

Output tables for 1xN statistical comparisons.

June 12, 2025

1 Average rankings of Friedman test

Average ranks obtained by each method in the Friedman test.

Friedman statistic (distributed according to chi-square with 15 degrees of freedom): 332.865809.

P-value computed by Friedman Test: 0.

Iman and Davenport statistic (distributed according to F-distribution with 15 and 525 degrees of freedom): 56.245197.

P-value computed by Iman and Daveport Test: -0.

| Algorithm | Ranking |
|-------------------------|---------|
| BestCyclicAssignment | 13.0278 |
| BestNearest | 6.7361 |
| CLARA | 10 |
| CoefficientPropagation | 11.3472 |
| CyclicAssignment | 13.9722 |
| Farthest-First | 3.25 |
| KMEANS | 4.2639 |
| NearestByCustomer | 7.3056 |
| NearestByDepot | 10.9167 |
| PAM | 8.4722 |
| Parallel | 7.3056 |
| RandomByElement | 15.9167 |
| Simplified | 6.4722 |
| Sweep | 6.4861 |
| ThreeCriteriaClustering | 3.3472 |
| UPGMC | 7.1806 |

Table 1: Average Rankings of the algorithms (Friedman)

2 Post hoc comparison (Friedman)

P-values obtained in by applying post hoc methods over the results of Friedman procedure.

| i | algorithm | $z = (R_0 - R_i)/SE$ | p | Holm | Hochberg | Hommel | Holland | Rom | Finner | Li |
|-----|-------------------------|----------------------|----------|----------|----------|----------|----------|----------|----------|----------|
| 15 | RandomByElement | 11.287682 | 0 | 0.003333 | 0.003414 | 0.003507 | 0.003414 | 0.003634 | 0.003414 | 0.003634 |
| 14 | CyclicAssignment | 9.554924 | 0 | 0.003571 | 0.003657 | 0.003757 | 0.006816 | 0.003634 | 0.003634 | 0.003634 |
| 13 | BestCyclicAssignment | 8.713298 | 0 | 0.003846 | 0.003938 | 0.004046 | 0.010206 | 0.003634 | 0.003634 | 0.003634 |
| 12 | CoefficientPropagation | 7.2157 | 0 | 0.004167 | 0.004265 | 0.004383 | 0.013585 | 0.003634 | 0.003634 | 0.003634 |
| 11 | NearestByDepot | 6.832018 | 0 | 0.004545 | 0.004652 | 0.004782 | 0.016952 | 0.003634 | 0.003634 | 0.003634 |
| 10 | CLARA | 6.015146 | 0 | 0.005 | 0.005116 | 0.00526 | 0.020308 | 0.003634 | 0.003634 | 0.003634 |
| 9 | PAM | 4.653693 | 0.000003 | 0.005556 | 0.005683 | 0.005844 | 0.023553 | 0.003634 | 0.003634 | 0.003634 |
| 8 | NearestByCustomer | 3.614039 | 0.000301 | 0.00625 | 0.006391 | 0.006574 | 0.026986 | 0.003634 | 0.003634 | 0.003634 |
| 7 | Parallel | 3.614039 | 0.000301 | 0.007143 | 0.007301 | 0.007513 | 0.030307 | 0.003634 | 0.003634 | 0.003634 |
| 6 | UPGMC | 3.502647 | 0.000461 | 0.008333 | 0.008512 | 0.008764 | 0.033617 | 0.003634 | 0.003634 | 0.003634 |
| 5 | BestNearest | 3.106588 | 0.001893 | 0.01 | 0.010206 | 0.010515 | 0.036916 | 0.003634 | 0.003634 | 0.003634 |
| 4 | Sweep | 2.883805 | 0.003929 | 0.0125 | 0.012741 | 0.013109 | 0.040204 | 0.003634 | 0.003634 | 0.003634 |
| 3 | Simplified | 2.871428 | 0.004086 | 0.016667 | 0.016952 | 0.016667 | 0.043481 | 0.003634 | 0.003634 | 0.003634 |
| 2 | KMEANS | 0.90351 | 0.366255 | 0.025 | 0.025321 | 0.025 | 0.046746 | 0.003634 | 0.003634 | 0.003634 |
| 1 | ThreeCriteriaClustering | 0.086638 | 0.930959 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 | 0.05 |

Table 2: Post Hoc comparison Table for $\alpha = 0.05$ (FRIEDMAN)

Bonferroni-Dunn's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.003333 .

