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```

Miscellaneous

1.1 VS Code Config

```
command": "clear; ./runner ${file} ${fileBasenameNoExtension} 0"
"command": "clear; ./runner ${file} ${fileBasenameNoExtension} 1"
"command": "clear: rm -r .cache"
runner:
#!/bin/bash
cp=$1; uf=$3; tmp='.cache'; bp="$tmp/$2"; ch="$tmp/${2}-hash"
ti="${li}\nTime: %es"
rc() {
    mkdir -p "$tmp"
    rc; echo -n "$(gh)" > "$ch"
gch() {
    if [[ -f "$ch" ]]; then cat $ch
    else echo -n 'NULL'; fi
    sha256sum $cp
    oh=\$(gch); nh=\$(gh)
    if [[ "$oh" == "$nh" ]]; then return 1
    else return 0; fi
    g++ $cp -02 -std=gnu++17 -Wall -Wextra -Wshadow -DLOCAL -o $bp
```

```
ulimit -s unlimited
    echo $li
    if nr; then
        if [[ -f "$bp" ]]; then rm "$bp"; fi
        sch; echo 'Compiling...'; echo $li; cc; echo $li
    if [[-f"$bp"]]; then
        echo 'Running...'; echo $li
        if (( $uf )); then command time -f "$ti" ./$bp < IN
        else command time -f "$ti" ./$bp; fi
        echo $li
ma
```

1.2 Day of Date

```
// 0-based
const vector<int> T = {
 0, 3, 2, 5, 0, 3,
 5, 1, 4, 6, 2, 4
int day(int d, int m, int y) {
 y -= (m < 3);
 return (y + y / 4 - y / 100 + y / 400 + T[m - 1] + d) % 7;
```

1.3 Number of Days since 1-1-1

1.4 Enumerate Subsets of a Bitmask

```
int x = 0;
do {
    // do stuff with the bitmask here
    x = (x + 1 + ~m) & m;
} while(x != 0);
```

1.5 Fast IO

```
int read() {
 char c;
 do {
  c = getchar_unlocked();
 } while(c < 33);
 int res = 0;
 int mul = 1;
 if(c == '-') {
   mul = -1;
   c = getchar_unlocked();
 while('0' <= c && c <= '9') {
   res = res * 10 + c - '0';
   c = getchar_unlocked();
 return res * mul;
void write(int x) {
 static char wbuf[10];
 if(x < 0) {
   putchar_unlocked('-');
   \times = - \times ;
 int idx = 0;
 while(x) {
  wbuf[idx++] = x \% 10;
   × /= 10;
 if(idx == 0)
   putchar_unlocked('0');
 for(int i = idx - 1; i >= 0; --i)
   putchar_unlocked(wbuf[i] + '0');
void write(const char* s) {
 while(*s) {
   putchar_unlocked(*s);
   ++s;
```

1.6 Int to Roman

```
const string R[] = {
    "M", "CM", "D", "CD", "C", "XC", "L",
    "XL", "X", "IX", "V", "IV", "I"
};

const int N[] = {
```

```
1000, 900, 500, 400, 100, 90,
50, 40, 10, 9, 5, 4, 1
};

string to_roman(int x) {
   if(x == 0) {
      return "O"; // Not decimal 0!
   }
   string res = "";
   for(int i = 0; i < 13; ++i)
      while(x >= N[i])
      x -= N[i], res += R[i];
   return res;
}
```

1.7 Josephus Problem

```
ll josephus(ll n, ll k) \{ // O(k \log n) \}
  if(n == 1)
   return 0;
  if(k == 1)
   return n - 1;
  if(k > n)
   return (josephus(n - 1, k) + k) % n;
  ll cnt = n / k;
  ll res = josephus(n - cnt, k);
 res -= n % k;
 if(res < 0)
   res += n;
  else
   res += res / (k - 1);
 return res;
int josephus(int n, int k) { // O(n)
  int res = 0;
 for(int i = 1; i <= n; ++i)
   res = (res + k) \% i;
  return res + 1;
```

1.8 Random Primes

36671 74101 724729 825827 924997 1500005681 2010408371 2010405347

1.9 RNG

```
// RNG - rand_int(min, max), inclusive
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
template<class T>
T rand_int(T mn, T mx) {
   return uniform_int_distribution<T>(mn, mx)(rng);
}
```

2 Data Structures

2.1 2D Segment Tree

```
\omega
```

```
lc(NULL), rc(NULL) {}
  typedef node* pnode;
  pnode root;
  Segtree(int l, int r) {
    root = new node(l, r);
  void update(pnode& nw, int x, int val) {
    int l = nw - > l, r = nw - > r, mid = (l + r) / 2;
    if(l == r)
      nw->val = val;
    else {
      assert(l <= x && x <= r);
      pnode& child = x <= mid ? nw->lc : nw->rc;
        child = new node(x, x, val);
      else if(child->l <= x && x <= child->r)
        update(child, x, val);
      else {
        do {
          if(x \le mid)
            r = mid;
          else
           l = mid + 1;
          mid = (l + r) / 2:
        } while((x <= mid) == (child->l <= mid));</pre>
        pnode nxt = new node(l, r);
        if(child->l <= mid)</pre>
          nxt->lc = child;
        else
         nxt->rc = child;
        child = nxt;
        update(nxt, x, val);
      nw->val = min(nw->lc ? nw->lc->val : INF,
                    nw->rc ? nw->rc->val : INF);
  int query(pnode& nw, int x1, int x2) {
    if(!nw)
      return INF;
    int& l = nw->l, &r = nw->r;
    if(r < x1 || x2 < l)
      return INF;
    if(x1 <= l && r <= x2)
      return nw->val;
    int ret = min(query(nw->lc, x1, x2),
                  query(nw->rc, x1, x2));
    return ret;
  void update(int x, int val) {
    assert(root->l <= x && x <= root->r);
    update(root, x, val);
  int query(int l, int r) {
    return query(root, l, r);
};
struct node {
  int l, r;
  Segtree y;
  node* lc, *rc;
  node(int _l, int _r) : l(_l), r(_r), y(0, MAX),
    lc(NULL), rc(NULL) {}
```

```
typedef node* pnode;
pnode root;
Segtree2D(int l, int r) {
 root = new node(l, r);
void update(pnode& nw, int x, int y, int val) {
  int& l = nw - > l, &r = nw - > r, mid = (l + r) / 2;
  if(l == r)
    nw->y.update(y, val);
  else {
    if(x \le mid) \{
      if(!nw->lc)
        nw->lc = new node(l, mid);
      update(nw->lc, x, y, val);
    } else {
      if(!nw->rc)
        nw - rc = new node(mid + 1, r);
      update(nw->rc, x, y, val);
    val = min(nw->lc ? nw->lc->y.query(y, y) : INF,
              nw \rightarrow rc ? nw \rightarrow rc \rightarrow y.query(y, y) : INF);
    nw->y.update(y, val);
int guery(pnode& nw, int x1, int x2, int y1, int y2) {
  if(!nw)
   return INF;
  int& l = nw - > l, &r = nw - > r;
  if(r < x1 \mid | x2 < l)
   return INF;
  if(x1 <= l && r <= x2)
   return nw->y.query(y1, y2);
  int ret = min(query(nw->lc, x1, x2, y1, y2),
                query(nw->rc, x1, x2, y1, y2));
  return ret;
void update(int x, int y, int val) {
 assert(root->l <= x && x <= root->r);
  update(root, x, y, val);
int query(int x1, int x2, int y1, int y2) {
  return query(root, x1, x2, y1, y2);
```

2.2 Fenwick RU-RQ

```
void updtRL(int l, int r, ll val) {
 updt(BIT1, l, val), updt(BIT1, r + 1, -val);
 updt(BIT2, l, val * (l - 1)), updt(BIT2, r + 1, -val * r);
ll query(int k) {
 return que(BIT1, k) * k - que(BIT2, k);
```

2.3 Heavy-Light Decomposition

```
struct HLD {
  vector<int> id, size, idx, up, root, st;
  vector<vector<int>> adj, chain;
 SegTree seg;
```

```
up(n, -1), adj(edges), seg(n) {
   precompute(0, -1);
   decompose(0, -1);
    int cnt = 0;
    st.resize(chain.size());
    for(int i = 0; i < (int) chain.size(); ++i) {</pre>
     st[i] = cnt;
     cnt += chain[i].size();
 void precompute(int pos, int dad) {
   size[pos] = 1;
   up[pos] = dad;
    for(auto& i : adj[pos]) {
     if(i != dad)
       precompute(i, pos);
        size[pos] += size[i];
 void decompose(int pos, int dad) {
   if(id[pos] == -1) {
      id[pos] = chain.size();
     root.push_back(pos);
     chain.emplace_back();
    idx[pos] = chain[id[pos]].size();
    chain[id[pos]].push_back(pos);
    int mx = 0, heavy = -1;
    for(auto& i : adj[pos]) {
     if(i != dad && size[i] > mx) {
       mx = size[i];
       heavy = i;
    if(heavy != -1)
     id[heavy] = id[pos];
    for(auto& i : adj[pos]) {
      if(i != dad)
       decompose(i, pos);
 void update(int ch, int l, int r, int val) {
   seg.update(st[ch] + l, st[ch] + r, val);
 int query(int ch, int l, int r, int val) {
   return seg.query(st[ch] + l, st[ch] + r, val);
// how to move from u to v
while(1) {
 if(hld.id[u] == hld.id[v]) {
   if(hld.idx[u] > hld.idx[v])
     swap(u, v);
   hld.update(hld.id[u], hld.idx[u], hld.idx[v], w);
   break;
 if(hld.id[u] < hld.id[v])</pre>
   swap(u, v);
 hld.update(hld.id[u], 0, hld.idx[u], w);
 // or hld.query(hld.id[u], 0, hld.idx[u]);
 u = hld.up[hld.root[hld.id[u]]];
```

HLD(const vector<vector<int>>& edges) :

n(edges.size()), id(n, -1), size(n, -1), idx(n, -1),

2.4 Li-Chao Tree

```
// max li-chao tree
// works for the range [0, MAX - 1]
// if min li-chao tree:
// replace every call to max() with min() and every > with <
// also replace -INF with INF
struct Func {
 ll m, c;
 ll operator()(ll x) {
    return x * m + c;
};
const int MAX = 1e9 + 1;
const ll INF = 1e18;
const Func NIL = {0, -INF};
struct Node {
 Func f;
 Node* lc;
  Node* rc;
  Node() : f(NIL), lc(nullptr), rc(nullptr) {}
 Node(const Node& n) : f(n.f), lc(nullptr), rc(nullptr) {}
Node* root = new Node;
void insert(Func f, Node* cur = root, int l = 0, int r = MAX - 1) {
  int m = l + (r - l) / 2;
  bool left = f(l) > cur->f(l);
  bool mid = f(m) > cur -> f(m);
  if(mid)
    swap(f, cur->f);
  if(l != r) {
    if(left != mid) {
      if(!cur->lc)
        cur->lc = new Node(*cur);
      insert(f, cur->lc, l, m);
    } else {
      if(!cur->rc)
        cur->rc = new Node(*cur);
      insert(f, cur->rc, m + 1, r);
ll query(ll x, Node* cur = root, int l = 0, int r = MAX - 1) {
  if(!cur)
    return -INF;
  if(l == r)
   return cur->f(x);
  int m = l + (r - l) / 2;
  if(x \le m)
    return max(cur->f(x), query(x, cur->lc, l, m));
  else
    return max(cur->f(x), query(x, cur->rc, m + 1, r));
```

2.5 Persistent Segment Tree

```
class PersistentSegtree {
private:
  int n, ptr, sz;
  struct P {
```

```
return node[idxr].val - node[idxl].val;
    int mid = (l + r) / 2;
   return query(node[idxl].l, node[idxr].l, l, mid, x, y)
           + query(node[idxl].r, node[idxr].r, mid + 1, r, x, y);
public:
 PersistentSegtree(int _n) : n(_n), ptr(0) {
   sz = 30 * n;
   node.reserve(sz);
    root.push_back(build(1, n));
 void update(int x, int val) {
   root.push_back(update(root.back(), 1, n, x, val));
 int query(int l, int r, int x, int y) {
    return query(root[l - 1], root[r], 1, n, x, y);
};
2.6 STL PBDS
// ost = ordered set
// omp = ordered map
#include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/tree_policy.hpp>
using namespace __gnu_pbds;
template<class T>
using ost = tree<T, null_type, less<T>, rb_tree_tag,
```

```
int val = 0, l, r;
vector<P> node;
vector<int> root;
int newNode() {
 node.emplace_back();
  return ptr++;
int copyNode(int idx) {
  node.push_back(node[idx]);
  return ptr++;
int build(int l, int r) {
  int idx = newNode();
  if(l == r)
   return idx;
  node[idx].l = build(l, (l + r) / 2);
  node[idx].r = build((l + r) / 2 + 1, r);
  return idx;
int update(int idx, int l, int r, int x, int val) {
  idx = copyNode(idx);
  if(l == r) {
   node[idx].val += val;
    return idx;
  int mid = (l + r) / 2;
  if(x \le mid)
   node[idx].l = update(node[idx].l, l, mid, x, val);
   node[idx].r = update(node[idx].r, mid + 1, r, x, val);
  node[idx].val = node[node[idx].l].val + node[node[idx].r].val;
  return idx;
int query(int idxl, int idxr, int l, int r, int x, int y) {
  if(y < l \mid | r < x)
   return 0:
  if(x <= l && r <= y)
```

```
tree_order_statistics_node_update>;
template<class T, class U>
using omp = tree<T, U, less<T>, rb_tree_tag,
     tree_order_statistics_node_update>;
```

