

ENGR-241 Laplace Lab

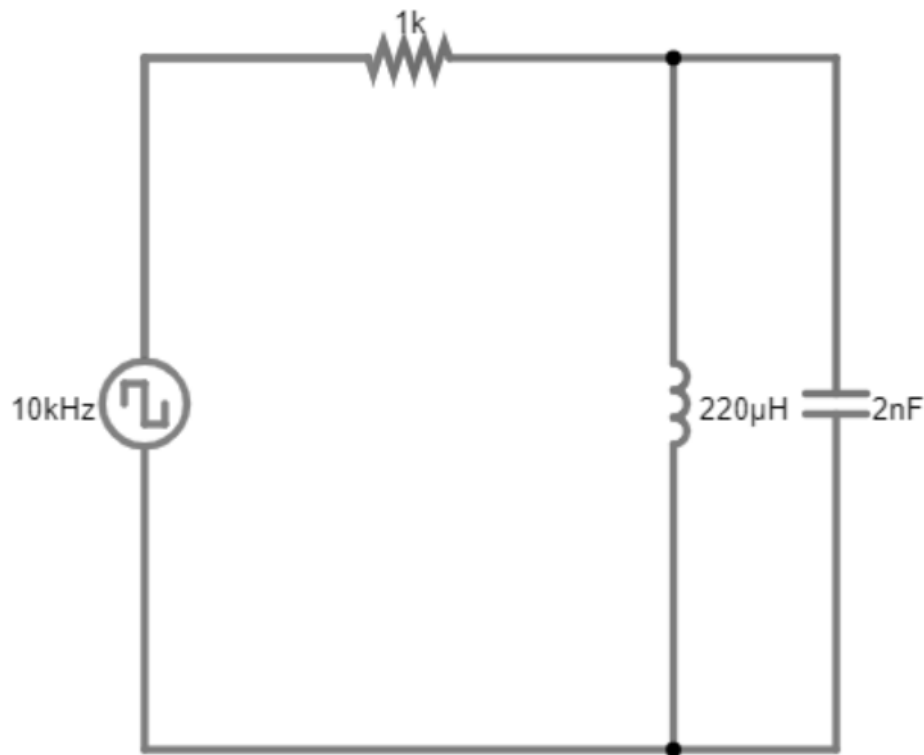
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Overview

For this lab we constructed an RLC circuit with a square wave input from the signal generator and viewed the voltage output on the oscilloscope. We calculated the equation for the output voltage using an Laplace transform and compared the results to the outputs found in our constructed circuit. We then simulated the circuit using Orcad to verify our results. We then graphed and compared all three output voltages.

Circuit Diagrams



Calculations

The calculations for the circuit were performed by transforming the system into the S domain and then performing partial fraction decomposition to determine the values of K_1 and K_1^* and using all of the found values in the general equation for the transformation back to the time domain.

1. Calculate the output voltage of the given circuit in the S domain.

Given:

$$R = 1k\Omega$$

$$C = 2000pF$$

$$L = 220\mu H$$

Solution:

$$V_o(s) = \frac{V_i/RC}{s^2 + (1/RC)s + 1/LC}$$

$$V_o(s) = \frac{5/1000 \times 2000 \times 10^{-12}}{s^2 + (1/1000 \times 2000 \times 10^{-12})s + (1/220 \times 10^{-6} \times 2000 \times 10^{-12})}$$

$$V_o(s) = \frac{2.5 \times 10^6}{s^2 + 500 \times 10^3 s + 2.7272727 \times 10^{12}}$$

$$\text{This is then equivalent to: } \frac{K_1}{s + 250 \times 10^3 - j1486680.867} + \frac{K_1^*}{s + 250 \times 10^3 + j1486680.867}$$

2. Calculate the values of K_1 and K_1^* using partial fraction decomposition.

Given:

$$V_o(s) = \frac{1.25 \times 10^6}{s^2 + 500 \times 10^3 s + 2.7272727 \times 10^{12}}$$

Solution:

Utilizing the partial fraction decomposition function of the TI-89 we were able to bypass the mathematical computation to find the values of K_1 and K_1^* .

$$K_1 = 0.765738 \angle 90$$

$$K_1^* = 0.765738 \angle -90$$

3. Determine the final expression for the output function in the time domain.

$$V_o(t) = 2|K|e^{-at} \cos(\omega t + \theta)u(t)$$

$$V_o(t) = 1.531476e^{-250000t} \sin(1.63239 \times 10^6 t)$$

