

Output tables for the test of Multiple comparisons.

June 6, 2025

1 Average rankings of Friedman test

Average ranks obtained by applying the Friedman procedure

Friedman statistic considering reduction performance (distributed according to chi-square with 17 degrees of freedom: 288.096842.

P-value computed by Friedman Test: 1.3832923695389354E-10.

Iman and Davenport statistic considering reduction performance (distributed according to F-distribution with 17 and 408 degrees of freedom: 50.505221.

P-value computed by Iman and Davenport Test: -2.220446049250313E-16.

Algorithm	Ranking
BestCyclicAssignment	9.96
BestNearest	6.6
CLARA	10.64
CoefficientPropagation	8.36
CyclicAssignment	14.12
Farthest-First	5.62
KMEANS	6.28
NearestByCustomer	8.22
NearestByDepot	10.96
PAM	18
Parallel	8.22
RandomByElement	16.74
RandomSequentialCyclic	13.8
SequentialCyclic	13.84
Simplified	6.88
Sweep	6.42
ThreeCriteriaClustering	4.98
UPGMC	1.36

Table 1: Average Rankings of the algorithms

2 Post hoc comparisons

Results achieved on post hoc comparisons for $\alpha = 0.05$, $\alpha = 0.10$ and adjusted p-values.

2.1 P-values for $\alpha = 0.05$

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.000327 .

Holm's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.000581 .

Shaffer's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.000327 .

