

ASSIGNMENT :- 1

1 Design an algorithm to perform deletion operation by searching an item in an array $A[100]$ having elements from lower bound LB to upper bound UB.

Ans

[Consider an array $A[100]$ having elements from LB to UB and item is given to be deleted from the array.]

Delete ($A[100]$, LB, UB, item)

Step 1: Start

Step 2: Let i , flag = 0

Step 3: for ($i = LB$ to UB), incr by 1

Step 3.1: If ($A[i] = \text{item}$), then

Step 3.1.1: flag = 1

Step 3.1.2: break

[End of if]

[End of for]

Step 4: If (flag = 0), then

Step 4.1: Display "Item to be deleted is not found"

Step 5: Else

Step 5.1: while ($i \leq UB$)

Step 5.1.1: $A[i] = A[i+1]$

Step 5.1.2: $i = i + 1$

[End of while]

Step 5.2: $UB = UB - 1$

[End of if]

Step 6: Exit

- 2 Write an algorithm to sort a list of elements present in an array $X[10]$ in ascending order.

Ans Consider an array $X[10]$ having elements from lb to ub for sorting in ascending order.]

Step 1: Start

Step 2: let i, j, temp

Step 3: for $(i=lb \text{ to } ub-1)$, incr by 1

Step 3.1: for $(j=i+1 \text{ to } ub)$, incr by 1

Step 3.1.1: if $(a[i] > a[j])$, then

Step 3.1.1.1: $\text{temp} = a[i], a[i] = a[j], a[j] = \text{temp}$

[End of if]

[End of for]

[End of for]

Step 4: exit

- 3 What is row-major order and column-major order?

Given a matrix $Q[7][8]$ having base address 1000. If the size of each memory is 4 bytes, and we need to find the address of $Q[4][3]$ then find the address in row-major order and also in column-major order.

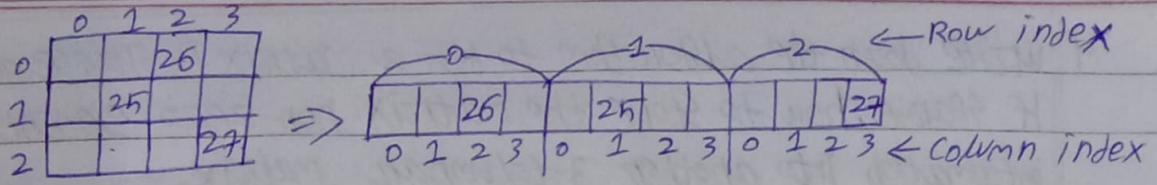
Ans ① Row-major order:- When the memory is occupied row by row sequentially then it is called the row major order. To find the address the formula is: $A[i][j] = \text{Base} + w * (n * i + j)$

where, Base = the starting or base address

w = the size of each element

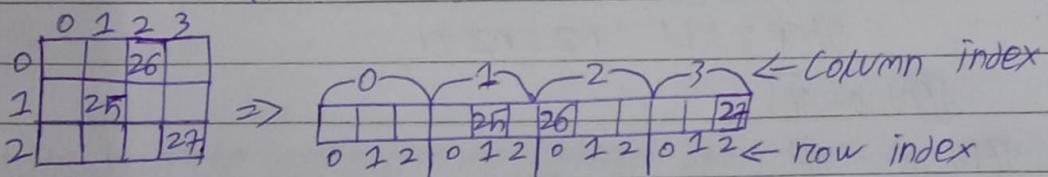
n = the total number of columns

i and j = the corresponding row and column address we are finding.



① Column major order :- When the memory of a matrix occupied serially column by column then it is called column major order. To find the address the formula is : $A[i][j] = \text{Base} + w * (j + m * i)$
where, Base = the starting or base address
 w = the size of each element
 m = the total number of rows

i and j = the corresponding row and column address we are finding.



Given, Base address = 1000, $w = 4$ bytes, $m = 7$, $n = 8$, $i = 4$, $j = 3$

The address in row-major order is :-

$$Q[i][j] = \text{Base} + w * (n * i + j)$$

$$\begin{aligned} Q[4][3] &= 1000 + 4 * (8 * 4 + 3) \\ &= 1000 + 4 * 35 \\ &= 1000 + 140 \\ &= 1140 \end{aligned}$$

The address in column-major order is :-

$$Q[i][j] = \text{Base} + w * (j + m * i)$$

$$\begin{aligned} Q[4][3] &= 1000 + 4 * (4 + 7 * 3) \\ &= 1000 + 4 * 25 \\ &= 1000 + 100 \\ &= 1100 \end{aligned}$$

4 Write down the algorithm to test a matrix is sparse or not.
If sparse, how to store the matrix non-zero elements information into another 3-columnar matrix.