2.7 Treap

```
// Complexity: O(log N) for split and merge
// empty treap: Treap* tr = nullptr;
// insert v at x: [l, r] = split(tr, x), m = Treap(v), merge lmr
// delete at x: [l, r] = split(tr, x), [m, r] = split(r, 1), merge lr
// lazy prop: propagate every time a node is accessed
mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
using Key = int;
struct Treap {
  Kev val;
  Treap* left;
  Treap* right:
  int prio, sz;
  Treap() {}
  Treap(int _val);
int size(Treap* tr) {
 return tr ? tr->sz : 0;
void update(Treap* tr) {
 tr->sz = 1 + size(tr->left) + size(tr->right);
Treap::Treap(Key _val) :
 val(_val), left(nullptr), right(nullptr), prio(rng()) {
  update(this);
pair<Treap*, Treap*> split(Treap* tr, int sz) {
  if(!tr) return {nullptr, nullptr};
  int left_sz = size(tr->left);
  if(sz <= left_sz) {</pre>
    auto [left, mid] = split(tr->left, sz);
    tr->left = mid;
    update(tr);
    return {left, tr};
  } else {
    auto [mid, right] = split(tr->right, sz - left_sz - 1);
    tr->right = mid;
    update(tr);
    return {tr, right};
Treap* merge(Treap* l, Treap* r) {
  if(!l)
    return r;
  if(!r)
  if(l->prio < r->prio) {
    l->right = merge(l->right, r);
    update(l);
    return l;
  } else {
    r->left = merge(l, r->left);
    update(r);
    return r;
```

2.8 Unordered Map Custom Hash

2.9 Mo's on Tree

```
\begin{split} ST(u) &\leq ST(v) \\ P &= LCA(u,v) \\ \text{If } P &= u, \text{ query } [ST(u),ST(v)] \\ \text{Else query } [EN(u),ST(v)] + [ST(P),ST(P)] \end{split}
```

2.10 Link-Cut Tree

```
// Represents a forest of unrooted trees. You can add and remove edges
// (as long as the result is still a forest), and check whether two
// nodes are in the same tree.
// Complexity: log(n)
struct Node { // Splay tree. Root's pp contains tree's parent.
 Node* p = 0, *pp = 0, *c[2];
 int sz = 0;
 Node() {
   c[0] = c[1] = 0;
   fix();
 void fix() {
   if(c[0]) c[0] -> p = this, sz += c[0] -> sz;
   if(c[1]) c[1] \rightarrow p = this, sz += c[1] \rightarrow sz;
    // (+ update sum of subtree elements etc. if wanted)
   return p ? p->c[1] == this : -1;
 void rot(int i, int b) {
   int h = i ^ b;
    Node* x = c[i], *y = (b == 2 ? x : x->c[h]), *z = (b ? y : x);
   if(y->p = p) p->c[up()] = y;
   c[i] = z -> c[i ^ 1];
    if(b < 2) x - c[h] = y - c[h ^ 1], z - c[h ^ 1] = b ? x : this;
    y - c[i ^ 1] = b ? this : x;
   fix();
   x \rightarrow fix();
    y->fix();
   if(p) p->fix();
    swap(pp, y->pp);
 // Splay this up to the root. Always finishes without flip set.
 void splay() {
   while(p) {
     int c1 = up(), c2 = p \rightarrow up();
```

```
if(c2 == -1) p->rot(c1, 2);
      else p->p->rot(c2, c1 != c2);
};
struct LinkCut {
 vector<Node> node;
  LinkCut(int N) : node(N + 1) {}
  void link(int u, int v) { // add an edge u --> v
   assert(!connected(u, v));
    access(&node[u]);
    access(&node[v]);
   node[u].c[0] = &node[v];
    node[v].p = &node[u];
    node[u].fix();
  void cut(int u, int v) { // remove an edge u --> v
   assert(connected(u, v));
    Node* x = &node[v], *top = &node[u];
    access(top);
    top->c[0] = top->c[0]->p = 0;
    top->fix();
  bool connected(int u, int v) { // are u, v in the same tree?
    return root(u) == root(v);
  int root(int u) { // find the root id of node u
    Node* x = &node[u];
    access(x);
    for(; x \rightarrow c[0]; x = x \rightarrow c[0]);
    x->splay();
    return (int)((vector<Node>::iterator)x - node.begin());
  // Move u to root aux tree. Return the root of the root aux tree.
  Node* access(Node* u) {
   u->splay();
    Node* last = u:
    if(Node*\& x = u->c[1]) {
     x->pp = u;
     x->p = 0;
     \times = 0;
     u->fix();
    for(Node * pp; (pp = u->pp) && (last = pp);) {
     pp->splay();
      if(pp->c[1]) pp->c[1]->p = 0, pp->c[1]->pp = pp;
     pp->c[1] = u;
     u->p = pp;
     u->pp = 0;
     pp->fix();
      u->splay();
    return last;
  int depth(int u) {
    access(&node[u]);
    return node[u].sz - 1;
  Node* lca(int u, int v) {
   access(&node[u]);
    return access(&node[v]);
};
```

3 Dynamic Programming

3.1 DP Convex Hull

Jangan Salah Baca Soal Lagi Bina Nusantara University

3.2 DP DNC

```
void f(int rem, int l, int r, int optl, int optr) {
    if(l > r)
        return;
    int mid = l + r >> l;
    int opt = MOD, optid = mid;
    for(int i = optl; i <= mid && i <= optr; ++i) {
        if(dp[rem - 1][i] + c[i][mid] < opt) {
            opt = dp[rem - 1][i] + c[i][mid];
            optid = i;
        }
    }
    dp[rem][mid] = opt;
    f(rem, l, mid - 1, optl, optid);
    f(rem, mid + 1, r, optid, optr);
    return;
}
rep(i, 1, n)dp[1][i] = c[0][i];
rep(i, 2, k)f(i, i, n, i, n);</pre>
```

3.3 DP Knuth-Yao

4 Geometry

4.1 Geometry Template

```
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```

```
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            x and y magnitude of the vector
        3.1.3. vec(double _x,double _y)
            constructor, set the vector to (_x,_y)
        3.1.4. vec(point A,point B)
            constructor, set the vector to vector AB (A->B)
/*General Double Operation*/
const double PI = acos(-1.0);
const double INFD = 1E9;
double between_d(double x, double l, double r) {
 return (min(l, r) \le x + EPS \&\& x \le max(l, r) + EPS);
double same_d(double x, double y) {
 return between_d(x, y, y);
double dabs(double x) {
  if(x < EPS)
    return -x;
  return x;
/*Point*/
struct point {
  double x, y;
  point() {
    x = y = 0.0;
  point(double _x, double _y) {
    \times = \_ \times ;
    y = _y;
  bool operator< (point other) {
    if(x < other.x + EPS)
      return true;
    if(x + EPS > other.x)
      return false;
    return y < other.y + EPS;
  bool operator == (point other) {
```

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```
return same_d(x, other.x) && same_d(y, other.y);
double e_dist(point P1, point P2) {
 return hypot(P1.x - P2.x, P1.y - P2.y);
double m_dist(point P1, point P2) {
 return dabs(P1.x - P2.x) + dabs(P1.y - P2.y);
double pointBetween(point P, point L, point R) {
 return (e_dist(L, P) + e_dist(P, R) == e_dist(L, R));
bool collinear(point P, point L,
               point R) { //newly added(luis), cek 3 poin segaris
  return P.x * (L.y - R.y) + L.x * (R.y - P.y) + R.x * (P.y - L.y) ==
         0; // bole gnti "dabs(x)<"EPS
/*Vector*/
struct vec {
 double x, y;
 vec() {
   \times = \vee = \odot.\odot;
 vec(double _x, double _y) {
   \times = \_\times;
   y = _y;
  vec(point A) {
   \times = A.\times;
   y = A.y;
 vec(point A, point B) {
   x = B.x - A.x;
    y = B.y - A.y;
vec scale(vec v, double s) {
 return vec(v.x * s, v.y * s);
vec flip(vec v) {
 return vec(-v.x, -v.y);
double dot(vec u, vec v) {
 return (u.x * v.x + u.y * v.y);
double cross(vec u, vec v) {
 return (u.x * v.y - u.y * v.x);
double norm_sq(vec v) {
 return (v.x * v.x + v.y * v.y);
point translate(point P, vec v) {
 return point(P.x + v.x, P.y + v.y);
point rotate(point P, point O, double angle) {
 vec v(0);
 P = translate(P, flip(v));
 return translate(point(P.x * cos(angle) - P.y * sin(angle),
                         P.x * sin(angle) + P.y * cos(angle)), v);
point mid(point P, point Q) {
 return point((P.x + Q.x) / 2, (P.y + Q.y) / 2);
double angle(point A, point O, point B) {
 vec OA(O, A), OB(O, B);
 return acos(dot(OA, OB) / sqrt(norm_sq(OA) * norm_sq(OB)));
int orientation(point P, point Q, point R) {
  vec PQ(P, Q), PR(P, R);
 double c = cross(PQ, PR);
```

```
if(c < -EPS)
   return -1;
  if(c > EPS)
   return 1;
 return 0;
/*Line*/
struct line {
 double a, b, c;
 line() {
   a = b = c = 0.0;
  line(double _a, double _b, double _c) {
   a = _a;
   b = b;
   C = _C;
  line(point P1, point P2) {
   if(P1 < P2)
     swap(P1, P2);
    if(same_d(P1.x, P2.x))
     a = 1.0, b = 0.0, c = -P1.x;
     a = -(P1.y - P2.y) / (P1.x - P2.x), b = 1.0, c = -(a * P1.x) - P1.y;
  line(point P, double slope) {
   if(same d(slope, INFD))
     a = 1.0, b = 0.0, c = -P.x;
   else
     a = -slope, b = 1.0, c = -(a * P.x) - P.y;
  bool operator== (line other) {
   return same_d(a, other.a) && same_d(b, other.b) && same_d(c, other.c);
 double slope() {
   if(same_d(b, 0.0))
     return INFD;
    return -(a / b);
bool paralel(line L1, line L2) {
 return same_d(L1.a, L2.a) && same_d(L1.b, L2.b);
bool intersection(line L1, line L2, point& P) {
 if(paralel(L1, L2))
   return false;
 P.x = (L2.b * L1.c - L1.b * L2.c) / (L2.a * L1.b - L1.a * L2.b);
 if(same_d(L1.b, 0.0))
   P.y = -(L2.a * P.x + L2.c);
 else
   P.y = -(L1.a * P.x + L1.c);
 return true;
double pointToLine(point P, point A, point B, point& C) {
 vec AP(A, P), AB(A, B);
 double u = dot(AP, AB) / norm_sq(AB);
 C = translate(A, scale(AB, u));
 return e_dist(P, C);
double lineToLine(line L1, line L2) {
 if(!paralel(L1, L2))
    return 0.0;
 return dabs(L2.c - L1.c) / sqrt(L1.a * L1.a + L1.b * L1.b);
/*Line Segment*/
struct segment
  point P, Q;
 line L;
  segment() {
    point T1;
    P = Q = T1;
```