i	algorithms	$z = (R_0 - R_i)/SE$	p	Holm
153	PAM vs. UPGMC	11.020109	0	0.000327
152	RandomByElement vs. UPGMC	10.185654	0	0.000329
151	PAM vs. ThreeCriteriaClustering	8.622706	0	0.000331
150	CyclicAssignment vs. UPGMC	8.450516	0	0.000333
149	SequentialCyclic vs. UPGMC	8.265082	0	0.000336
148	RandomSequentialCyclic vs. UPGMC	8.238591	0	0.000338
147	Farthest-First vs. PAM	8.198855	0	0.00034
146	RandomByElement vs. ThreeCriteriaClustering	7.78825	0	0.000342
145	KMEANS vs. PAM	7.76176	0	0.000345
144	PAM vs. Sweep	7.669042	0	0.000347
143	BestNearest vs. PAM	7.549834	0	0.00035
142	PAM vs. Simplified	7.3644	0	0.000352
141	Farthest-First vs. RandomByElement	7.3644	0	0.000355
140	KMEANS vs. RandomByElement	6.927304	0	0.000357
139	RandomByElement vs. Sweep	6.834587	0	0.00036
138	BestNearest vs. RandomByElement	6.715379	0	0.000362
137	RandomByElement vs. Simplified	6.529945	0	0.000365
136	NearestByCustomer vs. PAM	6.476963	0	0.000368
135	PAM vs. Parallel	6.476963	0	0.00037
134	CoefficientPropagation vs. PAM	6.384246	0	0.000373
133	NearestByDepot vs. UPGMC	6.357755	0	0.000376
132	CLARA vs. UPGMC	6.14583	0	0.000379
131	CyclicAssignment vs. ThreeCriteriaClustering	6.053113	0	0.000382
130	SequentialCyclic vs. ThreeCriteriaClustering	5.867678	0	0.000385
129	RandomSequentialCyclic vs. ThreeCriteriaClustering	5.841188	0	0.000388
128	BestCyclicAssignment vs. UPGMC	5.695489	0	0.000391
127	NearestByCustomer vs. RandomByElement	5.642508	0	0.000394
126	Parallel vs. RandomByElement	5.642508	0	0.000397
125	CyclicAssignment vs. Farthest-First	5.629263	0	0.0004
124	CoefficientPropagation vs. RandomByElement	5.549791	0	0.000403
123	Farthest-First vs. SequentialCyclic	5.443828	0	0.000407
122	Farthest-First vs. RandomSequentialCyclic	5.417337	0	0.00041
121	BestCyclicAssignment vs. PAM	5.32462	0	0.000413
120	CyclicAssignment vs. KMEANS	5.192167	0	0.000417
119	CyclicAssignment vs. Sweep	5.09945	0	0.00042
118	KMEANS vs. SequentialCyclic	5.006732	0.000001	0.000424
117	BestNearest vs. CyclicAssignment	4.980242	0.000001	0.000427
116	KMEANS vs. RandomSequentialCyclic	4.980242	0.000001	0.000431
115	SequentialCyclic vs. Sweep	4.914015	0.000001	0.000435
114	RandomSequentialCyclic vs. Sweep	4.887524	0.000001	0.000439
113	CLARA vs. PAM	4.874279	0.000001	0.000442
112	BestNearest vs. SequentialCyclic	4.794807	0.000002	0.000446
111	CyclicAssignment vs. Simplified	4.794807	0.000002	0.00045
110	BestNearest vs. RandomSequentialCyclic	4.768316	0.000002	0.000455
109	NearestByDepot vs. PAM	4.662354	0.000003	0.000459
108	CoefficientPropagation vs. UPGMC	4.635863	0.000004	0.000463
107	SequentialCyclic vs. Simplified	4.609373	0.000004	0.000467
106	RandomSequentialCyclic vs. Simplified	4.582882	0.000005	0.000472
105	NearestByCustomer vs. UPGMC	4.543146	0.000006	0.000476
104	Parallel vs. UPGMC	4.543146	0.000006	0.000481
103	BestCyclicAssignment vs. RandomByElement	4.490165	0.000007	0.000485
102	CLARA vs. RandomByElement	4.039824	0.000053	0.00049
101	NearestByDepot vs. ThreeCriteriaClustering	3.960352	0.000075	0.000495
100	CyclicAssignment vs. NearestByCustomer	3.90737	0.000093	0.0005
99	CyclicAssignment vs. Parallel	3.90737	0.000093	0.000505
98	NearestByDepot vs. RandomByElement	3.827899	0.000129	0.00051
97	CoefficientPropagation vs. CyclicAssignment	3.814653	0.000136	0.000515
96	CLARA vs. ThreeCriteriaClustering	3.748427	0.000178	0.000521
95	NearestByCustomer vs. SequentialCyclic	3.721936	0.000198	0.000526
94	Parallel vs. SequentialCyclic	3.721936	0.000198	0.000532
93	NearestByCustomer vs. RandomSequentialCyclic	3.695445	0.00022	0.000538
92	Parallel vs. RandomSequentialCyclic	3.695445	0.00022	0.000543
91	Simplified vs. UPGMC	3.655709	0.000256	0.000549
90	CoefficientPropagation vs. SequentialCyclic	3.629219	0.000284	0.000556
89	CoefficientPropagation vs. RandomSequentialCyclic	3.602728	0.000315	0.000562
88	Farthest-First vs. NearestByDepot	3.536501	0.000405	0.000568
87	BestNearest vs. UPGMC	3.470275	0.00052	0.000575
86	Sweep vs. UPGMC	3.351067	0.000805	0.000581
85	CLARA vs. Farthest-First	3.324576	0.000886	0.000588
84	BestCyclicAssignment vs. ThreeCriteriaClustering	3.298086	0.000973	0.000595
83	KMEANS vs. UPGMC	3.25835	0.001121	0.000602
82	KMEANS vs. NearestByDepot	3.099406	0.001939	0.00061
81	NearestByDepot vs. Sweep	3.006688	0.002641	0.000617
80	CLARA vs. KMEANS	2.887481	0.003883	0.000625
79	BestNearest vs. NearestByDepot	2.887481	0.003883	0.000633
78	BestCyclicAssignment vs. Farthest-First	2.874235	0.00405	0.000641
77	Farthest-First vs. UPGMC	2.821254	0.004784	0.000649
76	CLARA vs. Sweep	2.794763	0.005194	0.000658
75	PAM vs. RandomSequentialCyclic	2.781518	0.005411	0.000667
74	PAM vs. SequentialCyclic	2.755027	0.005869	0.000676
73	BestCyclicAssignment vs. CyclicAssignment	2.755027	0.005869	0.000685
72	NearestByDepot vs. Simplified	2.702046	0.006891	0.000694
71	BestNearest vs. CLARA	2.675555	0.007461	0.000704
70	CyclicAssignment vs. PAM	2.569593	0.010182	0.000714
69	BestCyclicAssignment vs. SequentialCyclic	2.569593	0.010182	0.000725
68	BestCyclicAssignment vs. RandomSequentialCyclic	2.543102	0.010987	0.000735
67	CLARA vs. Simplified	2.490121	0.01277	0.000746
66	BestCyclicAssignment vs. KMEANS	2.43714	0.014804	0.000758
65	ThreeCriteriaClustering vs. UPGMC	2.397404	0.016512	0.00076

