1)
$$V = \begin{pmatrix} 1 \\ -1 \\ 0 \end{pmatrix} \qquad V = \begin{pmatrix} 1 \\ 2 \\ 0 \end{pmatrix}$$

$$|v| = \sqrt{(1)^2 + (-1)^2 + 6^2}$$
 $|v| = \sqrt{(1)^2 + (2)^2 + (6)^2}$
 $|v| = \sqrt{2}$ $|v| = \sqrt{5}$

$$U \times V = \begin{pmatrix} (-1)(0) - (0)(2) \\ (0)(1) - (1)(0) \\ (1)(2) - (-1)(1) \end{pmatrix}$$

$$V \times V = (0,0,3)$$

$$\cup \times \vee = (1).(1) + (-1).(2) + (0)(0)$$

$$\frac{-1}{\sqrt{70}} = \cos \theta$$

$$sin\theta = \sqrt{1-cos^2\theta}$$

$$\sin \theta = \left(1 - \left(\frac{1}{\sqrt{100}}\right)^2\right)$$

$$U \times V = \begin{pmatrix} U_2 V_3 - U_3 V_2 \\ U_3 V_1 - U_1 V_3 \\ U_1 V_2 - U_2 V_1 \end{pmatrix}$$

$$SM\theta = \sqrt{1 - \cos^2\theta}$$

$$||\mathbf{v} \mathbf{x} \mathbf{v}|| = 3$$

$$A = \begin{pmatrix} 1 \\ 2 \end{pmatrix} \quad B = \begin{pmatrix} 0 \\ -1 \\ 3 \end{pmatrix} \quad C = \begin{pmatrix} 3 \\ 0 \\ 2 \end{pmatrix} \quad A = (1, -1, 2) \quad B = (0, -1, 3) \quad C = (3, 0, 2)$$

$$AB = \begin{pmatrix} (0) - (1) \\ (-1) - (-1) \\ (3) - (2) \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ 1 \end{pmatrix} = (-1, 0, 1)$$

$$AC = \begin{pmatrix} (3) - (1) \\ (0) - (-1) \\ (2) - (2) \end{pmatrix} = \begin{pmatrix} 2 \\ 1 \\ 0 \end{pmatrix} = (2, 1, 0)$$

$$AB = (-1, 0, 1) \quad AC = (2, 1, 0)$$

$$N = \begin{vmatrix}
i & J & k \\
-1 & 0 & 1 \\
2 & 1 & 0
\end{vmatrix}$$

$$N = i \begin{vmatrix} 0 & 1 \\
1 & 0 \end{vmatrix}$$

$$= (0)(0) - (1)(1) = (-1)(0) - (1)(2) = (-1)(1) - (0)(2)$$

$$N = \begin{vmatrix}
i & J & k \\
X_{AB} & J_{AB} & Z_{AB} \\
X_{AC} & J_{AC} & Z_{AC}
\end{vmatrix}$$

$$N = (-1, 2, -1)$$

$$A = (1, -1, 2)$$

$$-1(x-(1)) + 2(y-(-1)) + -1(z-(2)) = 0$$

$$-x+1+2y+2-2+2=0$$

3)
$$U \times V = \begin{vmatrix} i & j & k \\ U_{1} & U_{2} & U_{2} \\ V_{2} & V_{3} & V_{2} \end{vmatrix} = i \begin{vmatrix} U_{2} & U_{2} \\ V_{3} & V_{2} \end{vmatrix} - \int \begin{vmatrix} U_{1} & V_{2} \\ V_{3} & V_{2} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{3} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{3} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{2} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{5} \end{vmatrix} + k \begin{vmatrix} U_{4} & V_{4} \\ V_{4} & V_{$$

$$\begin{array}{c} (0 \times 0) = -(0 \times 0) \\ ($$

$$U \times V = \begin{bmatrix} i & 5 & k \\ U_1 & U_2 & U_3 \\ V_1 & V_2 & V_3 \end{bmatrix} = \begin{bmatrix} i & U_2 & U_3 \\ V_2 & V_3 \end{bmatrix} - \begin{bmatrix} U_1 & U_3 \\ V_1 & V_3 \end{bmatrix} + \begin{bmatrix} k & U_1 & U_2 \\ V_1 & V_2 \end{bmatrix}$$

