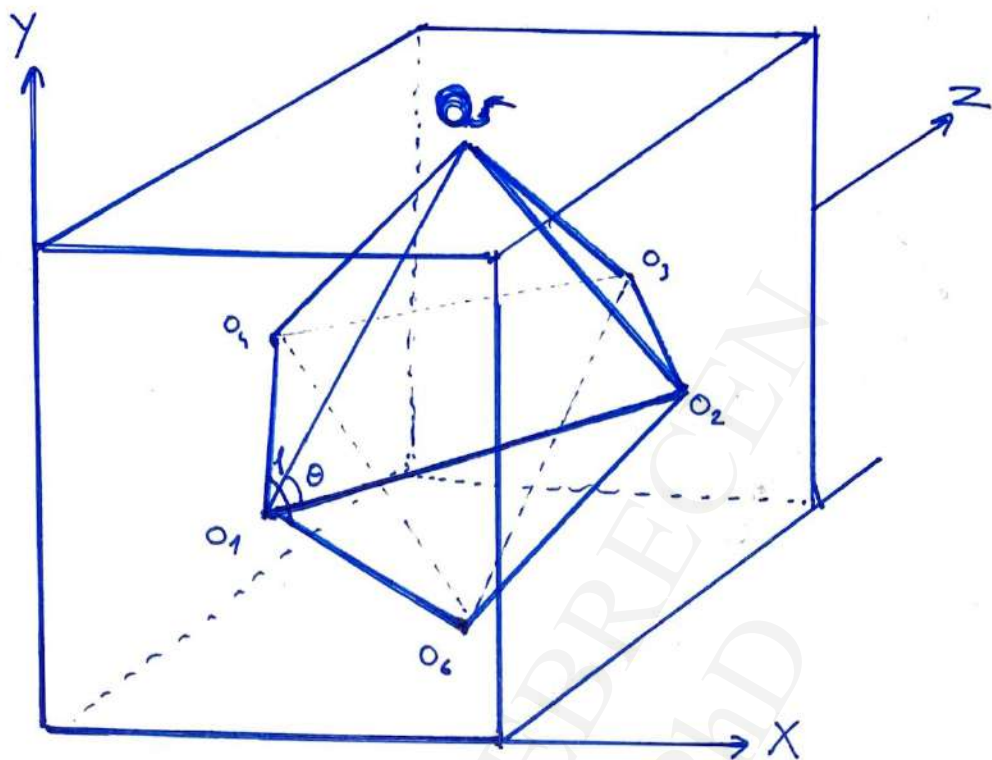


7)

$$p \cdot q = |p| \cdot |q| \cdot \cos \theta$$



$$\begin{aligned} O_{12} &= {}^{O_1}(0.5, 0.5, 0) \longrightarrow {}^{O_2}(1, 0.5, 0.5) = (0.5, 0, 0.5) \\ O_{14} &= {}^{O_1}(0.5, 0.5, 0) \longrightarrow {}^{O_4}(0, 0.5, 0.5) = (-0.5, 0, 0.5) \\ O_{15} &= {}^{O_1}(0.5, 0.5, 0) \longrightarrow {}^{O_5}(0.5, 1, 0.5) = (0, 0.5, 0.5) \\ O_{16} &= {}^{O_1}(0.5, 0.5, 0) \longrightarrow {}^{O_6}(0.5, 0, 0.5) = (0, -0.5, 0.5) \end{aligned}$$

$$|O_{12}| = \sqrt{\left(\frac{1}{2}\right)^2 + 0^2 + \left(\frac{1}{2}\right)^2} = \sqrt{\frac{1}{2}}$$

$$|O_{16}| = \sqrt{0^2 + \left(-\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2} = \sqrt{\frac{1}{2}}$$

$$|O_{15}| = \sqrt{0^2 + \left(\frac{1}{2}\right)^2 + \left(\frac{1}{2}\right)^2} = \sqrt{\frac{1}{2}}$$

$$|O_{14}| = \sqrt{\left(-\frac{1}{2}\right)^2 + 0^2 + \left(\frac{1}{2}\right)^2} = \sqrt{\frac{1}{2}}$$

$$O_{12} \cdot O_{15} = |O_{12}| \cdot |O_{15}| \cdot \cos \theta$$

$$\frac{1}{4} = \sqrt{\frac{1}{2}} \cdot \sqrt{\frac{1}{2}} \cdot \cos \theta$$

$$\frac{1}{4} = \frac{1}{2} \cdot \cos \theta$$

$$\frac{1}{2} = \cos \theta \longrightarrow \theta = 60^\circ$$

$$60^\circ = \theta$$

$$O_{14} \cdot O_{16} = |O_{14}| \cdot |O_{16}| \cdot \cos \phi$$

$$\frac{1}{4} = \sqrt{\frac{1}{2}} \cdot \sqrt{\frac{1}{2}} \cdot \cos \phi$$

$$\frac{1}{4} = \frac{1}{2} \cdot \cos \phi$$

$$\frac{1}{2} = \cos \phi \longrightarrow \phi = 60^\circ$$

$$60^\circ = \phi$$