2.2 P-values for $\alpha = 0.10$

Nemenyi's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.000654 .

Holm's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.00122 .

Shaffer's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.000654 .

i	algorithms	$z = (R_0 - R_i)/SE$	p	Holm
153	PAM vs. UPGMC	11.020109	0	0.000654
152	RandomByElement vs. UPGMC	10.185654	0	0.000658
151	PAM vs. ThreeCriteriaClustering	8.622706	0	0.000662
150	CyclicAssignment vs. UPGMC	8.450516	0	0.000667
149	SequentialCyclic vs. UPGMC	8.265082	0	0.000671
148	RandomSequentialCyclic vs. UPGMC	8.238591	0	0.000676
147	Farthest-First vs. PAM	8.198855	0	0.00068
146	RandomByElement vs. ThreeCriteriaClustering	7.78825	0	0.000685
145	KMEANS vs. PAM	7.76176	0	0.00069
144	PAM vs. Sweep	7.669042	0	0.000694
143	BestNearest vs. PAM	7.549834	0	0.000699
142	PAM vs. Simplified	7.3644	0	0.000704
141	Farthest-First vs. RandomByElement	7.3644	0	0.000709
140	KMEANS vs. RandomByElement	6.927304	0	0.000714
139	RandomByElement vs. Sweep	6.834587	0	0.000719
138	BestNearest vs. RandomByElement	6.715379	0	0.000725
137	RandomByElement vs. Simplified	6.529945	0	0.00073
136	NearestByCustomer vs. PAM	6.476963	0	0.000735
135	PAM vs. Parallel	6.476963	0	0.000741
134	CoefficientPropagation vs. PAM	6.384246	0	0.000746
133	NearestByDepot vs. UPGMC	6.357755	0	0.000752
132	CLARA vs. UPGMC	6.14583	0	0.000758
131	CyclicAssignment vs. ThreeCriteriaClustering	6.053113	0	0.000763
130	SequentialCyclic vs. ThreeCriteriaClustering	5.867678	0	0.000769
129	RandomSequentialCyclic vs. ThreeCriteriaClustering	5.841188	0	0.000775
128	BestCyclicAssignment vs. UPGMC	5.695489	0	0.000781
127	NearestByCustomer vs. RandomByElement	5.642508	0	0.000787
126	Parallel vs. RandomByElement	5.642508	0	0.000794
125	CyclicAssignment vs. Farthest-First	5.629263	0	0.0008
124	CoefficientPropagation vs. RandomByElement	5.549791	0	0.000806
123	Farthest-First vs. SequentialCyclic	5.443828	0	0.000813
122	Farthest-First vs. RandomSequentialCyclic	5.417337	0	0.00082
121	BestCyclicAssignment vs. PAM	5.32462	0	0.000826
120	CyclicAssignment vs. KMEANS	5.192167	0	0.000833
119	CyclicAssignment vs. Sweep	5.09945	0	0.00084
118	KMEANS vs. SequentialCyclic	5.006732	0.000001	0.000847
117	BestNearest vs. CyclicAssignment	4.980242	0.000001	0.000855
116	KMEANS vs. RandomSequentialCyclic	4.980242	0.000001	0.000862
115	SequentialCyclic vs. Sweep	4.914015	0.000001	0.00087
114	RandomSequentialCyclic vs. Sweep	4.887524	0.000001	0.000877
113	CLARA vs. PAM	4.874279	0.000001	0.000885
112	BestNearest vs. SequentialCyclic	4.794807	0.000002	0.000893
111	CyclicAssignment vs. Simplified	4.794807	0.000002	0.000901
110	BestNearest vs. RandomSequentialCyclic	4.768316	0.000002	0.000909
109	NearestByDepot vs. PAM	4.662354	0.000003	0.000917
