

13)

$$|p| + |q| \geq |p+q| \longrightarrow \text{Triangle Inequality}$$

$$|p| \cdot |q| \geq (p \cdot q) \longrightarrow \text{Cauch-Schwarz Inequality}$$

$$(|p| + |q|)^2 \geq (|p+q|)^2$$

$$|p|^2 + 2|p||q| + |q|^2 \geq |p+q|^2$$

$\underbrace{(p \cdot q)}$

$$|p|^2 + 2pq + |q|^2 \geq |p+q|^2$$

$$(|p| + |q|)^2 \geq |p+q|^2$$

$$\underline{|p| + |q| \geq |p+q|}$$