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```
line T2;
   L = T2;
 segment(point _P, point _Q) {
   P = P;
   Q = _Q;
   if(0 < P)
     swap(P, Q);
   line T(P, Q);
   L = T;
 bool operator == (segment other) {
   return P == other.P && Q == other.Q;
};
bool onSegment(point P, segment S) {
 if(orientation(S.P, S.Q, P) != 0)
 return between_d(P.x, S.P.x, S.Q.x) && between_d(P.y, S.P.y, S.Q.y);
bool s intersection(segment S1, segment S2) {
 double o1 = orientation(S1.P, S1.Q, S2.P);
 double o2 = orientation(S1.P, S1.0, S2.0);
 double o3 = orientation(S2.P, S2.Q, S1.P);
 double o4 = orientation(S2.P, S2.Q, S1.Q);
 if(o1 != o2 && o3 != o4)
   return true;
 if(o1 == 0 && onSegment(S2.P, S1))
   return true:
 if(o2 == 0 \&\& onSegment(S2.Q, S1))
   return true:
 if(o3 == 0 && onSegment(S1.P, S2))
   return true:
 if(o4 == 0 && onSegment(S1.Q, S2))
   return true;
 return false;
double pointToSegment(point P, point A, point B, point& C) {
 vec AP(A, P), AB(A, B);
 double u = dot(AP, AB) / norm_sq(AB);
 if(u < EPS) {
   C = A;
   return e_dist(P, A);
 if(u + EPS > 1.0) {
   C = B;
   return e_dist(P, B);
 return pointToLine(P, A, B, C);
double segmentToSegment(segment S1, segment S2) {
 if(s_intersection(S1, S2))
   return 0.0;
 double ret = INFD;
 point dummy;
 ret = min(ret, pointToSegment(S1.P, S2.P, S2.Q, dummy));
 ret = min(ret, pointToSegment(S1.Q, S2.P, S2.Q, dummy));
 ret = min(ret, pointToSegment(S2.P, S1.P, S1.Q, dummy));
 ret = min(ret, pointToSegment(S2.Q, S1.P, S1.Q, dummy));
 return ret;
/*Circle*/
struct circle {
 point P;
 double r;
 circle() {
   point P1;
   P = P1;
   r = 0.0;
 circle(point _P, double _r) {
```

```
P = _P;
    r = _r;
 circle(point P1, point P2) {
   P = mid(P1, P2);
    r = e_dist(P, P1);
 circle(point P1, point P2, point P3) {
   vector<point> T;
   T.clear();
   T.pb(P1);
   T.pb(P2);
    T.pb(P3);
    sort(T.begin(), T.end());
   P1 = T[0];
   P2 = T[1];
   P3 = T[2];
    point M1, M2;
   M1 = mid(P1, P2);
    M2 = mid(P2, P3);
    point Q2, Q3;
    Q2 = rotate(P2, P1, PI / 2);
    Q3 = rotate(P3, P2, PI / 2);
    vec P1Q2(P1, Q2), P2Q3(P2, Q3);
    point M3, M4;
    M3 = translate(M1, P102);
    M4 = translate(M2, P203);
    line L1(M1, M3), L2(M2, M4);
    intersection(L1, L2, P);
    r = e_dist(P, P1);
 bool operator==(circle other) {
    return (P == other.P && same_d(r, other.r));
bool insideCircle(point P, circle C) {
 return e_dist(P, C.P) <= C.r + EPS;</pre>
bool c_intersection(circle C1, circle C2, point& P1, point& P2) {
 double d = e_dist(C1.P, C2.P);
 if(d > C1.r + C2.r) {
   return false; //d+EPS kalo butuh
 if(d < dabs(C1.r - C2.r) + EPS)
   return false:
  double x1 = C1.P.x, y1 = C1.P.y, r1 = C1.r, x2 = C2.P.x, y2 = C2.P.y, r2 = C2.r;
 double a = (r1 * r1 - r2 * r2 + d * d) / (2 * d), h = sqrt(r1 * r1 - a * a);
  point T(x1 + a * (x2 - x1) / d, y1 + a * (y2 - y1) / d);
 P1 = point(T.x - h * (y2 - y1) / d, T.y + h * (x2 - x1) / d);
 P2 = point(T.x + h * (y2 - y1) / d, T.y - h * (x2 - x1) / d);
 return true;
bool lc_intersection(line L, circle O, point& P1, point& P2) {
 double a = L.a, b = L.b, c = L.c, x = 0.P.x, y = 0.P.y, r = 0.r;
  double A = a * a + b * b, B = 2 * a * b * y - 2 * a * c - 2 * b * b * x,
         C = b * b * x * x + b * b * y * y - 2 * b * c * y + c * c - b * b * r * r;
  double D = B * B - 4 * A * C;
  point T1, T2;
  if(same_d(b, 0.0)) {
    T1.x = c / a;
   if(dabs(x - T1.x) + EPS > r)
     return false;
    if(same_d(T1.x - r - x, 0.0) \mid | same_d(T1.x + r - x, 0.0)) 
     P1 = P2 = point(T1.x, y);
      return true;
    double dx = dabs(T1.x - x), dy = sqrt(r * r - dx * dx);
   P1 = point(T1.x, y - dy);
   P2 = point(T1.x, y + dy);
    return true;
```

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```
if(same_d(D, 0.0)) {
   T1.x = -B / (2 * A);
   T1.y = (c - a * T1.x) / b;
   P1 = P2 = T1;
   return true;
 if(D < EPS)
  return false;
 D = sqrt(D);
 T1.x = (-B - D) / (2 * A);
 T1.y = (c - a * T1.x) / b;
 P1 = T1:
 T2.x = (-B + D) / (2 * A);
 T2.y = (c - a * T2.x) / b;
 P2 = T2;
 return true:
bool sc_intersection(segment S, circle C, point& P1, point& P2) {
 bool cek = lc_intersection(S.L, C, P1, P2);
 if(!cek)
  return false:
 double x1 = S.P.x, y1 = S.P.y, x2 = S.Q.x, y2 = S.Q.y;
 bool b1 = between_d(P1.x, x1, x2) && between_d(P1.y, y1, y2);
 bool b2 = between_d(P2.x, x1, x2) && between_d(P2.y, y1, y2);
 if(P1 == P2)
  return b1;
 if(b1 || b2) {
   if(!b1)
     P1 = P2;
   if(!b2)
    P2 = P1:
   return true:
 return false;
/*Triangle*/
double t_perimeter(point A, point B, point C) {
 return e_dist(A, B) + e_dist(B, C) + e_dist(C, A);
double t_area(point A, point B, point C) {
 double s = t_perimeter(A, B, C) / 2;
 double ab = e_dist(A, B), bc = e_dist(B, C), ac = e_dist(C, A);
 return sqrt(s * (s - ab) * (s - bc) * (s - ac));
circle t_inCircle(point A, point B, point C) {
 vector<point> T;
 T.clear();
 T.pb(A);
 T.pb(B);
 T.pb(C);
 sort(T.begin(), T.end());
 A = T[0];
 B = T[1];
 double r = t_area(A, B, C) / (t_perimeter(A, B, C) / 2);
 double ratio = e_dist(A, B) / e_dist(A, C);
 vec BC(B, C);
 BC = scale(BC, ratio / (1 + ratio));
 point P;
 P = translate(B, BC);
 line AP1(A, P);
 ratio = e_dist(B, A) / e_dist(B, C);
 vec AC(A, C);
 AC = scale(AC, ratio / (1 + ratio));
 P = translate(A, AC);
 line BP2(B, P);
 intersection(AP1, BP2, P);
 return circle(P, r);
circle t_outCircle(point A, point B, point C) {
 return circle(A, B, C);
```

```
/*Polygon*/
struct polygon -
 vector<point> P;
  polygon()
   P.clear();
  polygon(vector<point>& _P) {
    P = P;
bool rayCast(point P, polygon& A) {
  point Q(P.x, 10000);
  line cast(P, Q);
  int cnt = 0;
  FOR(i, (int)(A.P.size()) - 1) {
    line temp(A.P[i], A.P[i + 1]);
    bool B = intersection(cast, temp, I);
    if(!B)
     continue;
    else if(I == A.P[i] \mid \mid I == A.P[i + 1])
    else if(pointBetween(I, A.P[i], A.P[i + 1]) && pointBetween(I, P, Q))
 return cnt % 2 == 1;
// line segment p-a intersect with line A-B.
point lineIntersectSeg(point p, point q, point A, point B) {
 double a = B.y - A.y;
  double b = A.x - B.x;
  double c = B.x * A.y - A.x * B.y;
  double u = fabs(a * p.x + b * p.y + c);
  double v = fabs(a * q.x + b * q.y + c);
  return point((p.x * v + q.x * u) / (u + v), (p.y * v + q.y * u) / (u + v));
// cuts polygon Q along the line formed by point a -> point b
// (note: the last point must be the same as the first point)
vector<point> cutPolygon(point a, point b, const vector<point>& Q) {
  vector<point> P;
  for(int i = 0; i < (int)Q.size(); i++) {</pre>
    double left1 = cross(toVec(a, b), toVec(a, Q[i]));
    double left2 = 0;
    if(i != (int)Q.size() - 1)
      left2 = cross(toVec(a, b), toVec(a, Q[i + 1]));
    if(left1 > -EPS)
     P.push_back(Q[i]);
    if(left1 * left2 < -EPS)</pre>
     P.push_back(lineIntersectSeg(Q[i], Q[i + 1], a, b));
  if(!P.empty() && !(P.back() == P.front()))
   P.push_back(P.front());
  return P;
circle minCoverCircle(polygon& A) {
  vector<point> p = A.P;
  point c;
  circle ret;
  double cr = 0.0;
  int i, j, k;
  c = p[0];
  for(i = 1; i < p.size(); i++) {
    if(e_dist(p[i], c) >= cr + EPS) {
     c = p[i], cr = 0;
      ret = circle(c, cr);
      for(j = 0; j < i; j++) {
        if(e_dist(p[j], c) >= cr + EPS) {
          c = mid(p[i], p[j]);
          cr = e_dist(p[i], c);
          ret = circle(c, cr);
```

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```
for (k = 0; k < j; k++) {
           if(e_dist(p[k], c) >= cr + EPS) {
             ret = circle(p[i], p[j], p[k]);
             c = ret.P;
             cr = ret.r;
 return ret;
/*Geometry Algorithm*/
double DP[110][110];
double minCostPolygonTriangulation(polygon& A) {
 if(A.P.size() < 3)
   return 0;
 FOR(i, A.P.size()) {
   for(int j = 0, k = i; k < A.P.size(); j++, k++) {
     if(k < j + 2)
       DP[j][k] = 0.0;
     else {
       DP[j][k] = INFD;
       REP(l, j + 1, k - 1) {
         double cost = e_dist(A.P[j], A.P[k]) + e_dist(A.P[k], A.P[l]) + e_dist(A.P[l])
         DP[j][k] = min(DP[j][k], DP[j][l] + DP[l][k] + cost);
 return DP[0][A.P.size() - 1];
```

4.2 Convex Hull

```
typedef double TD;
                                 // for precision shits
namespace GEOM {
 typedef pair<TD, TD> Pt;
                                 // vector and points
 const TD EPS = 1e-9;
 const TD maxD = 1e9;
 TD cross(Pt a, Pt b, Pt c) {
                                 // right hand rule
   TD v1 = a.first - c.first;
                                 // (a-c) X (b-c)
   TD v2 = a.second - c.second;
   TD u1 = b.first - c.first;
   TD u2 = b.second - c.second;
   return v1 * u2 - v2 * u1;
 TD cross(Pt a, Pt b) {
                                 // a X b
   return a.first * b.second - a.second * b.first;
 TD dot(Pt a, Pt b, Pt c) {
                                 // (a-c) . (b-c)
   TD v1 = a.first - c.first;
   TD v2 = a.second - c.second;
   TD u1 = b.first - c.first;
   TD u2 = b.second - c.second;
   return v1 * u1 + v2 * u2;
 TD dot(Pt a, Pt b) {
   return a.first * b.first + a.second * b.second;
 TD dist(Pt a, Pt b) {
   return sgrt((a.first - b.first) * (a.first - b.first) +
               (a.second - b.second) * (a.second - b.second));
 TD shoelaceX2(vector<Pt>& convHull) {
   TD ret = 0;
   for(int i = 0, n = convHull.size(); i < n; i++)</pre>
```

