d1x = a.x - pivot.x, d1y = a.y - pivot.y;
   double d2x = b.x - pivot.x, d2y = b.y - pivot.y;
   return (atan2(d1y,d1x) - atan2(d2y,d2x))<0;</pre>
}
point intersect (point s1, point e1,point s2, point e2){
   double x1,x2,x3,x4,y1,y2,y3,y4;
   x1 = s1.x; y1 = s1.y;
   x2 = e1.x; y2 = e1.y;
   x3 = s2.x; y3 = s2.y;
   x4 = e2.x; y4 = e2.y;
   double num1 = (x1*y2 - y1*x2) * (x3-x4) - (x1-x2) * (x3*y4 - y3*x4);
    double num2 = (x1*y2 - y1*x2) * (y3-y4) - (y1-y2) * (x3*y4 - y3*x4);
    double den = (x1-x2) * (y3-y4) - (y1-y2) * (x3-x4);
   double new_x = num1/den;
   double new_y = num2/den;
   return point(new_x,new_y);
}
void clip(vector <point> &poly_points, point point1, point point2){
   vector <point> new_points;
   new_points.clear();
   for (int i = 0; i < poly_points.size(); i++)</pre>
   {
       int k = (i+1) % poly_points.size();
       double i_pos = ccw(point1,point2,poly_points[i]);
       double k_pos = ccw(point1,point2,poly_points[k]);
       //in in
       if (i_pos <= 0 && k_pos <= 0)</pre>
           new_points.push_back(poly_points[k]);
       //out in
       else if (i_pos > 0 && k_pos <= 0)</pre>
                 new_points.push_back(intersect(point1,point2,poly_points[i],poly_points[k]));
           new_points.push_back(poly_points[k]);
       else if (i_pos <= 0 && k_pos > 0)
                 new_points.push_back(intersect(point1,point2,poly_points[i],poly_points[k]));
       //out out
       else
```

```
poly_points.clear();
   for (int i = 0; i < new_points.size(); i++)</pre>
       poly_points.push_back(new_points[i]);
double area (const vector <point> &P){
   double result =0.0:
   double x1, y1, x2, y2;
   for (int i =0; i<P.size()-1;i++){</pre>
       x1 = P[i].x;
       v1 = P[i].v;
       x2 = P[i+1].x;
       y2 = P[i+1].y;
       result += (x1*y2-x2*y1);
   return fabs(result)/2;
void suthHodgClip(vector <point> &poly_points, vector <point> clipper_points){
   for (int i=0; i<clipper_points.size(); i++)</pre>
       int k = (i+1) % clipper_points.size();
       clip(poly_points, clipper_points[i], clipper_points[k]);
vector<point> sortku (vector<point> P){
   int P0=0;
   int i;
   for (i = 1; i<3; i++){</pre>
       if (P[i].y<P[P0].y || (P[i].y == P[P0].y && P[i].x > P[P0].x)){
          P0 = i;
      }
   point temp = P[0];
   P[0] = P[P0];
   P[P0] = temp;
   pivot = P[0];
   sort(++P.begin(),P.end(),anglecmp);
   reverse(++P.begin(),P.end());
   return P;
   clipper_points = sortku(clipper_points);
   suthHodgClip(poly_points, clipper_points);
```

4 Graphs

4.1 Articulation Point and Bridge

```
// gr -> adj list
// vector vis, low -> initialize to -1
// int timer -> initialize to 0
void dfs(int pos, int dad = -1)
{
```

```
vis[pos] = low[pos] = timer++;
int kids = 0;
for(auto& i : gr[pos])
{
    if(i == dad) continue;
    if(vis[i] >= 0)
        low[pos] = min(low[pos], vis[i]);
    else
    {
        dfs(i, pos);
        low[pos] = min(low[pos], low[i]);
        if(low[i] > vis[pos])
            is_bridge(pos, i)
        if(low[i] >= vis[pos] && dad >= 0)
            is_articulation_point(pos)
        ++kids;
    }
}
if(dad == -1 && kids > 1)
    is_articulation_point(pos)
```

4.2 Centroid Decomposition

```
int build_cen(int nw){
   com_cen(nw,0); //fungsi untuk itung size subtree
   int siz = sz[nw]/2; bool found = false;
   while(!found){
      found = true;
      for(int i:v[nw]){
         if(!rem[i] && sz[i] < sz[nw]){
            if(sz[i] > siz) {found = false; nw = i; break;}
      }
    }
   }
}big
   rem[nw] = true;
   for(int i:v[nw])if(!rem[i])par_cen[build_cen(i)] = nw;
   return nw;
}
```

4.3 Dinic's Maximum Flow

```
// O(VE log(max_flow)) if scaling == 1
// O((V + E) sqrt(E)) if unit graph (turn scaling off)
// O((V + E) sqrt(V)) if bipartite matching (turn scaling off)
// indices are 0-based
const 11 INF = 1e18;
struct Dinic
{
    struct Edge
    {
        int v;
        ll cap, flow;
    }
}
```

