



# **Vidyavardhini's College of Engineering and Technology**

## **Department of Artificial Intelligence & Data Science**

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Experiment No. 5
Fractional Knapsack using Greedy Method
Date of Performance:
Date of Submission:



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### Experiment No. 5

**Title:** Fraction Knapsack

**Aim:** To study and implement Fraction Knapsack Algorithm

**Objective:** To introduce Greedy based algorithms

#### Theory:

Greedy method or technique is used to solve Optimization problems. A solution that can be maximized or minimized is called Optimal Solution.

The knapsack problem or rucksack problem is a problem in combinatorial optimization: Given a set of items, each with a mass and a value, determine the number of each item to include in a collection so that the total weight is less than or equal to a given limit and the total value is as large as possible. It derives its name from the problem faced by someone who is constrained by a fixed size knapsack and must fill it with the most valuable items. The most common problem being solved is the 0-1 knapsack problem, which restricts the number  $x_i$  of copies of each kind of item to zero or one.

In Knapsack problem we are given: 1)  $n$  objects 2) Knapsack with capacity  $m$ , 3) An object  $i$  is associated with profit  $W_i$ , 4) An object  $i$  is associated with profit  $P_i$ , 5) when an object  $i$  is placed in knapsack we get profit  $P_i X_i$ .

Here objects can be broken into pieces ( $X_i$  Values) The Objective of Knapsack problem is to maximize the profit.

#### Example:

In this version of Knapsack problem, items can be broken into smaller pieces. So, the thief may take only a fraction  $x_i$  of  $i^{\text{th}}$  item.

$$0 \leq x_i \leq 1$$

The  $i^{\text{th}}$  item contributes the weight  $x_i.w_i$  to the total weight in the knapsack and profit  $x_i.p_i$  to the total profit.



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greedy-fractional-knapsack ( $w[1..n], p[1..n], W$ )

for  $i=1$  to  $n$

do  $x[i] = 0$

weight = 0

for  $i=1$  to  $n$

if weight +  $w[i] \leq W$  then

$x[i] = 1$

weight = weight +  $w[i]$

else

$x[i] = (W - \text{weight}) / w[i]$

weight =  $W$

break

return  $x$

$0 + 10 \leq 60$

$x[1] = 1$

wt = 10

$i=2 \rightarrow A$

$10 + 40$

$50 \leq 60$

$x[2] = 2$

$10 + 40$

wt = 50

$i=3 \rightarrow C$

$(60 - 50) / 20$

$x[3] = 10 / 20 = 1/2$

wt = 60

$x = [A, B, 1/2 C]$

$x[i] = 0$

wt = 0

Ex:

$W = 60$

Total profit is  
 $100 + 280 + 120 \times (10/20)$   
 $580 + 60 = 640$

Total wt  
 $10 + 40 + 20 \times (10/20)$   
 $= 60$

Item	A	B	C	D
profit	280	100	120	120
weight	40	10	20	24
Ratio ( $\frac{p_i}{w_i}$ )	7	10	6	5

provided items are not sorted based on  $\frac{p_i}{w_i}$

sorted

Item	B	A	C	D
profit	100	280	120	120
weight	10	40	20	24
Ratio ( $\frac{p_i}{w_i}$ )	10	7	6	5



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### Algorithm:

Hence, the objective of this algorithm is to

$$\text{maximize } \sum_{i=1}^n (x_i \cdot p_i)$$

subject to constraint,

$$\sum_{i=1}^n (x_i \cdot w_i) \leq W$$

It is clear that an optimal solution must fill the knapsack exactly, otherwise we could add a fraction of one of the remaining items and increase the overall profit.

Thus, an optimal solution can be obtained by

$$\sum_{i=1}^n (x_i \cdot w_i) = W$$

In this context, first we need to sort those items according to the value of  $\frac{p_i}{w_i}$ , so that  $\frac{p_i}{w_i} \geq$

$\frac{p_{i+1}}{w_{i+1}}$ . Here,  $\mathbf{x}$  is an array to store the fraction of items.



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**Algorithm: Greedy-Fractional-Knapsack** ( $w[1..n]$ ,  $p[1..n]$ ,  $W$ )

```
for i = 1 to n
    do  $x[i] = 0$ 
weight = 0
for i = 1 to n
    if  $\text{weight} + w[i] \leq W$  then
         $x[i] = 1$ 
         $\text{weight} = \text{weight} + w[i]$ 
    else
         $x[i] = (W - \text{weight}) / w[i]$ 
         $\text{weight} = W$ 
        break
return x
```

### Implementation:

#### Code:

```
#include <stdio.h>

#define MAX_ITEMS 100

void fractionalKnapsack(int n, float values[], float weights[], float
capacity) {
    float x[MAX_ITEMS];
    float totalValue = 0;
    float weight = 0;
    int i;

    for (i = 0; i < n; ++i) {
        x[i] = 0;
    }

    for (i = 0; i < n; ++i) {
```



```
if (weight + weights[i] <= capacity) {
    x[i] = 1;
    totalValue += values[i];
    weight += weights[i];
} else {

    x[i] = (capacity - weight) / weights[i];
    totalValue += x[i] * values[i];
    weight = capacity;
    break;
}
}

printf("Fractional Knapsack Solution:\n");
printf("Selected fractions for each item:\n");
for (i = 0; i < n; ++i) {
    printf("Item %d: %.2f\n", i + 1, x[i]);
}
printf("Total value of selected items: %.2f\n", totalValue);
}

int main() {
    int n;
    float values[MAX_ITEMS], weights[MAX_ITEMS], capacity;
    int i;

    printf("Enter the number of items: ");
    scanf("%d", &n);

    printf("Enter the values and weights for each item:\n");
    for (i = 0; i < n; ++i) {
        printf("Item %d: ", i + 1);
        scanf("%f %f", &values[i], &weights[i]);
    }

    printf("Enter the knapsack capacity: ");
    scanf("%f", &capacity);
    fractionalKnapsack(n, values, weights, capacity);

    return 0;
}
```



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### Output:

```
PS C:\TURBOC3\BIN> cd "c:\TURBOC3\BIN\" ; if ($?) { gcc FK.C -o FK } ; if ($?) { .\FK }
Enter the number of items: 6
Enter the values and weights for each item:
Item 1: 6 4
Item 2: 5 6
Item 3: 4 7
Item 4: 7 8
Item 5: 9 4
Item 6: 5 2
Enter the knapsack capacity: 30
Fractional Knapsack Solution:
Selected fractions for each item:
Item 1: 1.00
Item 2: 1.00
Item 3: 1.00
Item 4: 1.00
Item 5: 1.00
Item 6: 0.50
Total value of selected items: 33.50
PS C:\TURBOC3\BIN> █
```

**Conclusion:** In conclusion, the fractional knapsack algorithm efficiently solves the fractional knapsack problem, which involves selecting items of maximum value to fit within a knapsack of limited capacity. Unlike the 0/1 knapsack problem, where items must be either entirely included or excluded from the knapsack, the fractional knapsack problem allows items to be included partially, enabling fractions of items to be selected based on their value-to-weight ratio.

This algorithm iteratively selects items based on their value-to-weight ratio, prioritizing items with higher ratios to maximize the total value of items included in the knapsack. It calculates the fraction of each item to include in the knapsack, ensuring that the total weight does not exceed the knapsack's capacity.