```
ret += cross(convHull[i], convHull[(i + 1) % n]);
  return ret;
vector<Pt> createConvexHull(vector<Pt>& points) {
  sort(points.begin(), points.end());
  vector<Pt> ret;
  for(int i = 0; i < points.size(); i++) {</pre>
    while(ret.size() > 1 &&
          cross(points[i], ret[ret.size() - 1], ret[ret.size() - 2]) < -EPS)</pre>
      ret.pop_back();
    ret.push_back(points[i]);
  for(int i = points.size() - 2, sz = ret.size(); i >= 0; i--) {
    while(ret.size() > sz &&
          cross(points[i], ret[ret.size() - 1], ret[ret.size() - 2]) < -EPS)</pre>
      ret.pop back();
    if(i == 0)
     break:
    ret.push_back(points[i]);
  return ret;
  bool isInside(Pt pv, vector<Pt>& x) { //using winding number
    int n = x.size(), wn = 0;
    x.push_back(x[0]);
    for(int i = 0; i < n; ++i) {
     if(((x[i + 1].first \le pv.first \&\& x[i].first >= pv.first) ||
          (x[i + 1].first >= pv.first && x[i].first <= pv.first)) &&
          ((x[i + 1].second <= pv.second && x[i].second >= pv.second) ||
           (x[i + 1].second >= pv.second && x[i].second <= pv.second))) {
        if(cross(x[i], x[i + 1], pv) == 0) {
          x.pop_back();
          return true:
    for(int i = 0; i < n; ++i) {
      if(x[i].second <= pv.second) {</pre>
        if(x[i + 1].second > pv.second && cross(x[i], x[i + 1], pv) > 0)
      } else if(x[i + 1].second <= pv.second && cross(x[i], x[i + 1], pv) < 0)
        --wn;
    x.pop_back();
    return wn != 0;
bool isInside(Pt pv, vector<Pt>& x) { //using winding number
  int n = x.size(), wn = 0;
  x.push_back(x[0]);
  for(int i = 0; i < n; ++i) {
   if(((x[i + 1].first \le pv.first \&\& x[i].first >= pv.first) ||
        (x[i + 1].first >= pv.first && x[i].first <= pv.first)) &&
        ((x[i + 1].second \le pv.second \&\& x[i].second >= pv.second) ||
         (x[i + 1].second >= pv.second && x[i].second <= pv.second))) {
      if(cross(x[i], x[i + 1], pv) == 0) {
        x.pop_back();
        return true;
  for(int i = 0; i < n; ++i) {
   if(x[i].second <= pv.second) {
      if(x[i + 1].second > pv.second && cross(x[i], x[i + 1], pv) > 0)
    } else if(x[i + 1].second <= pv.second && cross(x[i], x[i + 1], pv) < 0)
      --wn;
  x.pop_back();
  return wn != 0;
```

4.3 Closest Pair of Points

```
#define fi first
#define se second
typedef pair<int, int> pii;
struct Point {
 int x, y, id;
int compareX(const void* a, const void* b) {
 Point* p1 = (Point*)a, *p2 = (Point*)b;
 return (p1->x - p2->x);
int compareY(const void* a, const void* b) {
 Point* p1 = (Point*)a, *p2 = (Point*)b;
 return (p1->y - p2->y);
double dist(Point p1, Point p2) {
 return sqrt((double)(p1.x - p2.x) * (p1.x - p2.x) +
              (double)(p1.y - p2.y) * (p1.y - p2.y)
             );
pair<pii, double> bruteForce(Point P[], int n) {
 double min = 1e8;
 pii ret = pii(-1, -1);
  for(int i = 0; i < n; ++i)
   for(int j = i + 1; j < n; ++j)
      if(dist(P[i], P[j]) < min) {</pre>
       ret = pii(P[i].id, P[j].id);
        min = dist(P[i], P[j]);
 return pair<pii, double> (ret, min);
pair<pii, double> getmin(pair<pii, double> x, pair<pii, double> y) {
 if(x.fi.fi == -1 && x.fi.se == -1)
   return y;
 if(y.fi.fi == -1 && y.fi.se == -1)
   return x;
 return (x.se < y.se) ? x : y;</pre>
pair<pii, double> stripClosest(Point strip[], int size, double d) {
 double min = d:
 pii ret = pii(-1, -1);
 qsort(strip, size, sizeof(Point), compareY);
  for(int i = 0; i < size; ++i)
   for(int j = i + 1; j < size && (strip[j].y - strip[i].y) < min; ++j)
      if(dist(strip[i], strip[j]) < min) {</pre>
        ret = pii(strip[i].id, strip[j].id);
        min = dist(strip[i], strip[j]);
 return pair<pii, double>(ret, min);
pair<pii, double> closestUtil(Point P[], int n) {
 if(n <= 3)
   return bruteForce(P, n);
  int mid = n / 2;
 Point midPoint = P[mid];
 pair<pii, double> dl = closestUtil(P, mid);
 pair<pii, double> dr = closestUtil(P + mid, n - mid);
  pair<pii, double> d = getmin(dl, dr);
 Point strip[n];
  int j = 0;
  for(int i = 0; i < n; i++)
   if(abs(P[i].x - midPoint.x) < d.second)</pre>
      strip[j] = P[i], j++;
 return getmin(d, stripClosest(strip, j, d.second));
pair<pii, double> closest(Point P[], int n) {
 qsort(P, n, sizeof(Point), compareX);
```

```
return closestUtil(P, n);
}
Point P[50005];
int main() {
   int n;
   scanf("%d", &n);
   for(int a = 0; a < n; a++) {
        scanf("%d%d", &P[a].x, &P[a].y);
        P[a].id = a;
   }
   pair<pri>pair<pri>pair<in>i, double> hasil = closest(P, n);
   if(hasil.fi.fi > hasil.fi.se);
        swap(hasil.fi.fi, hasil.fi.se);
   printf("%d %d %.6lf\n", hasil.fi.fi, hasil.fi.se, hasil.se);
   return 0;
}
```

4.4 Smallest Enclosing Circle

```
// welzl's algo to find the 2d minimum enclosing circle of a set of points
// expected O(N)
// directions: remove duplicates and shuffle points, then call welzl(points)
struct Point {
 double x;
 double y;
struct Circle {
 double x, y, r;
 Circle() {}
 Circle(double _x, double _y, double _r): x(_x), y(_y), r(_r) {}
Circle trivial(const vector<Point>& r) {
 if(r.size() == 0)
    return Circle(0, 0, -1);
  else if(r.size() == 1)
    return Circle(r[0].x, r[0].y, 0);
  else if(r.size() == 2) {
    double cx = (r[0].x + r[1].x) / 2.0, cy = (r[0].y + r[1].y) / 2.0;
    double rad = hypot(r[0].x - r[1].x, r[0].y - r[1].y) / 2.0;
    return Circle(cx, cy, rad);
  } else {
    double x0 = r[0].x, x1 = r[1].x, x2 = r[2].x;
    double y0 = r[0].y, y1 = r[1].y, y2 = r[2].y;
    double d = (x0 - x2) * (y1 - y2) - (x1 - x2) * (y0 - y2);
    double cx = (((x0 - x2) * (x0 + x2) + (y0 - y2) * (y0 + y2)) / 2 *
                 (y1 - y2) - ((x1 - x2) * (x1 + x2) + (y1 - y2) * (y1 + y2)) / 2
                 * (y0 - y2)) / d;
    double cy = (((x1 - x2) * (x1 + x2) + (y1 - y2) * (y1 + y2)) / 2 *
                 (x0 - x2) - ((x0 - x2) * (x0 + x2) + (y0 - y2) * (y0 + y2)) / 2
                 *(x1 - x2)) / d;
    return Circle(cx, cy, hypot(x0 - cx, y0 - cy));
Circle welzl(const vector<Point>& p, int idx = 0, vector<Point> r = {}) {
 if(idx == (int) p.size() || r.size() == 3)
   return trivial(r);
  Circle d = welzl(p, idx + 1, r);
  if(hypot(p[idx].x - d.x, p[idx].y - d.y) > d.r) {
   r.push_back(p[idx]);
   d = welzl(p, idx + 1, r);
  return d;
```

4.5 Sutherland-Hodgman Algorithm

```
// Complexity: linear time
// Ada 2 poligon, cari poligon intersectionnya
// poly_point = hasilnya, clipper = pemotongnya
#include<bits/stdc++.h>
using namespace std;
const double EPS = 1e-9;
struct point {
 double x, y;
 point(double _x, double _y): x(_x), y(_y) {}
struct vec {
 double x, y;
 vec(double _x, double _y): x(_x), y(_y) {}
point pivot(0, 0);
vec toVec(point a, point b) {
 return vec(b.x - a.x, b.y - a.y);
double dist(point a, point b) {
 return hypot(a.x - b.x, a.y - b.y);
double cross(vec a, vec b) {
 return a.x * b.y - a.y * b.x;
bool ccw(point p, point q, point r) {
 return cross(toVec(p, q), toVec(p, r)) > 0;
bool collinear(point p, point q, point r) {
 return fabs(cross(toVec(p, q), toVec(p, r))) < EPS;</pre>
bool lies(point a, point b, point c) {
 if((c.x) = min(a.x, b.x) \&\& c.x \le max(a.x, b.x)) \&\&
      (c.y >= min(a.y, b.y) \&\& c.y <= max(a.y, b.y)))
   return true;
 else
   return false;
bool anglecmp(point a, point b) {
 if(collinear(pivot, a, b))
   return dist(pivot, a) < dist(pivot, b);</pre>
 double dlx = a.x - pivot.x, dly = a.y - pivot.y;
 double d2x = b.x - pivot.x, d2y = b.y - pivot.y;
 return (atan2(d1y, d1x) - atan2(d2y, d2x)) < 0;
point intersect(point s1, point e1, point s2, point e2) {
 double x1, x2, x3, x4, y1, y2, y3, y4;
 x1 = s1.x;
 y1 = s1.y;
 x2 = e1.x;
 y2 = e1.y;
 x3 = s2.x;
 y3 = s2.y;
 x4 = e2.x;
 double num1 = (x1 * y2 - y1 * x2) * (x3 - x4) - (x1 - x2) * (x3 * y4 - y3 * x4);
 double num2 = (x1 * y2 - y1 * x2) * (y3 - y4) - (y1 - y2) * (x3 * y4 - y3 * x4);
 double den = (x1 - x2) * (y3 - y4) - (y1 - y2) * (x3 - x4);
 double new_x = num1 / den;
 double new_y = num2 / den;
 return point(new_x, new_y);
void clip(vector <point>& poly_points, point point1, point point2) {
 vector <point> new_points;
 new_points.clear();
```

```
for(int i = 0; i < poly_points.size(); i++) -</pre>
    int k = (i + 1) % poly_points.size();
    double i_pos = ccw(point1, point2, poly_points[i]);
    double k_pos = ccw(point1, point2, poly_points[k]);
    if(i_pos <= 0 && k_pos <= 0)
     new_points.push_back(poly_points[k]);
    else if(i_pos > 0 && k_pos <= 0) {
     new_points.push_back(intersect(point1, point2, poly_points[i],
                                     poly_points[k]));
      new_points.push_back(poly_points[k]);
   else if(i_pos <= 0 && k_pos > 0) {
     new_points.push_back(intersect(point1, point2, poly_points[i],
                                     poly_points[k]));
   else {
 poly_points.clear();
  for(int i = 0; i < new_points.size(); i++)</pre>
   poly_points.push_back(new_points[i]);
double area(const vector <point>& P) {
 double result = 0.0:
 double x1, y1, x2, y2;
  for(int i = 0; i < P.size() - 1; i++) {
   x1 = P[i].x;
   y1 = P[i].y;
   x2 = P[i + 1].x:
   y2 = P[i + 1].y;
   result += (x1 * y2 - x2 * y1);
 return fabs(result) / 2;
void suthHodgClip(vector <point>& poly_points, vector <point> clipper_points) {
 for(int i = 0; i < clipper_points.size(); i++) {</pre>
    int k = (i + 1) % clipper_points.size();
   clip(poly_points, clipper_points[i], clipper_points[k]);
vector<point> sortku(vector<point> P) {
 int P0 = 0;
  int i;
  for(i = 1; i < 3; i++) {
   if(P[i].y < P[P0].y || (P[i].y == P[P0].y && P[i].x > P[P0].x))
     P0 = i;
  point temp = P[0];
 P[0] = P[P0];
 P[P0] = temp;
 pivot = P[0];
 sort(++P.begin(), P.end(), anglecmp);
 reverse(++P.begin(), P.end());
 return P;
 clipper_points = sortku(clipper_points);
 suthHodgClip(poly_points, clipper_points);
```

4.6 Centroid of Polygon

$$C_x = \frac{1}{6A} \sum_{i=0}^{n-1} (x_i + x_{i+1})(x_i \ y_{i+1} - x_{i+1} \ y_i)$$
$$C_y = \frac{1}{6A} \sum_{i=0}^{n-1} (y_i + y_{i+1})(x_i \ y_{i+1} - x_{i+1} \ y_i)$$

4.7 Pick Theorem

- A: Area of a simply closed lattice polygon
- B: Number of lattice points on the edges
- I: Number of points in the interior $A = I + \frac{B}{2} 1$

5 Graphs

5.1 Articulation Point and Bridge