108	CoefficientPropagation vs. UPGMC	4.635863	0.000004	0.000926
107	SequentialCyclic vs. Simplified	4.609373	0.000004	0.000935
106	RandomSequentialCyclic vs. Simplified	4.582882	0.000005	0.000943
105	NearestByCustomer vs. UPGMC	4.543146	0.000006	0.000952
104	Parallel vs. UPGMC	4.543146	0.000006	0.000962
103	BestCyclicAssignment vs. RandomByElement	4.490165	0.000007	0.000971
102	CLARA vs. RandomByElement	4.039824	0.000053	0.00098
101	NearestByDepot vs. ThreeCriteriaClustering	3.960352	0.000075	0.00099
100	CyclicAssignment vs. NearestByCustomer	3.90737	0.000093	0.001
99	CyclicAssignment vs. Parallel	3.90737	0.000093	0.00101
98	NearestByDepot vs. RandomByElement	3.827899	0.000129	0.00102
97	CoefficientPropagation vs. CyclicAssignment	3.814653	0.000136	0.001031
96	CLARA vs. ThreeCriteriaClustering	3.748427	0.000178	0.001042
95	NearestByCustomer vs. SequentialCyclic	3.721936	0.000198	0.001053
94	Parallel vs. SequentialCyclic	3.721936	0.000198	0.001064
93	NearestByCustomer vs. RandomSequentialCyclic	3.695445	0.00022	0.001075
92	Parallel vs. RandomSequentialCyclic	3.695445	0.00022	0.001087
91	Simplified vs. UPGMC	3.655709	0.000256	0.001099
90	CoefficientPropagation vs. SequentialCyclic	3.629219	0.000284	0.001111
89	CoefficientPropagation vs. RandomSequentialCyclic	3.602728	0.000315	0.001124
88	Farthest-First vs. NearestByDepot	3.536501	0.000405	0.001136
87	BestNearest vs. UPGMC	3.470275	0.00052	0.001149
86	Sweep vs. UPGMC	3.351067	0.000805	0.001163
85	CLARA vs. Farthest-First	3.324576	0.000886	0.001176
84	BestCyclicAssignment vs. ThreeCriteriaClustering	3.298086	0.000973	0.00119
83	KMEANS vs. UPGMC	3.25835	0.001121	0.001205
82	KMEANS vs. NearestByDepot	3.099406	0.001939	0.00122
81	NearestByDepot vs. Sweep	3.006688	0.002641	0.001235
80	CLARA vs. KMEANS	2.887481	0.003883	0.00125
79	BestNearest vs. NearestByDepot	2.887481	0.003883	0.001266
78	BestCyclicAssignment vs. Farthest-First	2.874235	0.00405	0.001282
77	Farthest-First vs. UPGMC	2.821254	0.004784	0.001299
76	CLARA vs. Sweep	2.794763	0.005194	0.001316
75	PAM vs. RandomSequentialCyclic	2.781518	0.005411	0.001333
74	PAM vs. SequentialCyclic	2.755027	0.005869	0.001351
73	BestCyclicAssignment vs. CyclicAssignment	2.755027	0.005869	0.00137
72	NearestByDepot vs. Simplified	2.702046	0.006891	0.001389
71	BestNearest vs. CLARA	2.675555	0.007461	0.001408
70	CyclicAssignment vs. PAM	2.569593	0.010182	0.001429
69	BestCyclicAssignment vs. SequentialCyclic	2.569593	0.010182	0.001449
68	BestCyclicAssignment vs. RandomSequentialCyclic	2.543102	0.010987	0.001471
67	CLARA vs. Simplified	2.490121	0.01277	0.001493
66	BestCyclicAssignment vs. KMEANS	2.43714	0.014804	0.001515
65	ThreeCriteriaClustering vs. UPGMC	2.397404	0.016512	0.001538