```
Edge(int _v, ll _cap) : v(_v), cap(_cap), flow(0) {}
};
int n;
11 lim;
vector<vector<int>> gr;
vector<Edge> e;
vector<int> idx, lv;
bool has_path(int s, int t)
   queue<int> q;
   q.push(s);
   lv.assign(n, -1);
   lv[s] = 0;
   while(!q.empty())
       int c = q.front();
       q.pop();
       if(c == t) break;
       for(auto& i : gr[c])
          11 cur_flow = e[i].cap - e[i].flow;
          if(lv[e[i].v] == -1 && cur_flow >= lim)
              lv[e[i].v] = lv[c] + 1;
              q.push(e[i].v);
      }
   return lv[t] != -1;
ll get_flow(int s, int t, ll left)
   if(!left || s == t) return left;
   while(idx[s] < (int) gr[s].size())</pre>
       int i = gr[s][idx[s]];
       if(lv[e[i].v] == lv[s] + 1)
          11 add = get_flow(
              e[i].v,
              min(left, e[i].cap - e[i].flow)
           if (add)
              e[i].flow += add;
              e[i ^ 1].flow -= add;
              return add;
       }
       ++idx[s];
   return 0;
Dinic(int vertices, bool scaling = 1) // toggle scaling here
   : n(vertices), lim(scaling ? 1 << 30 : 1), gr(n) {}
```

```
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```

```
void add_edge(int from, int to, ll cap, bool directed = 1)
{
    gr[from].push_back(e.size());
    e.emplace_back(to, cap);
    gr[to].push_back(e.size());
    e.emplace_back(from, directed ? 0 : cap);
}

ll get_max_flow(int s, int t) // call this
{
    ll res = 0;
    while(lim) // scaling
    {
        while(has_path(s, t))
        {
            idx.assign(n, 0);
            while(ll add = get_flow(s, t, INF)) res += add;
        }
        lim >>= 1;
    }
    return res;
}
```

4.4 Edmonds' Blossom

```
// Maximum matching on general graphs in O(V^2 E)
// Indices are 1-based
// Stolen from ko_osaga's cheatsheet
struct Blossom
{
   vector<int> vis, dad, orig, match, aux;
   vector<vector<int>> conn;
   int t, N;
   queue<int> Q;
   void augment(int u, int v)
       int pv = v;
       do
          pv = dad[v];
          int nv = match[pv];
          match[v] = pv;
          match[pv] = v;
          v = nv;
       } while(u != pv);
   int lca(int v, int w)
       ++t;
       while(true)
          if(v)
          {
```

```
if(aux[v] == t) return v;
          aux[v] = t;
          v = orig[dad[match[v]]];
       swap(v, w);
void blossom(int v, int w, int a)
   while(orig[v] != a)
       dad[v] = w;
       w = match[v];
       if(vis[w] == 1)
          Q.push(w);
          vis[w] = 0;
       orig[v] = orig[w] = a;
       v = dad[w];
}
bool bfs(int u)
   fill(vis.begin(), vis.end(), -1);
   iota(orig.begin(), orig.end(), 0);
   Q = queue<int>();
   Q.push(u);
   vis[u] = 0;
   while(!Q.empty())
       int v = Q.front(); Q.pop();
       for(int x : conn[v])
          if(vis[x] == -1)
              dad[x] = v; vis[x] = 1;
              if(!match[x])
                  augment(u, x);
                  return 1;
              Q.push(match[x]);
              vis[match[x]] = 0;
          else if(vis[x] == 0 && orig[v] != orig[x])
              int a = lca(orig[v], orig[x]);
              blossom(x, v, a);
              blossom(v, x, a);
      }
   }
   return false;
Blossom(int n) : // n = vertices
   vis(n + 1), dad(n + 1), orig(n + 1), match(n + 1),
```

```
aux(n + 1), conn(n + 1), t(0), N(n)
   for(int i = 0; i <= n; ++i)</pre>
   {
       conn[i].clear();
       match[i] = aux[i] = dad[i] = 0;
}
void add_edge(int u, int v)
    conn[u].push_back(v);
    conn[v].push_back(u);
int solve() // call this for answer
{
   int ans = 0;
   vector<int> V(N - 1);
   iota(V.begin(), V.end(), 1);
   shuffle(V.begin(), V.end(), mt19937(0x94949));
   for(auto x : V)
   {
       if(!match[x])
           for(auto y : conn[x])
              if(!match[y])
                  match[x] = y, match[y] = x;
                  ++ans;
                  break;
          }
       }
   for(int i = 1; i <= N; ++i)</pre>
       if(!match[i] && bfs(i)) ++ans;
    return ans;
}
```

4.5 Eulerian Path or Cycle

};

```
// finds a eulerian path / cycle
// visits each edge only once
// properties:
// - cycle: degrees are even
// - path: degrees are even OR degrees are even except for 2 vertices
// how to use: g = adjacency list g[n] = connected to n, undirected
// if there is a vertex u with an odd degree, call dfs(u)
// else call on any vertex
// ans = path result
vector<set<int>> g;
```

```
vector<int> ans;

void dfs(int u)
{
    while(g[u].size())
    {
        int v = *g[u].begin();
        g[u].erase(v);
        g[v].erase(u);
        dfs(v);
    }
    ans.push_back(u);
}
```

4.6 Hierholzer's Algorithm

```
// Eulerian on Directed Graph
stack<int> path; vector<int> euler;
inline void hierholzer()
   path.push(0); int cur=0;
   while (!path.empty())
       if (!adj[cur].empty())
          path.push(cur);
          int next=adj[cur].back();
          adj[cur].pob();
          cur=next;
      }
      else
          euler.pb(cur);
          cur=path.top();
          path.pop();
   reverse(euler.begin(),euler.end());
```

