

# **Engineering Graphics**

## **Lecture Notes**

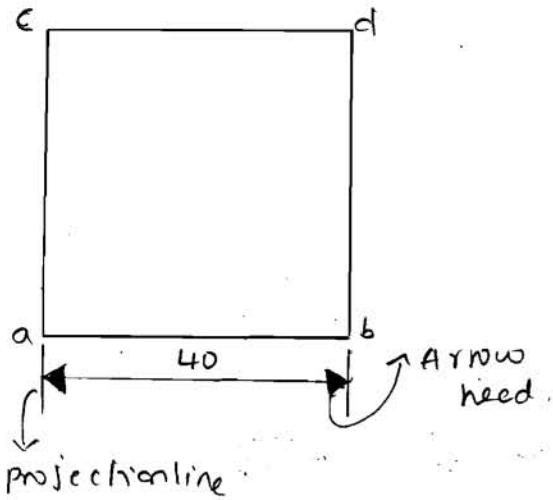
# **UNIT-I**

# **Content**

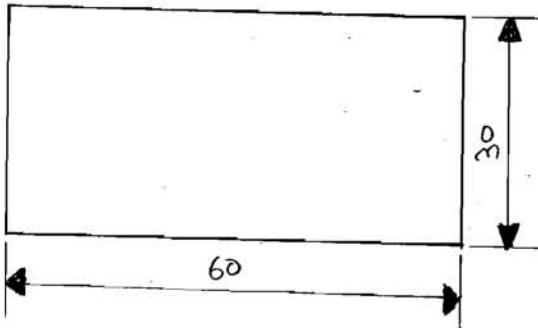
**Introduction to Engineering Drawing:** Principles of Engineering Graphics and their Significance, Conic Sections including the Rectangular Hyperbola – General method only. Cycloid, Epicycloid and Hypocycloid, Scales – Plain & Diagonal.

# BASIC CONCEPTS

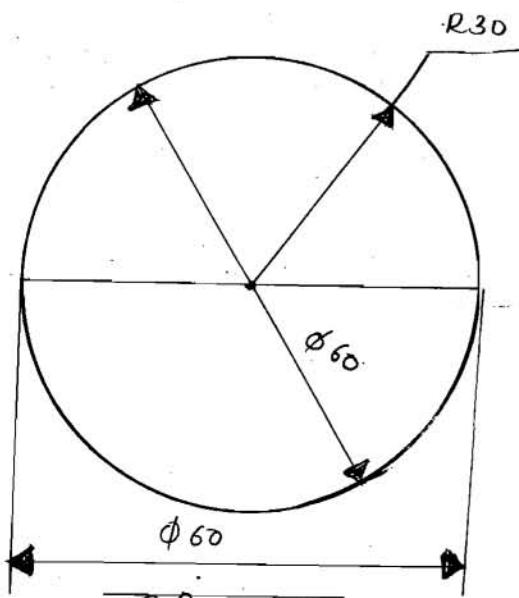
(1)



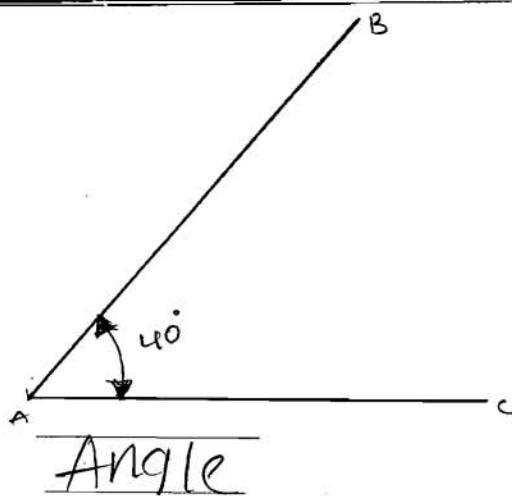
SQUARE.



Rectangle

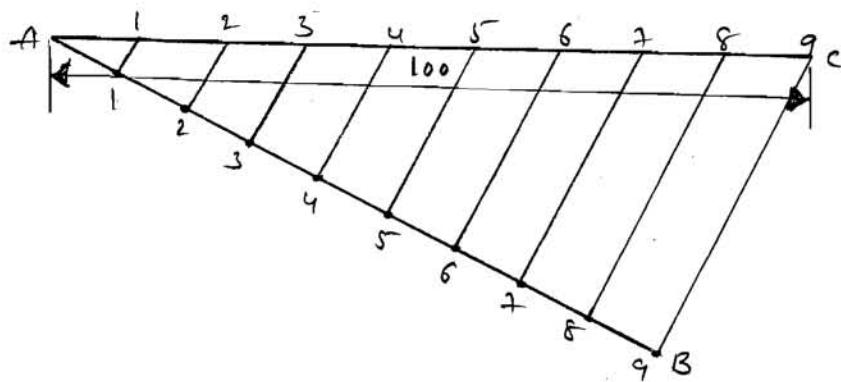


Circle

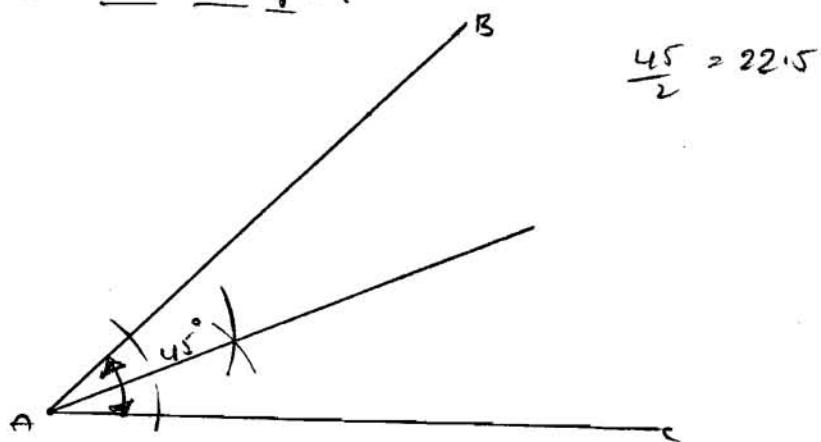


Divide a line into number of equal parts

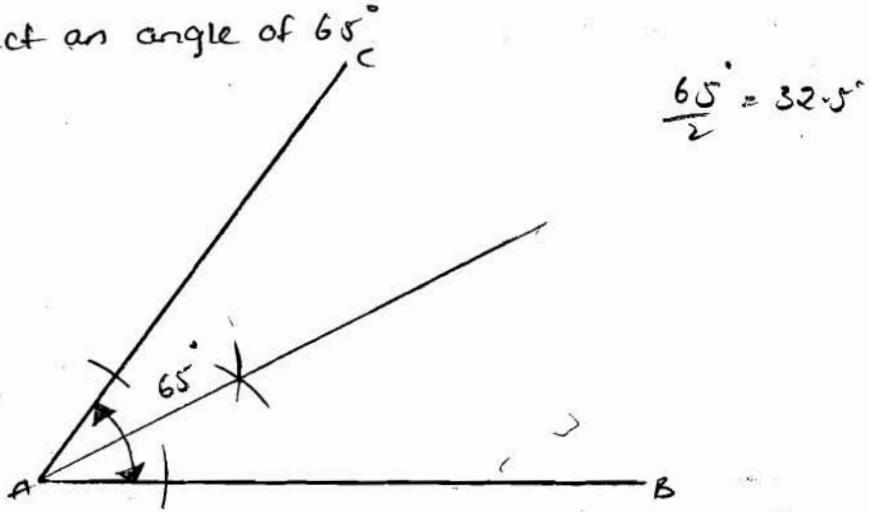
$$n=9$$



Bisecting an angle :-

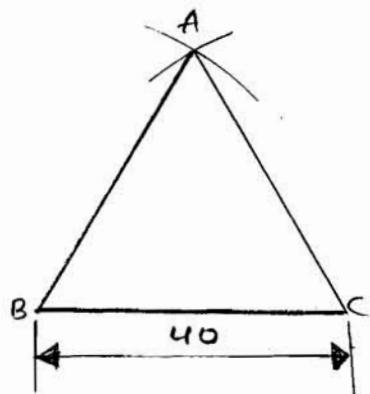


Bisect an angle of  $65^\circ$



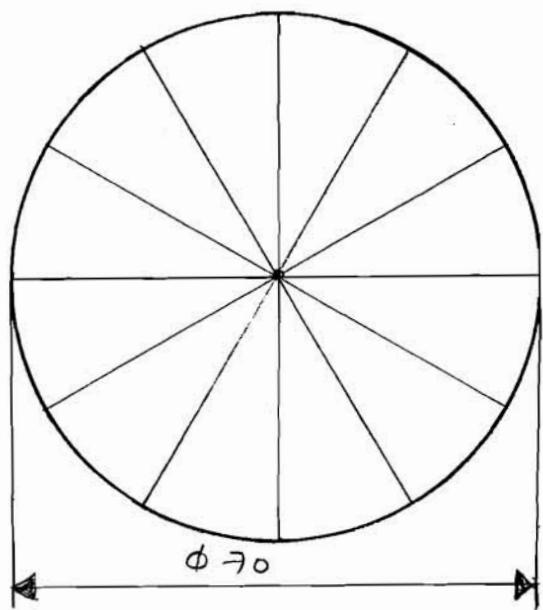
$$\frac{65}{2} = 32.5^\circ$$

Construct an equilateral triangle of side 40mm



Divide a circle of diameter 70mm into 12 equal parts

$$n = 12 \text{ equal parts}$$

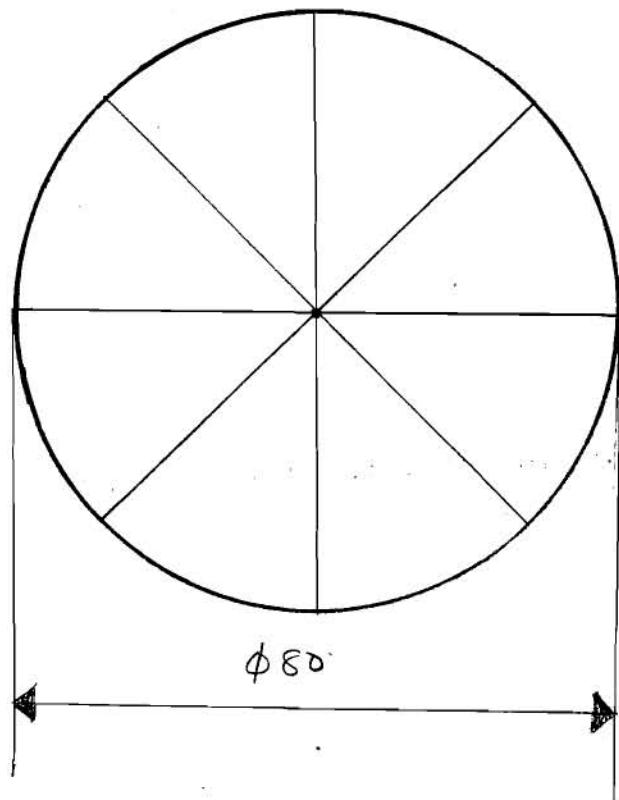


$$\frac{360}{12} = 30^\circ$$

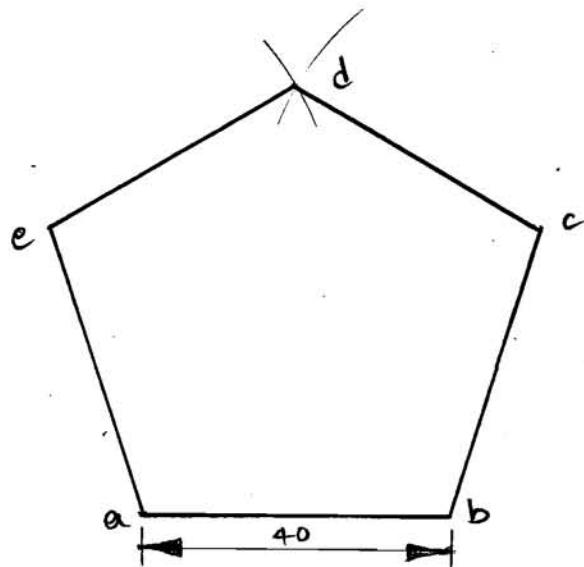
Divide a circle of diameter 80 mm into 8 equal parts.

$n = 8$  equal parts

$$\frac{360^\circ}{8} = 45^\circ$$

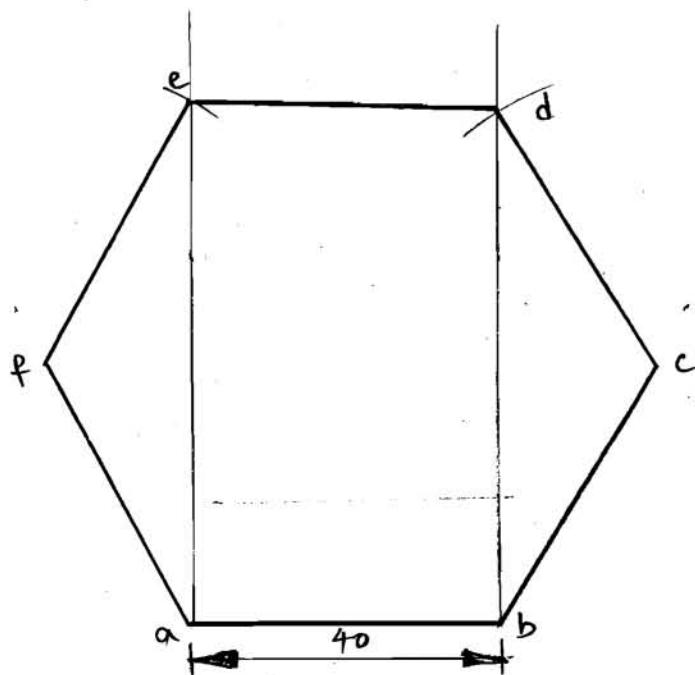


Construct a Pentagon of side 40mm



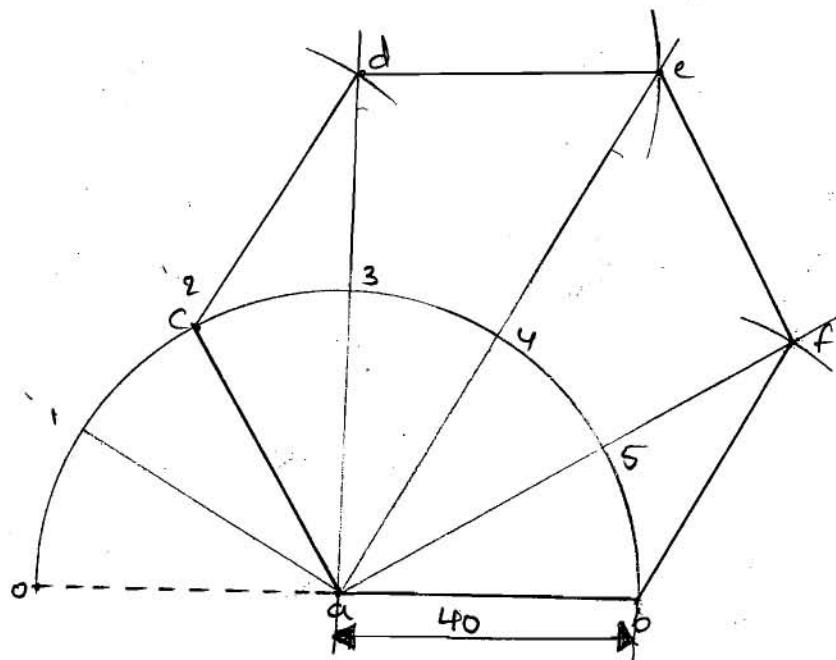
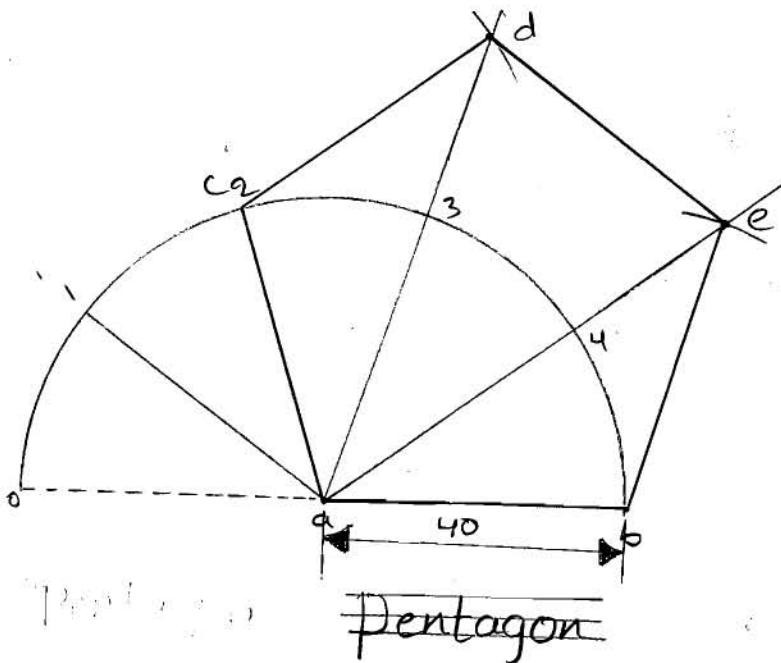
Pentagon

