

Sunday, 3 March 2024

Total marks: 100

Duration: 1 hour

CSE 102 - Data Structures and Algorithms  
Mid-semester Examination, Winter 2024

*Calculators are allowed to use. Use of mobile devices/ computers/ tablets is prohibited. Using books/ notes or any other reference material is not permitted. Attempt **all** questions; options are provided within questions, if any. Show all of your working.*

**Question 1:**

- (a) Define a doubly linked list. Write pseudocode for operations: Insert, Delete, and Search. [20 marks]
- (b) Explain the Counting sort ~~linear search~~ algorithm and derive its time complexity. [20 marks]

**Question 2:**

Solve using recursion tree method (without using Master's theorem):

$$T(n) = 2T\left(\frac{n}{2}\right) + n^2$$

Show all your working and calculations. [25 marks]

**OR**

Prove by induction that the  $i^{\text{th}}$  Fibonacci number satisfies the equation:

$$F_i = \frac{(\phi^i - \hat{\phi}^i)}{\sqrt{5}}$$

where  $\phi$  is the golden ratio and  $\hat{\phi}$  is its conjugate given by:

$$\phi = \frac{1 + \sqrt{5}}{2}, \hat{\phi} = \frac{1 - \sqrt{5}}{2}. \quad [25 \text{ marks}]$$

**Question 3:**

Describe an algorithm that, given  $n$  integers in the range 0 to  $k$ , preprocesses its input and then answers any query about how many of the  $n$  integers fall into a range  $[a : b]$  in  $O(1)$  time. Your algorithm should use  $\theta(n + k)$  preprocessing time. [35 marks]

OR

For a given expression string, 'exp' develop an algorithm to determine if the pairs and orderings of brackets '{', '}', '(', ')', '[', and ']' are correct within the expression. Write pseudocode for your algorithm. [35 marks]

Example:

For Input: exp = "[()]{00}"

Output: Balanced

Explanation: All brackets are correctly paired and ordered.

For Input: exp = "[()]"

Output: Not Balanced

Explanation: The brackets at positions 1 and 4 are not correctly balanced because there's a closing ']' before the closing '('.

$$2 \times \left( \frac{n}{2^2} \right) + \frac{n^2}{4}$$

$$2 \left( \frac{n}{2^2} \right) + \frac{n^2}{4}$$