正弦稳态电路相量分析法 例题



例 3 己知 $u_S = 4\cos(100t - 45^\circ)$ V, $i_S = 2.236\sqrt{2}\cos(100t + 153.43^\circ)$ A, C = 0.01F,

$$L_1 = L_2 = 0.01$$
H, $R_1 = R_2 = 1\Omega$, 求电流 $i_2(t)$ 。

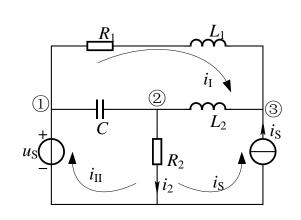
解: 回路电流法

$$\dot{U}_{S} = 2\sqrt{2}\angle 45^{\circ}V = (2 - j2)V$$

 $\dot{I}_{S} = 2.236\angle 153.43^{\circ}A = (-2 + j)A$

$$(R_1 + j\omega L_1 + j\omega L_2 + \frac{1}{j\omega C})\dot{I}_I - \frac{1}{j\omega C}\dot{I}_{II} + j\omega L_2\dot{I}_S = 0$$

$$-\frac{1}{\mathrm{j}\omega C}\dot{I}_{\mathrm{I}} + (R_2 + \frac{1}{\mathrm{j}\omega C})\dot{I}_{\mathrm{II}} + R_2\dot{I}_{\mathrm{S}} = \dot{U}_{\mathrm{S}}$$



$$\begin{cases} \dot{I}_{I} = -jA = 1 \angle 90^{\circ}A \\ \dot{I}_{II} = 3A \end{cases}$$

$$\Rightarrow \dot{I}_{2} = \dot{I}_{II} + \dot{I}_{S} = \sqrt{2} \angle 45^{\circ}A$$

$$\dot{i}_{2}(t) = 2\cos(100t + 45^{\circ})A$$

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节点电压法

$$\dot{U}_{\rm n1} = \dot{U}_{\rm S}$$

$$-j\omega C\dot{U}_{n1} + (j\omega C + \frac{1}{R_2} + \frac{1}{j\omega L_2})\dot{U}_{n2} - \frac{1}{j\omega L_2}\dot{U}_{n3} = 0$$

$$-\frac{1}{R_{1} + j\omega L_{1}}\dot{U}_{n1} - \frac{1}{j\omega L_{2}}\dot{U}_{n2} + (\frac{1}{R_{1} + j\omega L_{1}} + \frac{1}{j\omega L_{2}})\dot{U}_{n3} = \dot{I}_{S}$$

$$\begin{cases} \dot{U}_{n2} = \sqrt{2} \angle 45^{\circ} V \\ \dot{U}_{n3} = \sqrt{2} \angle -45^{\circ} V \end{cases} \Rightarrow \dot{I}_{2} = \dot{U}_{n2} / R_{2} = \sqrt{2} \angle 45^{\circ} A$$

$$i_2(t) = 2\cos(100t + 45^\circ)A$$