

Q1\_\_\_question\_below\_\_\_Answers : \_\_\_ (edited/suggested by: \_\_\_Vinay\_\_\_)

\_Answers : \_\_\_a,c,d\_\_\_ (edited/suggested by: \_\_\_Kashank\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Neeraj\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Ashish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Harish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Bachal\_\_\_)

(use notations and conventions from the class) Consider the problem of linear regression where we minimize the loss

$$\mathcal{L}_1 = \frac{1}{N} \sum_{i=1}^N \alpha_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \lambda_1 g(\mathbf{w})$$

where  $g()$  is a regularization term. We also write the loss in matrix form as

$$\mathcal{L}_2 = \frac{1}{N} [\mathbf{Y} - \mathbf{X}\mathbf{w}]^T \mathbf{A} [\mathbf{Y} - \mathbf{X}\mathbf{w}] + \lambda_2 g(\mathbf{w}).$$

If  $\mathbf{A} = \mathbf{I}$ ,  $\alpha_i = 1$  for all  $i$ , and  $\lambda_1 = \lambda_2 = 1$ , then

(A) Both the loss functions are identical i.e.,  $\mathcal{L}_1 = \mathcal{L}_2$

(B)  $\mathcal{L}_1$  is a scalar and  $\mathcal{L}_2$  is a vector

(C) The optima of the first objective  $\mathbf{w}_1^*$  is same as the optima of  $\mathcal{L}_2$ , i.e.,  $\mathbf{w}_2^*$

(D) At the optima, value of the losses are same. i.e.,  $\mathcal{L}_1^* = \mathcal{L}_2^*$

(E) none of the above

Q2 \_\_\_ question \_below \_\_\_ Answers : \_\_\_ (edited/suggested by: \_Vinay\_\_\_)

\_Answers : \_\_\_b,d\_\_\_ (edited/suggested by: \_\_Kashank\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Neeraj\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Ashish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Harish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Bachal\_\_\_)

(use notations and conventions from the class) Consider the problem of linear regression where we minimize the loss

$$\mathcal{L}_1 = \frac{1}{N} \sum_{i=1}^N \alpha_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \lambda_1 g(\mathbf{w})$$

where  $g()$  is a regularization term. We also write the loss in matrix form as

$$\mathcal{L}_2 = \frac{1}{N} [\mathbf{Y} - \mathbf{X}\mathbf{w}]^T \mathbf{A} [\mathbf{Y} - \mathbf{X}\mathbf{w}] + \lambda_2 g(\mathbf{w}).$$

If  $\mathcal{L}_1 = \mathcal{L}_2$  for all  $\mathbf{w}$ , then

(A)  $A_{ii} = \frac{1}{\alpha_i}$  else zero

(B)  $A$  is a diagonal matrix

(C)  $A_{ij} = \alpha_i \cdot \alpha_j$

(D)  $A_{ii} = \alpha_i$  else zero

(E) none of the above

Q3 \_\_\_ question \_below \_\_\_ Answers : \_\_\_ (edited/suggested by: \_Vinay\_\_\_)

\_Answers : \_\_\_b,c,d\_\_\_ (edited/suggested by: \_\_Kashank\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Neeraj\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Ashish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Harish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_Bachal\_\_\_)

(use notations and conventions from the class) Consider the problem of linear regression where we minimize the loss

$$\mathcal{L}_1 = \frac{1}{N} \sum_{i=1}^N \alpha_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \lambda_1 g(\mathbf{w})$$

where  $g()$  is a regularization term. We also write the loss in matrix form as

$$\mathcal{L}_2 = \frac{1}{N} [\mathbf{Y} - \mathbf{X}\mathbf{w}]^T \mathbf{A} [\mathbf{Y} - \mathbf{X}\mathbf{w}] + \lambda_2 g(\mathbf{w}).$$