```
// gr -> adj list
// vector vis, low -> initialize to -1
// int timer -> initialize to 0
void dfs(int pos, int dad = -1) {
 vis[pos] = low[pos] = timer++;
 int kids = 0;
 for(auto& i : gr[pos]) {
   if(i == dad)
     continue;
   if(vis[i] >= 0)
     low[pos] = min(low[pos], vis[i]);
   else {
     dfs(i, pos);
     low[pos] = min(low[pos], low[i]);
     if(low[i] > vis[pos])
       is_bridge(pos, i)
       if(low[i] >= vis[pos] && dad >= 0)
         is_articulation_point(pos)
         ++kids;
 if(dad == -1 && kids > 1)
   is_articulation_point(pos)
```

5.2 SCC and Strong Orientation

```
#define N 10020
vector<int> adj[N];
bool vis[N], ins[N];
int disc[N], low[N], gr[N];
stack<int> st;
int id, grid;
void scc(int cur, int par) {
 disc[cur] = low[cur] = ++id;
 vis[cur] = ins[cur] = 1;
 st.push(cur);
  for(int to : adj[cur]) {
    //if (to==par) continue; // ini untuk SO(scc undirected)
    if(!vis[to])
      scc(to, cur);
    if(ins[to])
      low[cur] = min(low[cur], low[to]);
  if(low[cur] == disc[cur]) {
    grid++; // group id
    while(ins[cur]) {
      gr[st.tp] = grid;
      ins[st.tp] = 0;
      st.pop();
```

5.3 Centroid Decomposition

```
int build_cen(int nw) {
 com_cen(nw, 0); //fungsi untuk itung size subtree
  int siz = sz[nw] / 2;
 bool found = false;
 while(!found) {
    found = true;
    for(int i : v[nw]) {
     if(!rem[i] && sz[i] < sz[nw]) {</pre>
        if(sz[i] > siz) {
          found = false;
          nw = i;
          break;
 big
 rem[nw] = true;
  for(int i : v[nw])if(!rem[i])
     par_cen[build_cen(i)] = nw;
  return nw;
```

5.4 Dinic's Maximum Flow

```
// O(VE log(max_flow)) if scaling == 1
// O((V + E) sqrt(E)) if unit graph (turn scaling off)
// O((V + E) sqrt(V)) if bipartite matching (turn scaling off)
// indices are 0-based
const ll INF = 1e18;
struct Dinic {
  struct Edge {
    int v;
    ll cap, flow;
    Edge(int _v, ll _cap): v(_v), cap(_cap), flow(0) {}
  int n;
  ll lim;
  vector<vector<int>> gr;
  vector<Edge> e;
  vector<int> idx, lv;
  bool has_path(int s, int t) {
    queue<int> q;
    q.push(s);
    lv.assign(n, -1);
    lv[s] = 0;
    while(!q.empty()) {
      int c = q.front();
      q.pop();
      if(c == t)
        break;
      for(auto& i : gr[c]) {
        ll cur_flow = e[i].cap - e[i].flow;
        if(lv[e[i].v] == -1 && cur_flow >= lim) {
          lv[e[i].v] = lv[c] + 1;
          q.push(e[i].v);
    return lv[t] != -1;
  ll get_flow(int s, int t, ll left) {
    if(!left || s == t)
      return left;
    while(idx[s] < (int) gr[s].size()) {</pre>
```

```
15
```

```
int i = gr[s][idx[s]];
      if(lv[e[\check{i}].v] == lv[s] + 1) {
       ll add = get_flow(e[i].v, t, min(left, e[i].cap - e[i].flow));
         e[i].flow += add;
         e[i ^ 1].flow -= add;
         return add;
     ++idx[s];
   return 0;
 Dinic(int vertices, bool scaling = 1) : // toggle scaling here
   n(vertices), lim(scaling ? 1 << 30 : 1), gr(n) {}
 void add_edge(int from, int to, ll cap, bool directed = 1) {
   gr[from].push_back(e.size());
   e.emplace_back(to, cap);
   gr[to].push back(e.size());
   e.emplace_back(from, directed ? 0 : cap);
 ll get_max_flow(int s, int t) { // call this
   ll res = 0;
   while(lim) { // scaling
     while(has_path(s, t)) {
       idx.assign(n, 0);
       while(ll add = get_flow(s, t, INF))
         res += add;
     lim >>= 1:
   return res;
};
```

5.5 Minimum Cost Maximum Flow

```
using FlowT = ll:
using CostT = ll;
const FlowT F_INF = 1e18;
const CostT C INF = 1e18;
const int MAX_V = 1e5 + 5;
const int MAX_E = 1e6 + 5;
namespace MCMF {
 int n, E;
 int adj[MAX_E], nxt[MAX_E], lst[MAX_V], frm[MAX_V], vis[MAX_V];
 FlowT cap[MAX_E], flw[MAX_E], totalFlow;
 CostT cst[MAX_E], dst[MAX_V], totalCost;
 void init(int _n) {
   fill_n(lst, n, -1), E = 0;
 void add(int u, int v, FlowT ca, CostT co) {
   adj[E] = v, cap[E] = ca, flw[E] = 0, cst[E] = +co;
   nxt[E] = lst[u], lst[u] = E++;
   adj[E] = u, cap[E] = 0, flw[E] = 0, cst[E] = -co;
   nxt[E] = lst[v], lst[v] = E++;
  int spfa(int s, int t) {
   fill_n(dst, n, C_INF), dst[s] = 0;
   queue<int> que;
   que.push(s);
   while(que.size()) {
     int u = que.front();
```

```
que.pop();
      for(int e = lst[u]; e != -1; e = nxt[e])
        if(flw[e] < cap[e]) {</pre>
          int v = adj[e];
          if(dst[v] > dst[u] + cst[e]) {
            dst[v] = dst[u] + cst[e];
            frm[v] = e;
            if(!vis[v]) {
              vis[v] = 1;
              que.push(v);
      vis[u] = 0;
    return dst[t] < C_INF;</pre>
  pair<FlowT, CostT> solve(int s, int t) {
    totalCost = 0, totalFlow = 0;
    while(1) {
      if(!spfa(s, t))
       break;
      FlowT mn = F INF;
      for(int v = t, e = frm[v]; v != s; v = adj[e ^ 1], e = frm[v])
       mn = min(mn, cap[e] - flw[e]);
      for(int v = t, e = frm[v]; v != s; v = adj[e ^ 1], e = frm[v]) {
        flw[e] += mn;
        flw[e ^ 1] -= mn;
      totalFlow += mn;
      totalCost += mn * dst[t];
    return {totalFlow, totalCost};
};
```

5.6 Flows with Demands

```
let S0 be the source and T0 be the original sink
1. add 2 additional nodes, call them Si and T1
2. connect S0 to nodes normally
3. connect nodes to TO normally
4. for each edge(U, V), cap = original cap - demand
5. for each node N:
   1. add an edge(S1, N), cap = sum of inward demand to N
   2. add an edge(N, T1), cap = sum of outward demand from N
6. add an edge (T_0, S_0), cap = INF
7. the above is not a typo!
8. run max flow normally
9. for each edge(S1, V) and (U, T1), check if flow == cap
if step #9 fails, then it is not possible to satisfy the given demand
```

Mathematically, let d(e) be the demand of edge e. Let V be the set of every vertex in the graph.

- $c'(S_1, v) = \sum_{u \in V} d(u, v)$ for each edge (s', v).
- $c'(v, T_1) = \sum_{v \in V} d(v, w)$ for each edge (v, t').
- c'(u,v) = c(u,v) d(u,v) for each edge (u,v) in the old network.
- $c'(T_0, S_0) = \infty$

5.7 Hungarian

```
template <typename TD> struct Hungarian {
 TD INF = 1e9; //max_inf
 vector<vector<TD> > adj; // cost[left][right]
 vector<TD> hl, hr, slk;
```

```
vector<int> fl, fr, vl, vr, pre;
 deque<int> q;
 Hungarian(int _n) {
   n = _n;
   adj = vector<vector<TD> >(n, vector<TD> (n, 0));
  int check(int i) {
   if(vl[i] = 1, fl[i] != -1)
     return q.push_back(fl[i]), vr[fl[i]] = 1;
    while(i != -1)
     swap(i, fr[fl[i] = pre[i]]);
    return 0;
  void bfs(int s) {
   slk.assign(n, INF);
   vl.assign(n, 0);
   vr = vl;
    q.assign(vr[s] = 1, s);
    for(TD d;;) {
      for(; !q.empty(); q.pop_front()) {
        for(int i = 0, j = q.front(); i < n; i++) {</pre>
          if(d = hl[i] + hr[j] - adj[i][j], !vl[i] && d <= slk[i]) {</pre>
            if(pre[i] = j, d)
              slk[i] = d;
            else if(!check(i))
              return;
      for(int i = 0; i < n; i++) if(!vl[i] && d > slk[i])
         d = slk[i];
      for(int i = 0; i < n; i++) {
        if(vl[i])
         hl[i] += d;
       else
         slk[i] -= d;
        if(vr[i])
         hr[i] -= d;
      for(int i = 0; i < n; i++) if([vl[i] \& \& !slk[i] \& \& !check(i))
         return;
  TD solve() {
   fl.assign(n, -1);
    fr = fl;
   hl.assign(n, 0);
   hr = hl;
    pre.assign(n, 0);
    for(int i = 0; i < n; i++)
     hl[i] = *max_element(adj[i].begin(), adj[i].begin() + n);
    for(int i = 0; i < n; i++)
     bfs(i);
    TD ret = 0;
    for(int i = 0; i < n; i++) if(adj[i][fl[i]])</pre>
       ret += adj[i][fl[i]];
    return ret;
}; //i will be matched with fl[i]
```

5.8 Edmonds' Blossom

```
// Maximum matching on general graphs in O(V^2 E)
// Indices are 1-based
// Stolen from ko_osaga's cheatsheet
struct Blossom {
 vector<int> vis, dad, orig, match, aux;
 vector<vector<int>> conn;
 int t, N;
```

```
queue<int> Q;
void augment(int u, int v) {
  do {
   pv = dad[v];
   int nv = match[pv];
   match[v] = pv;
   match[pv] = v;
    \vee = n \vee ;
  } while(u != pv);
int lca(int v, int w) {
  while(true) {
   if(v) {
      if(aux[v] == t)
       return v;
      aux[v] = t;
      v = orig[dad[match[v]]];
    swap(v, w);
void blossom(int v, int w, int a) {
 while(orig[v] != a) {
   dad[v] = w;
   w = match[v];
    if(vis[w] == 1) {
     0.push(w);
     vis[w] = 0;
    orig[v] = orig[w] = a;
    v = dad[w];
bool bfs(int u) {
  fill(vis.begin(), vis.end(), -1);
  iota(orig.begin(), orig.end(), 0);
 Q = queue<int>();
  Q.push(u);
  vis[u] = 0;
  while(!Q.empty()) {
    int v = Q.front();
   Q.pop();
    for(int x : conn[v]) {
     if(vis[x] == -1) {
        dad[x] = v;
        vis[x] = 1;
        if(!match[x]) {
          augment(u, x);
          return 1;
        Q.push(match[x]);
        vis[match[x]] = 0;
      } else if(vis[x] == 0 && orig[v] != orig[x]) {
        int a = lca(orig[v], orig[x]);
        blossom(x, v, a);
        blossom(v, x, a);
  return false;
Blossom(int n) : // n = vertices
  vis(n + 1), dad(n + 1), orig(n + 1), match(n + 1),
  aux(n + 1), conn(n + 1), t(0), N(n) {
```

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```
for(int i = 0; i <= n; ++i) {
     conn[i].clear();
     match[i] = aux[i] = dad[i] = 0;
 void add_edge(int u, int v) {
   conn[u].push_back(v);
   conn[v].push_back(u);
 int solve() { // call this for answer
   int ans = 0;
   vector<int> V(N - 1);
   iota(V.begin(), V.end(), 1);
   shuffle(V.begin(), V.end(), mt19937(0x94949));
   for(auto x : V)
     if(!match[x]) {
       for(auto y : conn[x]) {
         if(!match[y]) {
           match[x] = y, match[y] = x;
           ++ans;
           break:
   for(int i = 1; i <= N; ++i) {
     if(!match[i] && bfs(i))
       ++ans;
   return ans;
};
```

5.9 Eulerian Path or Cycle

```
// finds a eulerian path / cycle
// visits each edge only once
// - cycle: degrees are even
// - path: degrees are even OR degrees are even except for 2 vertices
// how to use: g = adjacency list g[n] = connected to n, undirected
// if there is a vertex u with an odd degree, call dfs(u)
// else call on any vertex
// ans = path result
vector<set<int>> g;
vector<int> ans;
void dfs(int u) {
 while(g[u].size()) {
   int v = *g[u].begin();
   g[u].erase(v);
   g[v].erase(u);
   dfs(v);
 ans.push_back(u);
```

