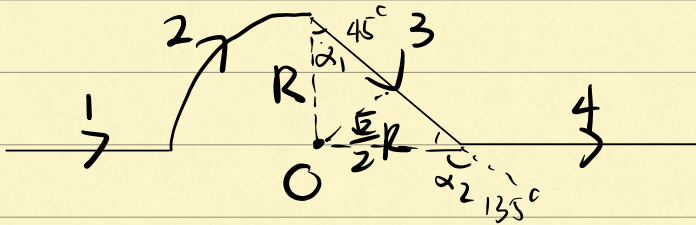


1. 一根无限长导线弯成如图形状, 设导线都处于同一平面内, 其中第2段是半径为  $R$  的  $1/4$  圆弧, 其余部分为直线, 导线中通有电流  $I$ , 求图中  $O$  点处磁感应强度



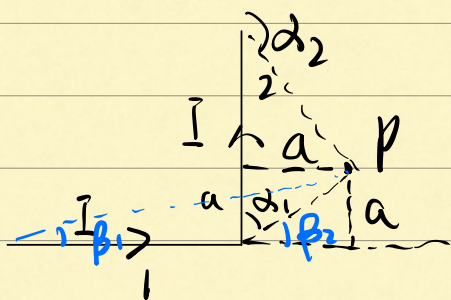
$$B_{1O} = B_{4O} = 0$$

$$\begin{aligned} B_{2O} &= \frac{\mu_0 I}{2R} \cdot \frac{\theta}{2\pi} \\ &= \frac{\mu_0 I}{2R} \cdot \frac{\pi}{4\pi} \\ &= \frac{\mu_0 I}{8R} \quad (\otimes) \end{aligned}$$

$$\begin{aligned} B_{3O} &= \frac{\mu_0 I}{4\pi r} (\cos\alpha_1 - \cos\alpha_2) \quad r = \frac{\sqrt{2}}{2}R \\ &= \frac{\sqrt{2}\mu_0 I}{2\pi R} \left( \frac{\sqrt{2}}{2} + \frac{\sqrt{2}}{2} \right) \\ &= \frac{\mu_0 I}{2\pi R} \quad (\otimes) \end{aligned}$$

$$\begin{aligned} B &= B_{2O} + B_{3O} \\ &= \frac{\mu_0 I}{8R} + \frac{\mu_0 I}{2\pi R} \\ &= \frac{\mu_0 I}{2R} \left( \frac{1}{4} + \frac{1}{\pi} \right) \quad (\otimes) \end{aligned}$$

2. 一无限长载有电流  $I$  的直导线在一处折成直角,  $P$  点位于导线所在平面内, 距一条折线的延长线和另一条导线的距离都为  $a$ , 求  $P$  点的磁感强度



$$\begin{aligned}
 B_{p1} &= \frac{\mu_0 I}{4\pi x} (\cos\beta_1 - \cos\beta_2) \\
 &= \frac{\mu_0 I}{4\pi a} \left(1 - \frac{\sqrt{2}}{2}\right) \\
 &= \frac{\mu_0 I}{4\pi a} \left(\frac{2-\sqrt{2}}{2}\right) \\
 &= \frac{\mu_0 I (2-\sqrt{2})}{8\pi a} \quad \text{①}
 \end{aligned}$$

$$\begin{aligned}
 B_{p2} &= \frac{\mu_0 I}{4\pi x} (\cos\alpha_1 - \cos\alpha_2) \\
 &= \frac{\mu_0 I}{4\pi a} \left(\frac{\sqrt{2}}{2} + 1\right) \\
 &= \frac{\mu_0 I (\sqrt{2}+2)}{8\pi a} \quad \text{②}
 \end{aligned}$$

以向里方向为正方向

$$B = B_{p1} - B_{p2} = -\frac{2\sqrt{2}\mu_0 I}{8\pi a} = -\frac{\sqrt{2}\mu_0 I}{4\pi a} \quad \text{③}$$