Holm's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.025 .

Hochberg's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.016667 .

Hommel's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.025 .

Holland's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.025321 .

Rom's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.016667 .

Finner's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.046746 .

Li's procedure rejects those hypotheses that have an unadjusted p-value ≤ 0.003634 .

3 Adjusted P-Values (Friedman)

Adjusted P-values obtained through the application of the post hoc methods (Friedman).

| i | algorithm | unadjusted p | p_{Bonf} | p_{Holm} | $p_{Hochberg}$ | p_{Hommel} |
|----|-------------------------|--------------|------------|------------|----------------|--------------|
| 1 | RandomByElement | 0 | 0 | 0 | 0 | 0 |
| 2 | CyclicAssignment | 0 | 0 | 0 | 0 | 0 |
| 3 | BestCyclicAssignment | 0 | 0 | 0 | 0 | 0 |
| 4 | CoefficientPropagation | 0 | 0 | 0 | 0 | 0 |
| 5 | NearestByDepot | 0 | 0 | 0 | 0 | 0 |
| 6 | CLARA | 0 | 0 | 0 | 0 | 0 |
| 7 | PAM | 0.000003 | 0.000049 | 0.000029 | 0.000029 | 0.000029 |
| 8 | NearestByCustomer | 0.000301 | 0.004522 | 0.002412 | 0.00211 | 0.001809 |
| 9 | Parallel | 0.000301 | 0.004522 | 0.002412 | 0.00211 | 0.001809 |
| 10 | UPGMC | 0.000461 | 0.00691 | 0.002764 | 0.002764 | 0.002764 |
| 11 | BestNearest | 0.001893 | 0.028389 | 0.009463 | 0.009463 | 0.00757 |
| 12 | Sweep | 0.003929 | 0.058935 | 0.015716 | 0.012259 | 0.011787 |
| 13 | Simplified | 0.004086 | 0.061293 | 0.015716 | 0.012259 | 0.012259 |
| 14 | KMEANS | 0.366255 | 5.493832 | 0.732511 | 0.732511 | 0.732511 |
| 15 | ThreeCriteriaClustering | 0.930959 | 13.96439 | 0.930959 | 0.930959 | 0.930959 |

Table 3: Adjusted p -values (FRIEDMAN) (I)

| i | algorithm | unadjusted p | $p_{Holland}$ | p_{Rom} | p_{Finner} | p_{Li} |
|----|-------------------------|----------------|---------------|-----------|--------------|----------|
| 1 | RandomByElement | 0 | 0 | 0 | 0 | 0 |
| 2 | CyclicAssignment | 0 | 0 | 0 | 0 | 0 |
| 3 | BestCyclicAssignment | 0 | 0 | 0 | 0 | 0 |
| 4 | CoefficientPropagation | 0 | 0 | 0 | 0 | 0 |
| 5 | NearestByDepot | 0 | 0 | 0 | 0 | 0 |
| 6 | CLARA | 0 | 0 | 0 | 0 | 0 |
| 7 | PAM | 0.000003 | 0.000029 | 0.000028 | 0.000007 | 0.000000 |
| 8 | NearestByCustomer | 0.000301 | 0.002409 | 0.002006 | 0.000565 | 0.004360 |
| 9 | Parallel | 0.000301 | 0.002409 | 0.002006 | 0.000565 | 0.004360 |
| 10 | UPGMC | 0.000461 | 0.002761 | 0.002628 | 0.000691 | 0.006660 |
| 11 | BestNearest | 0.001893 | 0.009427 | 0.008999 | 0.00258 | 0.026660 |
| 12 | Sweep | 0.003929 | 0.015624 | 0.012259 | 0.004909 | 0.053860 |
| 13 | Simplified | 0.004086 | 0.015624 | 0.012259 | 0.004909 | 0.055860 |
| 14 | KMEANS | 0.366255 | 0.598368 | 0.732511 | 0.38657 | 0.841360 |
| 15 | ThreeCriteriaClustering | 0.930959 | 0.930959 | 0.930959 | 0.930959 | 0.930959 |

Table 4: Adjusted p -values (FRIEDMAN) (II)