

1.2.16

$$P = (P_x, P_y, P_z)$$

$$u_P = \frac{P}{|P|} \quad \text{From 15}$$

$$X = (x_1, x_2, x_3), Y = (y_1, y_2, y_3)$$

$$X \cdot Y = x_1 y_1 + x_2 y_2 + x_3 y_3$$

$$u_P \cdot i = \left(\frac{P_1}{|P|}, \frac{P_2}{|P|}, \frac{P_3}{|P|} \right) \cdot (1, 0, 0) = \frac{P_1}{|P|}$$

$$u_P \cdot j = \left(\frac{P_1}{|P|}, \frac{P_2}{|P|}, \frac{P_3}{|P|} \right) \cdot (0, 1, 0) = \frac{P_2}{|P|}$$

$$u_P \cdot k = \left(\frac{P_1}{|P|}, \frac{P_2}{|P|}, \frac{P_3}{|P|} \right) \cdot (0, 0, 1) = \frac{P_3}{|P|}$$

$$P = |P| \cdot \cos \theta$$

$$\cos^2 \theta_1 + \cos^2 \theta_2 + \cos^2 \theta_3 = 1$$

Replace $P = u_P$ quantities lead to 1

$$\cos^2 \theta_1 = \frac{P_1}{|P|}, \cos^2 \theta_2 = \frac{P_2}{|P|}, \cos^2 \theta_3 = \frac{P_3}{|P|}$$

$$P = (P_x, P_y, P_z) = |P| (\cos \theta_1, \cos \theta_2, \cos \theta_3)$$