Construct a Hexagon of side 40mm

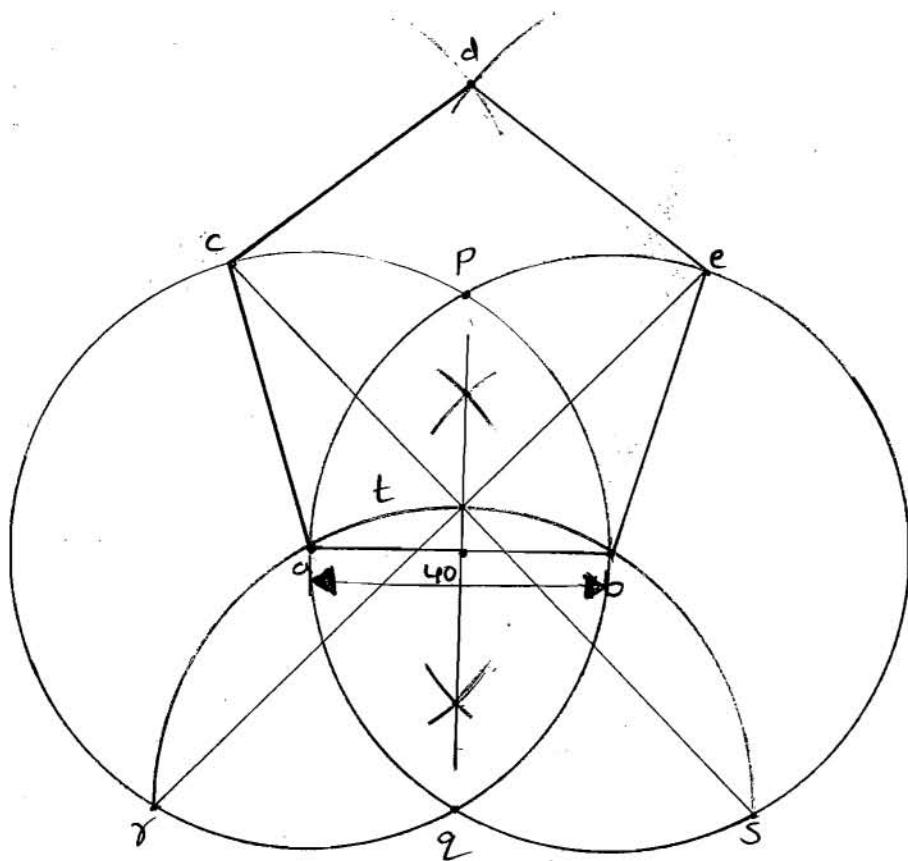


Hexagon

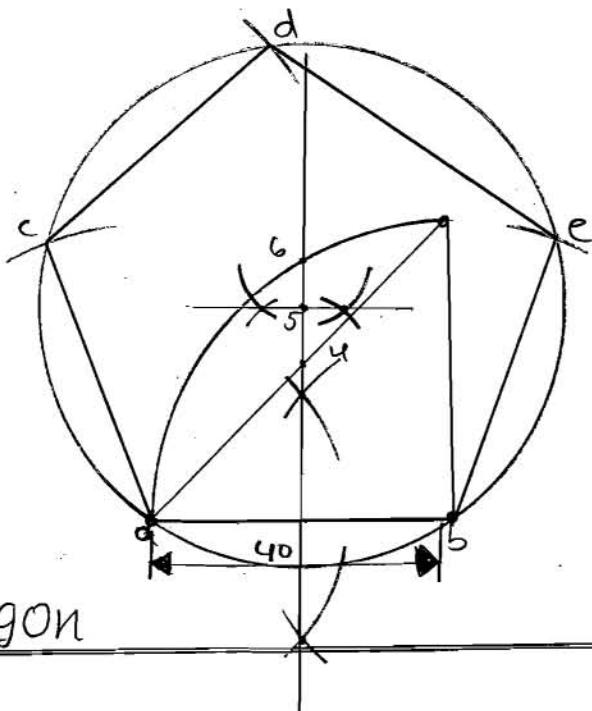
Draw a regular Pentagon and regular Hexagon having 40mm side length

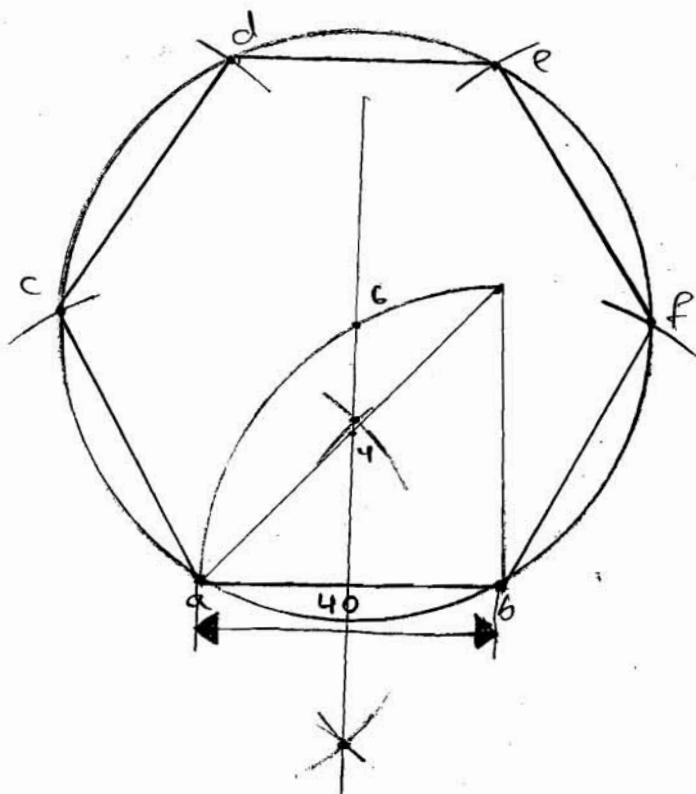


Q:- Draw a regular Pentagon of side 40 mm by using arcs of circle method

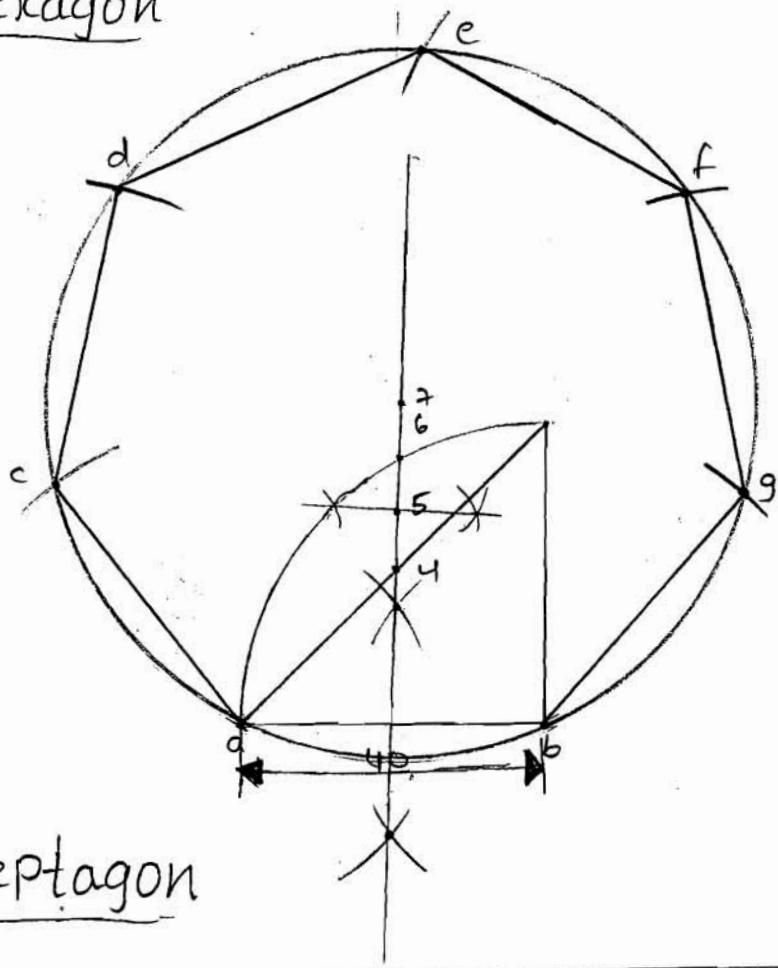


⇒ Special method of construction of any polygon.