4.7 Hungarian

```
template <typename TD> struct Hungarian {
   TD INF = 1e9; //max_inf
   int n; vector<vector<TD> > adj; // cost[left][right]
   vector<TD> hl,hr,slk;
   vector<int> fl,fr,vl,vr,pre;
   deque<int> q;
   Hungarian(int _n) {
        n=_n; adj = vector<vector<TD> >(n, vector<TD> (n, 0));
   }
   int check(int i) {
        if (vl[i]=1,fl[i]!=-1) return q.push_back(fl[i]), vr[fl[i]]=1;
        while (i!=-1) swap(i,fr[fl[i]=pre[i]]); return 0;
```

```
void bfs(int s) {
       slk.assign(n,INF); vl.assign(n,0); vr=vl; q.assign(vr[s]=1,s);
       for (TD d;;) {
           for (;!q.empty();q.pop_front()) {
              for (int i=0,j=q.front();i<n;i++) {</pre>
                  if (d=hl[i]+hr[j]-adj[i][j],!vl[i]&&d<=slk[i]) {</pre>
                      if (pre[i]=j,d) slk[i]=d; else if (!check(i)) return;
           d=INF:
           for (int i = 0; i < n; i++) if (!vl[i]&&d>slk[i]) d=slk[i];
           for (int i = 0; i < n; i++) {</pre>
              if (vl[i]) hl[i]+=d; else slk[i]-=d;
              if (vr[i]) hr[i]-=d:
           for (int i = 0; i < n; i++) if (!vl[i]&&!slk[i]&&!check(i)) return;</pre>
       }}
   TD solve() {
       fl.assign(n,-1); fr=fl; hl.assign(n,0); hr=hl; pre.assign(n,0);
       for (int i = 0; i < n; i++) hl[i]=*max_element(adj[i].begin(),adj[i].begin()+n);</pre>
       for (int i = 0; i < n; i++) bfs(i);</pre>
       TD ret=0:
       for (int i = 0; i < n; i++) if (adj[i][f1[i]]) ret+=adj[i][f1[i]];</pre>
       return ret:
}; //i wiLL be matched with fl[i]
```

4.8 Minimum Cost Maximum Flow

```
// 1-based index
template<class T>
using rpq = priority_queue<T, vector<T>, greater<T>>;
const 11 INF = 1e18;
struct MCMF
   struct Edge
       int v;
       11 cap, cost;
       int rev:
       Edge(int _v, ll _cap, ll _cost, int _rev) :
          v(_v), cap(_cap), cost(_cost), rev(_rev) {}
   };
   11 flow. cost:
   int st, ed, n;
   vector<ll> dist, H;
   vector<int> pv, pe;
   vector<vector<Edge>> adj;
   bool dijkstra()
   {
       rpq<pair<ll, int>> pq;
       dist.assign(n + 1, INF);
       dist[st] = 0;
```

```
pq.emplace(0, st);
       while(!pq.empty())
           auto [cst, pos] = pq.top();
          pq.pop();
          if(dist[pos] < cst) continue;</pre>
          for(int i = 0; i < (int) adj[pos].size(); ++i)</pre>
              auto& e = adj[pos][i];
              int nxt = e.v;
              11 nxt_cst = dist[pos] + e.cost + H[pos] - H[nxt];
              if(e.cap > 0 && nxt_cst < dist[nxt])</pre>
                  dist[nxt] = nxt_cst;
                  pe[nxt] = i;
                  pv[nxt] = pos;
                  pq.emplace(nxt_cst, nxt);
          }
      }
       return dist[ed] != INF;
   MCMF(int _n) : n(_n), pv(n + 1), pe(n + 1), adj(n + 1) {}
   void add_edge(int u, int v, ll cap, ll cst)
       adj[u].emplace_back(v, cap, cst, adj[v].size());
       adj[v].emplace_back(u, 0, -cst, adj[u].size() - 1);
   pair<11, 11> solve(int _st, int _ed)
       st = _st, ed = _ed;
       flow = 0, cost = 0;
       H.assign(n + 1, 0);
       while(dijkstra())
          for(int i = 0; i <= n; ++i)</pre>
              H[i] += dist[i];
          11 f = INF;
          for(int i = ed; i != st; i = pv[i])
              f = min(f, adj[pv[i]][pe[i]].cap);
          flow += f;
          cost += f * H[ed];
          for(int i = ed; i != st; i = pv[i])
              auto& e = adj[pv[i]][pe[i]];
              e.cap -= f;
              adj[i][e.rev].cap += f;
          }
       return {flow, cost};
};
```

4.9 SCC and Strong Orientation

```
#define N 10020
vector<int> adj[N];
bool vis[N], ins[N];
int disc[N], low[N], gr[N];
stack<int> st;
int id,grid;
void scc(int cur, int par)
{
   disc[cur]=low[cur]=++id;
   vis[cur]=ins[cur]=1;
   st.push(cur);
   for(int to : adj[cur])
       //if (to==par) continue; // ini untuk SO(scc undirected)
       if (!vis[to]) scc(to.cur):
       if (ins[to]) low[cur]=min(low[cur],low[to]);
   if(low[cur] == disc[cur])
       grid++; // group id
       while(ins[cur])
          gr[st.tp]=grid; ins[st.tp]=0; st.pop();
```

5 Math

5.1 Berlekamp-Massey

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
typedef long long 11;
#define SZ 233333
const int MOD=1e9+7; //or any prime
11 qp(11 a,11 b)
{
   ll x=1; a%=MOD;
   while(b)
       if(b&1) x=x*a%MOD:
       a=a*a%MOD: b>>=1:
   return x;
namespace linear_seq {
   vector<int> BM(vector<int> x)
       //ls: (shortest) relation sequence (after filling zeroes) so far
       //cur: current relation sequence
       vector<int> ls,cur;
       //lf: the position of ls (t')
       //ld: delta of ls (v')
       int 1f = -1, 1d = -1;
```