5.10 Hierholzer's Algorithm

```
// Eulerian on Directed Graph
stack<int> path;
vector<int> euler;
inline void hierholzer() {
   path.push(0);
   int cur = 0;
   while(!path.empty()) {
```

```
if(!adj[cur].empty()) {
   path.push(cur);
   int next = adj[cur].back();
   adj[cur].pob();
   cur = next;
} else {
   euler.pb(cur);
   cur = path.top();
   path.pop();
}
reverse(euler.begin(), euler.end());
}
```

5.11 2-SAT

```
struct TwoSAT {
 int n;
 vector<vector<int>> g, gr;
  vector<int> comp, topological_order, answer;
  vector<bool> vis;
  TwoSAT() {}
  TwoSAT(int _n) :
   n(_n), g(2 * n), gr(2 * n), comp(2 * n), answer(2 * n), vis(2 * n) {}
  void add_edge(int u, int v) {
   g[u].push_back(v);
    gr[v].push_back(u);
  // For the following three functions
  // int x, bool val: if 'val' is true, we take the variable to be x.
  // Otherwise we take it to be x's complement.
  // At least one of them is true
  void add_clause_or(int i, bool f, int j, bool p) {
   add_{edge}(i + (f ? n : 0), j + (p ? 0 : n));
    add_{edge}(j + (p ? n : 0), i + (f ? 0 : n));
  // Only one of them is true
  void add_clause_xor(int i, bool f, int j, bool p) {
   add_clause_or(i, f, j, p);
    add_clause_or(i, !f, j, !p);
  // Both of them have the same value
  void add_clause_and(int i, bool f, int j, bool p) {
   add_clause_xor(i, !f, j, p);
  // Topological sort
  void dfs(int u) {
    vis[u] = true;
    for(const auto& v : g[u])
     if(!vis[v])
        dfs(v);
    topological_order.push_back(u);
  // Extracting strongly connected components
  void scc(int u, int id) {
   vis[u] = true;
    comp[u] = id;
    for(const auto& v : gr[u])
     if(!vis[v])
        scc(v, id);
```

```
bool satisfiable() {
   fill(vis.begin(), vis.end(), false);
   for(int i = 0; i < 2 * n; i++)
     if(!vis[i])
       dfs(i);
   fill(vis.begin(), vis.end(), false);
   reverse(topological_order.begin(), topological_order.end());
   for(const auto& v : topological_order)
     if(!vis[v])
       scc(v, id++);
   // Constructing the answer
   for(int i = 0; i < n; i++) {
     if(comp[i] == comp[i + n])
       return false;
     answer[i] = (comp[i] > comp[i + n] ? 1 : 0);
   return true;
};
```

6 Math

6.1 Extended Euclidean GCD

```
// computes x and y such that ax + by = gcd(a, b) in O(log (min(a, b)))
// returns {gcd(a, b), x, y}
tuple<int, int, int> gcd(int a, int b) {
  if(b == 0) return {a, 1, 0};
  auto [d, x1, y1] = gcd(b, a % b);
  return {d, y1, x1 - y1* (a / b)};
}
```

6.2 Generalized CRT

```
template<typename T>
T extended_euclid(T a, T b, T& x, T& y) {
 if(b == 0) {
   \times = 1;
   y = 0;
   return a;
 T xx, yy, gcd;
 gcd = extended_euclid(b, a % b, xx, yy);
 y = xx - (yy * (a / b));
 return gcd;
template<typename T>
T MOD(T a, T b) {
 return (a % b + b) % b;
// return x, lcm. x = a % n && x = b % m
template<typename T>
pair<T, T> CRT(T a, T n, T b, T m) {
 T gcd = extended_euclid(n, m, _n, _m);
 if(n == m) {
   if(a == b)
      return pair<T, T>(a, n);
      return pair<T, T>(-1, -1);
  } else if(abs(a - b) % gcd != 0)
    return pair<T, T>(-1, -1);
    T lcm = m * n / gcd;
    T x = MOD(a + MOD(n * MOD(_n * ((b - a) / gcd), m / gcd), lcm), lcm);
```

```
return pair<T, T>(x, lcm);
}
```

6.3 Generalized Lucas Theorem

```
/*Special Lucas : (n,k) % p^x
 fctp[n] = Product of the integers less than or equal
  to n that are not divisible by p
 Precompute fctp*/
LL p
LL E(LL n, int m) {
 LL tot = 0;
 while(n != 0)
   tot += n / m, n /= m;
 return tot;
LL funct(LL n, LL base) {
 LL ans = fast(fctp[base], n / base, base) * fctp[n % base] % base;
  return ans;
LL F(LL n, LL base) {
 LL ans = 1;
 while(n != 0) {
   ans = (ans * funct(n, base)) % base;
   n /= p;
 return ans;
LL special_lucas(LL n, LL r, LL base) {
 p = fprime(base);
 LL pow = E(n, p) - E(n - r, p) - E(r, p);
 LL TOP = fast(p, pow, base) * F(n, base) % base;
 LL BOT = F(r, base) * F(n - r, base) % base;
 return (TOP * fast(BOT, totien(base) - 1, base)) % base;
//End of Special Lucas
```

6.4 Linear Diophantine

```
//FOR SOLVING MINIMUM ABS(X) + ABS(Y)
ll x, y, newX, newY, target = 0;
ll extGcd(ll a, ll b) {
 if(b == 0) {
   x = 1, y = 0;
   return a;
 ll ret = extGcd(b, a % b);
 newX = y;
 newY = x - y * (a / b);
 x = newX;
 y = newY;
 return ret;
ll fix(ll sol, ll rt) {
 ll ret = 0;
  //CASE SOLÚTION(X/Y) < TARGET
 if(sol < target)</pre>
   ret = -floor(abs(sol + target) / (double)rt);
  //CASE SOLUTION(X/Y) > TARGET
  if(sol > target)
   ret = ceil(abs(sol - target) / (double)rt);
  return ret;
ll work(ll a, ll b, ll c) {
 ll gcd = extGcd(a, b);
 ll solX = x * (c / gcd);
 ll solY = y * (c / gcd);
 a /= gcd;
```

```
b /= gcd;
ll fi = abs(fix(solX, b));
ll se = abs(fix(solY, a));
ll lo = min(fi, se);
ll hi = max(fi, se);
ll ans = abs(solX) + abs(solY);
for(ll i = lo; i <= hi; i++) {
   ans = min(ans, abs(solX + i * b) + abs(solY - i * a));
   ans = min(ans, abs(solX - i * b) + abs(solY + i * a));
}
return ans;
}</pre>
```

6.5 Modular Linear Equation

```
// finds all solutions to ax = b (mod n)
vi modular_linear_equation_solver(int a, int b, int n) {
   int x, y;
   vi ret;
   int g = extended_euclid(a, n, x, y);
   if(!(b % g)) {
        x = mod(x * (b / g), n);
        for(int i = 0; i < g; i++)
            ret.push_back(mod(x + i * (n / g), n));
   }
   return ret;
}</pre>
```

6.6 Miller-Rabin and Pollard's Rho

```
namespace MillerRabin {
 const vector<ll> primes = { // deterministic up to 2^64 - 1
   2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37
 ll gcd(ll a, ll b) {
   return b ? gcd(b, a % b) : a;
 ll powa(ll x, ll y, ll p) { // (x ^{\wedge} y) % p
   if(!y)
     return 1;
   if(y & 1)
     return ((\_int128) \times powa(x, y - 1, p)) \% p;
   ll temp = powa(x, y >> 1, p);
   return ((__int128) temp * temp) % p;
 bool miller_rabin(ll n, ll a, ll d, int s) {
   ll x = powa(a, d, n);
   if(x == 1 | | x == n - 1)
     return 0;
   for(int i = 0; i < s; ++i) {
     x = ((__int128) x * x) % n;
     if(x == n - 1)
       return 0;
   return 1;
 bool is_prime(ll x) { // use this
   if(x < 2)
     return 0;
   int r = 0;
   lld = x - 1;
   while((d & 1) == 0) {
     d >>= 1;
     ++r;
   for(auto& i : primes) {
     if(x == i)
       return 1;
     if(miller_rabin(x, i, d, r))
```

```
return 0;
   return 1;
namespace PollardRho {
 mt19937_64 generator(chrono::steady_clock::now()
                       .time_since_epoch().count());
 uniform_int_distribution<ll> rand_ll(0, LLONG_MAX);
 ll f(ll x, ll b, ll n) { // (x^2 + b) % n}
   return (((__int128) x * x) % n + b) % n;
 ll rho(ll n) {
   if(n \% 2 == 0)
     return 2;
   ll b = rand_ll(generator);
    ll x = rand_ll(generator);
    ll y = x;
    while(1) {
     x = f(x, b, n);
     y = f(f(y, b, n), b, n);
     ll d = MillerRabin::gcd(abs(x - y), n);
     if(d != 1)
       return d;
  void pollard_rho(ll n, vector<ll>& res) {
   if(n == 1)
   if(MillerRabin::is_prime(n)) {
     res.push_back(n);
     return;
    ll d = rho(n);
   pollard_rho(d, res);
   pollard_rho(n / d, res);
  vector<ll> factorize(ll n, bool sorted = 1) { // use this
   vector<ll> res;
   pollard_rho(n, res);
   if(sorted)
     sort(res.begin(), res.end());
    return res;
```

6.7 Berlekamp-Massey

```
#include <bits/stdc++.h>
using namespace std;
#define pb push_back
typedef long long ll;
#define SZ 233333
const int MOD = 1e9 + 7; //or any prime
ll qp(ll a, ll b) {
 ll \times = 1;
 a %= MOD;
  while(b)
    if(b & 1)
     x = x * a % MOD;
    a = a * a % MOD;
    b >>= 1;
  return x;
namespace linear_seq {
  vector<int> BM(vector<int> x) {
    //ls: (shortest) relation sequence (after filling zeroes) so far
    //cur: current relation sequence
```

vector<int> ls, cur;
//lf: the position of ls (t')

//ld: delta of ls (v')

int lf = -1, ld = -1;

//evaluate at position i

 $if((t - x[i]) \% MOD == 0) {$

continue; //good so far

ll t = 0;

for(int i = 0; i < int(x.size()); ++i) {</pre>

for(int j = 0; j < int(cur.size()); ++j)</pre>

t = (t + x[i - j - 1] * (ll)cur[j]) % MOD;

```
//first non-zero position
     if(!cur.size()) {
       cur.resize(i + 1);
       lf = i;
       ld = (t - x[i]) \% MOD;
       continue;
      //cur=cur-c/ld*(x[i]-t)
     ll k = -(x[i] - t) * ap(ld, MOD - 2) % MOD/*1/ld*/;
     vector<int> c(i - lf - 1); //add zeroes in front
     for(int j = 0; j < int(ls.size()); ++j)</pre>
       c.pb(-ls[j]*k % MOD);
     if(c.size() < cur.size())</pre>
       c.resize(cur.size());
      for(int j = 0; j < int(cur.size()); ++j)</pre>
       c[j] = (c[j] + cur[j]) % MOD;
     //if cur is better than ls, change ls to cur
     if(i - lf + (int)ls.size() >= (int)cur.size())
       ls = cur, lf = i, ld = (t - x[i]) % MOD;
     cur = c;
   for(int i = 0; i < int(cur.size()); ++i)</pre>
     cur[i] = (cur[i] % MOD + MOD) % MOD;
   return cur;
 int m; //length of recurrence
//a: first terms
//h: relation
 ll a[SZ], h[SZ], t_[SZ], s[SZ], t[SZ];
//calculate p*q mod f
 void mull(ll* p, ll* q) {
   for(int i = 0; i < m + m; ++i)
     t_{[i]} = 0;
   for(int i = 0; i < m; ++i) if(p[i])</pre>
       for(int j = 0; j < m; ++j)
         t_{[i + j]} = (t_{[i + j]} + p[i] * q[j]) % MOD;
   for(int i = m + m - 1; i >= m; --i) if(t_[i])
        //miuns t_{i-m}(x^m-\sum_{j=0}^{m-1} x^{m-j-1}h_{j})
       for(int j = m - 1; ~j; --j)
         t_{[i-j-1]} = (t_{[i-j-1]} + t_{[i]} * h[j]) % MOD;
   for(int i = 0; i < m; ++i)
     p[i] = t_[i];
 ll calc(ll K) {
   for(int i = m; ~i; --i)
     s[i] = t[i] = 0;
   s[0] = 1;
   if(m != 1)
     t[1] = 1;
   else
     t[0] = h[0];
   //binary-exponentiation
   while(K) {
     if(K & 1)
       mull(s, t);
     mull(t, t);
     K >>= 1;
```

```
ll su = 0;
    for(int i = 0; i < m; ++i)
      su = (su + s[i] * a[i]) % MOD;
    return (su % MOD + MOD) % MOD;
  int work(vector<int> x, ll n) {
    if(n < int(x.size()))</pre>
     return x[n];
    vector < int > v = BM(x);
    m = v.size();
    if(!m)
     return 0;
    for(int i = 0; i < m; ++i)
     h[i] = v[i], a[i] = x[i];
    return calc(n);
using linear_seq::work;
const vector<int> sequence = {
 0, 2, 2, 28, 60, 836, 2766
};
int main() {
 cout << work(sequence, 7) << '\n';</pre>
```