$$\downarrow \qquad \qquad \downarrow \qquad \qquad \qquad \qquad \downarrow \qquad \qquad \qquad \downarrow \qquad \qquad \downarrow$$

$$V \times V = -(V \times V)$$

$$\bigvee \times \cup = \begin{vmatrix} i & f & k \\ v_1 & v_2 & v_3 \\ v_1 & v_2 & v_3 \end{vmatrix} = i \begin{vmatrix} v_2 & v_3 \\ v_2 & v_3 \end{vmatrix} - f \begin{vmatrix} v_1 & v_3 \\ v_1 & v_3 \end{vmatrix} + k \begin{vmatrix} v_1 & v_2 \\ v_1 & v_2 \end{vmatrix}$$

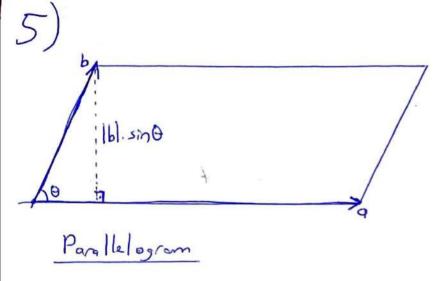
$$\downarrow \qquad \qquad \downarrow \qquad \qquad \downarrow$$

$$i \left[(v_2 v_3 - v_3 v_2) \right] - J \left[(v_1 v_2 - v_3 v_1) \right] + k \left[(v_1 v_2) - (v_2 v_1) \right]$$

$$V \times U = i(v_2 v_3 - v_3 v_2) - J(v_1 v_3 - v_3 v_1) + k(v_1 v_2 - v_2 v_1)$$

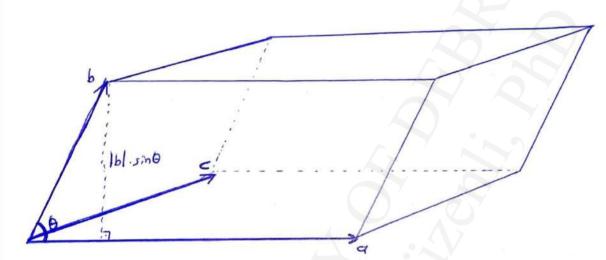
$$= (v_2 v_3 - v_3 v_2) - (v_1 v_3 - v_3 v_1) + (v_1 v_2 - v_2 v_1)$$

$$(v_{2} v_{3} - v_{3} v_{2}) - (v_{1} v_{3} - v_{3} v_{1}) + (v_{1} v_{2} - v_{2} v_{1}) = - (v_{3} v_{2} - v_{2} v_{3}) - (v_{3} v_{1} - v_{1} v_{3}) + (v_{2} v_{1} - v_{1} v_{3})$$



Area =
$$|a| \cdot |b| \cdot sin \theta$$

= $(\overrightarrow{a} \times \overrightarrow{b})$



Parallelepiped

$$\Omega_{i} = \frac{1}{2} \left(\vec{a} \times \vec{b} \right)$$

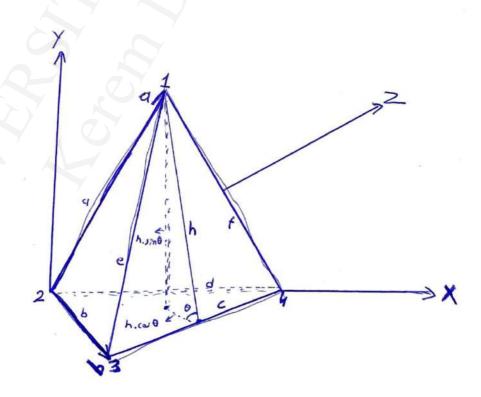
$$n_1 = \frac{1}{2} \cdot (a \times b)$$
 $n_2 = \frac{1}{2} \cdot (b \times c)$
 $n_3 = \frac{1}{2} \cdot (c \times f)$
 $n_4 = \frac{1}{2} \cdot (d \times f)$