```
for(int i=0;i<int(x.size());++i)</pre>
       11 t=0:
       //evaluate at position i
       for(int j=0;j<int(cur.size());++j)</pre>
           t=(t+x[i-j-1]*(11)cur[j])%MOD;
       if((t-x[i])%MOD==0) continue; //good so far
       //first non-zero position
       if(!cur.size())
           cur.resize(i+1):
           lf=i; ld=(t-x[i])%MOD;
           continue:
       //cur=cur-c/ld*(x[i]-t)
       11 k=-(x[i]-t)*qp(1d,MOD-2)%MOD/*1/1d*/;
       vector<int> c(i-lf-1); //add zeroes in front
       c.pb(k);
       for(int j=0;j<int(ls.size());++j)</pre>
           c.pb(-ls[j]*k%MOD);
       if(c.size() < cur.size()) c.resize(cur.size());</pre>
       for(int j=0;j<int(cur.size());++j)</pre>
           c[j]=(c[j]+cur[j])%MOD;
       //if cur is better than ls, change ls to cur
       if(i-lf+(int)ls.size()>=(int)cur.size())
           ls=cur,lf=i,ld=(t-x[i])%MOD;
       cur=c;
   for(int i=0;i<int(cur.size());++i)</pre>
       cur[i]=(cur[i]%MOD+MOD)%MOD;
   return cur;
int m; //length of recurrence
//a: first terms
//h: relation
ll a[SZ],h[SZ],t_[SZ],s[SZ],t[SZ];
//calculate p*q mod f
void mull(11*p,11*q)
   for(int i=0;i<m+m;++i) t_[i]=0;</pre>
   for(int i=0;i<m;++i) if(p[i])</pre>
       for(int j=0;j<m;++j)</pre>
           t_{[i+j]}=(t_{[i+j]}+p[i]*q[j])%MOD;
   for(int i=m+m-1;i>=m;--i) if(t_[i])
       //miuns t_[i]x^{i-m}(x^m-\sum_{j=0}^{m-1} x^{m-j-1}h_j)
       for(int j=m-1; ~j; --j)
           t_{[i-j-1]}=(t_{[i-j-1]}+t_{[i]}*h_{[j]})%MOD;
   for(int i=0;i<m;++i) p[i]=t_[i];</pre>
ll calc(ll K)
   for(int i=m;~i;--i)
       s[i]=t[i]=0;
   //init
   s[0]=1; if(m!=1) t[1]=1; else t[0]=h[0];
   //binary-exponentiation
   while(K)
       if(K&1) mull(s,t);
       mull(t,t); K>>=1;
```

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```
11 su=0;
       for(int i=0;i<m;++i) su=(su+s[i]*a[i])%MOD;</pre>
       return (su%MOD+MOD)%MOD;
    int work(vector<int> x,ll n)
       if(n<int(x.size())) return x[n];</pre>
       vector<int> v=BM(x); m=v.size(); if(!m) return 0;
       for(int i=0;i<m;++i) h[i]=v[i],a[i]=x[i];</pre>
       return calc(n);
   }
using linear_seq::work;
const vector<int> sequence = {
   0, 2, 2, 28, 60, 836, 2766
};
int main()
{
    cout<<work(sequence, 7) << '\n';</pre>
```

5.2 Catalan

```
long long cat(long long n){
   long long ret = 1;
   for(long long i = 0; i < n; i++){
      ret = ret*(2*n-i);
      ret = ret/(i+1);
   }
   ret = ret/(n+1);
   return ret;
}

ll superCatalan(int n){
   if(n <= 2)return 1;
   return (3*(2*n-3)*sc(n-1)-(n-3)*sc(n-2)) / n;
} // 1,1,1,3,11,45, 197, 903, 4279, 20793, 103049</pre>
```

5.3 Extended Euclidean GCD

```
// computes x and y such that ax + by = gcd(a, b) in O(log (min(a, b)))
// returns {gcd(a, b), x, y}
tuple<int, int, int> gcd(int a, int b)
{
   if(b == 0) return {a, 1, 0};
   auto [d, x1, y1] = gcd(b, a % b);
   return {d, y1, x1 - y1 * (a / b)};
}
```

5.4 Fast Fourier Transform

```
using ld = double; // change to long double if reach 10^18
using cd = complex<ld>;
const ld PI = acos(-(ld)1);
void fft(vector<cd> &a, int sign = 1)
   int n = a.size();
   ld theta = sign * 2 * PI / n;
   for(int i = 0, j = 1; j < n-1; j++)
       for(int k = n >> 1; k > (i ^= k); k >>= 1);
       if(j < i) swap(a[i], a[j]);</pre>
   for(int m, mh = 1; (m = mh << 1) <= n; mh = m)</pre>
       int irev = 0;
       for(int i = 0; i < n; i += m)</pre>
          cd w = exp(cd(0, theta*irev));
          for(int k = n >> 2; k > (irev ^= k); k >>= 1);
          for(int j = i; j < mh + i; j++)</pre>
              int k = j+mh;
              cd x = a[j] - a[k];
              a[j] += a[k];
              a[k] = w * x;
          }
      }
   if(sign == -1) for(cd &i : a) i /= n;
vector<ll> multiply(vector<ll> const& a, vector<ll> const &b)
   vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
   int n = 1;
   while(n < a.size() + b.size()) n <<= 1;</pre>
   fa.resize(n); fb.resize(n);
   fft(fa); fft(fb);
   for(int i = 0: i < n: i++) fa[i] *= fb[i]:
   fft(fa, -1);
   vector<ll> res(n);
   for(int i = 0; i < n; i++) res[i] = round(fa[i].real());</pre>
   return res;
```