Ans [Consider a matrix $A[m][n]$ having elements. Declare a 3-columnar matrix $SP[nz+1][3]$ where nz is non-zeros count.]
sparse ($A[m][n]$, $SP[nz+1][3]$)

Step 1: Start

Step 2: Let $nz=0, i, j$

Step 3: for $i=0$ to $m-1$, incr by 1

 Step 3.1: for $j=0$ to $n-1$, incr by 1

 Step 3.1.1: If $(A[i][j]) \neq 0$, then
 Step 3.1.1.1: $nz=nz+1$
 [End of if]
 [End of for]
 [End of for]

Step 4: If $(nz \geq (m*n)/2)$, then

 Step 4.1: DISPLAY "It is not sparse"

Step 5: else

 Step 5.1: DISPLAY "It is sparse"
 Step 5.2: call alternate ($A[m][n]$, $SP[nz+1][3]$)
[End of if]

Step 6: Stop

Alternate ($A[m][n]$, $SP[nz+1][3]$)

Step 1: Start

Step 2: Let $i, j, k = 1$

Step 3: $SP[0][0] = m$, $SP[0][1] = n$, $SP[0][2] = nz$

Step 4: for ($i=0$ to $m-1$), incr by 1

Step 4.1: for ($j=0$ to $n-1$), incr by 1

Step 4.1.1: if ($A[i][j] \neq 0$), then

Step 4.1.1.1: $SP[k][0] = i$, $SP[k][1] = j$, $SP[k][2] = A[i][j]$

Step 4.1.1.2: $k = k + 1$

[end of if]

[end of for]

[end of for]

Step 5: exit

5 Write down the algorithm to perform push and pop operations on a given stack using an array.

Ans

Push :-

[Consider a stack [size], initially top = -1]

push(stack[size], top, item)

Step 1: Start

Step 2: If $top = size - 1$, then

Step 2.1: DISPLAY "Stack is full or overflow"

Step 3: else

Step 3.1: $top = top + 1$

Step 3.2: $stack[top] = item$

[end of if]

Step 4: Stop

POP :-

[Consider a Stack[SIZE] having elements and top contains index of top most element.]

POP (Stack[SIZE], top)

Step 1: Start

Step 2: if (top = -1), then

Step 2.1: Display "Stack is empty or underflow"

Step 3: else

Step 3.1: let temp = stack [top]

Step 3.2: Display "Popped value is", temp

Step 3.3: top = top - 1

[end of if]

Step 4: STOP

- 6 Write down the algorithm to convert a given infix expression into equivalent postfix ~~prefix~~ notation using stack.

Ans

[Given an infix expression Q and we need to find equivalent postfix expression P. Declare a stack where top represents top most element. Here i is the index for Q and j is the index for P.]

InfixtoPostfix (P, j, Q, i, Stack, top)

Step 1: Start

Step 2: Push '(' to stack and put ')' at the end of Q

Step 3: while (stack is not empty)

Step 3.1: Scan symbol for Q[i]

Step 3.2: If Q[i] is operand then put the operand at the end of P[j]

Step 3.3: Else if Q[i] is ')' then push ')' into the stack [top]

Step 3.4: Else if Q[i] is operators (X), then

STEP 3.4.1: While ($\text{stack}[\text{Top}]$ is operator AND

$\text{Priority}(\text{stack}[\text{Top}]) \geq \text{Priority}(Q[i])$)

STEP 3.4.1.1: Pop operator from $\text{stack}[\text{Top}]$ and
put at the end of $P[j]$.