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6.8 Fast Fourier Transform

```
using ld = double; // change to long double if reach 10^18
using cd = complex<ld>;
const ld PI = acos(-(ld)1);
void fft(vector<cd>& a, int sign = 1) {
  int n = a.size();
  ld theta = sign * 2 * PI / n;
  for(int i = 0, j = 1; j < n - 1; j++) {
    for(int k = n >> 1; k > (i ^= k); k >>= 1);
    if(j < i)
      swap(a[i], a[j]);
  for(int m, mh = 1; (m = mh << 1) <= n; mh = m) {
    int irev = 0;
    for(int i = 0; i < n; i += m) {
      cd w = exp(cd(0, theta * irev));
      for(int k = n >> 2; k > (irev ^= k); k >>= 1);
      for(int j = i; j < mh + i; j++) {
        int k = j + mh;
        cd \times = a[i] - a[k];
        a[j] += a[k];
        a[k] = w * x;
  if(sign == -1) for(cd& i : a)
      i /= n;
vector<ll> multiply(vector<ll> const& a, vector<ll> const& b) {
  vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
  int n = 1;
  while(n < a.size() + b.size())</pre>
   n <<= 1;
  fa.resize(n);
  fb.resize(n);
  fft(fa);
  fft(fb);
  for(int i = 0; i < n; i++)
    fa[i] *= fb[i];
  fft(fa, -1);
```

6.9 Number Theoretic Transform

vector<ll> res(n);

return res;

for(int i = 0; i < n; i++)

res[i] = round(fa[i].real());

```
namespace FFT {
 /* ---- Adjust the constants here ---- */
 const int LN = 24; \frac{1}{23}
 const int N = 1 \ll LN;
 typedef long long LL; // 2**23 * 119 + 1. 998244353
// `MOD` must be of the form 2** `LN` * k + 1, where k odd.
 const LL MOD = 9223372036737335297; // 2**24 * 54975513881 + 1.
 const LL PRIMITIVE_ROOT = 3; // Primitive root modulo `MOD`.
 /* ---- End of constants ---- */
 LL root[N];
 inline LL power(LL x, LL y) {
   LL ret = 1;
   for(; y; y >>= 1) {
     if(y & 1)
       ret = ( int128) ret * x % MOD;
     x = (__int128) \times \times \times \% MOD;
   return ret;
  inline void init_fft() {
   const LL UNITY = power(PRIMITIVE_ROOT, MOD - 1 >> LN);
   root[0] = 1;
   for(int i = 1; i < N; i++)
     root[i] = (__int128) UNITY * root[i - 1] % MOD;
   return;
// n = 2^k is the length of polynom
 inline void fft(int n, vector<LL>& a, bool invert) {
   for(int i = 1, j = 0; i < n; ++i) {
     int bit = n \gg 1;
     for(; j >= bit; bit >>= 1)
       j -= bit;
     i += bit;
     if(i < j)
       swap(a[i], a[j]);
   for(int len = 2; len <= n; len <<= 1) {
     LL wlen = (invert ? root[N - N / len] : root[N / len]);
     for(int i = 0; i < n; i += len) {</pre>
       LL w = 1;
       for(int j = 0; j<len >> 1; j++) {
         LL u = a[i + j];
         LL v = (_int128) a[i + j + len / 2] * w % MOD;
         a[i + j] = ((\_int128) u + v) % MOD;
         a[i + j + len / 2] = ((__int128) u - v + MOD) % MOD;
         w = (__int128) w * wlen % MOD;
   if(invert) {
     LL inv = power(n, MOD - 2);
     for(int i = 0; i < n; i++)
       a[i] = (__int128) a[i] * inv % MOD;
   return;
  inline vector<LL> multiply(vector<LL> a, vector<LL> b) {
   int len = 1 << 32 - __builtin_clz(a.size() + b.size() - 2);</pre>
   a.resize(len, 0);
   b.resize(len, 0);
   fft(len, a, false);
```

```
fft(len, b, false);
   c.resize(len);
   for(int i = 0; i < len; ++i)
     c[i] = (\_int128) a[i] * b[i] % MOD;
   fft(len, c, true);
   return c;
//FFT::init_fft(); wajib di panggil init di awal
```

6.10 Gauss-Jordan

```
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// Gauss-Jordan elimination with full pivoting.
    (1) solving systems of linear equations (AX=B)
     (2) inverting matrices (AX=I)
     (3) computing determinants of square matrices
// Running time: O(n^3)
             a[][] = an nxn matrix
              b[][] = an nxm matrix
// OUTPUT: X
                    = an nxm matrix (stored in b[][])
             A^{-1} = an nxn matrix (stored in a[][])
             returns determinant of a[][]
const double EPS = 1e-10;
typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;
T GaussJordan(VVT& a, VVT& b) {
 const int n = a.size();
  const int m = b[0].size();
  VI irow(n), icol(n), ipiv(n);
  T det = 1;
  for(int i = 0; i < n; i++) {
    int p_{j} = -1, p_{k} = -1;
    for(int j = 0; j < n; j++) if(!ipiv[j])</pre>
        for(int k = 0; k < n; k++) if(!ipiv[k])
            if(pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) {
              pj = j;
               pk = k;
    if(fabs(a[pj][pk]) < EPS) {</pre>
      cerr << "Matrix is singular." << endl;</pre>
      exit(0);
    ipiv[pk]++;
    swap(a[pj], a[pk]);
    swap(b[pj], b[pk]);
    if(pj != pk)
      det *= -1;
    irow[i] = pj;
    icol[i] = pk;
    T c = 1.0 / a[pk][pk];
    det *= a[pk][pk];
    a[pk][pk] = 1.0;
    for(int p = 0; p < n; p++)
      a[pk][p] *= c;
    for(int p = 0; p < m; p++)
      b[pk][p] *= c;
    for(int p = 0; p < n; p++) if(p != pk) {
        c = a[p][pk];
        a[p][pk] = 0;
        for(int q = 0; q < n; q++)
          a[p][q] -= a[pk][q] * c;
         for(int q = 0; q < m; q++)
```

```
b[p][q] -= b[pk][q] * c;
 for(int p = n - 1; p >= 0; p--) if(irow[p] != icol[p]) {
     for(int k = 0; k < n; k++)
       swap(a[k][irow[p]], a[k][icol[p]]);
 return det;
int main() {
 const int n = 4;
 const int m = 2;
 double A[n][n] = { {1, 2, 3, 4}, {1, 0, 1, 0}, {5, 3, 2, 4}, {6, 1, 4, 6} };
 double B[n][m] = { {1, 2}, {4, 3}, {5, 6}, {8, 7} };
 VVT a(n), b(n);
 for(int i = 0; i < n; i++) {
   a[i] = VT(A[i], A[i] + n);
   b[i] = VT(B[i], B[i] + m);
 double det = GaussJordan(a, b);
 // expected: 60
 cout << "Determinant: " << det << endl;</pre>
 // expected: -0.233333 0.166667 0.133333 0.0666667
              0.166667 0.166667 0.333333 -0.333333
              0.233333 0.833333 -0.133333 -0.0666667
              0.05 -0.75 -0.1 0.2
 cout << "Inverse: " << endl;</pre>
 for(int i = 0; i < n; i++) {
   for(int j = 0; j < n; j++)
    cout << a[i][j] << ' ';
   cout << endl;
 // expected: 1.63333 1.3
              -0.166667 0.5
 cout << "Solution: " << endl;</pre>
 for(int i = 0; i < n; i++) {
   for(int j = 0; j < m; j++)
     cout << b[i][j] << ' ';
   cout << endl;
```

6.11 Derangement

```
der[0] = 1;
der[1] = 0;
for(int i = 2; i <= 10; ++i)
  der[i] = (ll)(i - 1) * (der[i - 1] + der[i - 2]);</pre>
```

6.12 Bernoulli Number

$$\sum_{k=1}^{n} k^{m} = \frac{1}{m+1} \sum_{i=0}^{n} {m+1 \choose i} B_{i}^{+} n^{m+1-i} = m! \sum_{i=0}^{m} \frac{B_{i}^{+} n^{m+1-i}}{i!(m+1-i)!} B_{n}^{+} = 1 - \sum_{i=0}^{n-1} {n \choose i} \frac{B_{i}^{+}}{n-i+1}, \quad B_{0}^{+} = 1$$

6.13 Forbenius Number

(X * Y) - (X + Y) and total count is(X - 1) * (Y - 1) / 2

6.14 Stars and Bars with Upper Bound

$$P = (1 - X^{r_1+1}) \dots (1 - X^{r_n+1}) = \sum_i c_i X^{e_i}$$

$$Ans = \sum_i c_i {N - e_i + n - 1 \choose n - 1}$$

6.15 Arithmetic Sequences

```
U_n = a + (n-1)a_1 + \frac{(n-1)(n-2)}{1\times 2}a_2 + \dots + \frac{(n-1)(n-2)(n-3)\dots}{1\times 2\times 3\times \dots}a_r
S_n = n \times a + \frac{n(n-1)}{1\times 2}a_1 + \frac{n(n-1)(n-2)}{1\times 2\times 3}a_2 + \dots + \frac{n(n-1)(n-2)(n-3)\dots}{1\times 2\times 3\dots}a_r
```

6.16 FWHT

```
// Desc : Transform a polynom to obtain a_i * b_j * x^(i XOR j) or combinations
// Time : O(N log N) with N = 2^K
// OP => c00 c01 c10 c11 | c00 c01 c10 c11 inv
// XOR => +1 +1 +1 -1 | +1 +1 +1 -1 | div the inverse with size = n
// AND => 1 +1 0 1 | 1 -1 0 1 | no comment
// OR => 1 0 +1 1 | 1 0 -1 1 | no comment
typedef vector<long long> vec;
void FWHT(vec& a) {
  int n = a.size();
  for(int lvl = 1; 2 * lvl <= n; lvl <<= 1) {
    for(int j = 0; j < lvl; j++) { // do not forget to modulo
        long long u = a[i + j], v = a[i + lvl + j];
        a[i + j] = u + v; // c00 * u + c01 * v
        a[i + lvl + j] = u - v; // c10 * u + c11 * v
    }
} // you can convolve as usual</pre>
```