5.5 Fibonacci Check

5.6 Gauss-Jordan

```
// Gauss-Jordan elimination with full pivoting.
//
// Uses:
// (1) solving systems of linear equations (AX=B)
// (2) inverting matrices (AX=I)
// (3) computing determinants of square matrices
//
// Running time: O(n^3)
//
// INPUT: a[][] = an nxn matrix
//
            b[][] = an nxm matrix
11
// OUTPUT: X = an nxm matrix (stored in b[][])
//
            A^{-1} = an nxn matrix (stored in a[][])
            returns determinant of a[][]
//
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan(VVT &a, VVT &b) {
   const int n = a.size();
   const int m = b[0].size();
   VI irow(n), icol(n), ipiv(n);
   T det = 1:
   for (int i = 0; i < n; i++) {
       int pj = -1, pk = -1;
       for (int j = 0; j < n; j++) if (!ipiv[j])</pre>
           for (int k = 0; k < n; k++) if (!ipiv[k])
               if (p_j == -1 \mid | fabs(a[j][k]) > fabs(a[p_j][pk])) { p_j = j; pk = k; }
       if (fabs(a[pj][pk]) < EPS) { cerr << "Matrix is singular." << endl; exit(0); }</pre>
       ipiv[pk]++;
       swap(a[pj], a[pk]);
       swap(b[pj], b[pk]);
       if (pj != pk) det *= -1;
       irow[i] = pj;
       icol[i] = pk;
       T c = 1.0 / a[pk][pk];
       det *= a[pk][pk];
       a[pk][pk] = 1.0;
       for (int p = 0; p < n; p++) a[pk][p] *= c;</pre>
       for (int p = 0; p < m; p++) b[pk][p] *= c;</pre>
       for (int p = 0; p < n; p++) if (p != pk) {</pre>
           c = a[p][pk];
           a[p][pk] = 0;
           for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;</pre>
           for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
   for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
       for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);</pre>
   return det;
int main() {
   const int n = 4;
```

```
const int m = 2;
   double A[n][n] = { {1,2,3,4},{1,0,1,0},{5,3,2,4},{6,1,4,6} };
   double B[n][m] = \{ \{1,2\}, \{4,3\}, \{5,6\}, \{8,7\} \};
   VVT a(n), b(n);
   for (int i = 0; i < n; i++) {</pre>
       a[i] = VT(A[i], A[i] + n);
       b[i] = VT(B[i], B[i] + m);
   double det = GaussJordan(a, b);
   // expected: 60
   cout << "Determinant: " << det << endl;</pre>
   // expected: -0.233333 0.166667 0.133333 0.0666667
               0.166667 0.166667 0.333333 -0.333333
   11
   //
               0.233333 0.833333 -0.133333 -0.0666667
   11
               0.05 -0.75 -0.1 0.2
   cout << "Inverse: " << endl;</pre>
   for (int i = 0; i < n; i++) {</pre>
       for (int j = 0; j < n; j++)
           cout << a[i][j] << ' ';
       cout << endl;</pre>
   // expected: 1.63333 1.3
   11
               -0.166667 0.5
   11
               2.36667 1.7
   11
               -1.85 -1.35
   cout << "Solution: " << endl;</pre>
   for (int i = 0; i < n; i++) {</pre>
       for (int j = 0; j < m; j++)
           cout << b[i][j] << ' ';
       cout << endl;</pre>
   }
}
```

5.7 Generalized CRT

```
template<typename T>
T extended_euclid(T a, T b, T &x, T &y) {
   if (b == 0) {
       x = 1;
       y = 0;
       return a;
   T xx, yy, gcd;
   gcd = extended_euclid(b, a % b, xx, yy);
   x = yy;
   y = xx - (yy * (a / b));
   return gcd;
template<typename T>
T MOD(T a, T b) { return (a%b + b) % b; }
// return x, lcm. x = a % n && x = b % m
template<typename T>
pair<T,T> CRT(T a, T n, T b, T m) {
   T _n, _m;
   T gcd = extended_euclid(n, m, _n, _m);
   if (n == m) {
```

```
if (a == b) return pair<T,T>(a, n);
  else return pair<T,T>(-1, -1);
} else if (abs(a-b) % gcd != 0) return pair<T,T>(-1, -1);
else {
    T lcm = m * n / gcd;
    T x = MOD(a + MOD(n*MOD(_n*((b-a)/gcd), m/gcd), lcm), lcm);
    return pair<T,T>(x, lcm);
}}
```

5.8 Generalized Lucas Theorem

```
/*Special Lucas : (n,k) % p^x
 fctp[n] = Product of the integers less than or equal
 to n that are not divisible by p
 Precompute fctp*/
LL p
LL E(LL n, int m) {
   LL tot = 0;
   while(n!=0){
       tot += n/m, n/=m;
   return tot;
LL funct(LL n,LL base){
   LL ans = fast(fctp[base],n/base,base) * fctp[n%base] %base;
   return ans:
LL F(LL n, LL base) {
   LL ans = 1:
   while(n!=0){
       ans = (ans * funct(n,base))%base;
       n/=p;
   return ans:
LL special_lucas(LL n,LL r,LL base){
   p = fprime(base);
   LL pow = E(n,p) - E(n-r,p) - E(r,p);
   LL TOP = fast(p,pow,base) * F(n,base)%base;
   LL BOT = F(r,base) * F(n-r,base)%base;
   return (TOP * fast(BOT, totien(base) - 1, base))%base;
//End of Special Lucas
```