2.3 Adjusted p-values

i	hypothesis	unadjusted p	P_{Neme}	P_{Holm}	P_{Shap}
1	PAM vs .UPGMC	0	0	0	0
2	RandomByElement vs .UPGMC	0	0	0	0
3	PAM vs .ThreeCriteriaClustering	0	0	0	0
4	CyclicAssignment vs .UPGMC	0	0	0	0
5	SequentialCyclic vs .UPGMC	0	0	0	0
6	RandomSequentialCyclic vs .UPGMC	0	0	0	0
7	Farthest-First vs .PAM	0	0	0	0
8	RandomByElement vs .ThreeCriteriaClustering	0	0	0	0
9	KMEANS vs .PAM	0	0	0	0
10	PAM vs .Sweep	0	0	0	0
11	BestNearest vs .PAM	0	0	0	0
12	PAM vs .Simplified	0	0	0	0
13	Farthest-First vs .RandomByElement	0	0	0	0
14	KMEANS vs .RandomByElement	0	0	0	0
15	RandomByElement vs .Sweep	0	0	0	0
16	BestNearest vs .RandomByElement	0	0	0	0
17	RandomByElement vs .Simplified	0	0	0	0
18	NearestByCustomer vs .PAM	0	0	0	0
19	PAM vs .Parallel	0	0	0	0
20	CoefficientPropagation vs .PAM	0	0	0	0
21	NearestByDepot vs .UPGMC	0	0	0	0
22	CLARA vs .UPGMC	0	0	0	0
23	CyclicAssignment vs .ThreeCriteriaClustering	0	0	0	0
24	SequentialCyclic vs .ThreeCriteriaClustering	0	0.000001	0.000001	0.000001
25	RandomSequentialCyclic vs .ThreeCriteriaClustering	0	0.000001	0.000001	0.000001
26	BestCyclicAssignment vs .UPGMC	0	0.000002	0.000002	0.000002
27	NearestByCustomer vs .RandomByElement	0	0.000003	0.000002	0.000002
28	Parallel vs .RandomByElement	0	0.000003	0.000002	0.000002
29	CyclicAssignment vs .Farthest-First	0	0.000003	0.000002	0.000002
30	CoefficientPropagation vs .RandomByElement	0	0.000004	0.000004	0.000004
31	Farthest-First vs .SequentialCyclic	0	0.000008	0.000006	0.000006
32	Farthest-First vs .RandomSequentialCyclic	0	0.000009	0.000007	0.000007
33	BestCyclicAssignment vs .PAM	0	0.000015	0.000012	0.000012
34	CyclicAssignment vs .KMEANS	0	0.000032	0.000025	0.000025
35	CyclicAssignment vs .Sweep	0	0.000052	0.000041	0.000041
36	KMEANS vs .SequentialCyclic	0.000001	0.000085	0.000065	0.000065
37	BestNearest vs .CyclicAssignment	0.000001	0.000097	0.000074	0.000074
38	KMEANS vs .RandomSequentialCyclic	0.000001	0.000097	0.000074	0.000074
39	SequentialCyclic vs .Sweep	0.000001	0.000137	0.000103	0.000103
40	RandomSequentialCyclic vs .Sweep	0.000001	0.000156	0.000116	0.000116
41	CLARA vs .PAM	0.000001	0.000167	0.000123	0.000123
42	BestNearest vs .SequentialCyclic	0.000002	0.000249	0.000182	0.000182
43	CyclicAssignment vs .Simplified	0.000002	0.000249	0.000182	0.000182
44	BestNearest vs .RandomSequentialCyclic	0.000002	0.000284	0.000204	0.000204
45	NearestByDepot vs .PAM	0.000003	0.000478	0.000341	0.000341
46	CoefficientPropagation vs .UPGMC	0.000004	0.000544	0.000384	0.000384
47	SequentialCyclic vs .Simplified	0.000004	0.000618	0.000432	0.000432
48	RandomSequentialCyclic vs .Simplified	0.000005	0.000702	0.000486	0.000486
49	NearestByCustomer vs .UPGMC	0.000006	0.000848	0.000582	0.000582
50	Parallel vs .UPGMC	0.000006	0.000848	0.000582	0.000582