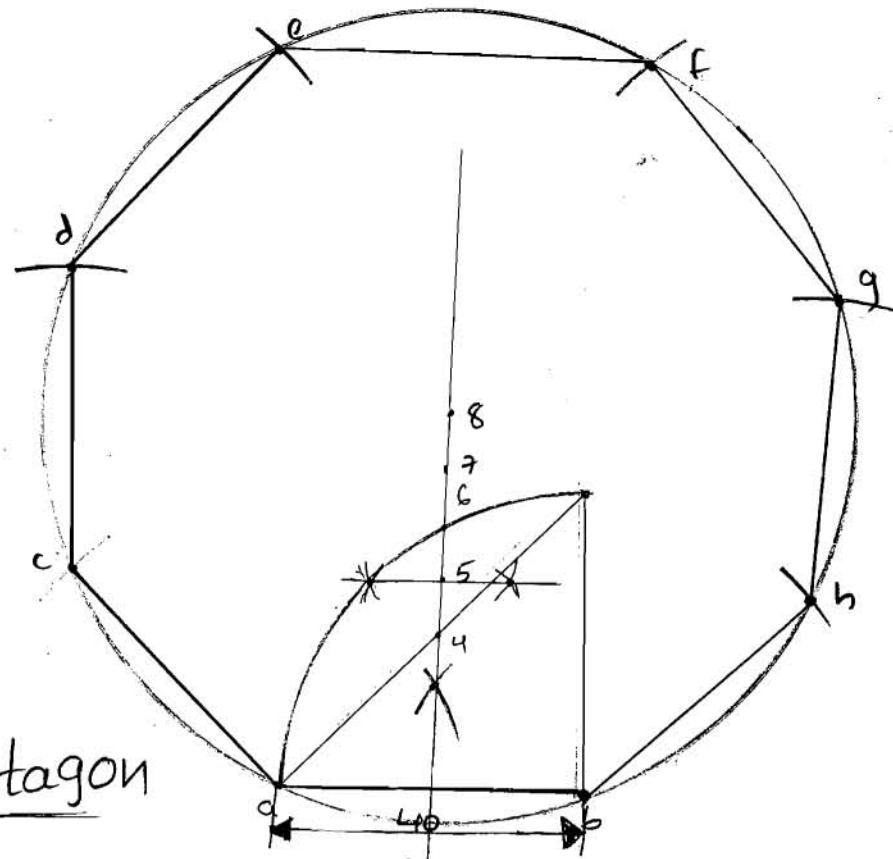




Hexagon

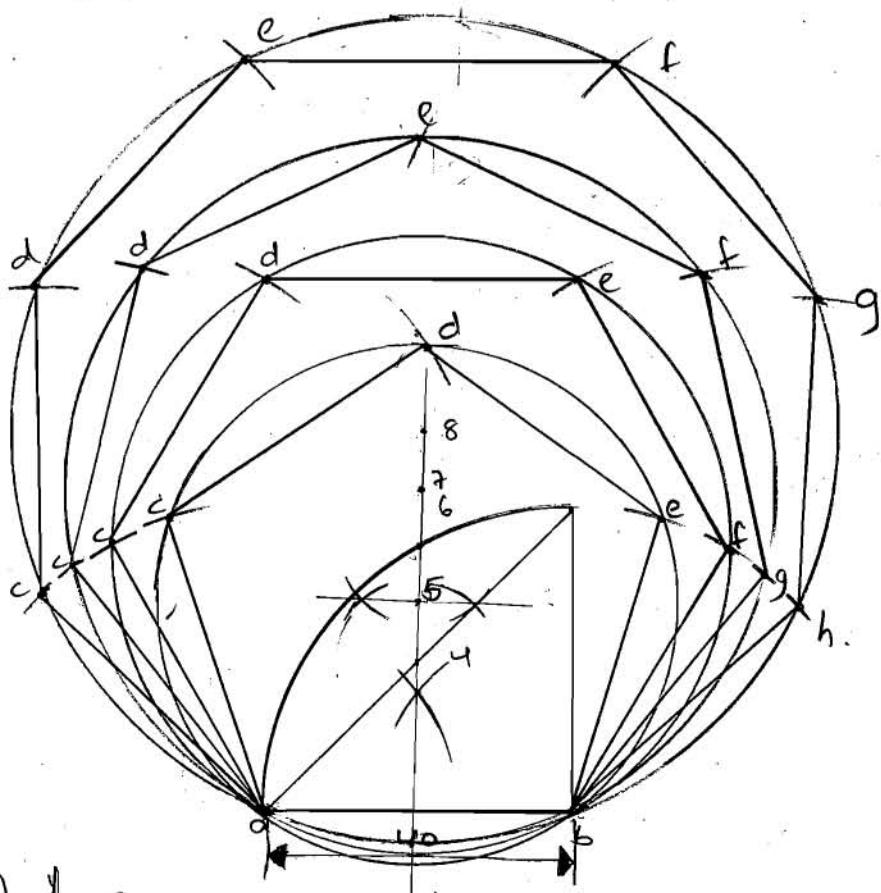


Septagon



Octagon

Octagon

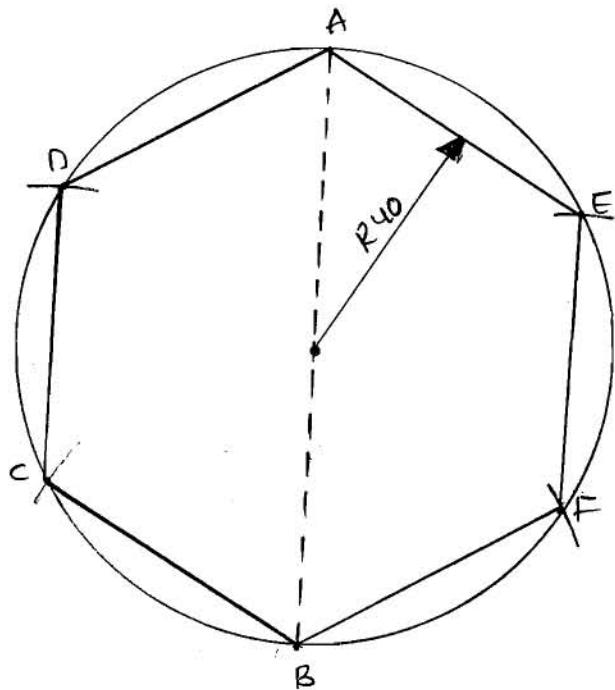


Polygon

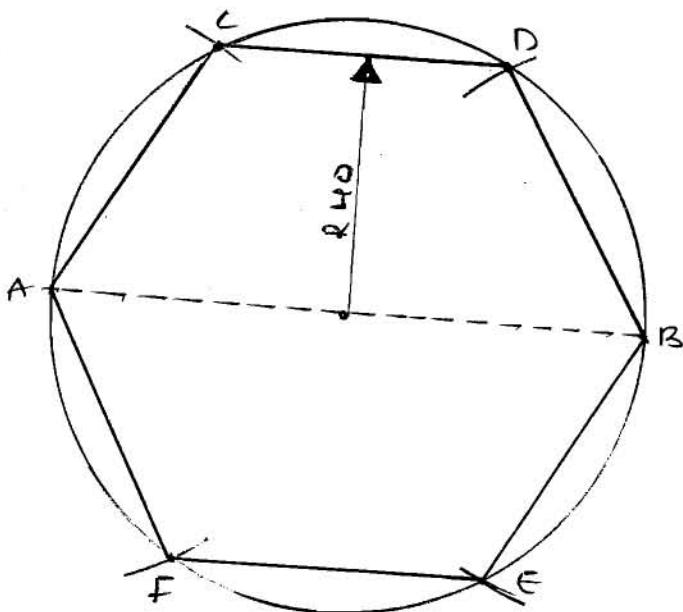
Construct a Hexagon of side 40mm

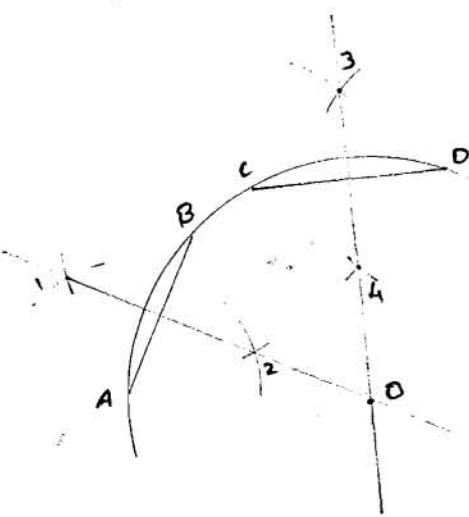
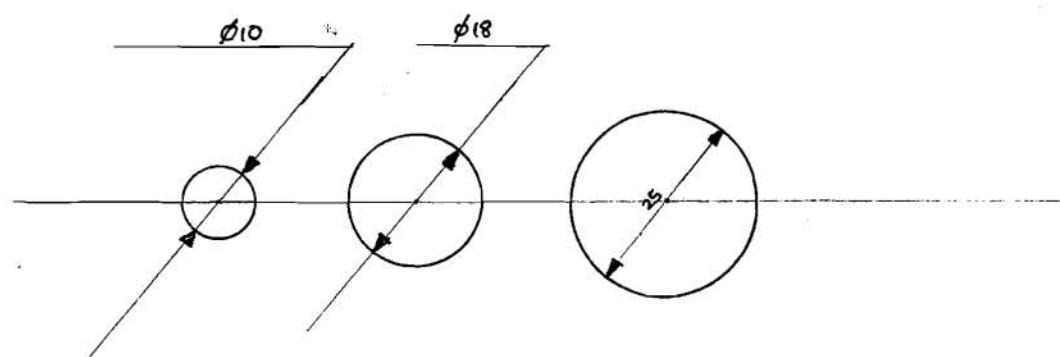
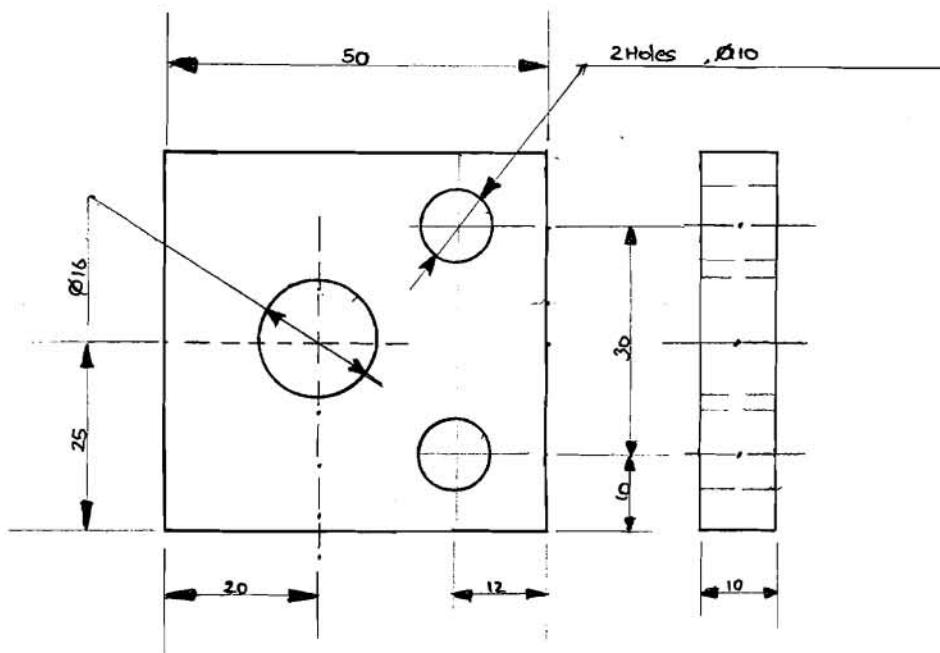
- a) Side is vertical.
- b) side is horizontal.

a)



b)

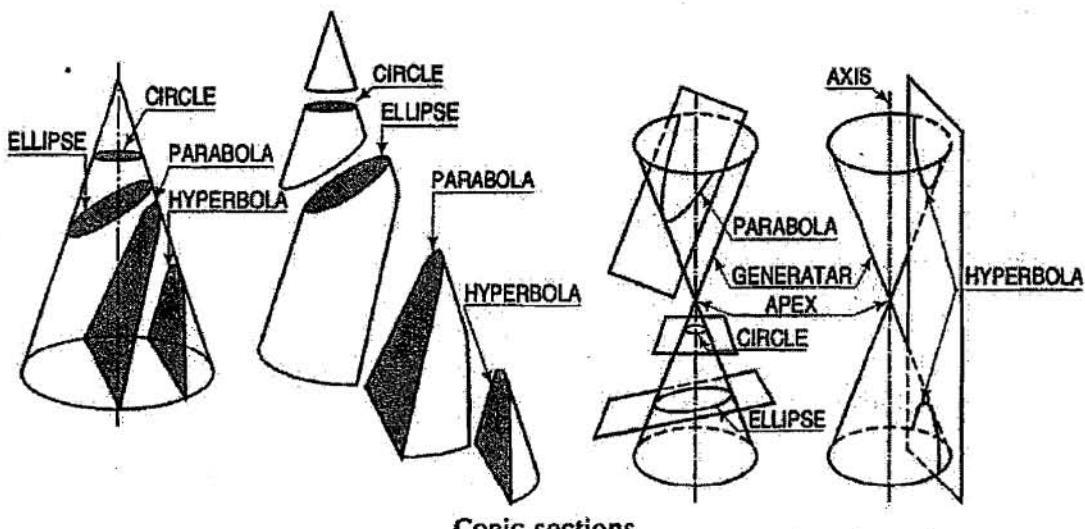




# Unit-I

## Conic Sections:

The section obtained by the intersection of a right circular cone by a plane in different positions relative to the axis of the cone are called conics.



- (i) When the section plane is inclined to the axis and cuts all the generators on one side of the apex, the section is an ellipse
- (ii) When the section plane is inclined to the axis and is parallel to one of the generators, the section is a parabola
- (iii) A hyperbola is a plane curve having two separate parts or branches, formed when two cones that point towards one another are intersected by a plane that is parallel to the axes of the cones.

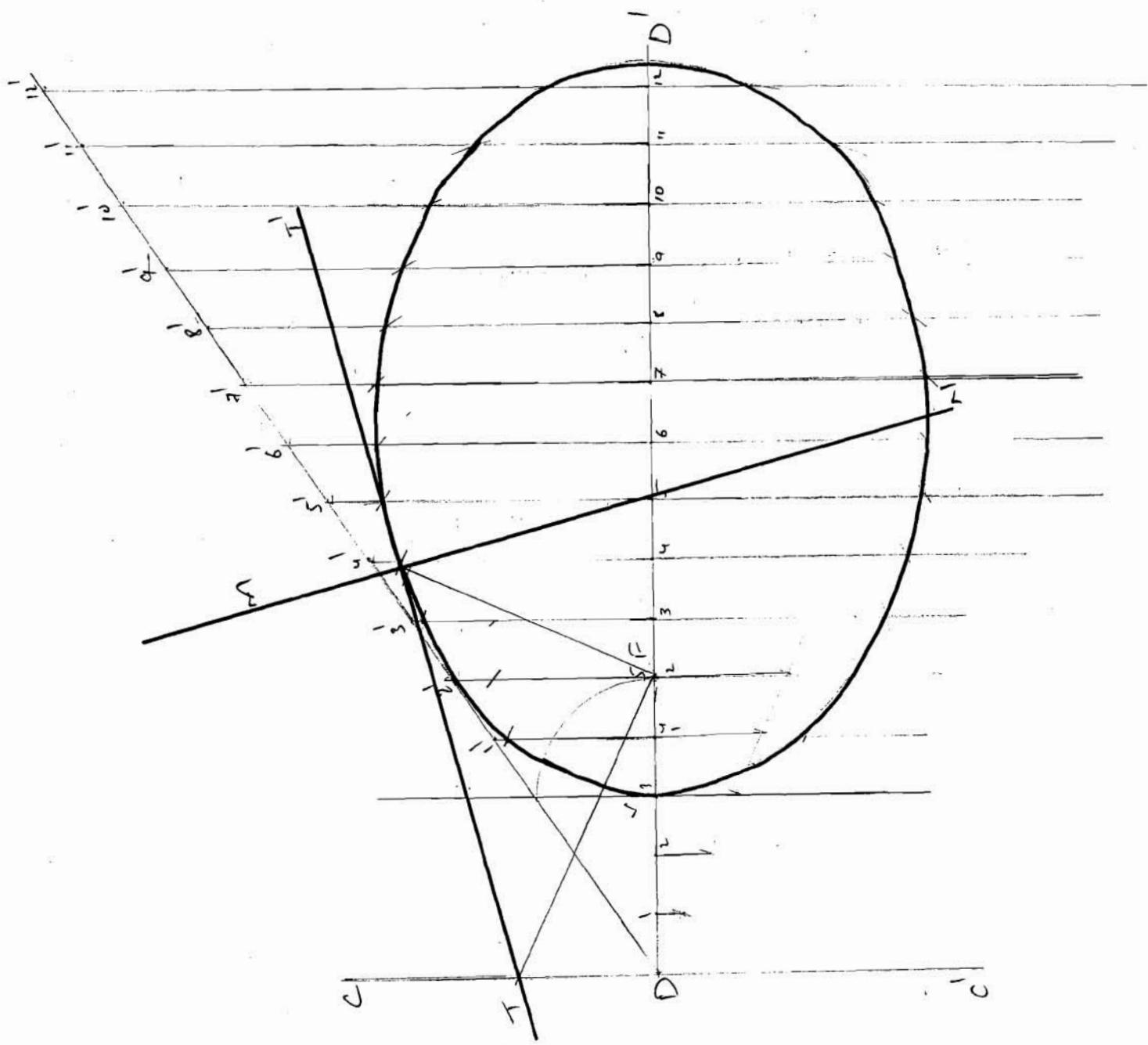
The conic may be defined as the locus of a point moving in a plane in such a way that the ratio of its distances from a fixed point and a fixed straight line is always constant. The fixed point is called the focus and the fixed line, the directrix.

The ratio  $\frac{\text{distance of the point from the focus}}{\text{distance of the point from the directrix}}$  is called eccentricity and is denoted by  $e$ . It is always less than 1 for ellipse, equal to 1 for parabola and greater than 1 for hyperbola i.e.

- (i) ellipse :  $e < 1$
- (ii) parabola :  $e = 1$
- (iii) hyperbola :  $e > 1$ .

The line passing through the focus and perpendicular to the directrix is called the axis. The point at which the conic cuts its axis is called the vertex.

Draw a ellipse when the distance of its focus from its directrix is 50mm and eccentricity is  $\frac{2}{3}$  also, draw a tangent and a normal to the ellipse at point 70mm away from directrix.

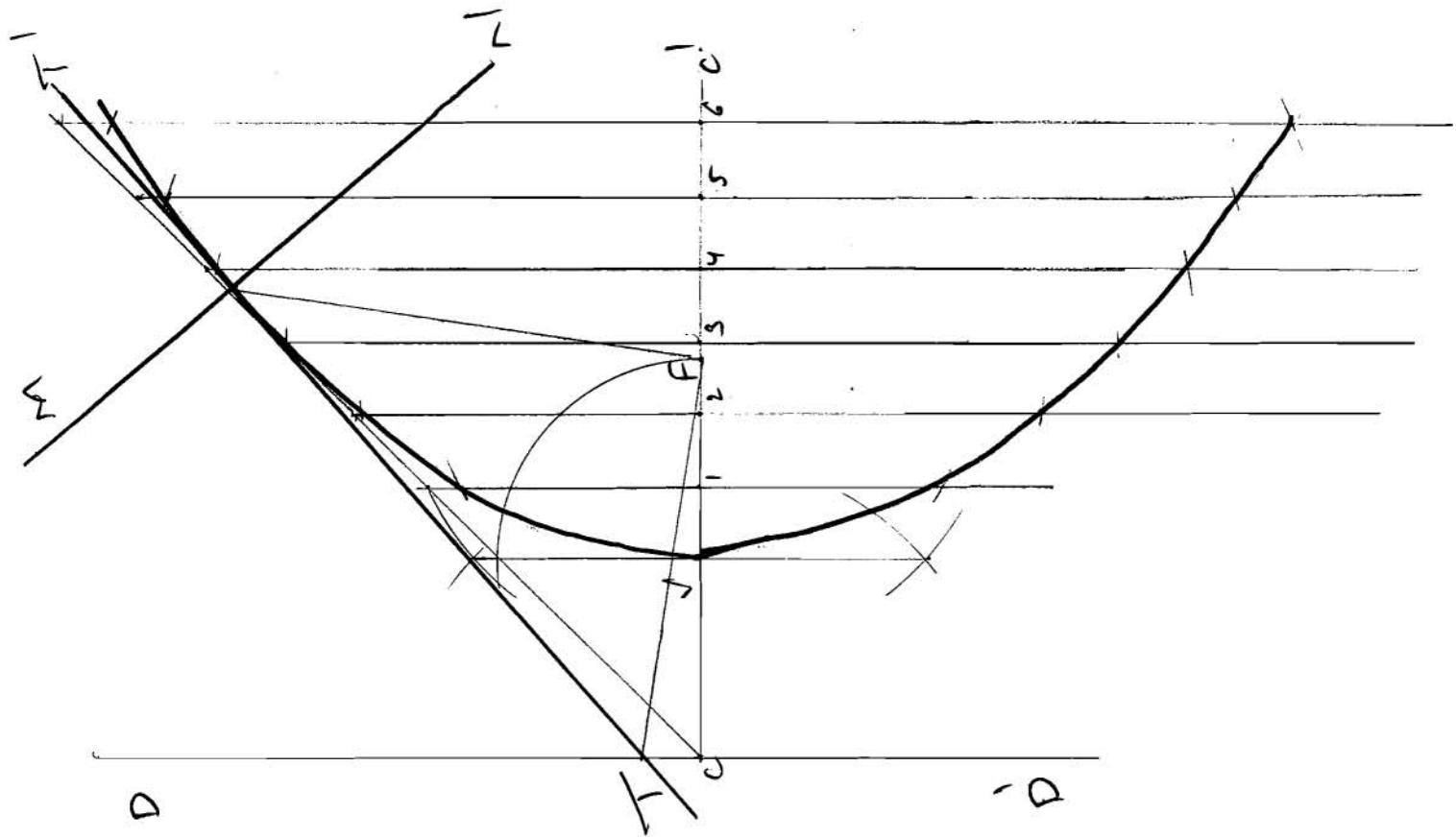


1. Draw focus F on OX's AB such that AF = 50mm.
2. Divide AF in 5 equal parts. mark vertex V<sub>1</sub> on 3<sup>rd</sup> division from A. and draw vertical line V<sub>1</sub>E equal to V<sub>1</sub>F . Join A to E and produce it to some distance.
3. Mark a point I anywhere on line AB (less than 1cm). Draw a perpendicular line through I and meet AE produced at point I'.
4. with centre F and radius I-I', draw arcs to intersect the perpendicular line I-I' at points P<sub>1</sub> and P<sub>1</sub>'. These are the loci points of ellipse
5. similarly ,mark other point .These gives some more loci points of ellipse like ;P<sub>2</sub> and P<sub>2</sub>',P<sub>3</sub> and P<sub>3</sub>',P<sub>4</sub> and P<sub>4</sub>',etc.
6. Join all the loci points of ellipse and obtain the required ellipse. and the required ellipse

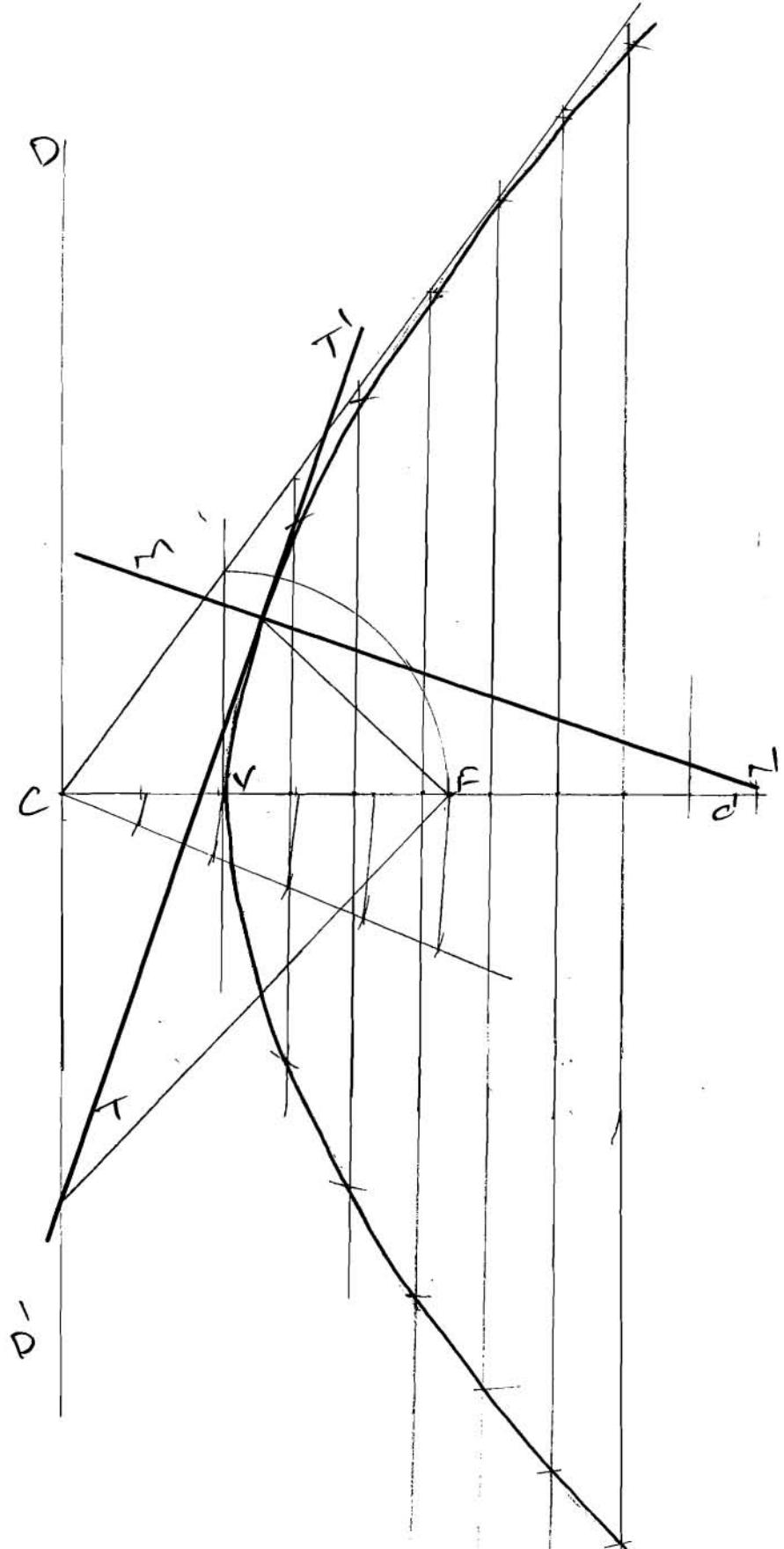
Tangent and normal to an ellipse.