See  $\mathcal{L}_2$  closely,

- (A) When  $\mathbf{A}$  is not a diagonal matrix, this loss does not make any sense. Don't use.
- (B) When  $\mathbf{A}$  is a diagonal matrix, this is equivalent to weighing each sample independently.
- (C) When  $\mathbf{A}$  is PD, we can do cholesky decomposition of  $\mathbf{A}$  as  $\mathbf{L}\mathbf{L}^T$  and an equivalent formulation is possible in  $\mathcal{L}_1$  is each sample getting transformed as  $\mathbf{L}^T \mathbf{x}_i$  (as in LMNN/Metric Learning)
- (D) When  $\mathbf{A}$  is a rank deficient matrix, an equivalent formulation is possible in  $\mathcal{L}_1$  with a dimensionality reduction (this could be proved with eigen decomposition).
- (E) None of the above

Q4 \_\_\_question\_below\_\_\_ Answers : \_\_\_ (edited/suggested by: \_\_\_Vinay\_\_\_)

\_Answers : \_b\_ (edited/suggested by: \_\_\_Kashank\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Neeraj\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Ashish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Harish\_\_\_)

\_Answers : \_\_\_ (edited/suggested by: \_\_\_Bachal\_\_\_)

(use notations and conventions from the class) Consider the problem of linear regression where we minimize the loss

$$\mathcal{L}_1 = \frac{1}{N} \sum_{i=1}^N \alpha_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \lambda_1 g(\mathbf{w})$$

where  $g(\cdot)$  is a regularization term. We also write the loss in matrix form as

$$\mathcal{L}_2 = \frac{1}{N} [\mathbf{Y} - \mathbf{X}\mathbf{w}]^T \mathbf{A} [\mathbf{Y} - \mathbf{X}\mathbf{w}] + \lambda_2 g(\mathbf{w}).$$

If  $\mathbf{A} = \mathbf{I}$ ,  $\alpha_i = 2$  for all  $i$ , and  $\lambda_1 = \lambda_2 = 0$ , then

- (A) At the optima, value of the losses are same.  $\mathcal{L}_1^* = \mathcal{L}_2^*$
- (B) The optima of the first objective  $\mathbf{w}_1^*$  is same as the optima of  $\mathcal{L}_2$ , i.e.,  $\mathbf{w}_2^*$
- (C) Both the loss functions are identical i.e.,  $\mathcal{L}_1 = \mathcal{L}_2$
- (D)  $\mathcal{L}_1$  is a scalar and  $\mathcal{L}_2$  is a vector
- (E) none of the above

Q5\_\_\_\_question\_below\_\_\_\_Answers : \_\_\_\_\_ (edited/suggested by: \_\_Vinay\_\_\_\_)

\_Answers : \_e\_\_\_\_\_ (edited/suggested by: \_\_Kashank\_\_\_\_)

\_Answers : \_\_\_\_\_ (edited/suggested by: \_\_Neeraj\_\_\_\_)

\_Answers : \_\_\_\_\_ (edited/suggested by: \_\_Ashish\_\_\_\_)

\_Answers : \_\_\_\_\_ (edited/suggested by: \_\_Harish\_\_\_\_)

\_Answers : \_\_\_\_\_ (edited/suggested by: \_\_Bachal\_\_\_\_)

(use notations and conventions from the class) Consider the problem of linear regression where we minimize the loss

$$\mathcal{L}_1 = \frac{1}{N} \sum_{i=1}^N \alpha_i (y_i - \mathbf{w}^T \mathbf{x}_i)^2 + \lambda_1 g(\mathbf{w})$$

where  $g()$  is a regularization term. We also write the loss in matrix form as

$$\mathcal{L}_2 = \frac{1}{N} [\mathbf{Y} - \mathbf{X}\mathbf{w}]^T \mathbf{A} [\mathbf{Y} - \mathbf{X}\mathbf{w}] + \lambda_2 g(\mathbf{w}).$$

If  $\mathbf{A} = \mathbf{I}$ ,  $\alpha_i = 1$  for all  $i$ , and  $\lambda_1 \neq \lambda_2 \neq 0$ , then

- (A) The smaller the lambda, the better the solution
- (B) The optimal parameters  $\mathbf{w}^*$  is independent of  $\lambda_i$ .
- (C) The larger the lambda, the better the solution.
- (D) When lambda is nonzero (positive), loss will increase (since  $g(w)$  is also positive in practice), better to use  $\lambda = 0$ .
- (E) None of the above.