51	BestCyclicAssignment vs .RandomByElement	0.000007	0.001089	0.000733	0.000733
52	CLARA vs .RandomByElement	0.000053	0.008184	0.005456	0.005456
53	NearestByDepot vs .ThreeCriteriaClustering	0.000075	0.01145	0.007559	0.007559
54	CyclicAssignment vs .NearestByCustomer	0.000093	0.014276	0.009331	0.009331
55	CyclicAssignment vs .Parallel	0.000093	0.014276	0.009331	0.009331
56	NearestByDepot vs .RandomByElement	0.000129	0.019774	0.012666	0.012666
57	CoefficientPropagation vs .CyclicAssignment	0.000136	0.020865	0.013228	0.013228
58	CLARA vs .ThreeCriteriaClustering	0.000178	0.027226	0.017083	0.017083
59	NearestByCustomer vs .SequentialCyclic	0.000198	0.030248	0.018782	0.018782
60	Parallel vs .SequentialCyclic	0.000198	0.030248	0.018782	0.018782
61	NearestByCustomer vs .RandomSequentialCyclic	0.00022	0.033584	0.020414	0.020414
62	Parallel vs .RandomSequentialCyclic	0.00022	0.033584	0.020414	0.020414
63	Simplified vs .UPGMC	0.000256	0.03924	0.023339	0.023339
64	CoefficientPropagation vs .SequentialCyclic	0.000284	0.043495	0.025585	0.025585
65	CoefficientPropagation vs .RandomSequentialCyclic	0.000315	0.048179	0.028026	0.028026
66	Farthest-First vs .NearestByDepot	0.000405	0.062036	0.035681	0.035681
67	BestNearest vs .UPGMC	0.00052	0.079549	0.045234	0.045234
68	Sweep vs .UPGMC	0.000805	0.123166	0.069231	0.069231
69	CLARA vs .Farthest-First	0.000886	0.135486	0.07527	0.07527
70	BestCyclicAssignment vs .ThreeCriteriaClustering	0.000973	0.14894	0.081771	0.081771
71	KMEANS vs .UPGMC	0.001121	0.171455	0.093012	0.093012
72	KMEANS vs .NearestByDepot	0.001939	0.296681	0.159006	0.159006
73	NearestByDepot vs .Sweep	0.002641	0.404089	0.213929	0.213929
74	CLARA vs .KMEANS	0.003883	0.594161	0.310673	0.310673
75	BestNearest vs .NearestByDepot	0.003883	0.594161	0.310673	0.310673
76	BestCyclicAssignment vs .Farthest-First	0.00405	0.619661	0.315906	0.315906
77	Farthest-First vs .UPGMC	0.004784	0.731896	0.36834	0.36834
78	CLARA vs .Sweep	0.005194	0.794647	0.394727	0.394727
79	PAM vs .RandomSequentialCyclic	0.005411	0.827812	0.40579	0.40579
80	PAM vs .SequentialCyclic	0.005869	0.897915	0.434286	0.434286
81	BestCyclicAssignment vs .CyclicAssignment	0.005869	0.897915	0.434286	0.434286
82	NearestByDepot vs .Simplified	0.006891	1.054388	0.496182	0.496182
83	BestNearest vs .CLARA	0.007461	1.141465	0.529699	0.529699
84	CyclicAssignment vs .PAM	0.010182	1.557817	0.712727	0.712727
85	BestCyclicAssignment vs .SequentialCyclic	0.010182	1.557817	0.712727	0.712727
86	BestCyclicAssignment vs .RandomSequentialCyclic	0.010987	1.681059	0.747137	0.747137
87	CLARA vs .Simplified	0.01277	1.953805	0.855588	0.855588
88	BestCyclicAssignment vs .KMEANS	0.014804	2.265007	0.977062	0.977062
89	ThreeCriteriaClustering vs .UPGMC	0.016512	2.526294	1.073262	1.073262