

SYMBOLIC DATA MINING

- Frequent: If $\text{supp}(X) \geq \text{min-supp}$, then X is frequent
- Closed-Itemset: An itemset, doesn't have a superset with same supp
- Generator: An itemset, doesn't have a subset with same supp

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

Itemset: A, AB, BCE...

$$\text{Support}(A) = 4$$

$$\text{Support}(AB) = 3$$

$$\text{Support}(BCE) = 3$$

Min-Support: Threshold

One Size Larger Superset:

| SAME | X |

| SAME | Y |

⇓

| SAME | X | Y |

APRIORI (breadth-first) (levelwise)

FC₁
A 4
B 4
C 4
~~D 1~~
E 4

F₁
A 4
B 4
C 4
E 4

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

FC₂
AB 3
AC 3
AE 3
BC 3
BE 4
CE 3

F₂
AB 3
AC 3
AE 3
BC 3
BE 4
CE 3

min-supp = 2

FC₃
ABC 2
ABE 3
ACE 2
BCE 3

F₃
ABC 2
ABE 3
ACE 2
BCE 3

FC₄
ABCE 2

F₄
ABCE 2

FC₅

F₅ = 15

∅ stop!

APRIORI - CLOSE (breadth-first) (levelwise)

FC₁

A	4
B	4
C	4
D	1
E	4

F₁

itemset	support	closed?
A	4	yes
B	4	yes no
C	4	yes
E	4	yes no

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

FC₂

AB	3
AC	3
AE	3
BC	3
BE	4
CE	3

F₂

itemset	support	closed?
AB	3	yes no
AC	3	yes
AE	3	yes no
BC	3	yes no
BE	4	yes
CE	3	yes no

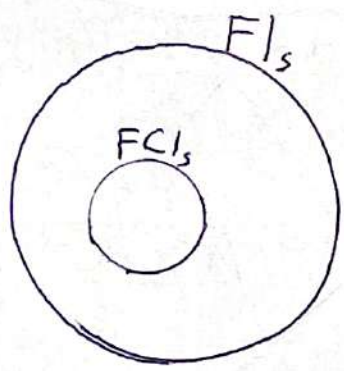
min-sup = 3

FC₃

ABC	2
ABE	3
ACE	2
BCE	3

F₃

itemset	support	closed?
ABE	3	yes
BCE	3	yes



FC₄

∅ stop!

F_{1s} = 12

FC_{1s} = 6

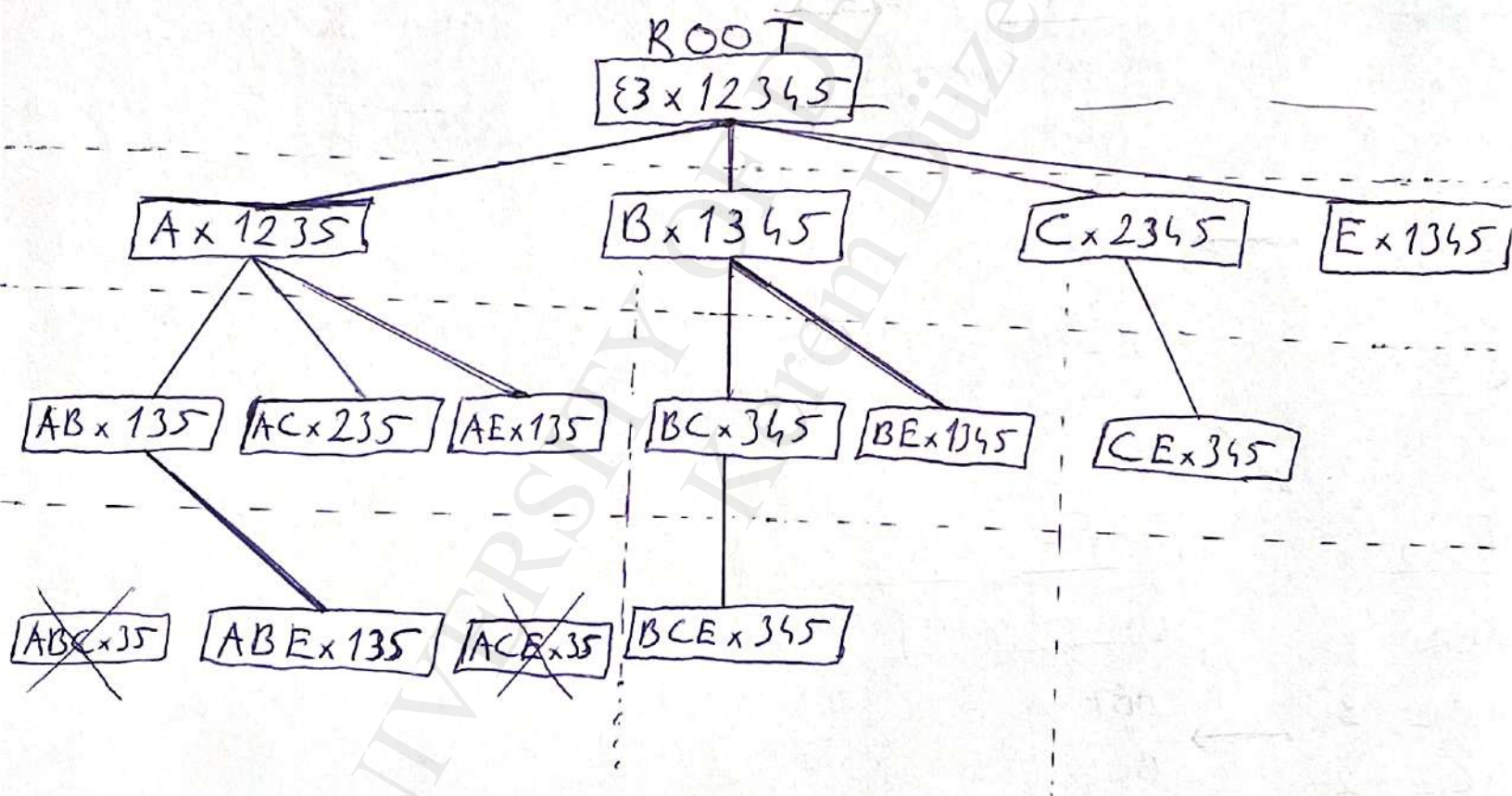
ECLAT (vertical) (depth-first)