1. Mark a point P on ellipse at 70mm from directrix and join PF.
2. Draw a line PT perpendicular to line PF to meet directrix PP' at point T.
3. Join TP and produce to some point T'. The line TT' is required tangent.
4. Through point P, draw a line NN' perpendicular to TT'. The line NN' is the required normal.

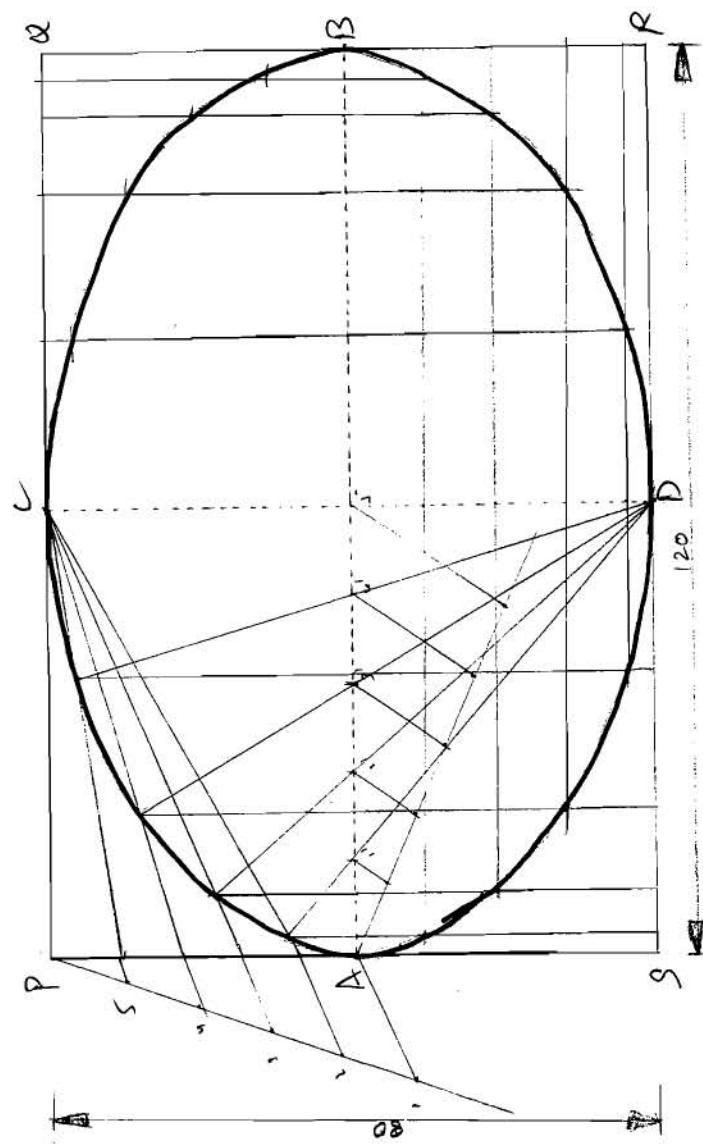
Draw parabola when the distance between its focus and directrix is 55 mm also a tangent and a normal at a point 65mm from directrix.



1) Draw a hyperbola when the distance of its focus from its directrix is 58mm and eccentricity is  $3/2$  also draw a tangent and a normal to the hyperbola at a point 30mm from the directrix.

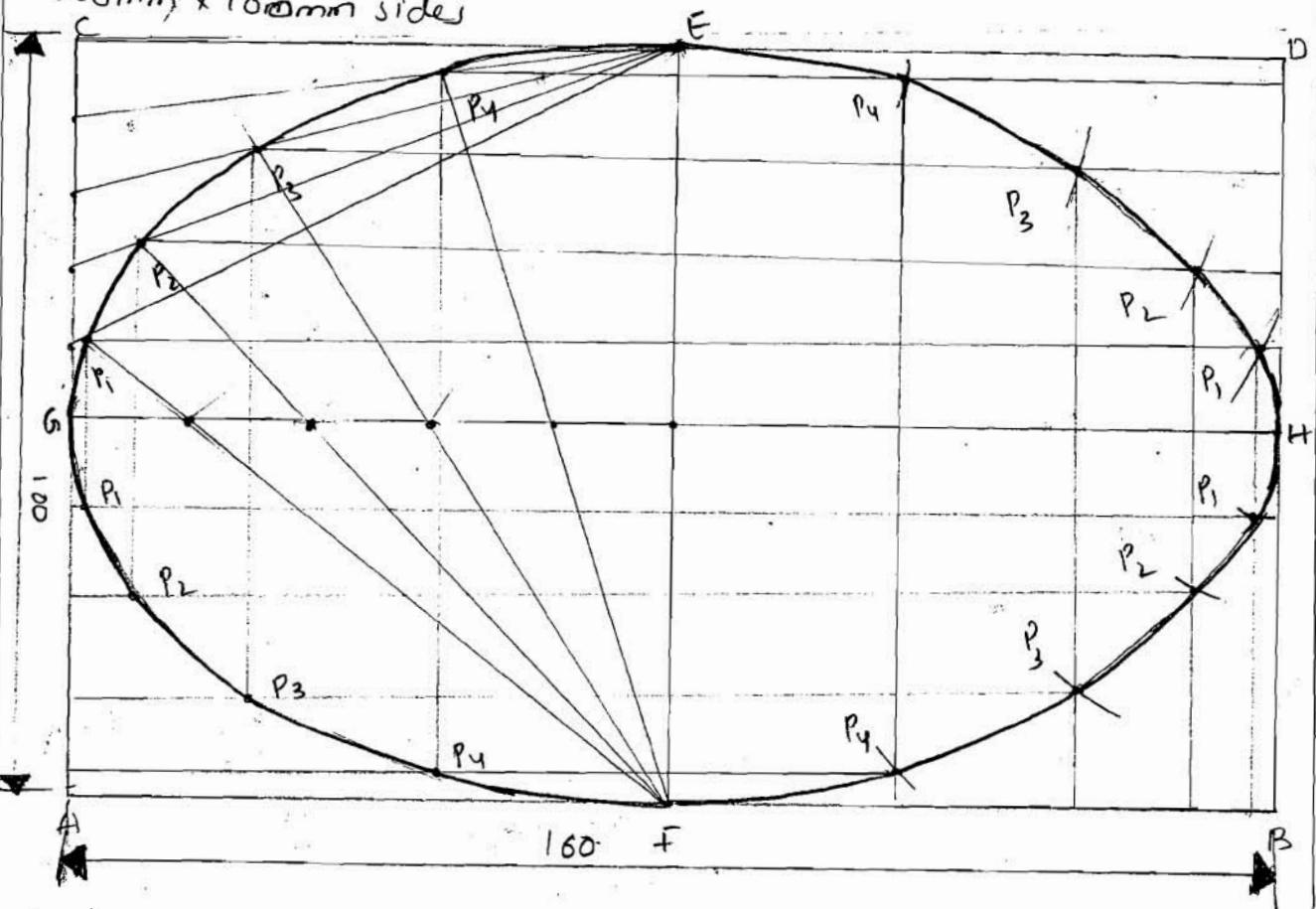


Draw an ellipse having 120mm long major axis and 80mm minor axis.

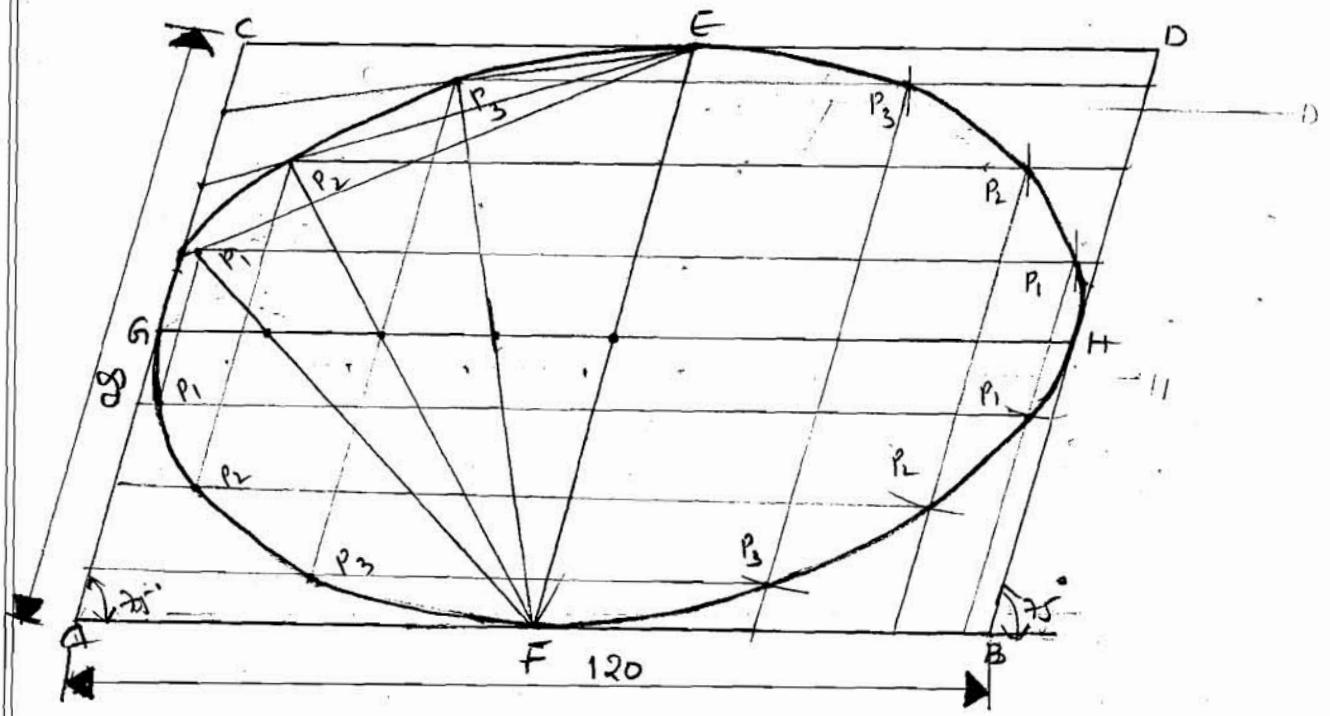


Q:- Inscribe the largest possible ellipse in a rectangle with

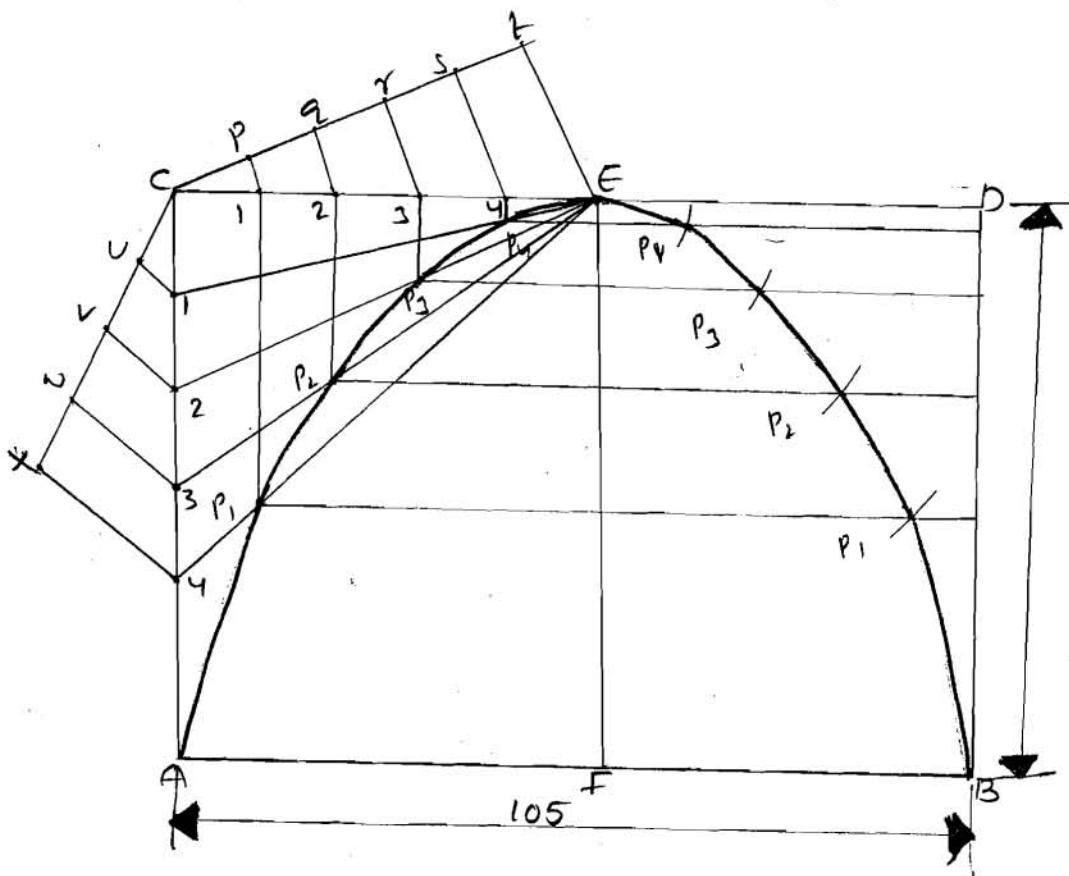
160mm x 100mm sides



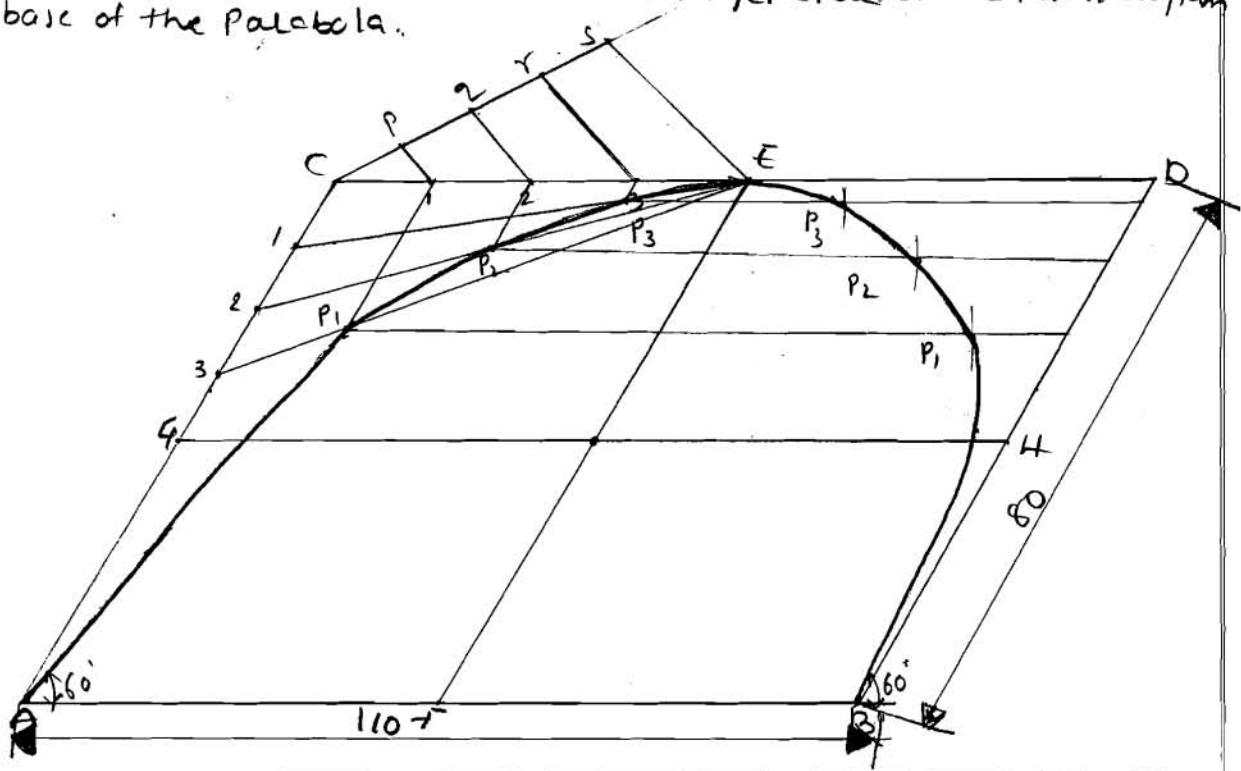
Q:- The sides of a Parallelogram are 120mm & 80mm. The included angle between them is  $75^\circ$ . Inscribe an ellipse in the given figure.



