

13) $|p| + |q| \geq |p+q| \longrightarrow \text{Triangle Inequality}$

$|p| \cdot |q| \geq (p \cdot q) \longrightarrow \text{Cauchy-Schwarz Inequality}$

$$(|p| + |q|)^2 \geq (|p+q|)^2$$

$$|p|^2 + 2 \underbrace{|p||q|}_{(p \cdot q)} + |q|^2 \geq |p+q|^2$$

$$|p|^2 + 2pq + |q|^2 \geq |p+q|^2$$

$$(|p| + |q|)^2 \geq |p+q|^2$$

$$\underline{|p| + |q| \geq |p+q|}$$