齐性定理



例1 图示电路中电阻 $R_0=R_2=R_4=R_6=4\Omega$, $R_1=R_3=R_5=8\Omega$ 。(1)若使 $I_0=1$ A,求 U_S 的值。(2)若 $U_S=66$ V,求各支路电流。

$$I_{3} = \frac{U_{3}}{R_{6}} = \frac{R_{2}I_{2} + R_{1}I_{1}}{R_{3}} = 1.25A$$

$$U_{S} \qquad U_{5} \qquad R_{5} \qquad U_{3} \qquad R_{3} \qquad U_{1} \qquad R_{1}$$

$$I_{1} = I_{2} + I_{3} = 2.75A$$

$$I_{2} = I_{1} + I_{0} = 1.5A$$

$$I_{3} = \frac{U_{3}}{R_{3}} = \frac{R_{2}I_{2} + R_{1}I_{1}}{R_{3}} = 1.25A$$

$$I_{4} = I_{2} + I_{3} = 2.75A$$

$$I_{5} = \frac{U_{5}}{R_{5}} = \frac{R_{4}I_{4} + R_{3}I_{3}}{R_{5}} = 2.625A$$

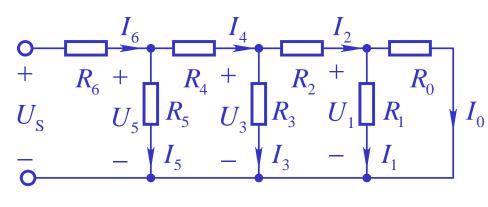
$$I_{6} = I_{4} + I_{5} = 5.375A$$

$$U_{8} = R_{6}I_{6} + R_{5}I_{5} = 42.5V$$

$$I_{1} = I_{1} + I_{0} = 1.5A$$

齐性定理

 $U_{\rm S} = 66$ V 时是42.5V的1.553倍,所以电路中所有的电压、电流均应该增大1.553倍,据此可以求出电路中其它各处电压电流。



$$k = \frac{66\text{V}}{42.5\text{V}} = 1.553$$

$$I_1' = kI_1 = 1.553 \times 0.5 = 0.776$$
A

$$I_2' = kI_2 = 1.553 \times 1.5 = 2.33$$
A

$$I_0' = kI_3 = 1.94A$$

$$I_4' = kI_4 = 4.27A$$

$$I_5' = kI_5 = 4.08A$$

$$I_6' = kI_6 = 8.35$$
A