

1.2.12

$$(P - \lambda q) \cdot (P - \lambda q) \geq 0 \quad \text{apply square}$$

$$|P|^2 - 2\lambda P \cdot q + \lambda^2 |q|^2 \geq 0 \quad \text{apply } \lambda \text{ value } \frac{P \cdot q}{|q|^2}$$

$$|P|^2 - 2 \frac{P \cdot q}{|q|^2} \cdot P \cdot q + \left( \frac{P \cdot q}{|q|^2} \right)^2 \cdot |q|^2 \geq 0$$

$$|P|^2 - 2 \frac{(P \cdot q)^2}{|q|^2} + \frac{(P \cdot q)^2}{|q|^2} \geq 0$$

$$|P|^2 - \frac{(P \cdot q)^2}{|q|^2} \geq 0$$

$$|P|^2 \cdot |q|^2 \geq 0$$

$$|P| \cdot |q| \geq P \cdot q$$

Since the dot product greater than zero  
They are in same direction and not aligned.