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7 Strings

7.1 Aho-Corasick

```
const int K = 26;
struct Vertex {
  int next[K];
  bool leaf = 0;
  int p = -1, ans = 0;
  char pch;
  int link = -1, mlink = -1;
  //magic link, is the link to find the nearest leaf
  int go[K];
  Vertex(int p = -1, char ch = '$') : p(p), pch(ch) {
    fill(begin(next), end(next), -1);
    fill(begin(go), end(go), -1);
vector<Vertex> t;
int add_string(string const& s) {
  int v = 0;
  for(char ch : s) {
    int c = ch - 'a';
    if(t[v].next[c] == -1) {
      t[v].next[c] = t.size();
      t.emplace_back(v, ch);
    v = t[v].next[c];
  t[v].leaf = 1;
  return v;
int go(int v, char ch);
int get_link(int v) {
  if(t[v].link == -1) {
    if(v == 0 || t[v].p == 0)
     t[v].link = 0;
      t[v].link = go(get_link(t[v].p), t[v].pch);
```

```
return t[v].link;
int get_mlink(int v) {
 if(t[v].mlink == -1) {
   if(v == 0 || t[v].p == 0)
     t[v].mlink = 0;
   else {
     t[v].mlink = go(get_link(t[v].p), t[v].pch);
     if(t[v].mlink && !t[t[v].mlink].leaf) {
       if(t[t[v].mlink].mlink == -1)
         get_mlink(t[v].mlink);
       t[v].mlink = t[t[v].mlink].mlink;
 return t[v].mlink;
int go(int v, char ch) {
 int c = ch - 'a';
 if(t[v].go[c] == -1) {
   if(t[v].next[c] != -1)
     t[v].go[c] = t[v].next[c];
     t[v].go[c] = v == 0 ? 0 : go(get_link(v), ch);
 return t[v].go[c];
//t.pb(Vertex());
7.2 Eertree
```

```
Eertree - keep track of all palindromes and its occurences
  This code refers to problem Longest Palindromic Substring
https://www.spoj.com/problems/LPS/
#include <bits/stdc++.h>
using namespace std;
typedef long long ll;
struct node {
 int next[26];
 int sufflink;
 int len, cnt;
const int N = 1e5 + 69;
int n;
string s;
node tree[N];
int idx, suff;
int ans = 0;
void init_eertree() {
 idx = suff = 2;
 tree[1].len = -1, tree[1].sufflink = 1;
 tree[2].len = 0, tree[2].sufflink = 1;
bool add_letter(int x) {
 int cur = suff, curlen = 0;
  int nw = s[x] - 'a';
  while(1) {
    curlen = tree[cur].len;
    if(x - curlen - 1 >= 0 \&\& s[x - curlen - 1] == s[x])
    cur = tree[cur].sufflink;
  if(tree[cur].next[nw]) {
    suff = tree[cur].next[nw];
```

```
return 0;
 tree[cur].next[nw] = suff = ++idx;
 tree[idx].len = tree[cur].len + 2;
 ans = max(ans, tree[idx].len);
 if(tree[idx].len == 1)
   tree[idx].sufflink = 2;
   tree[idx].cnt = 1;
   return 1;
 while(1) {
   cur = tree[cur].sufflink;
   curlen = tree[cur].len;
   if(x - curlen - 1 >= 0 \&\& s[x - curlen - 1] == s[x]) {
     tree[idx].sufflink = tree[cur].next[nw];
     break:
 tree[idx].cnt = tree[tree[idx].sufflink].cnt + 1;
 return 1;
int main() {
 ios::sync_with_stdio(0);
 cin.tie(0);
 cin >> n >> s;
 init_eertree();
 for(int i = 0; i < n; i++)
  add_letter(i);
 cout << ans << '\n';
 return 0;
```

7.3 Manacher's Algorithm

```
// Computes lps array. lps[i] means the longest palindromic substring centered at i (↔
    when i is even, it is between characters. when it is odd, it is on characters)lps↔
    [0] = 0; lps[1] = 1;
REP(i, 2, 2 * str.size()) {
 int l = i / 2 - lps[i] / 2;
  int r = (i - 1) / 2 + lps[i] / 2;
 while(1) { // widen
   if(l == 0 || r + 1 == str.size())
     break;
   if(str[l - 1] != str[r + 1])
     break;
    l--, r++;
  lps[i] = r - l + 1;
  if(lps[i] > 2) {
    int j = i - 1, k = i + 1; // while lps[j] inside lps[i]
   while(lps[j] - j < lps[i] - i)</pre>
     lps[k++] = lps[j--];
    lps[k] = lps[i] - (i - j); // set lps[k] to edge of lps[i]
    i = k - 1; // jump to mirror, which is k
```

7.4 Suffix Array

```
// stores result in sa and lcp
// if lcp is needed, call SuffixArray(str, 1)
struct SuffixArray {
  int n;
 vector<int> sa, lcp, rnk, cnt;
  vector<pair<int, int>> p;
  SuffixArray(const string& s, bool calc_lcp = 0) :
   n(s.length()), sa(n), lcp(calc_lcp?n:0), rnk(n),
```

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```
cnt(max(n, 256)), p(n) {
    for(int i = 0; i < n; ++i)
     rnk[i] = s[i];
    iota(sa.begin(), sa.end(), 0);
    for(int i = 1; i < n; i <<= 1)
     update_sa(i);
   if(!calc_lcp)
     return;
   vector<int> phi(n), plcp(n);
   phi[sa[0]] = -1;
    for(int i = 1; i < n; ++i)
     phi[sa[i]] = sa[i - 1];
    int l = 0;
    for(int i = 0; i < n; ++i) {
     if(phi[i] == -1)
       plcp[i] = 0;
     else {
       while((i + l < n) \&\& (phi[i] + l < n)
              \&\& (s[i + l] == s[phi[i] + l]))
       plcp[i] = l;
        l = max(l - 1, 0);
    for(int i = 0; i < n; ++i)
     lcp[i] = plcp[sa[i]];
 void update_sa(int len) {
   sort_sa(len);
   sort_sa(0);
    for(int i = 0; i < n; ++i) p[i] = {rnk[i], rnk[(i + len) % n]};</pre>
   auto lst = p[sa[0]];
   rnk[sa[0]] = 0;
    int cur = 0;
    for(int i = 1; i < n; ++i) {</pre>
     if(lst != p[sa[i]]) {
       lst = p[sa[i]];
       ++cur;
     rnk[sa[i]] = cur;
 void sort_sa(int offset) {
   fill(cnt.begin(), cnt.end(), 0);
    for(int i = 0; i < n; ++i)
     ++cnt[rnk[(i + offset) % n]];
    int sum = 0;
    for(int i = 0; i < (int) cnt.size(); ++i) {</pre>
     int temp = cnt[i];
     cnt[i] = sum;
     sum += temp;
   vector<int> temp(n);
    for(int i = 0; i < n; ++i) {
     int cur = cnt[rnk[(sa[i] + offset) % n]]++;
     temp[cur] = sa[i];
       = move(temp);
};
```

7.5 Suffix Automaton

```
Struct state {
    int len, link;
    map<char, int>next; //use array if TLE
};

const int MAXLEN = 100005;
    state st[MAXLEN * 2];
```

```
int sz, last;
void sa_init() -
  sz = last = 0;
  st[0].len = 0;
  st[0].link = -1;
  st[0].next.clear();
  ++sz;
void sa_extend(char c) {
  int cur = sz++;
  st[cur].len = st[last].len + 1;
  st[cur].next.clear();
  for(p = last; p != -1 && !st[p].next.count(c); p = st[p].link)
    st[p].next[c] = cur;
  if(p == -1)
    st[cur].link = 0;
  else {
    int q = st[p].next[c];
    if(st[p].len + 1 == st[q].len)
      st[cur].link = q;
    else {
      int clone = sz++;
      st[clone].len = st[p].len + 1;
      st[clone].next = st[q].next;
      st[clone].link = st[q].link;
      for(; p != -1 && st[p].next[c] == q; p = st[p].link)
        st[p].next[c] = clone;
      st[q].link = st[cur].link = clone;
  last = cur;
// forwarding
for(int i = 0; i < m; i++) {
  while(cur >= 0 && st[cur].next.count(pa[i]) == 0) {
    cur = st[cur].link;
    if(cur != -1)
      len = st[cur].len;
  if(st[cur].next.count(pa[i])) {
    len++;
    cur = st[cur].next[pa[i]];
  } else
    len = cur = 0;
// shortening abc -> bc
if(l == m) {
  if(l <= st[st[cur].link].len)</pre>
    cur = st[cur].link;
// finding lowest and highest length
int lo = st[st[cur].link].len + 1;
int hi = st[cur].len;
//Finding number of distinct substrings
//answer = distsub(0)
LL d[MAXLEN * 2];
LL distsub(int ver) {
  LL tp = 1;
  if(d[ver])
    return d[ver];
  for(map<char, int>::iterator it = st[ver].next.begin();
      it != st[ver].next.end(); it++)
    tp += distsub(it->second);
  d[ver] = tp;
  return d[ver];
//Total Length of all distinct substrings
//call distsub first before call lesub
```

LL ans[MAXLEN \star 2];

LL lesub(int ver) { LL tp = 0;if(ans[ver])

ans[ver] = tp; return ans[ver];

return ans[ver];

int v = it->second;

 $if(K \le d[v])$ {

if(K == 0) {

} else {

return;

K -= d[v];

//in int main do this

cin >> S; //input

sa_extend(S[a]); minshift(0);

void minshift(int ver) {

minshift(it->second);

string lcs(string s, string t) {

best = 0, bestpos = 0;

if(st[v].next.count(t[i])) {

 $if(tp == t) {$

break;

//end of function

sa_extend(s[i]);

v = st[v].link;

l = st[v].length;

int v = 0, l = 0,

t = S.length();

K--;

} else

int main() { string S; sa_init();

tp = 0;

S += S;

//the function int tp, t;

tp++;

break;

sa_init();

for(map<char, int>::iterator it = st[ver].next.begin();

for(map<char, int>::iterator it = st[ver].next.begin();

for(map<char, int>::iterator it = st[ver].next.begin();

it != st[ver].next.end(); it++)

//find the k-th lexicographical substring void kthsub(int ver, int K, string& ret) {

ret.push_back(it->first);

ret.push back(it->first); kthsub(v, K, ret);

for(int a = 0; a < S.size(); a++)</pre>

it != st[ver].next.end(); it++) {

// LONGEST COMMON SUBSTRING OF TWO STRINGS

for(int i = 0; i < (int)s.length(); ++i)

for(int i = 0; i < (int)t.length(); ++i) {</pre>

while(v && ! st[v].next.count(t[i])) {

cout << st[ver].len - t + 1 << endl;

it != st[ver].next.end(); it++) {

tp += lesub(it->second) + d[it->second];

```
25
of
25
```

```
// Smallest Cyclic Shift to obtain lexicographical smallest of All possible
```

```
v = st[v].next[t[i]];
    ++l;
  if(l > best)
   best = l, bestpos = i;
return t.substr(bestpos - best + 1, best);
```

8 OEIS

8.1 A000108 (Catalan)

```
Catalan numbers
f(n) = nCk(2n,n) / (n+1) = nCk(2n,n) - nCk(2n,n+1) = f(n-1) * 2*(2*n-1) / (n+1)
1, 1, 2, 5, 14, 42, 132, 429, 1430, 4862, 16796, 58786, 208012, 742900,
2674440, 9694845, 35357670, 129644790, 477638700, 1767263190, 6564120420,
24466267020, 91482563640, 343059613650, 1289904147324, 4861946401452,
18367353072152, 69533550916004, 263747951750360, 1002242216651368,
3814986502092304
```

8.2 A000127

```
Maximal number of regions obtained by joining n points around a circle by
straight lines
f(n) = (n^4 - 6*n^3 + 23*n^2 - 18*n + 24) / 24
1, 2, 4, 8, 16, 31, 57, 99, 163, 256, 386, 562, 794, 1093, 1471, 1941, 2517,
3214, 4048, 5036, 6196, 7547, 9109, 10903, 12951, 15276, 17902, 20854, 24158,
27841, 31931, 36457, 41449, 46938, 52956, 59536, 66712, 74519, 82993, 92171,
102091, 112792, 124314
```

8.3 A001434

```
Number of graphs with n nodes and n edges.
0, 0, 1, 2, 6, 21, 65, 221, 771, 2769, 10250, 39243, 154658, 628635, 2632420,
11353457, 50411413, 230341716, 1082481189, 5228952960, 25945377057,
132140242356, 690238318754
```

8.4 A018819

```
Binary partition function: number of partitions of n into powers of 2
f(2m+1) = f(2m); f(2m) = f(2m-1) + f(m)
1, 1, 2, 2, 4, 4, 6, 6, 10, 10, 14, 14, 20, 20, 26, 26, 36, 36, 46, 46, 60,
60, 74, 74, 94, 94, 114, 114, 140, 140, 166, 166, 202, 202, 238, 238, 284,
284, 330, 330, 390, 390, 450, 450, 524, 524, 598, 598, 692, 692, 786, 786,
900, 900, 1014, 1014, 1154, 1154, 1294, 1294
```

8.5 A092098

```
3-Portolan numbers: number of regions formed by n-secting the angles of
an equilateral triangle.
long long solve(long long n) {
    long long res = (n \% 2 == 1 ? 3*n*n - 3*n + 1 : 3*n*n - 6*n + 6);
    const int bats = n/2 - 1;
    for (long long i=1; i<=bats; i++) for (long long j=1; j<=bats; j++) {
        long long num = i * (n-j) * n;
        long long denum = (n-i) * j + i * (n-j);
        res -= 6 * (num % denum == 0 && num / denum <= bats);
    } return res:
1, 6, 19, 30, 61, 78, 127, 150, 217, 246, 331, 366, 469, 510, 625, 678, 817,
870, 1027, 1080, 1261, 1326, 1519, 1566, 1801, 1878, 2107, 2190, 2437, 2520,
2791, 2886, 3169, 3270, 3559, 3678, 3997, 4110, 4447, 4548, 4921, 5034, 5419,
5550, 5899, 6078, 6487
```