5.9 Linear Diophantine

```
//FOR SOLVING MINIMUM ABS(X) + ABS(Y)
11 x,y,newX,newY,target=0;
11 extGcd(11 a,11 b){
    if(b==0){
        x=1,y=0;
        return a;
    }
11 ret = extGcd(b,a%b);
```

```
newX = y;
   newY = x - y * (a/b);
   x = newX:
   y = newY;
   return ret;
11 fix(ll sol,ll rt){
   11 ret = 0:
   //CASE SOLUTION(X/Y) < TARGET
   if(sol < target)ret = -floor(abs(sol+target)/(double)rt);</pre>
   //CASE SOLUTION(X/Y) > TARGET
   if(sol > target)ret = ceil(abs(sol-target)/(double)rt);
   return ret:
ll work(ll a, ll b, ll c){
   11 gcd = extGcd(a,b);
   11 \text{ solX} = x*(c/gcd);
   11 \text{ solY} = y*(c/gcd);
   a/=gcd;b/=gcd;
   11 fi = abs(fix(solX,b));
   11 se = abs(fix(solY,a));
   11 lo = min(fi.se):
   11 hi = max(fi,se);
   11 ans = abs(solX) + abs(solY);
   for(ll i = lo; i<=hi; i++){</pre>
       ans = min(ans, abs(solX+i*b) + abs(solY-i*a));
       ans = min(ans, abs(solX-i*b) + abs(solY+i*a));
   return ans;
```

5.10 Miller-Rabin and Pollard's Rho

```
namespace MillerRabin
   const vector<ll> primes = { // deterministic up to 2^64 - 1
      2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37
   11 gcd(11 a, 11 b)
   {
      return b ? gcd(b, a % b) : a;
   ll powa(ll x, ll y, ll p) // (x ^ y) % p
      if(!y) return 1;
       if(y & 1) return ((__int128) x * powa(x, y - 1, p)) % p;
      ll temp = powa(x, y >> 1, p);
      return ((__int128) temp * temp) % p;
   bool miller_rabin(ll n, ll a, ll d, int s)
      11 x = powa(a, d, n);
       if(x == 1 | | x == n - 1) return 0:
      for(int i = 0; i < s; ++i)</pre>
          x = ((_int128) x * x) % n;
          if(x == n - 1) return 0;
```

```
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```

```
return 1;
   bool is_prime(ll x) // use this
       if(x < 2) return 0;
       int r = 0;
       11 d = x - 1:
       while((d \& 1) == 0)
          d >>= 1:
          ++r;
       for(auto& i : primes)
          if(x == i) return 1;
          if(miller_rabin(x, i, d, r)) return 0;
       return 1:
}
namespace PollardRho
   mt19937_64 generator(chrono::steady_clock::now()
                      .time_since_epoch().count());
   uniform_int_distribution<ll> rand_ll(0, LLONG_MAX);
   11 f(11 x, 11 b, 11 n) // (x^2 + b) % n
       return (((__int128) x * x) % n + b) % n;
   ll rho(ll n)
       if(n % 2 == 0) return 2;
       11 b = rand_ll(generator);
       11 x = rand_ll(generator);
       11 y = x;
       while(1)
       {
          x = f(x, b, n);
          y = f(f(y, b, n), b, n);
          11 d = MillerRabin::gcd(abs(x - y), n);
          if(d != 1) return d;
       }
   }
   void pollard_rho(ll n, vector<ll>& res)
       if(n == 1) return;
       if(MillerRabin::is_prime(n))
          res.push_back(n);
          return;
       11 d = rho(n);
       pollard_rho(d, res);
       pollard_rho(n / d, res);
    vector<ll> factorize(ll n, bool sorted = 1) // use this
       vector<ll> res:
```

```
pollard_rho(n, res);
  if(sorted) sort(res.begin(), res.end());
  return res;
}
```

5.11 Modular Linear Equation

```
// finds all solutions to ax = b (mod n)
vi modular_linear_equation_solver(int a, int b, int n) {
   int x, y; vi ret; int g = extended_euclid(a, n, x, y);
   if (!(b%g)) {
        x = mod(x*(b / g), n);
        for (int i = 0; i < g; i++)
            ret.push_back(mod(x + i*(n / g), n));
   }
   return ret;
}</pre>
```

5.12 Number Theoretic Transform

```
namespace FFT {
   /* ---- Adjust the constants here ---- */
   const int LN = 24; \frac{1}{23}
   const int N = 1 << LN;</pre>
   typedef long long LL; // 2**23 * 119 + 1. 998244353
   // 'MOD' must be of the form 2**'LN' * k + 1, where k odd.
   const LL MOD = 9223372036737335297; // 2**24 * 54975513881 + 1.
   const LL PRIMITIVE_ROOT = 3; // Primitive root modulo 'MOD'.
   /* ---- End of constants ---- */
   LL root[N];
   inline LL power(LL x, LL y) {
      LL ret = 1;
       for (; y; y >>= 1) {
          if (y & 1) ret = (__int128) ret * x % MOD;
          x = (_int128) x * x % MOD;
      return ret;
   inline void init_fft() {
       const LL UNITY = power(PRIMITIVE_ROOT, MOD-1 >> LN);
       root[0] = 1;
       for (int i=1; i<N; i++) {</pre>
          root[i] = (__int128) UNITY * root[i-1] % MOD;
       }return;
   // n = 2<sup>k</sup> is the length of polynom
   inline void fft(int n, vector<LL> &a, bool invert) {
       for (int i=1, j=0; i<n; ++i) {</pre>
          int bit = n \gg 1:
          for (; j>=bit; bit>>=1) j -= bit;
          j += bit;
          if (i < j) swap(a[i], a[j]);</pre>
```

