

1.2.16

$$\mathbf{P} = (P_x, P_y, P_z)$$

$$UP = \frac{\mathbf{P}}{|\mathbf{P}|} \quad \text{from 15}$$

$$\mathbf{x} = (x_1, x_2, x_3) \cdot \mathbf{y} = (y_1, y_2, y_3)$$

$$\mathbf{x} \cdot \mathbf{y} = x_1 y_1 + x_2 y_2 + x_3 y_3$$

$$UP \cdot i = \frac{P_1}{|\mathbf{P}|}, \frac{P_2}{|\mathbf{P}|}, \frac{P_3}{|\mathbf{P}|} \cdot (1, 0, 0) = \frac{P_1}{|\mathbf{P}|}$$

$$UP \cdot j = \frac{P_1}{|\mathbf{P}|}, \frac{P_2}{|\mathbf{P}|}, \frac{P_3}{|\mathbf{P}|} \cdot (0, 1, 0) = \frac{P_2}{|\mathbf{P}|}$$

$$UP \cdot k = \frac{P_1}{|\mathbf{P}|}, \frac{P_2}{|\mathbf{P}|}, \frac{P_3}{|\mathbf{P}|} \cdot (0, 0, 1) = \frac{P_3}{|\mathbf{P}|}$$

$$P = |\mathbf{P}| \cdot \cos \theta$$

$$\cos^2 \theta_1 + \cos^2 \theta_2 + \cos^2 \theta_3 = 1$$

Replace $P = UP \cdot z$ and this lead to 1

$$\cos^2 \theta_1 = \frac{P_1}{|\mathbf{P}|}, \cos^2 \theta_2 = \frac{P_2}{|\mathbf{P}|}, \cos^2 \theta_3 = \frac{P_3}{|\mathbf{P}|}$$

$$\mathbf{P} = (P_x, P_y, P_z) = |\mathbf{P}| (\cos \theta_1, \cos \theta_2, \cos \theta_3)$$