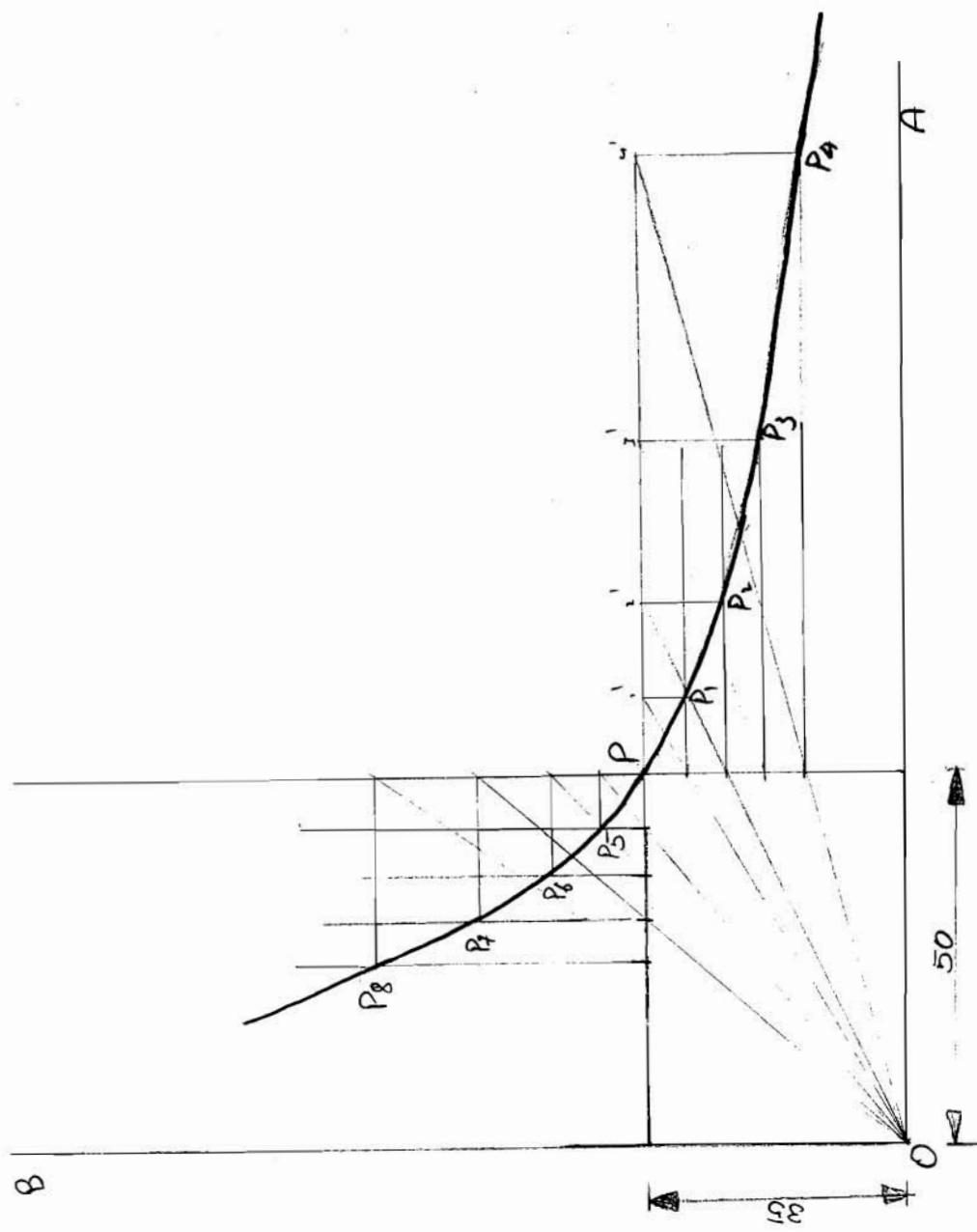
Q: Draw a Parabola given the width and height of its enclosing rectangle as 105mm x 75mm respectively.



Q: Inscribe a Parabola in a parallelogram of 110x80mm sides, The included angle being  $60^\circ$ . Consider the longer side of the parallelogram as base of the Parabola.

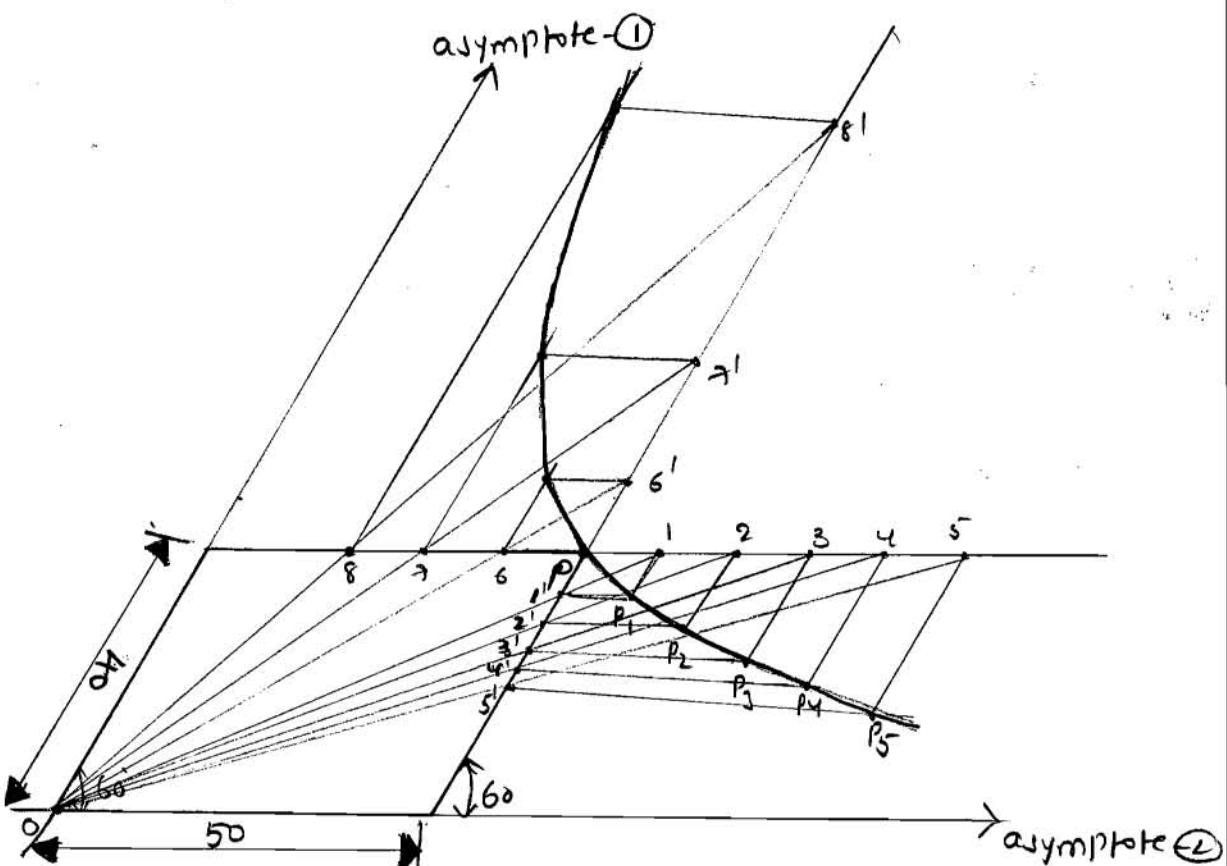


A point P of the hyperbola is situated at a distance of 35mm and 50mm from the pair of asymptotes. The asymptotes are perpendicular to each other. Draw hyperbola using orthogonal asymptotes method.



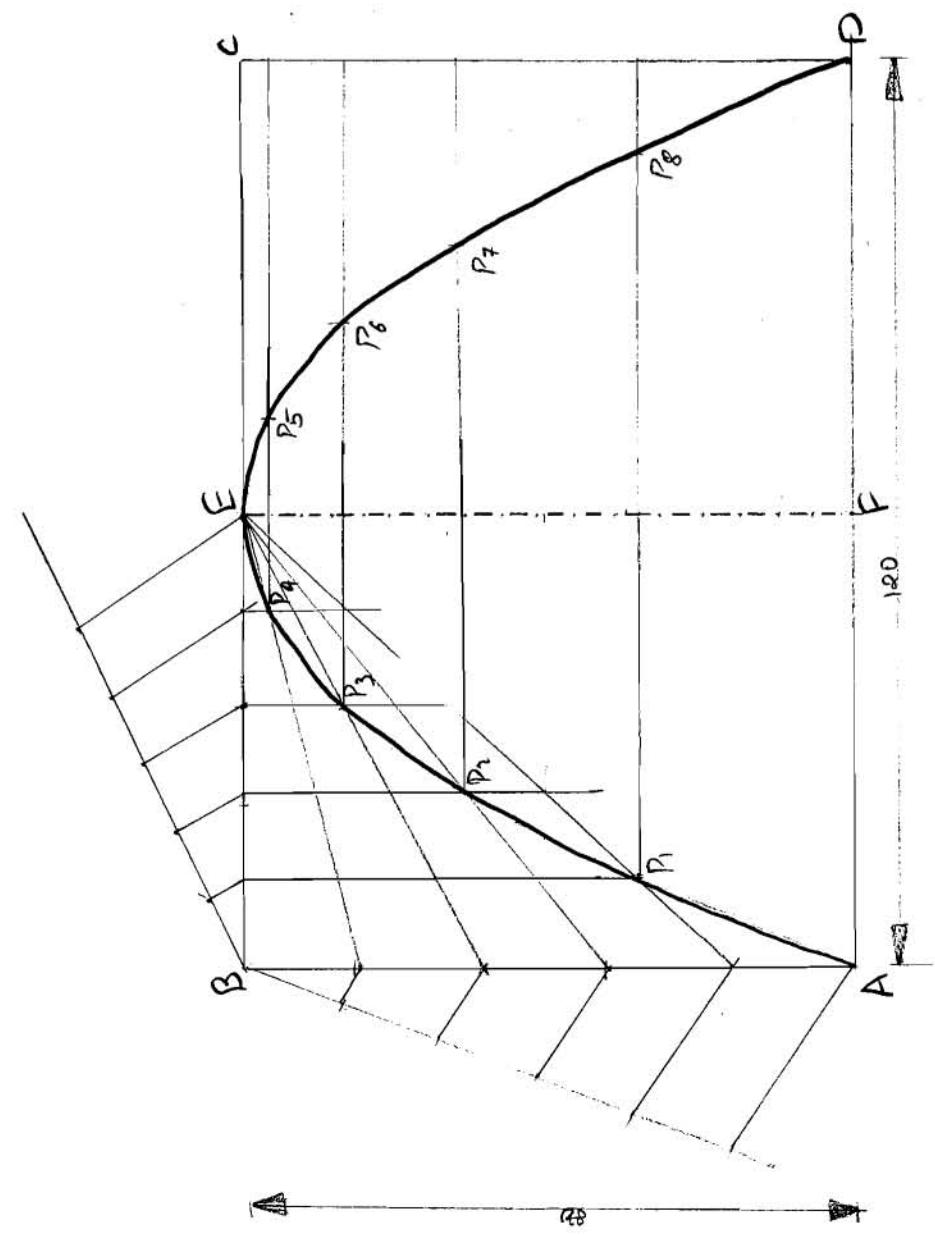
1. Draw asymptotes OA and OB perpendicular to each other.
2. Mark P such that  $OA = 35 \text{ mm}$  and  $OB = 50 \text{ mm}$ .
3. Draw CD, EF parallel to OA, OB respectively pass through P.
4. Mark points 1, 2, 3, etc., on PD at equal distance.
5. Join O<sub>1</sub>, O<sub>2</sub>, O<sub>3</sub> etc., to intersect the line CP at 1', 2', 3' etc.
6. Draw lines from points 1, 2, 3, etc., parallel to OB to intersect lines drawn from points 1', 2', 3' parallel to OA at points P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub> etc.
7. Mark point 5, 6, 7 etc., on CP at equal distance.
8. Repeat step 5, 6 with 5, 6, 7 etc points. you will get  
q. P<sub>5</sub>, P<sub>6</sub>, P<sub>7</sub> etc.
9. Draw a smooth curve passing through P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>5</sub>, P<sub>6</sub>, P<sub>7</sub> etc., to get required rectangular hyperbola.

Q:- Draw a hyperbola when its asymptotes are inclined at  $60^\circ$  to each other and it passes through a point 'P'. At a distance of 40mm and 50mm from the Asymptotes.



Hyperbola

Draw a parabola of base 120mm and axis 80mm by rectangular method.

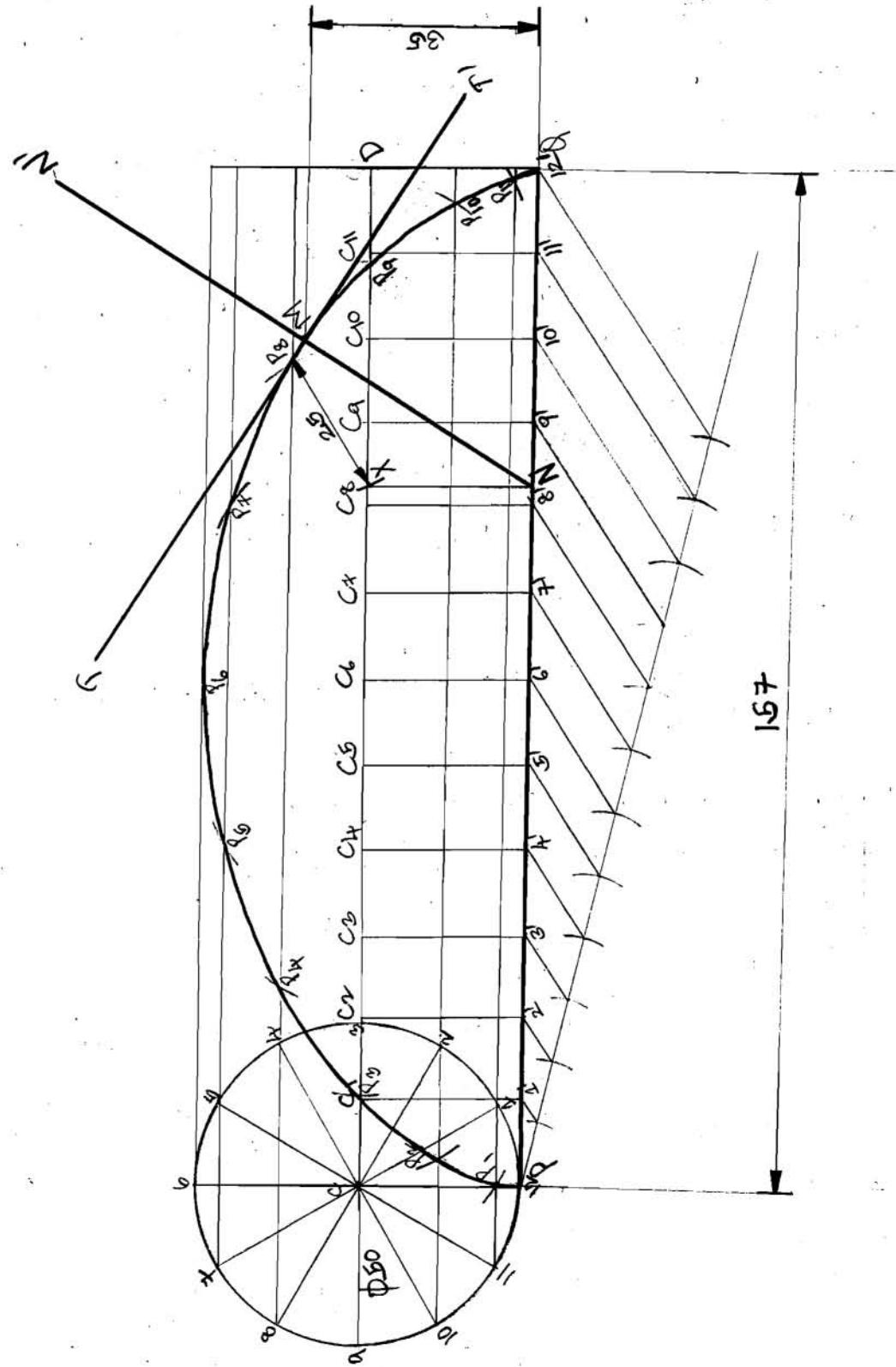


1. Draw a rectangle ABCD taking  $A = 120\text{ mm}$  and  $AD = 80\text{ mm}$
2. Mark E and F as the midpoints of AB and CD respectively.  
Join EF to represent the axis.
3. Divide FD and DA, into equal number of parts, say 4.  
mark division of side DA as 1,2,3 and divisions of FD as 1',2',3'. Now join F with points 1,2,3.
4. Through 1',2',3' draw lines parallel to axis EF to meet  $F_1, F_2, F_3$  at  $P_1, P_2, P_3$  respectively.
5. As the curve is symmetric about axis, obtain points  $P'_1, P'_2, P'_3$  of the curve by drawing horizontal lines through points  $P_1, P_2, P_3$  and making them equal on both sides of axis EF.
6. Draw a smooth curve passing through A,  $P_3, P_2, P_1, F, P'_1, P'_2, P'_3$  and B to get the required parabola.