[End of while]

STEP 3.4.2: Push operator $Q[i]$ into $\text{stack}[\text{Top}]$

STEP 3.5: Else if $Q[i]$ is ')' then

STEP 3.5.1: While ($\text{stack}[\text{Top}]$ not equal to '(')

STEP 3.5.1.1: Pop operator from $\text{stack}[\text{Top}]$ and
put at the end of $P[j]$

[End of while]

STEP 3.5.2: Delete ')' from $\text{stack}[\text{Top}]$

[End of if]

[End of while]

STEP 4: Display "Postfix Expression is", P

STEP 5: STOP

7 Write down the algorithm to perform Insertion and Deletion operations on a linear queue implemented using an array.

Ans Insertion Algorithm:

Consider a queue [SIZE], Front = -1, Rear = -1 initially. Given an item for insertion
Insertion (Q[SIZE], Front, Rear, Item)

STEP 1: Start

STEP 2: If (Rear = SIZE - 1), then

STEP 2.1: Display "queue overflow"

STEP 3: Else if (Front = -1 AND Rear = -1), then

STEP 3.1: Front = 0, Rear = 0

STEP 3.2: Q[Rear] = Item

STEP 4: Else

STEP 4.1: Q[Front + Rear] = Item

[End of if]

Step 5: STOP

Deletion Algorithms:-

[Consider a queue $Q[\text{size}]$, initially $\text{Front} = -1$, $\text{Rear} = -1$.
Temp declared to hold the deleted value.]

Deletion ($Q[\text{size}]$, Front, Rear, Temp)

Step 1: Start

Step 2: If ($\text{front} = -1$ AND $\text{rear} = -1$), then

Step 2.1: Display "queue underflow"

Step 3: Else if ($\text{front} = \text{rear}$), then

Step 3.1: $\text{temp} = Q[\text{front}]$

Step 3.2: $\text{Front} = -1$, $\text{Rear} = -1$

Step 3.3: Display "Deleted value is", temp

Step 4: Else

Step 4.1: $\text{temp} = Q[\text{front}]$

Step 4.2: $\text{Front} = \text{Front} + 1$

Step 4.3: Display "Deleted value is", temp

End of If]

Step 5: Stop

8 Given infix expression $Q = A - S / D + (E * F \wedge G) - H$

Find its equivalent postfix using stack.

Ans First put ')' at the end of infix expression Q and
push 'C' to Stack[Top].

Symbol	Stack	Postfix Expression
(
A	(A
-	(-	A
S	(-	AS
/	(-1	AS
D	(-1	ASD
+	(+	ASD/-

C	(+ C	ASD/-
E	(+ C	ASD/-E
*	(+ C *	ASD/-E
F	(+ C *	ASD/-EF
^	(+ C * ^	ASD/-EF
G	(+ C * ^	ASD/-EFG
)	(+	ASD/-EFG ^ *
-	(-	ASD/-EFG ^ * +
H	(-	ASD/-EFG ^ * + H
)	empty	ASD/-EFG ^ * + H -

9 Given two arrays $A[5]$ and $B[7]$ having elements in ascending order. Design an algorithm to apply merging operation on both arrays and generate the resultant list into array $C[12]$ in ascending order.

Ans Consider $A[5]$ and $B[7]$ having elements in ascending order from $lb1$ to $ub1$ and $lb2$ to $ub2$ and a resultant array $C[12]$ having $lb3$ and $ub3$

Merging $(A[5], lb1, ub1, B[7], lb2, ub2, C[12], lb3, ub3)$

Step 1: Start

Step 2: Let i, j, k

Step 3: $i = lb1, j = lb2, k = 0$

Step 4: while ($i \leq ub1$ AND $j \leq ub2$)

Step 4.1: if ($A[i] < B[j]$), then

Step 4.1.1: $C[k] = A[i], i = i + 1, k = k + 1$

Step 4.2: else

Step 4.2.1: $C[k] = B[j], j = j + 1, k = k + 1$

[end of if]

[end of while]

Step 5: while ($j \leq ub1$)

Step 5.1: $C[k] = B[j], j = j + 1, k = k + 1, i = i + 1$

[end of while]

Step 6: while ($j \leq ub_2$)

Step 6.1: $C[k] = B[j]$, $k=k+1$, $j=j+1$

[end of while]

Step 7: $lb_3 = 0$, $ub_3 = k-1$

Step 8: stop

10 write down the algorithm to evaluate a given postfix expression using stack.

Ans Consider a postfix expression P given for evaluation.

Declare stack [size], top, i, A, B, R.

PostfixEvaluation (P , stack, i, top, A, B, R)

Step 1: Start

Step 2: put ')' at the end of postfix P .