1 \rightarrow ABDE

$$2 \rightarrow AC$$
$$3 \rightarrow ABCE$$
$$1 \rightarrow BCE$$
$$5 \rightarrow ABCE$$

A	B	C	D	E
1	1	2	1	1
2	3	3		3
3	4	4		4
5	5	5		5

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

$$\min - \sup p = 3$$


ASSOCIATION RULE

<u>FC₁</u>		<u>F₁</u>
A 4	→	A 4
B 4		B 4
C 4		C 4
D 1		E 4
E 4		

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

<u>FC₂</u>		<u>F₂</u>
AB 3	→	AB 3
AC 3		AC 3
AE 3		AE 3
BC 3		BC 3
BE 4		BE 4
CE 3		CE 3

min-sup = 3

2 Steps:

1) Find all FIs

2) Generate association rules from FIs

<u>FC₃</u>		<u>F₃</u>
ABC 2	→	ABE 3
ABE 3		BCE 3
ACE 2		
BCE 3		

$r: A \rightarrow B$

$$\text{supp}(r) = \text{supp}(A \cup B) \rightarrow 3$$

$$\text{conf}(r) = \frac{\text{supp}(A \cup B)}{\text{supp}(A)} \rightarrow \frac{3}{4} = 75\%$$

$FIs = 12$

FC₄

∅

$r: BE \rightarrow A$

$$\text{supp}(r) = \text{supp}(ABE) \rightarrow 3$$

$$\text{conf}(r) = \frac{\text{supp}(ABE)}{\text{supp}(BE)} \rightarrow \frac{3}{4} = 75\%$$

APRORI - RARE

FC_1	R_1	F_1															
A 4	D 1	<table border="1"><thead><tr><th>itemset</th><th>support</th><th>closed</th></tr></thead><tbody><tr><td>A</td><td>4</td><td>yes</td></tr><tr><td>B</td><td>4</td><td>yes</td></tr><tr><td>C</td><td>4</td><td>yes</td></tr><tr><td>E</td><td>4</td><td>yes</td></tr></tbody></table>	itemset	support	closed	A	4	yes	B	4	yes	C	4	yes	E	4	yes
itemset	support	closed															
A	4	yes															
B	4	yes															
C	4	yes															
E	4	yes															
B 4																	
C 4																	
D 1																	
E 4																	

	A	B	C	D	E
1	X	X		X	X
2	X		X		
3	X	X	X		X
4		X	X		X
5	X	X	X		X

FC_2	R_2	F_2																					
AB 3		<table border="1"><thead><tr><th>itemset</th><th>support</th><th>closed</th></tr></thead><tbody><tr><td>AB</td><td>3</td><td>yes</td></tr><tr><td>AC</td><td>3</td><td>yes</td></tr><tr><td>AE</td><td>3</td><td>yes</td></tr><tr><td>BC</td><td>3</td><td>yes</td></tr><tr><td>BE</td><td>4</td><td>yes</td></tr><tr><td>CE</td><td>3</td><td>yes</td></tr></tbody></table>	itemset	support	closed	AB	3	yes	AC	3	yes	AE	3	yes	BC	3	yes	BE	4	yes	CE	3	yes
itemset	support	closed																					
AB	3	yes																					
AC	3	yes																					
AE	3	yes																					
BC	3	yes																					
BE	4	yes																					
CE	3	yes																					
AC 3	\emptyset																						
AE 3																							
BC 3																							
BE 4																							
CE 4																							

min-sup = 3

FC_3	R_3	F_3
ABC 2	ABC 2	ABE 3 (yes)
ABE 3	ACE 2	BCE 3 (yes)
ACE 2		
BCE 3		

$$F|_S = 12$$

$$FC|_S = 6$$

$$\text{Minimal-Rare} = 3$$

\emptyset

• **Minimal-Rare Itemset**: An itemset that is not frequent, but all subsets are frequent