## **Cycloids:**

These curves are generated by a fixed point on the circumference of a circle, which rolls without slipping along a fixed straight line or a circle. The rolling circle is called generating circle and the fixed straight line or circle is termed directing line or directing circle. Cycloidal curves are used in tooth profile of gears of a dial gauge.

Draw a cycloid of a circle of diameter sum for one revolution also draw a tangent and a normal to the curve at a point 35mm above base line.

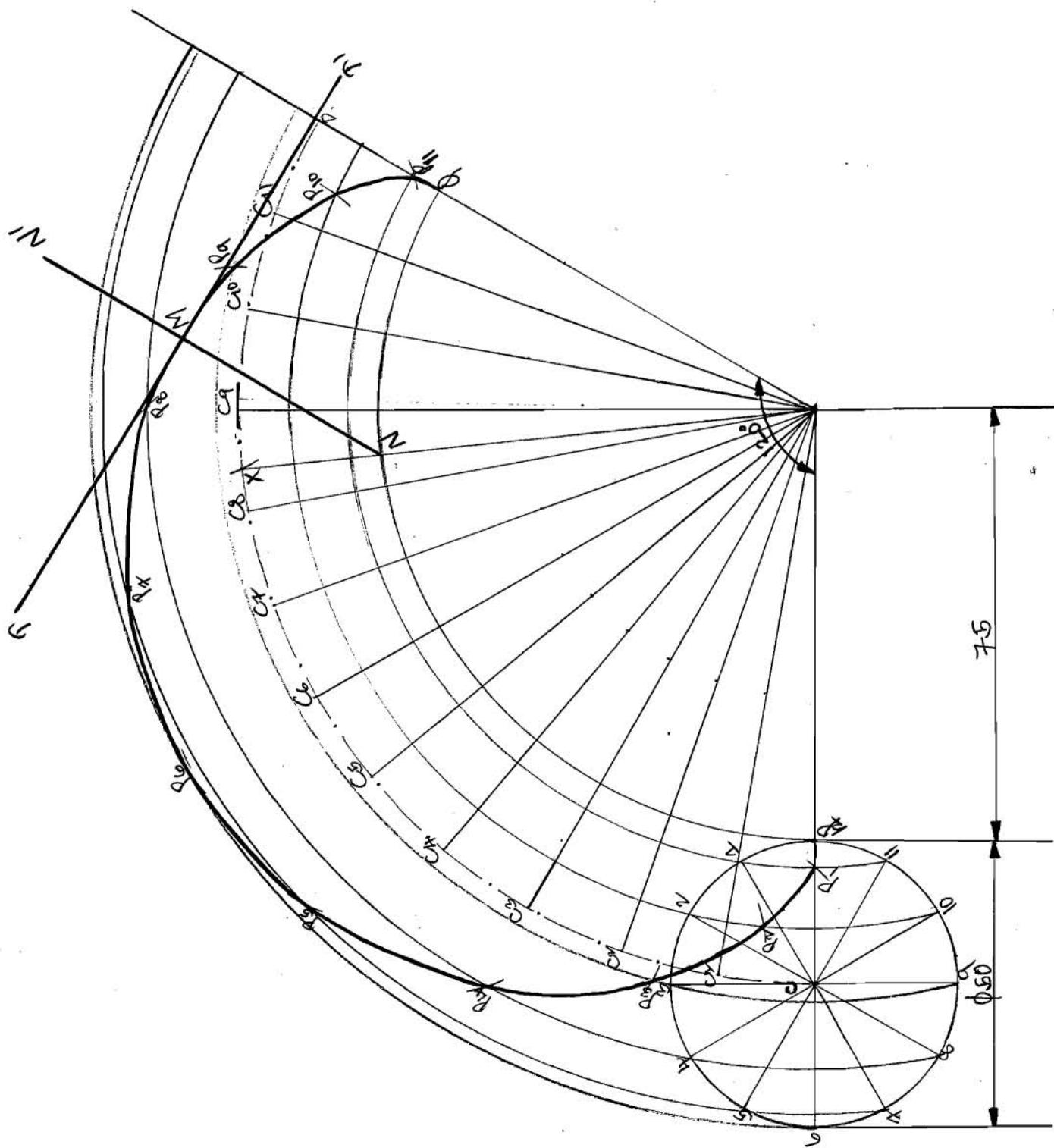


1. Draw a circle of diameter 50mm with centre c.
2. Draw the directing line PQ =  $\pi D = 157$  mm long, horizontal and tangential to the circle.
3. Divide the circle into 12 equal parts and mark the divisions as 1, 2, 3 etc. Draw lines through points 1, 2, 3, etc., parallel to PQ.
4. Divide PQ into 12 equal parts and mark the divisions as 1', 2', 3', etc.
5. Erect vertical lines from points 1', 2', 3' etc. to meet the centre line CO at C<sub>1</sub>, C<sub>2</sub>, C<sub>3</sub>, etc. When the circle rolls through 1/12<sup>th</sup> rotation, point 1 of the circle will coincide with 1' centre C<sub>1</sub> will move to C<sub>1</sub>. The point P will move to new position P<sub>1</sub> lying on the horizontal line through point 1 at a distance of 25 mm from C<sub>1</sub>.
6. Draw an arc with centre C<sub>1</sub> and radius 25mm to intersect the horizontal line through point 1 at point P<sub>1</sub>.
7. Similarly, draw arc with centre C<sub>2</sub>, C<sub>3</sub>, C<sub>4</sub> etc.
8. Draw a smooth curve passing through P<sub>1</sub>, P<sub>2</sub>, P<sub>3</sub>, P<sub>4</sub> etc. to get the required cycloid.

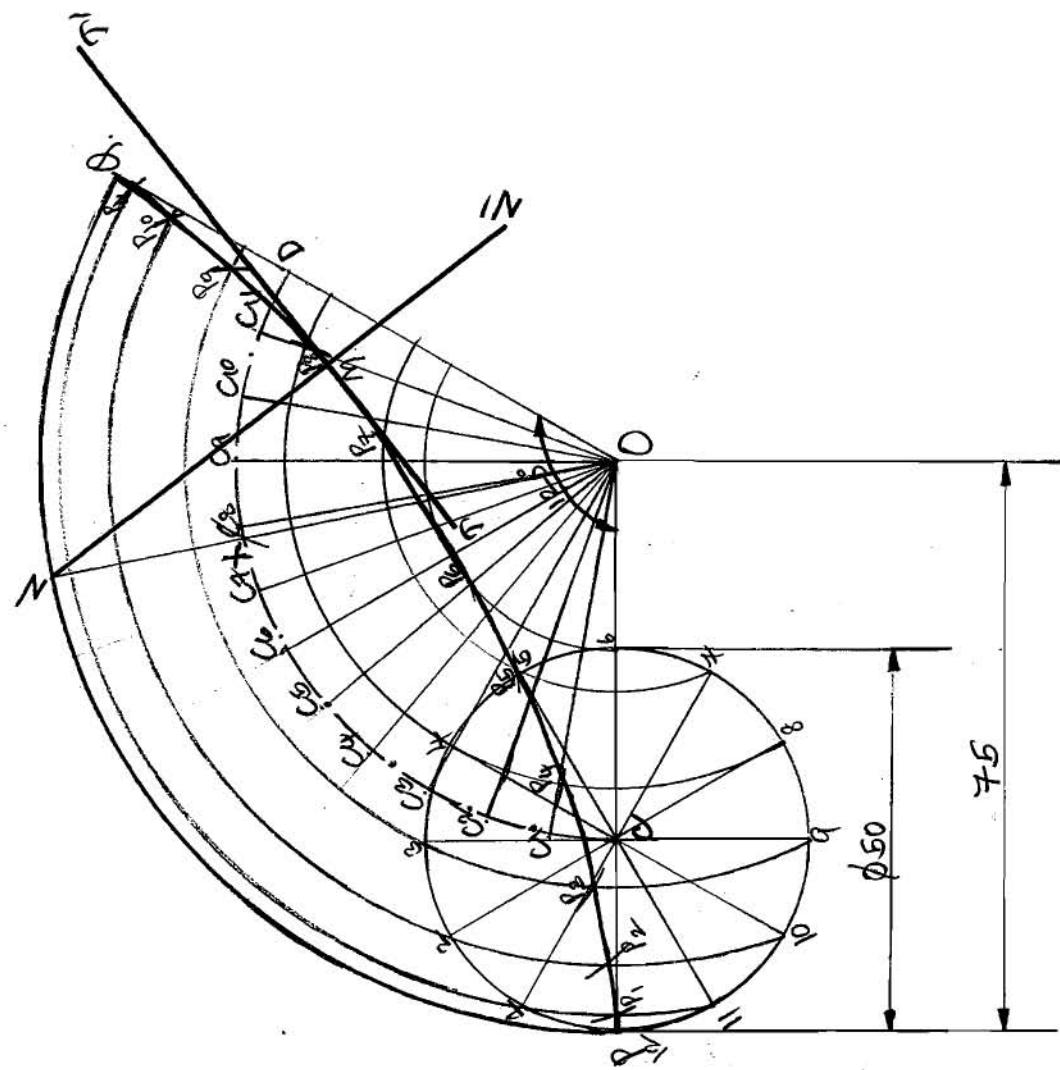
Tangent and normal to the cycloid:

1. Mark a point M on the cycloid 35mm above PQ.
2. Draw an arc with centre M and radius 25mm, to intersect the centre line at X.
3. Draw a vertical line from X to meet PQ at N.
4. Join NM and produce to N'. This line NN' is the required normal.
5. Through point M draw a line TT' perpendicular to NN'. This line TT' is the required tangent.

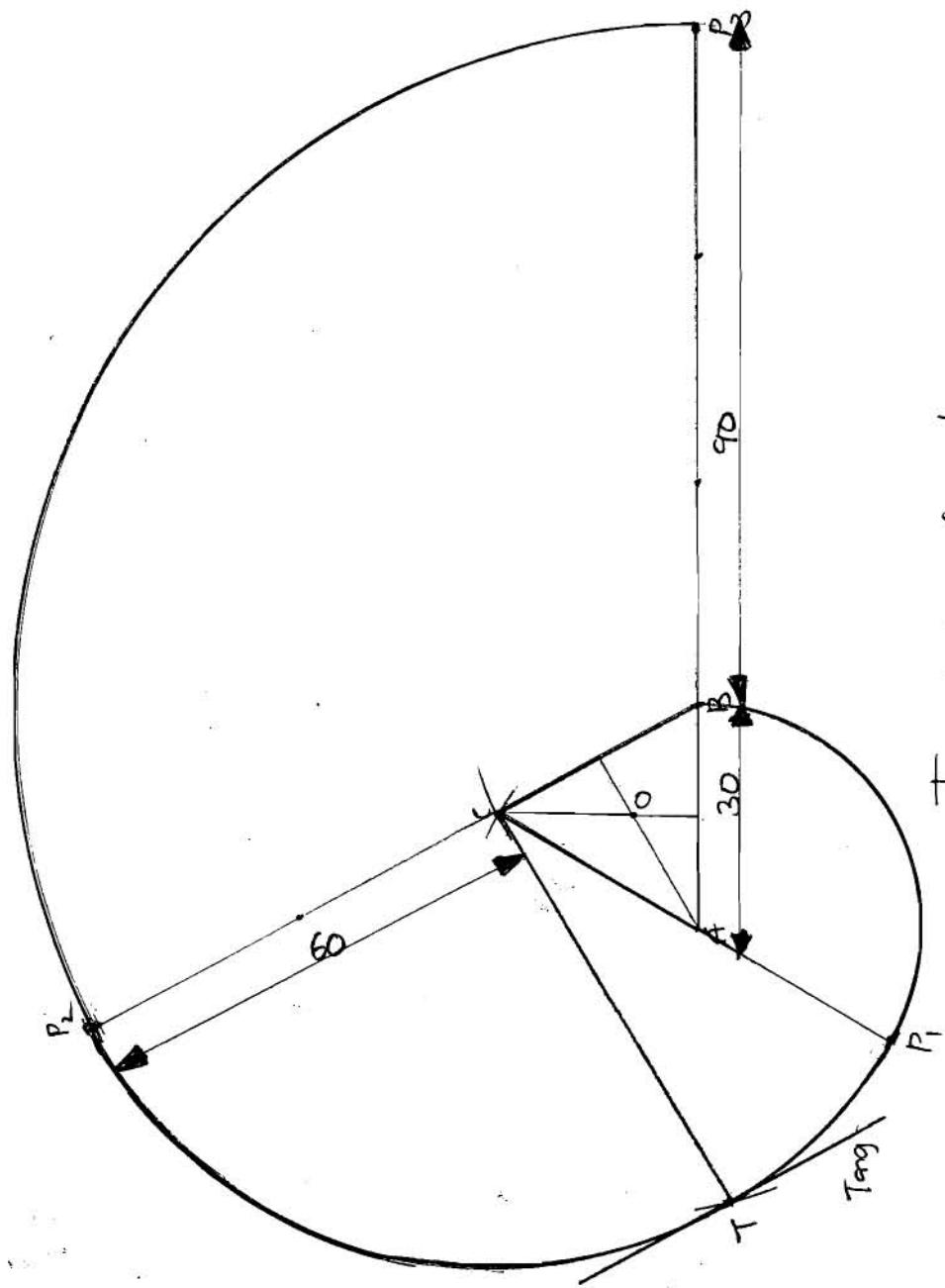
Draw an epicycloid of a circle of diameter 50mm which rolls outside a circle of diameter 150mm for one revolution also draw a tangent and normal to epicycloid at a point 110mm from the centre of directrix circle.