Step 3: while ($(P[i]) \neq ')'$)

Step 3.1: If ($P[i]$ is operand), then

Step 3.1.1: push $P[i]$ into stack top

Step 3.2: else if ($P[i]$ is operator) then

Step 3.2.1: $A = \text{pop 1st element from stack}$

Step 3.2.2: $B = \text{pop 2nd element from stack}$

Step 3.2.3: $R = P[i] A$

Step 3.2.4: push R into stack top

[end of if]

[end of while]

Step 4: DISPLAY "Result is", stack top

Step 5: stop

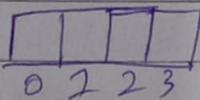
II Given a stack $STK[SIZE]$ where $SIZE = 4$. Initially the $TOP = -1$. Apply the below list of operations on the stack and elaborate the execution process in detail. $PUSH(10)$, $PUSH(20)$, $POP()$, $PUSH(30)$, $PUSH(40)$, $PUSH(50)$, $PUSH(60)$, $POP()$, $POP()$, $POP()$, $PUSH(70)$.

Ans

Initially:-

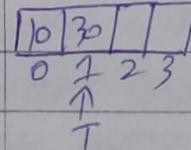
$STK[4]$

$TOP = -1$



$PUSH(30)$:-

$TOP = \cancel{-1} 1$

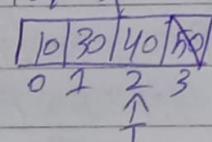


$POP()$:-

$TOP = 3$

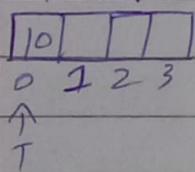
let $temp = STK[Top] = 60$

$TOP = \cancel{3} 2$



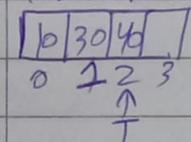
$PUSH(10)$:-

$TOP = \cancel{1} 0$



$PUSH(40)$:-

$TOP = \cancel{2} 3$

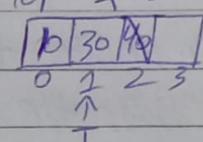


$POP()$:-

$TOP = 2$

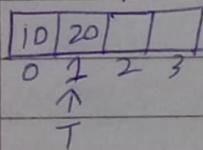
let $temp = STK[Top] = 40$

$TOP = \cancel{2} 1$



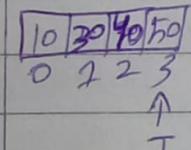
$PUSH(20)$:-

$TOP = \cancel{1} 1$



$PUSH(50)$:-

$TOP = \cancel{3} 3$

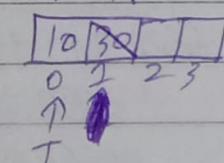


$POP()$:-

$TOP = 1$

let $temp = STK[Top] = 30$

$TOP = \cancel{1} 0$

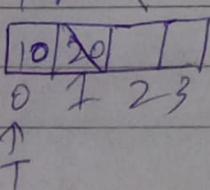


$POP()$:-

$TOP = 1$

let $temp = STK[Top]$
 $= 20$

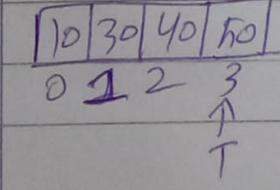
$TOP = \cancel{1} 0$



$PUSH(60)$:-

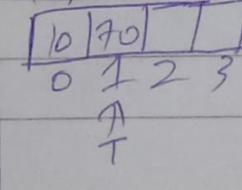
$TOP = 3 = SIZE - 1$

AS TOP IS EQUAL TO
SIZE-1. Therefore
the stack is full.



$PUSH(70)$:-

$TOP = \cancel{1} 1$



Q12 Given a list of elements from lb to ub in an array $A[0:n]$.

Write two algorithms to perform:

- (a) Insertion of an item at a specific location
- (b) Search for a given item.

Ans (a) Given an array $A[0:n]$ having elements from lb to ub and an item to be inserted at a specific location between lb to ub
 Insertion ($A[0:n]$, lb , ub , Item, Position)

Step 1: Start

Step 2: Let i

Step 3: for $(i = ub \text{ to position})$, decr by 1

$$\text{Step 3.1: } A[i+1] = A[i]$$

[End of for]

Step 4: $A[\text{position}] = \text{Item}$

Step 5: $ub = ub + 1$

Step 6: Stop

(b) Given an item to search for its position. Hence let us search whether the element is exist or not.

