

\mathbb{R}^3

$$16) \quad p = (p_1, p_2, p_3)$$

$$\boxed{u_p = \frac{p}{|p|}}$$

standard unit vectors

$$i(1, 0, 0) \quad j(0, 1, 0) \quad k(0, 0, 1)$$

$$|p| = \sqrt{p_1^2 + p_2^2 + p_3^2}$$

$$a = (a_1, a_2, a_3)$$

$$b = (b_1, b_2, b_3)$$

$$a \cdot b = (a_1 b_1 + a_2 b_2 + a_3 b_3)$$

$$u_p \cdot i = \left(\frac{p_1}{|p|}, \frac{p_2}{|p|}, \frac{p_3}{|p|} \right) \cdot (1, 0, 0) = \frac{p_1}{|p|}$$

$$u_p \cdot j = \left(\frac{p_1}{|p|}, \frac{p_2}{|p|}, \frac{p_3}{|p|} \right) \cdot (0, 1, 0) = \frac{p_2}{|p|}$$

$$u_p \cdot k = \left(\frac{p_1}{|p|}, \frac{p_2}{|p|}, \frac{p_3}{|p|} \right) \cdot (0, 0, 1) = \frac{p_3}{|p|}$$

$$\boxed{p = |p| \cdot \cos \theta}$$

$$\cos \alpha_1 = \frac{p_1}{|p|}$$

$$\cos \alpha_2 = \frac{p_2}{|p|}$$

$$\cos \alpha_3 = \frac{p_3}{|p|}$$

$$\boxed{\cos^2 \alpha_1 + \cos^2 \alpha_2 + \cos^2 \alpha_3 = 1}$$

$$\left(\frac{p_1}{|p|} \right)^2 + \left(\frac{p_2}{|p|} \right)^2 + \left(\frac{p_3}{|p|} \right)^2 = 1$$

$$\frac{p_1^2 + p_2^2 + p_3^2}{(\sqrt{p_1^2 + p_2^2 + p_3^2})^2} = 1$$

$$\boxed{p = |p| (\cos \alpha_1, \cos \alpha_2, \cos \alpha_3)}$$

$$p_1 = |p| \cdot \cos \alpha_1$$

$$p_2 = |p| \cdot \cos \alpha_2$$

$$p_3 = |p| \cdot \cos \alpha_3$$

$$p = (p_1, p_2, p_3) = |p| (\cos \alpha_1, \cos \alpha_2, \cos \alpha_3)$$