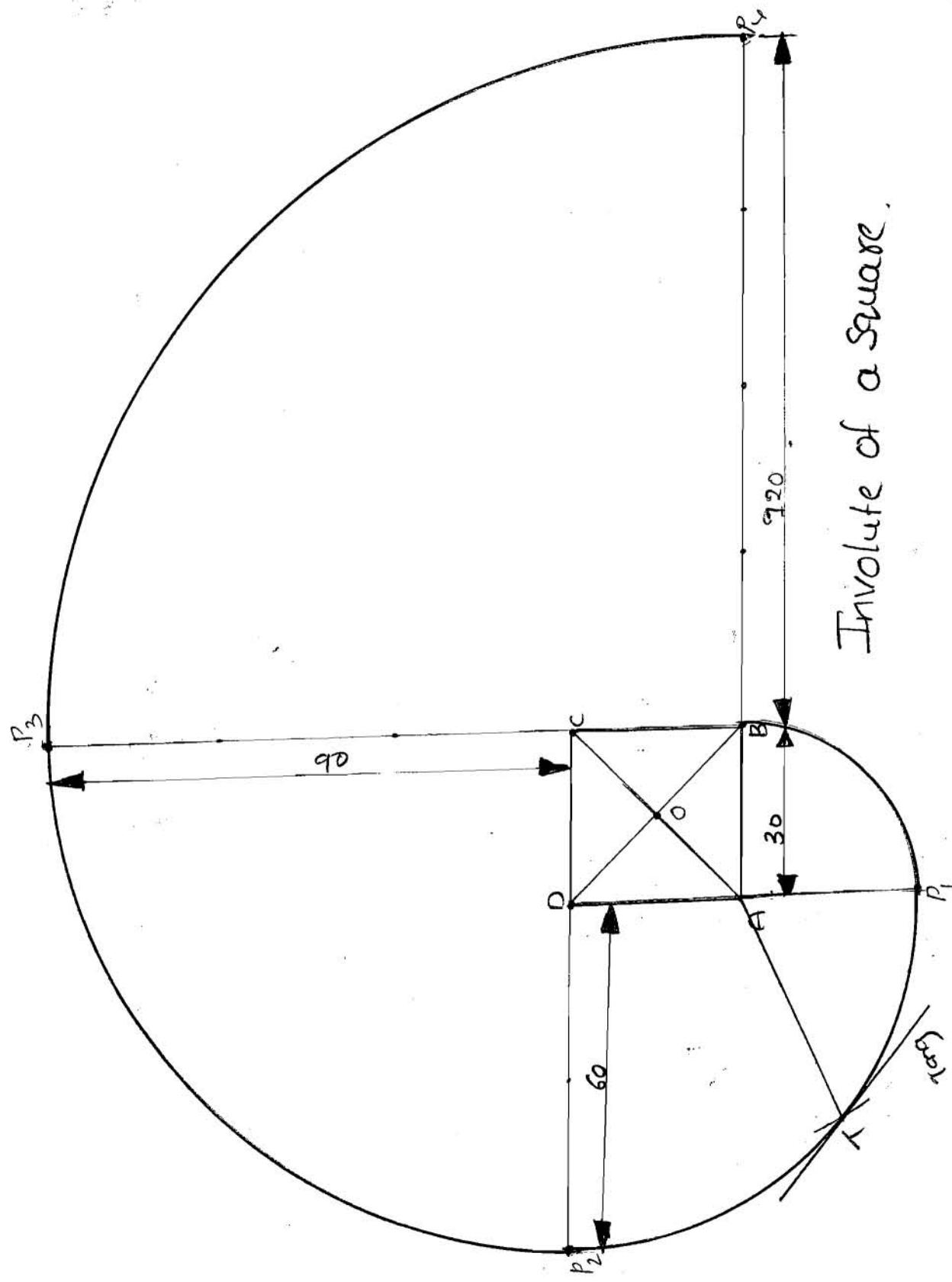
Draw a hypocycloid of a circle of diameter 50mm which rolls inside a circle of diameter 100mm for one revolution also draw a tangent and normal to hypocycloid at a point 40mm from the centre of the directing circle.



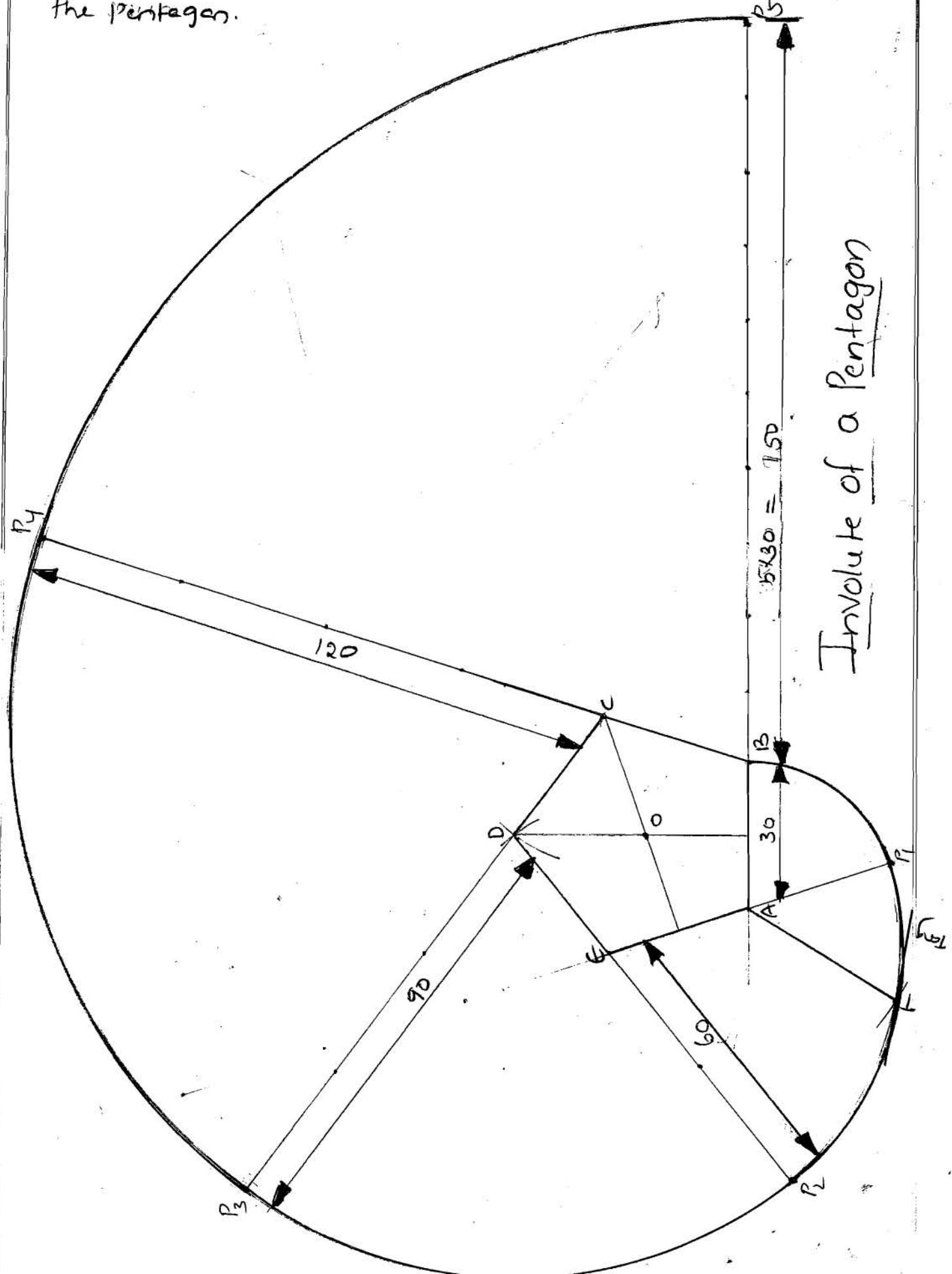
Draw an Involute for a triangular plane of side length 30mm and also draw tangent and Normal at a Point 55mm from the Center of the triangle.



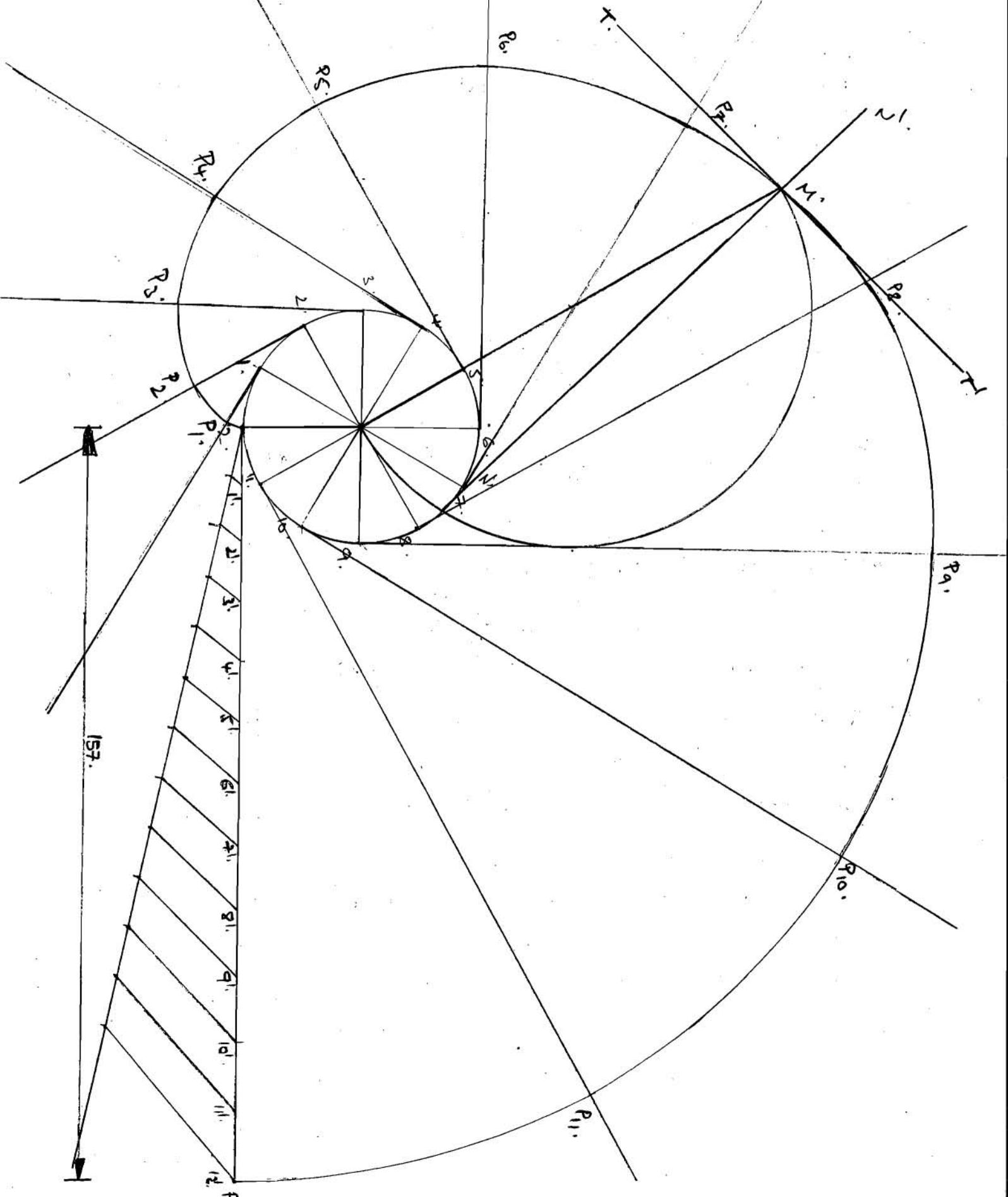
Construct an Involute curve for a square of side 30 mm and also draw tangent and Normal at a distance of 60 mm from the center of the square.



- Q: Draw an Involute curve for Pentagon of side 30 mm and also draw tangent and Normal at a distance of 60 mm from the centre of the pentagon.



~~Draw an involute of circle of diameter 60mm also draw normal and tangent at a point 100mm from the centre of circle.~~



1. Draw a circle of diameter 50mm and divide it into 12 equal parts. mark them as 1, 2, 3, etc.
2. Draw line PQ =  $\pi D = 157\text{mm}$ . divide it into 12 equal parts. mark them as 1', 2', 3', etc.
3. Draw tangents to circle at 1, 2, 3 etc.
4. Draw an arc with centre 1 and radius  $P_1'$  to intersect the tangent line through point 1' at  $P_1$ .
5. Draw an arc with centre 2 and radius  $P_2'$  to intersect the tangent line through point 2' at  $P_2$ .
6. Similarly, draw arc with centres 3, 4, 5 etc and radii  $P_3', P_4', P_5'$  etc., respectively to intersect the tangent line through points 3, 4, 5 etc., at points  $P_3, P_4, P_5$  etc., respectively.
7. Draw a smooth curve to pass through  $P_1, P_2, P_3$  etc., and obtain required involute.

Tangent and normal to involute:

1. Mark a point M on involute at radial distance 100m from O.
2. Join OM and mark O<sub>1</sub> as its mid point.
3. Draw a semi-circle in clockwise direction with O<sub>1</sub> as centre and diameter OM to intersect the base circle at N.
4. Join MN and produce it to N'. The line NN' is the required normal.
5. Through point M, draw a line  $TT'$  perpendicular to NN'. The line  $TT'$  is required tangent.

## Scales:

Drawings of small objects can be prepared of the same size as the objects they represent. A 150 mm long pencil may be shown by a drawing of 150 mm length. Drawings drawn of the same size as the objects, are called full-size drawings. The ordinary full-size scales are used for such drawings.

A scale is defined as the ratio of the linear dimensions of element of the object as represented in a drawing to the actual dimensions of the same element of the object itself.

**Representative fraction:** The ratio of the length of the object represented on drawing to the actual length of the object represented is called the Representative Fraction (i.e. R.F.).

$$R.F. = \frac{\text{Length of the drawing}}{\text{Actual length of object}}$$

### Types of scales

The scales used in practice are classified as under:

- (1) Plain scales
- (2) Diagonal scales
- (3) Vernier scales

# Plain Scale

1. A 1cm length of the drawing represents 5m length of the object. Then find R.F value.

Sol:-

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$$

$$R.F = \frac{1\text{cm}}{5\text{m}}$$

$$= \frac{1\text{cm}}{500\text{cm}}$$

$$\therefore R.F = \frac{1}{500} = 1:500$$

2. A 5cm long line represents 3 km length of a road find the R.F value.

Sol:-

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$$

$$= \frac{5\text{cm}}{3\text{km}}$$

$$R.F = \frac{5\text{cm}}{3 \times 10^5 \text{cm}}$$

$$\therefore R.F = \frac{5}{3 \times 10^5}$$

$$\begin{aligned} \because 1\text{km} &= 10\text{hm} \\ &= 10 \times 10\text{dm} \\ &= 10 \times 10 \times 10\text{dm} \\ &= 10 \times 10 \times 10 \times 10 \text{cm} \\ \therefore 1\text{km} &= 10^5 \text{cm}. \end{aligned}$$

3. Find the R.F value of a 2cm = 1m

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$$

$$= \frac{2\text{cm}}{1\text{m}}$$

$$R.F = \frac{2\text{cm}}{1 \times 100 \text{cm}}$$

$$\therefore R.F = \frac{1}{100} = 1:100$$

4. In a map of India, a distance of 36 km between two localities is shown by a line of 45 cm long calculate its R.F.

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual Length of the object}}$$

$$R.F > \frac{45\text{cm}}{36\text{ km}}$$

$$R.F = \frac{5}{\frac{45\text{cm}}{36 \times 10^5\text{cm}}}$$

$$\therefore R.F = \boxed{\frac{5}{4 \times 10^5}}$$

5. A Rectangular Plot of 100 km<sup>2</sup> is represented by a rectangular area of 4 sq cm. Find the R.F.

$$\text{Rectangular Plot} = 100\text{ km}^2$$

$$\text{Area of Drawing} = 4\text{ cm}^2$$

$$R.F = \sqrt{\frac{\text{L.O.I.D}}{\text{A.L.O}}}$$

$$R.F = \sqrt{\frac{\text{Area of O.I.D}}{\text{Actual Area of O}}}$$

$$R.F = \sqrt{\frac{4\text{cm}^2}{100\text{ km}^2}}$$

$$R.F = \frac{2\text{cm}}{10\text{ km}} = \frac{2\text{cm}}{100 \times 10^5\text{cm}} = \frac{1}{5 \times 10^5}$$

6. A cube of 5 cm side represents a tank of 8000 cu.m volume. Find the R.F

$$\text{Cube side length} = 5\text{cm}$$

$$\text{Tank volume} = 8000\text{ m}^3$$

$$R.F = \sqrt[3]{\frac{\text{Volume of O.I.D}}{\text{Actual Vol. of O}}}$$

$$= \sqrt[3]{\frac{5^3 \text{ cm}^3}{8000 \text{ m}^3}} = \frac{5 \text{ cm}}{20 \text{ m}} = \frac{5 \text{ cm}}{\frac{20 \times 100 \text{ cm}}{4}}$$

$$\therefore R.F = \frac{1}{400}$$

7. The area of a field is  $50,000 \text{ m}^2$  the length and breadth of the field on the map is 15cm and 8cm respectively. Find the value of R.F.

$$R.F = \sqrt{\frac{15^2 \times 8^2 \text{ cm}^2}{50,000 \text{ m}^2}}$$

$$R.F = \sqrt{\frac{3}{1250}} \times \frac{\text{cm}}{\text{m}}$$

$$R.F = \frac{1}{5} \sqrt{\frac{3}{50}} \times \frac{\text{cm}}{100 \text{ cm}} = \frac{1}{500} \sqrt{\frac{3}{50}}$$

$$\therefore R.F = \frac{1}{500} \sqrt{\frac{3}{50}}$$

8. A Room of  $1728 \text{ m}^3$  volume is shown by a cube of 4cm side. Find the R.F.

$$R.F = \sqrt[3]{\frac{4^3 \text{ cm}^3}{1728 \text{ m}^3}}$$

$$= \sqrt[3]{\frac{4^3 \text{ cm}^3}{3^3 \times 4^3 \text{ m}^3}}$$

$$= \frac{1 \text{ cm}}{3 \text{ m}}$$

$$= \frac{1 \text{ cm}}{3 \times 100 \text{ cm}}$$

$$\therefore R.F = \frac{1}{300}$$

$$\therefore \boxed{R.F = 1:300}$$

# PLAIN SCALES

Plain scale:

1. Construct a scale of 1:60 to show meters and decimeters and long enough to measure upto 6m. Mark on it a distance of 4.7m, 3.6m.