Search ($A[0:n]$, lb , ub , item)

Step 1: Start

Step 2: Let i , flag = 0

Step 3: for $(i = lb \text{ to } ub)$, incr by 1

Step 3.1: If $(A[i] = \text{item})$, then

Step 3.1.1: flag = 1

Step 3.1.2: break

[End of if]

[End of for]

Step 4: if ($\text{flag} = 0$), then

Step 4.1: DISPLAY "Item is not found"

Step 5: else

Step 5.1: DISPLAY "Item found"

End of IF

Step 6: STOP

13 Given a linear queue $\text{QUEUE}[\text{size}]$ where $\text{size} = n$.

Initially $\text{Front} = -1$ and $\text{Rear} = -1$

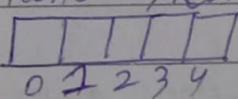
APPLY the below lists of operations on the queue and elaborate the execution process in details. Insert(1), Insert(2), Insert(3), Delete(), DeleteC(), Insert(4), Insert(5), DeleteA(), Insert(6), Insert(7).

Ans

Initially :-

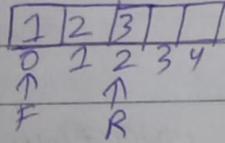
QUEUE[5]

$\text{Front} = -1, \text{Rear} = -1$



Insert(3) :-

$\text{Front} = 0, \text{Rear} = 2$



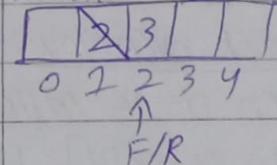
DeleteC() :-

$\text{Front} = 1$

$\text{Rear} = 2$

Let $\text{temp} = \text{QUEUE}[\text{Front}]$
 $= 2$

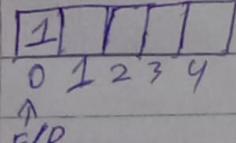
$\text{Front} = \text{Front} + 1 = 2$



Insert(1) :-

$\text{Front} = 2$

$\text{Rear} = 3$



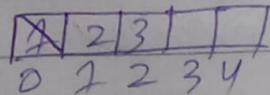
Delete()

$\text{Front} = 0$

$\text{Rear} = 2$

let $\text{temp} = \text{QUEUE}[\text{Front}]$
 $= 1$

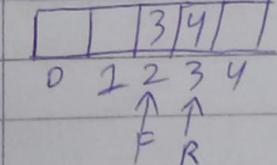
$\text{Front} = \text{Front} + 1 = 1$



Insert(4) :-

$\text{Front} = 2$

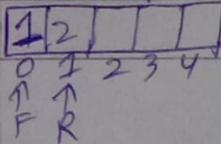
$\text{Rear} = 3$



Insert(2) :-

$\text{Front} = 0$

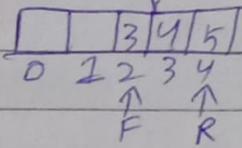
$\text{Rear} = 1$



Insert(5):-

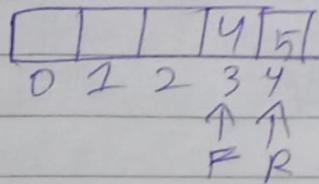
Front = 2

Rear = 4

Insert(6):-

Front = 3, Rptr = 4

As Rear = size - 1. Therefore stack is full or overflow

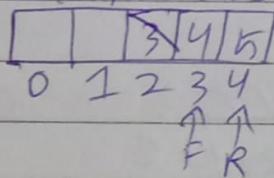
Delete():-

Front = 2

Rear = 4

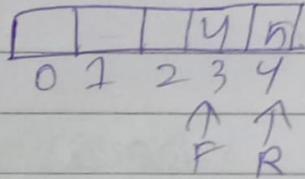
let temp = queue[Front]
= 3

Front = Front + 1 = 3

Insert(7):-

Front = 3, Rear = 4

As Rear = size - 1. Therefore stack is full or overflow

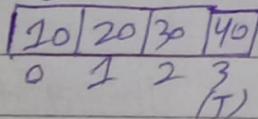
14 List out:-

@ The stack overflow and underflow conditions and

@ Linear queue overflow and underflow conditions.

