

对称三相电路的功率



任意三相电路，不论负载是星形还是角形连接

有功功率 $P = U_A I_A \cos \varphi_A + U_B I_B \cos \varphi_B + U_C I_C \cos \varphi_C$
 $= 3U_P I_P \cos \varphi = 1.5U_m I_m \cos \varphi = \sqrt{3}U_l I_l \cos \varphi$

无功功率 $Q = U_A I_A \sin \varphi_A + U_B I_B \sin \varphi_B + U_C I_C \sin \varphi_C$
 $= 3U_P I_P \sin \varphi = 1.5U_m I_m \sin \varphi = \sqrt{3}U_l I_l \sin \varphi$

视在功率 $S = \sqrt{P^2 + Q^2} = 3U_P I_P = 1.5U_m I_m = \sqrt{3}U_l I_l$

三相电路对称时 $U_A = U_B = U_C = U_P = U_m / \sqrt{2}$ 对称三相功率因数
 $I_A = I_B = I_C = I_P = I_m / \sqrt{2}$ $\lambda = \frac{P}{S} = \cos \varphi$
 $\varphi_A = \varphi_B = \varphi_C = \varphi$

三相平衡制 $p = u_A i_A + u_B i_B + u_C i_C = 3U_P I_P \cos \varphi = \sqrt{3}U_l I_l \cos \varphi = P$

对称三相电路的功率 例题

例1 某对称三相负载各相阻抗为 $Z=(6+j8)\Omega$ ，接于线电压为380V的对称三相电源上，分别计算负载为星形和角形接法时负载相电压、相电流及消耗的平均功率。

解：功率因数为 $\lambda = \cos \varphi = \frac{6}{\sqrt{6^2 + 8^2}} = 0.6$

星形 $U_l = 380\text{V} = 220\sqrt{3}\text{V}$

$$U_P = \frac{380\text{V}}{\sqrt{3}} = 220\text{V}$$

$$I_P = I_l = \frac{U_P}{|Z|} = \frac{220\text{V}}{10\Omega} = 22\text{A}$$

$$P = 3U_P I_P \lambda =$$

$$3 \times 220 \times 22 \times 0.6 = 8712 \text{ W}$$

角形 $U_l = U_P = 380\text{V} = 220\sqrt{3}\text{V}$

$$U_{P\Delta} = \sqrt{3}U_{PY}$$

$$I_{P\Delta} = \sqrt{3}I_{PY}$$

$$P_{\Delta} = 3P_Y$$

$$I_P = \frac{U_P}{|Z|} = \frac{380\text{V}}{10\Omega} = 38\text{A},$$

$$I_l = \sqrt{3}I_P = \sqrt{3} \times 38\text{A} = 66\text{A}$$

$$P = 3U_P I_P \lambda =$$

$$3 \times 380 \times 38 \times 0.6 = 26136\text{W}$$