

# Output tables for 1xN statistical comparisons.

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## 1 Average rankings of Friedman test

Average ranks obtained by each method in the Friedman test.

Friedman statistic (distributed according to chi-square with 15 degrees of freedom): 278.220588.

P-value computed by Friedman Test: 0.

Iman and Davenport statistic (distributed according to F-distribution with 15 and 525 degrees of freedom): 37.198191.

P-value computed by Iman and Davenport Test: 0.

Algorithm	Ranking
BestCyclicAssignment	8.7778
BestNearest	7.5972
CLARA	10.125
CoefficientPropagation	7.3889
CyclicAssignment	13.8056
Farthest-First	5.5833
KMEANS	5.5139
NearestByCustomer	8.5972
NearestByDepot	12.1389
PAM	10.1389
Parallel	8.5972
RandomByElement	15.6528
Simplified	7.7083
Sweep	7.4167
ThreeCriteriaClustering	5.1389
UPGMC	1.8194

Table 1: Average Rankings of the algorithms (Friedman)

## 2 Post hoc comparison (Friedman)

P-values obtained in by applying post hoc methods over the results of Friedman procedure.

$i$	algorithm	$z = (R_0 - R_i)/SE$	$p$	Holm	Hochberg	Hommel	Holland	Rom	Finner	Li
15	RandomByElement	12.327337	0		0.003333		0.003414	0.003507	0.003414	0.052469
14	CyclicAssignment	10.681217	0		0.003571		0.003657	0.003757	0.006816	0.052469
13	NearestByDepot	9.195995	0		0.003846		0.003938	0.004046	0.010206	0.052469
12	PAM	7.41373	0		0.004167		0.004265	0.004383	0.013585	0.052469
11	CLARA	7.401353	0		0.004545		0.004652	0.004782	0.016952	0.052469
10	BestCyclicAssignment	6.200799	0		0.005		0.005116	0.00526	0.020308	0.052469
9	NearestByCustomer	6.0399	0		0.005556		0.005683	0.005844	0.023653	0.052469
8	Parallel	6.0399	0		0.00625		0.006391	0.006574	0.026986	0.052469
7	Simplified	5.247782	0		0.007143		0.007301	0.007513	0.030307	0.052469
6	BestNearest	5.148767	0		0.008333		0.008512	0.008764	0.033617	0.052469
5	Sweep	4.987868	0.000001		0.01		0.010206	0.010515	0.036916	0.052469
4	CoefficientPropagation	4.963115	0.000001		0.0125		0.012741	0.013109	0.040204	0.052469
3	Farthest-First	3.354125	0.000796		0.016667		0.016952	0.016667	0.043481	0.052469
2	KMEANS	3.292241	0.000994		0.025		0.025321	0.025	0.046746	0.052469
1	ThreeCriteriaClustering	2.958066	0.003096		0.05		0.05	0.05	0.05	0.05

Table 2: Post Hoc comparison Table for  $\alpha = 0.05$  (FRIEDMAN)

Bonferroni-Dunn's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.003333$ .

Hochberg's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.05$ .

Hommel's procedure rejects all hypotheses.

Rom's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.05$ .

Li's procedure rejects those hypotheses that have an unadjusted p-value  $\leq 0.05$ .

### 3 Adjusted P-Values (Friedman)

Adjusted P-values obtained through the application of the post hoc methods (Friedman).

i	algorithm	unadjusted $p$	$p_{Bonf}$	$p_{Halm}$	$p_{Hochberg}$	$p_{Hommel}$
1	RandomByElement	0	0	0	0	0
2	CyclicAssignment	0	0	0	0	0
3	NearestByDepot	0	0	0	0	0
4	PAM	0	0	0	0	0
5	CLARA	0	0	0	0	0
6	BestCyclicAssignment	0	0	0	0	0
7	NearestByCustomer	0	0	0	0	0
8	Parallel	0	0	0	0	0
9	Simplified	0	0.000002	0.000001	0.000001	0.000001
10	BestNearest	0	0.000004	0.000002	0.000002	0.000001
11	Sweep	0.000001	0.000009	0.000003	0.000003	0.000002
12	CoefficientPropagation	0.000001	0.00001	0.000003	0.000003	0.000003
13	Farthest-First	0.000796	0.011942	0.002388	0.001988	0.001592
14	KMEANS	0.000994	0.014909	0.002388	0.001988	0.001988
15	ThreeCriteriaClustering	0.003096	0.046436	0.003096	0.003096	0.003096

Table 3: Adjusted  $p$ -values (FRIEDMAN) (I)

i	algorithm	unadjusted $p$	$p_{Holland}$	$p_{Rom}$	$p_{Finner}$	$p_{Li}$
1	RandomByElement	0	0	0	0	0
2	CyclicAssignment	0	0	0	0	0
3	NearestByDepot	0	0	0	0	0
4	PAM	0	0	0	0	0
5	CLARA	0	0	0	0	0
6	BestCyclicAssignment	0	0	0	0	0
7	NearestByCustomer	0	0	0	0	0
8	Parallel	0	0	0	0	0
9	Simplified	0	0.000001	0.000001	0	0
10	BestNearest	0	0.000002	0.000001	0	0
11	Sweep	0.000001	0.000003	0.000003	0.000001	0.000001
12	CoefficientPropagation	0.000001	0.000003	0.000003	0.000001	0.000001
13	Farthest-First	0.000796	0.002387	0.001988	0.000919	0.000796
14	KMEANS	0.000994	0.002387	0.001988	0.001065	0.000994
15	ThreeCriteriaClustering	0.003096	0.003096	0.003096	0.003096	0.003096

Table 4: Adjusted  $p$ -values (FRIEDMAN) (II)