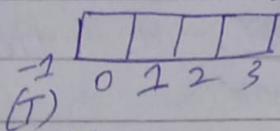
Ans @ Stack overflow:- When the stack is full then "top = size - 1", then it is called stack overflow.

Let stack [4] having elements.



If we try to insert (80), then it will not be possible and it will display "Stack overflow".

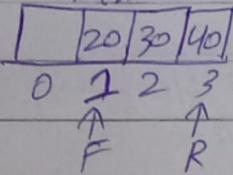
Stack underflow :- when the "top = -1 or NULL", then the stack is empty or underflow. Let $\text{stack}[Y]$ is declared with the $\text{top} = -1$ initially



If we try to delete(), then it will not be possible and it will display "Stack underflow".

② Linear queue overflow :-

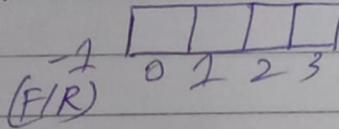
when the queue is full then "Rear = size-1", then it is called queue overflow. Let a queue[Y] having elements



If we try to insert(50), then it will not be inserted and it will display "queue overflow".

Linear queue ~~overflow~~ underflow :-

when the "Front = -1 AND Rear = -1", then the queue is empty or underflow. Let a queue[Y] is declared with the Front = -1 and Rear = -1 initially



If we try to delete(), then it will not be executed and it will display "queue underflow" -

15 Define the terms:

① Abstract Datatype, Linked list, queue, tree, stack.

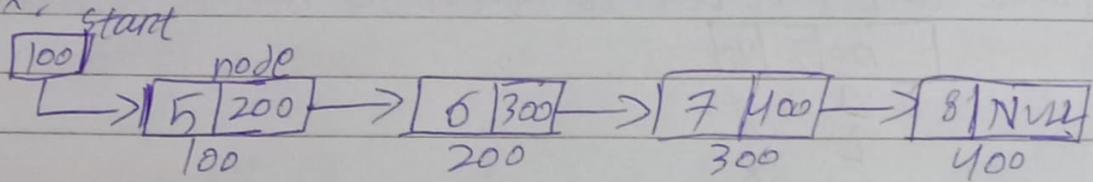
Ans Abstract Datatype) - It is the most suitable datatype for a data model.

Linked LIST:- It is the collection of non-consecutive nodes connected in serial manner. A node contains 2 parts:-

② Info Part:- It hold the value

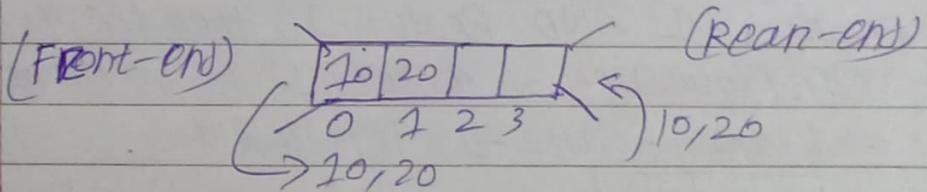
③ Linked part:- It hold the address of next node.

Ex:-



queue:- A Linear datastructure (i.e. either array or linkedlist) which implements "First In First Out" concept (FIFO).

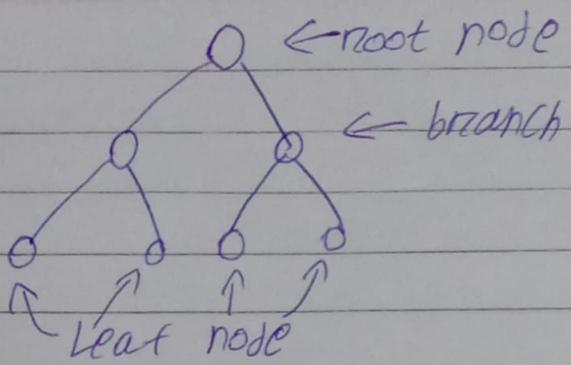
Let us consider a Q[4] having elements.



Tree:- A group of memory locations (node) in which if there is hierarchical relationship exists or top-to-down relationship exists among them, then it is called tree.

Hence the top most memory is the root node. From root node it is connected to different nodes called branches.

At the bottom level whatever the nodes available called leaves (leaf node). Let us consider a binary tree.



Stack: A linear datastructure that implements "Last In First Out" concept is called stack. The concept of stack can be implemented using either array or linked list. Let us consider $S[4]$ having elements