$$n_q = \frac{1}{2} \cdot (d \times f)$$

$$n_1 + n_2 + n_3 + n_4 = 0$$



Tetrahedron



$$a \times b = \begin{vmatrix} i & 5 & k \\ a_1 & a_2 & a_3 \\ b_1 & b_2 & b_3 \end{vmatrix} = i \begin{vmatrix} a_2 & a_3 \\ b_2 & b_3 \end{vmatrix} - J \begin{vmatrix} a_1 & a_3 \\ b_1 & b_3 \end{vmatrix} + k \begin{vmatrix} a_1 & a_2 \\ b_1 & b_2 \end{vmatrix}$$

$$i (a_2b_3 - a_3b_2) - J(a_1b_3 - a_3b_4) + k (a_1b_2 - a_2b_4)$$

$$a \times b = \begin{vmatrix} a_{2}b_{3} - a_{3}b_{2} \\ a_{3}b_{1} - a_{1}b_{3} \\ a_{4}b_{2} - a_{2}b_{1} \end{vmatrix}$$

$$C \times d = \begin{vmatrix} i & 5 & k \\ c_1 & c_2 & c_3 \\ d_1 & d_2 & d_3 \end{vmatrix} = i \begin{vmatrix} c_2 & c_3 \\ d_2 & d_3 \end{vmatrix} - \int \begin{vmatrix} c_1 & c_3 \\ d_1 & d_1 \end{vmatrix} + k \begin{vmatrix} c_1 & c_2 \\ d_1 & d_2 \end{vmatrix}$$

$$i (c_2 d_3 - c_3 d_2) - \int (c_1 d_3 - c_3 d_1) + k (c_1 d_2 - c_2 d_1)$$

$$C \times d = \begin{vmatrix} c_2 d_1 - c_1 d_2 \\ c_3 d_1 - c_1 d_3 \\ c_1 d_2 - c_2 d_1 \end{vmatrix}$$

$$(a \times b)(c \times d) = \begin{vmatrix} a_2b_1 - a_3b_2 \\ a_3b_1 - a_1b_3 \\ a_1b_2 - a_2b_1 \end{vmatrix} \begin{vmatrix} c_2d_3 - c_3d_2 \\ c_3d_1 - c_4d_3 \\ c_1d_2 - c_2d_1 \end{vmatrix}$$

$$(a_{2}b_{3}-a_{3}b_{2})(c_{2}d_{3}-c_{3}d_{2}) = (a_{2}b_{3}c_{2}d_{3}-a_{2}b_{3}c_{3}d_{2}-a_{3}b_{2}c_{2}d_{3}+a_{3}b_{2}c_{3}d_{2})$$

$$(a_{3}b_{4}-a_{1}b_{3})(c_{3}d_{1}-c_{1}d_{3}) = (a_{3}b_{1}c_{3}d_{1}-a_{3}b_{1}c_{4}d_{3}-a_{1}b_{3}c_{3}d_{4}+a_{1}b_{3}c_{4}d_{3}) + (a_{1}b_{2}-a_{2}b_{1})(c_{4}d_{2}-c_{2}d_{1}) = (a_{1}b_{2}c_{4}d_{2}-a_{1}b_{2}c_{2}d_{1}-a_{2}b_{1}c_{1}d_{2}+a_{2}b_{1}c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{4}d_{2}-c_{2}d_{1}) = (a_{1}b_{2}c_{4}d_{2}-a_{1}b_{2}c_{2}d_{1}-a_{2}b_{1}c_{1}d_{2}+a_{2}b_{1}c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{4}d_{2}-c_{2}d_{1}) = (a_{1}b_{2}c_{1}d_{2}-a_{1}b_{2}c_{2}d_{1}-a_{2}b_{1}c_{1}d_{2}+a_{2}b_{1}c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{4}d_{2}-c_{2}d_{1}) = (a_{1}b_{2}c_{1}d_{2}-a_{1}b_{2}c_{2}d_{1}-a_{2}b_{1}c_{1}d_{2}+a_{2}b_{1}c_{2}d_{1}) + (a_{1}b_{2}-a_{1}b_{2}c_{1}d_{2}-a_{1}b_{2}c_{2}d_{1}) + (a_{1}b_{2}-a_{1}b_{2}c_{2}d_{1}) + (a_{1}b_{2}-a_{1}b_{2}c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-c_{2}d_{1}) + (a_{1}b_{2}-a_{2}b_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{2}-c_{2}d_{1}) + (a_{1}b_{2}-c_{2}d_{1})(c_{1}d_{2}-c_{2}d_{1}) + (a_{1}b_{$$

