

## Math 300 Assignment 7.5

ALGORITHM. The Bubble Sort

```
procedure bubblesort( $a_1, \dots, a_n$ : real numbers with  $n \geq 2$ )  
for  $i := 1$  to  $n - 1$   
    for  $j = 1$  to  $n - i$   
        if  $a_j > a_{j+1}$  then interchange  $a_j$  and  $a_{j+1}$   
 $\{a_1, \dots, a_n$  is in increasing order}
```

ALGORITHM. Merging Two Lists

```
procedure merge( $L_1, L_2$ : sorted lists)  
 $L :=$  empty list  
while  $L_1$  and  $L_2$  are both nonempty  
    remove smaller of first elements of  $L_1$  and  $L_2$  from its list; put it at the right end of  $L$   
    if this removal makes one list empty then remove all elements from the other list and append them to  $L$   
return  $L$   $\{L$  is the merged list with elements in increasing order}
```

ALGORITHM. Merge Sort

```
procedure mergesort( $L = a_1, \dots, a_n$ )  
if  $n > 1$  then  
     $m := \lfloor n/2 \rfloor$   
     $L_1 := a_1, a_2, \dots, a_m$   
     $L_2 := a_{m+1}, a_{m+2}, \dots, a_n$   
     $L := \text{merge}(\text{mergesort}(L_1), \text{mergesort}(L_2))$   
 $\{L$  is now sorted into elements in nondecreasing order}
```

Use either Maplesoft, MATHLAB, SageMath, or Python for the following exercises.

1. (5 points) Write a computer program that implements the Bubble Sort.
2. (10 points) Write a computer program that implements the Merge Sort. Note that you need to implement the *Merge Two Lists* algorithm first.