```
for (int len=2; len<=n; len<<=1) {</pre>
       LL wlen = (invert ? root[N - N/len] : root[N/len]);
       for (int i=0: i<n: i+=len) {</pre>
          LL w = 1;
          for (int j=0; j<len>>1; j++) {
              LL u = a[i+j];
              LL v = (_int128) a[i+j + len/2] * w % MOD;
              a[i+j] = ((__int128) u + v) % MOD;
              a[i+j + len/2] = ((\_int128) u - v + MOD) % MOD;
              w = (__int128) w * wlen % MOD;
       }
   if (invert) {
       LL inv = power(n, MOD-2);
       for (int i=0; i<n; i++) a[i] = (__int128) a[i] * inv % MOD;
   }return;
inline vector<LL> multiply(vector<LL> a, vector<LL> b) {
   vector<LL> c;
   int len = 1 << 32 - __builtin_clz(a.size() + b.size() - 2);</pre>
   a.resize(len, 0); b.resize(len, 0);
   fft(len, a, false); fft(len, b, false);
   c.resize(len):
   for (int i = 0; i < len; ++i)c[i] = (__int128) a[i]*b[i]%MOD;</pre>
   fft(len, c, true);
   return c;
//FFT::init_fft(); wajib di panggil init di awal
```

6 Miscellaneous

6.1 Dates

}

6.1.1 Day of Date

```
// 0-based
const vector<int> T = {
    0, 3, 2, 5, 0, 3,
    5, 1, 4, 6, 2, 4
}
int day(int d, int m, int y)
{
    y -= (m < 3);
    return (y + y / 4 - y / 100 + y / 400 + T[m - 1] + d) % 7;
}</pre>
```

6.1.2 Number of Days since 1-1-1

```
int rdn(int d, int m, int y)
{
```

```
if(m < 3) --y, m += 12;
return 365 * y + y / 4 - y / 100 + y / 400
+ (153 * m - 457) / 5 + d - 306;
```

6.2 Enumerate Subsets of a Bitmask

```
int x = 0; do {
    // do stuff with the bitmask here
    x = (x + 1 + ~m) & m;
} while(x != 0);
```

6.3 Fast IO

```
int read()
   char c;
   do
       c = getchar_unlocked();
   } while(c < 33);</pre>
   int res = 0;
   int mul = 1;
   if(c == '-')
   {
      mul = -1;
       c = getchar_unlocked();
   while('0' <= c && c <= '9')
      res = res * 10 + c - '0';
      c = getchar_unlocked();
   return res * mul:
void write(int x)
   static char wbuf[10]:
   if(x < 0)
      putchar_unlocked('-');
      x = -x;
   int idx = 0;
   while(x)
       wbuf[idx++] = x % 10;
      x /= 10;
   if(idx == 0)
   {
      putchar_unlocked('0');
```

```
for(int i = idx - 1; i >= 0; --i)
{
     putchar_unlocked(wbuf[i] + '0');
}

void write(const char* s)
{
     while(*s)
     {
        putchar_unlocked(*s);
        ++s;
     }
}
```

6.4 Int to Roman

```
const string R[] = {
    "M", "CM", "D", "CD", "C", "XC", "L",
    "XL", "X", "IX", "V", "IV", "IV", "I"
};

const int N[] = {
    1000, 900, 500, 400, 100, 90,
    50, 40, 10, 9, 5, 4, 1
};

string to_roman(int x)
{
    if (x == 0) return "0"; // Not decimal 0!
        string res = "";
    for (int i = 0; i < 13; ++i)
            while (x >= N[i]) x -= N[i], res += R[i];
    return res;
}
```

6.5 Josephus Problem

```
11 josephus(11 n, 11 k) // 0(k log n)
{
    if(n == 1) return 0;
    if(k == 1) return n - 1;
    if(k > n) return (josephus(n - 1, k) + k) % n;
    ll cnt = n / k;
    ll res = josephus(n - cnt, k);
    res -= n % k;
    if(res < 0) res += n;
    else res += res / (k - 1);
    return res;
}
int josephus(int n, int k) // 0(n)
{
    int res = 0;</pre>
```

```
for(int i = 1; i <= n; ++i)
    res = (res + k) % i;
return res + 1;</pre>
```

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6.6 Random

```
// RNG - rand_int(min, max), inclusive
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());

template<class T>
T rand_int(T mn, T mx)
{
    return uniform_int_distribution<T>(mn, mx)(rng);
}
```

7 Strings

7.1 Aho-Corasick

```
const int K = 26;
struct Vertex {
   int next[K];
   bool leaf = 0;
   int p = -1, ans = 0;
   char pch;
    int link = -1, mlink = -1;
   //magic link, is the link to find the nearest leaf
   int go[K];
   Vertex(int p=-1, char ch='$') : p(p), pch(ch) {
       fill(begin(next), end(next), -1);
       fill(begin(go), end(go), -1);
};
vector<Vertex> t;
int add_string(string const& s) {
   int v = 0:
   for (char ch : s) {
       int c = ch - 'a':
       if (t[v].next[c] == -1) {
           t[v].next[c] = t.size();
           t.emplace_back(v, ch);
       } v = t[v].next[c];
   t[v].leaf = 1;
   return v;
int go(int v, char ch);
int get_link(int v) {
   if (t[v].link == -1) {
       if (v == 0 || t[v].p == 0) t[v].link = 0;
       else t[v].link = go(get_link(t[v].p), t[v].pch);
```