$$a. c = a_1 + a_1 + a_2 + a_2 + a_3 + a_1 + a_2 + a_2 + a_2 + a_2 + a_3 + a_3 + a_3 + a_4 + a_4 + a_4 + a_5 + a_5$$

det
$$(a,b,c) = (a \times b) \times c$$

$$\times \times (Y \times Z) = (X \cdot Z) \cdot Y - (X \cdot Y) \cdot Z$$

$$(a \times b) \times (c \times d) = [\det(a,c,d)] \cdot b - [\det(b,c,d)] \cdot a - [\det(a,b,d)] \cdot c - [\det(a,b,c)] \cdot d - [\det(a,b,c)] \cdot$$

$$(a \times b) \times (c \times d) = [(a \times b), d] \cdot c - [(a \times b), c] \cdot d$$

$$= [det(a, b, d)] \cdot c - [det(a, b, c)] \cdot d$$

$$(a \times b) \times (c \times d) = ((c \times d).b).b - ((c \times d).b).d$$

$$= [det(a,c,d)].b - [det(b,c,d)].q$$

9)
$$T: R^3 \rightarrow R^3$$
 $T(X) = a \times X$ $x, y \in R^3$

Homogeneity

(b)

$$T(c\mathbf{X}) = a \times (c\mathbf{X}) = c(a \times X) = cT(X)$$

$$R^{3} \{e_{1}, e_{2}, e_{3}\} = e_{1} = (1,0,0) \quad e_{2} = (0,1,0) \quad e_{3} = (0,0,1)$$

$$T(e_{1}) = a \times e_{1} = \begin{vmatrix} i & 5 & k \\ a_{1} & a_{2} & a_{3} \\ 1 & 0 & 0 \end{vmatrix} = i \begin{vmatrix} a_{2} & a_{3} \\ 0 & 0 \end{vmatrix} - J \begin{vmatrix} a_{1} & a_{1} \\ 1 & 0 \end{vmatrix} + k \begin{vmatrix} a_{1} & a_{2} \\ 1 & 0 \end{vmatrix}$$

$$= \begin{pmatrix} 0 & a_{3} & -a_{2} \end{pmatrix}$$

$$T(e_2) = a \times e_2 = \begin{vmatrix} i & 5 & k \\ a_1 & a_2 & a_3 \\ 0 & 1 & 0 \end{vmatrix} = i \begin{vmatrix} a_2 & a_3 \\ 1 & 0 \end{vmatrix} - T \begin{vmatrix} a_1 & a_2 \\ 0 & 0 \end{vmatrix} + k \begin{vmatrix} a_1 & a_2 \\ 0 & 1 \end{vmatrix}$$

$$T(e_{j}) = a \times e_{j} = \begin{vmatrix} 1 & 5 & 2 \\ a_{1} & a_{1} & a_{2} \\ 0 & 0 & 1 \end{vmatrix} = \begin{vmatrix} a_{1} & a_{2} \\ 0 & 1 \end{vmatrix} - \int_{0}^{a_{1}} \begin{vmatrix} a_{1} & a_{2} \\ 0 & 1 \end{vmatrix} + \frac{1}{2} \begin{vmatrix} a_{1} & a_{2} \\ 0 & 0 \end{vmatrix}$$

$$[T] = [T(e_1) \quad T(e_2) \quad T(e_3)] = \begin{bmatrix} 0 & -\alpha_3 & +\alpha_2 \\ +\alpha_3 & 0 & -\alpha_4 \\ -\alpha_2 & +\alpha_4 & 0 \end{bmatrix}$$