```
return t[v].link;
int get_mlink(int v) {
   if (t[v].mlink == -1) {
       if (v == 0 || t[v].p == 0) t[v].mlink = 0;
       else{
          t[v].mlink = go(get_link(t[v].p), t[v].pch);
          if(t[v].mlink && !t[t[v].mlink].leaf){
              if(t[t[v].mlink].mlink==-1)get_mlink(t[v].mlink);
              t[v].mlink = t[t[v].mlink].mlink;
   } return t[v].mlink:
int go(int v, char ch) {
   int c = ch - 'a';
   if (t[v].go[c] == -1) {
       if (t[v].next[c] != -1) t[v].go[c] = t[v].next[c];
       else t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
   } return t[v].go[c];
//t.pb(Vertex());
```

7.2 Eertree

```
/*
  Eertree - keep track of all palindromes and its occurences
  This code refers to problem Longest Palindromic Substring
https://www.spoj.com/problems/LPS/
#include <bits/stdc++.h>
using namespace std;
typedef long long 11;
struct node {
   int next[26]:
   int sufflink;
   int len, cnt;
};
const int N = 1e5+69:
int n;
string s;
node tree[N]:
int idx, suff;
int ans = 0:
void init_eertree() {
   idx = suff = 2:
   tree[1].len = -1, tree[1].sufflink = 1;
   tree[2].len = 0, tree[2].sufflink = 1;
bool add_letter(int x) {
   int cur = suff, curlen = 0;
   int nw = s[x] - a;
```

```
while(1) {
       curlen = tree[cur].len:
       if(x-curlen-1 >= 0 && s[x-curlen-1] == s[x])
       cur = tree[cur].sufflink;
   if(tree[cur].next[nw]) {
       suff = tree[cur].next[nw];
      return 0;
   tree[cur].next[nw] = suff = ++idx;
   tree[idx].len = tree[cur].len + 2;
   ans = max(ans, tree[idx].len);
   if(tree[idx].len == 1) {
       tree[idx].sufflink = 2;
      tree[idx].cnt = 1;
      return 1;
   while(1) {
       cur = tree[cur].sufflink;
       curlen = tree[cur].len;
      if(x-curlen-1) = 0 && s[x-curlen-1] == s[x]) {
          tree[idx].sufflink = tree[cur].next[nw];
          break;
      }
   tree[idx].cnt = tree[tree[idx].sufflink].cnt + 1;
   return 1;
int main() {
   ios::sync_with_stdio(0); cin.tie(0);
   cin >> n >> s;
   init_eertree();
   for(int i = 0; i < n; i++) {</pre>
      add_letter(i);
   }
   cout << ans << '\n';
   return 0;
}
```

7.3 Manacher's Algorithm

```
// Computes lps array. lps[i] means the longest palindromic substring centered at i (when i is even,
   it is between characters. when it is odd, it is on characters)lps[0] = 0; lps[1] = 1;
REP(i,2,2*str.size()){
   int l = i/2 - lps[i]/2;
   int r = (i-1)/2 + lps[i]/2;
   while(1){ // widen
      if(1 == 0 || r+1 == str.size())break;
```

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7.4 Suffix Array

```
// stores result in sa and lcp
// if lcp is needed, call SuffixArray(str, 1)
struct SuffixArray
   int n;
   vector<int> sa, lcp, rnk, cnt;
   vector<pair<int, int>> p;
   SuffixArray(const string& s, bool calc_lcp = 0) :
       n(s.length()), sa(n), lcp(calc_lcp ? n : 0), rnk(n),
       cnt(max(n, 256)), p(n)
       for(int i = 0; i < n; ++i) rnk[i] = s[i];</pre>
       iota(sa.begin(), sa.end(), 0);
       for(int i = 1; i < n; i <<= 1) update_sa(i);</pre>
       if(!calc_lcp) return;
       vector<int> phi(n), plcp(n);
       phi[sa[0]] = -1;
       for(int i = 1; i < n; ++i) phi[sa[i]] = sa[i - 1];</pre>
       int 1 = 0;
       for(int i = 0; i < n; ++i)
          if(phi[i] == -1) plcp[i] = 0;
          else
              while((i + 1 < n) && (phi[i] + 1 < n)</pre>
                    && (s[i + 1] == s[phi[i] + 1])) ++1;
```

```
plcp[i] = 1;
               1 = \max(1 - 1, 0);
       for(int i = 0; i < n; ++i) lcp[i] = plcp[sa[i]];</pre>
   void update_sa(int len)
       sort_sa(len); sort_sa(0);
       for(int i = 0; i < n; ++i) p[i] = {rnk[i], rnk[(i + len) % n]};</pre>
       auto lst = p[sa[0]];
       rnk[sa[0]] = 0;
       int cur = 0:
       for(int i = 1; i < n; ++i)</pre>
           if(lst != p[sa[i]])
               lst = p[sa[i]];
               ++cur;
           rnk[sa[i]] = cur;
   void sort_sa(int offset)
       fill(cnt.begin(), cnt.end(), 0);
       for(int i = 0; i < n; ++i) ++cnt[rnk[(i + offset) % n]];</pre>
       int sum = 0;
       for(int i = 0; i < (int) cnt.size(); ++i)</pre>
           int temp = cnt[i];
           cnt[i] = sum;
           sum += temp;
       vector<int> temp(n);
       for(int i = 0; i < n; ++i)</pre>
           int cur = cnt[rnk[(sa[i] + offset) % n]]++;
           temp[cur] = sa[i];
       sa = move(temp);
   }
};
```