Ans

$$R.F = \frac{1}{60}$$

Long enough to measure upto 6m

Mark a distance = 4.7m, 3.6m.

$$R.F = \frac{L.O.I.D}{A.L.O(OI)}$$

A.L.O (OI) Max length of object

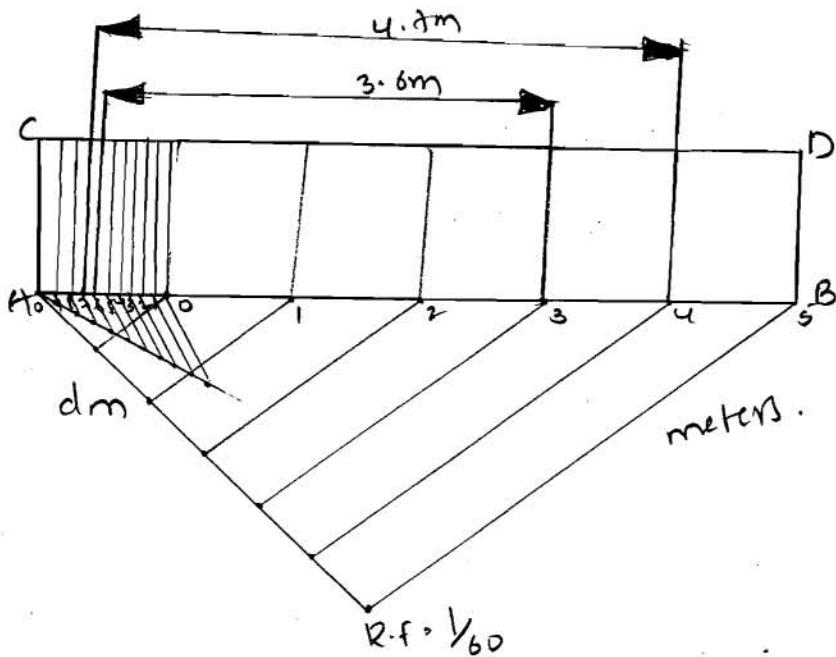
$$\frac{1}{60} = \frac{L.O.I.D}{6m}$$

$$\frac{6m}{60} = L.O.I.D$$

$$\frac{1}{10} = L.O.I.D$$

$$L.O.I.D = \frac{1}{10}m = 10cm$$

$$L.O.I.D = 100mm$$



2. Construct a scale of  $1\text{cm} = 1\text{m}$  to read meters and decimeters and long enough to measure upto  $14\text{m}$ . Show a distance of  $12.4\text{m}$ .

A:  $1\text{cm} = 1\text{meter}$ .

$$\text{Max length} = 14\text{m}$$

$$\text{Marking distance} = 12.4\text{m}$$

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$$

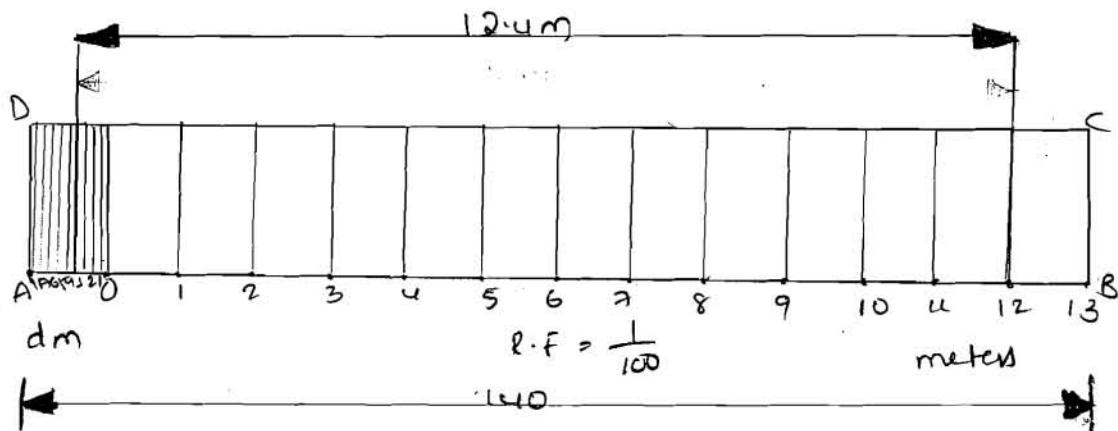
$$R.F = \frac{1\text{cm}}{1\text{m}} = \frac{1\text{cm}}{100\text{cm}} = \frac{1}{100}$$

$$\frac{1}{100} = \frac{L.O.I.D}{14\text{m}}$$

$$\frac{14\text{m}}{100} = L.O.I.D$$

$$L.O.I.D = \frac{14 \times 100\text{cm}}{100} = 140\text{cm}$$

$$L.O.I.D = 140\text{mm}$$



3. A length of 1 decameter (10m) is represented by 5cm - Find the R.F and construct a plimscale to measure upto 2.5dm and mark a distance of 19m on it.

A:  $R.F = ?$

$$1 \text{ Dm} = 5 \text{ cm}$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$R.F = \frac{5 \text{ cm}}{10 \text{ m}} = \frac{5}{1000}$$

$$R.F = \frac{1}{200}$$

$$\frac{1}{200} = \frac{L.O.I.D}{2.5 \text{ Dm}}$$

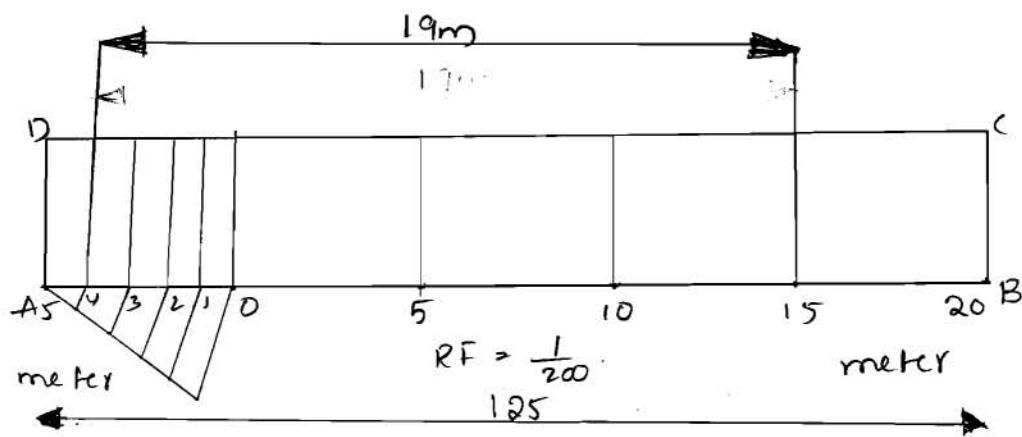
$$L.O.I.D = \frac{2.5 \text{ Dm}}{200}$$

$$= 2.5 \times \frac{5}{1000 \text{ cm}} \\ = \frac{2.5}{200}$$

$$L.O.I.D = 12.5 \text{ cm (or) } 125 \text{ mm}$$

$$\text{mark length} = 2.5 \text{ Dm}$$

$$\text{marking distance} = 19 \text{ m.}$$



4. A rectangular plot of  $100 \text{ km}^2$  is represented by a rectangular area of  $4 \text{ cm}^2$ . Draw a scale to show  $50 \text{ km}$  and mark a distance of  $41 \text{ km}$  on it.

$$A: R.F = \sqrt{\frac{4 \text{ cm}^2}{100 \text{ km}^2}}$$

$$R.F = \frac{2 \text{ cm}}{10 \text{ km}} \\ = \frac{2 \text{ cm}}{10 \times 10^5 \text{ cm}} = \frac{1}{5 \times 10^5}$$

$$\text{Max length} = 50 \text{ km}$$

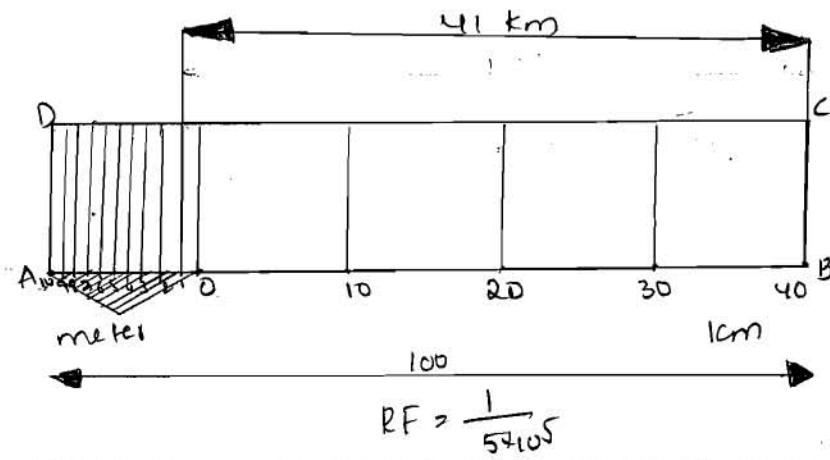
marking distance  $\approx 41 \text{ km}$ .

$$R.F = \frac{\text{length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{1}{5 \times 10^5} = \frac{L.O.I.D}{50 \text{ km}}$$

$$L.O.I.D = \frac{50 \times 10^5 \text{ cm}}{5 \times 10^5} \\ = 10 \text{ cm}$$

$$\boxed{L.O.I.D = 100 \text{ mm}}$$



5- Construct a scale of 1:14. to read feet and inches and long enough to measure 7 feet. Show a distance of 5ft and 10 inches on it.

$$R.F = \frac{1}{14}$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{1}{14} = \frac{L.O.I.D}{7 \text{ feet}}$$

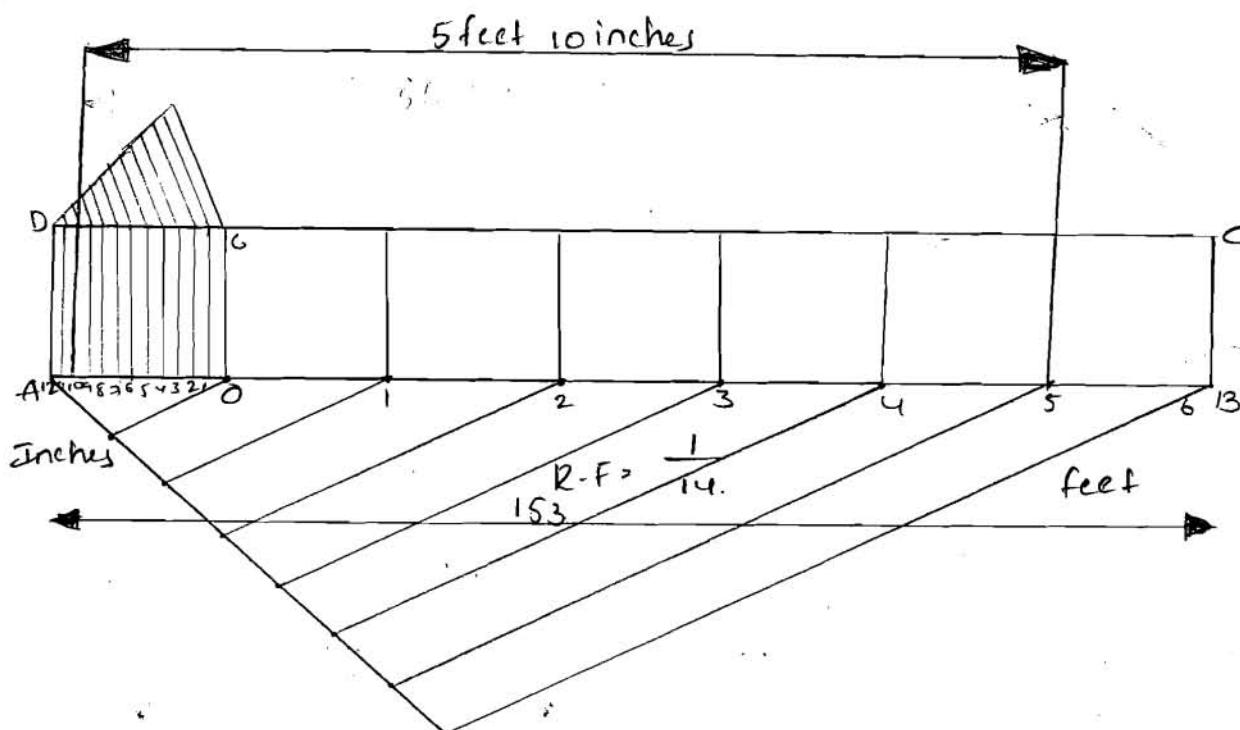
$$\frac{7 \times 12 \times 2.54 \text{ cm}}{14} = L.O.I.D$$

$$L.O.I.D = 15.24 \text{ cm} \\ \approx 15.3 \text{ cm}$$

$$L.O.I.D = 153 \text{ mm.}$$

Marking distance = 5 feet 10 inches

Mark length = 7 feet



6. Construct a scale of 1:54 to show yards and feet and long enough to measure 9 yards. Mark a distance of 6 yard 2 feet.

$$R.F = \frac{1}{54}$$

$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$

$$\frac{1}{54} = \frac{L.O.I.D}{9 \text{ yards}}$$

$$\frac{9 \text{ yards}}{54} = L.O.I.D$$

$$\frac{9 \times 3 \times 12 \times 2.54 \text{ cm}}{54} = L.O.I.D$$

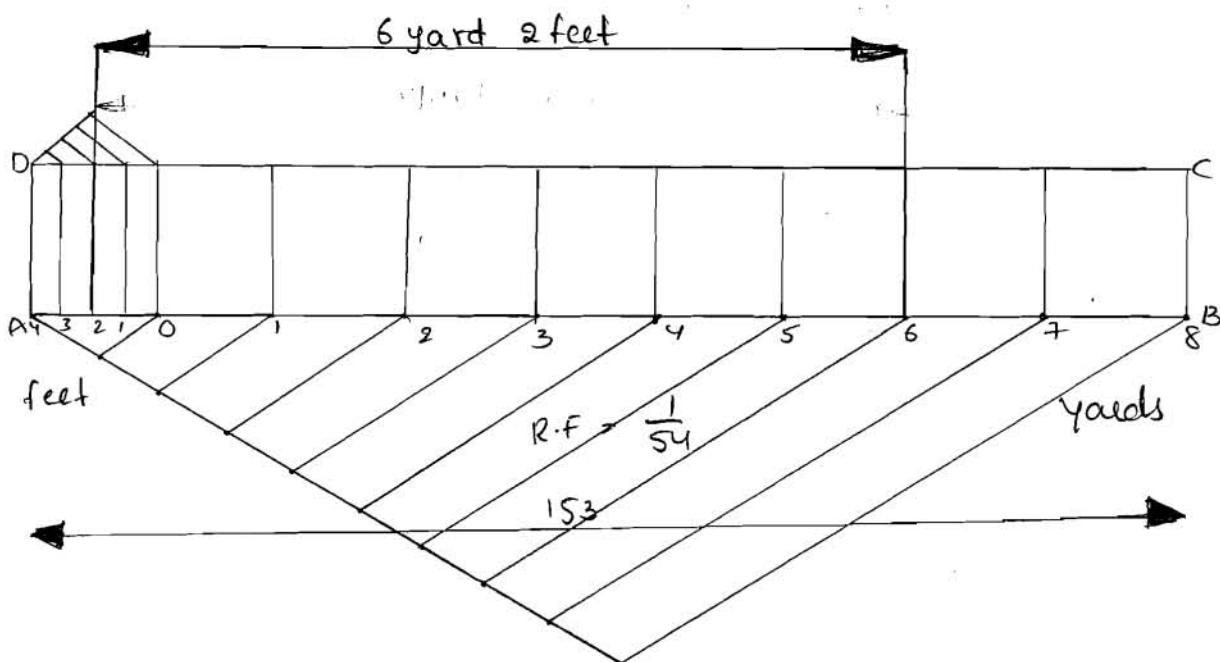
$$L.O.I.D = 15.24 \text{ cm}$$

$$\approx 15.3 \text{ cm}$$

$$L.O.I.D = 153 \text{ mm}$$

$\therefore$  mark length = 9 yards

$\therefore$  marking distance = 6 yard and 2 feet.



7. A cube of 5cm side represents a tank of  $8000\text{ m}^3$ . Find R-f and construct a scale to measure upto 60m and mark a distance of 47m

$$A: R \cdot f = \frac{5^3 \text{ cm}^3}{\sqrt[3]{8000 \text{ m}^3}}$$

$$R.F = \frac{5\text{ cm}}{20\text{ m}} = \frac{1\text{ cm}}{400\text{ cm}}$$

$$R \cdot F = \frac{1}{400}$$

$$R.F = \frac{\text{length of object in drawing}}{\text{Actual length of object}}$$

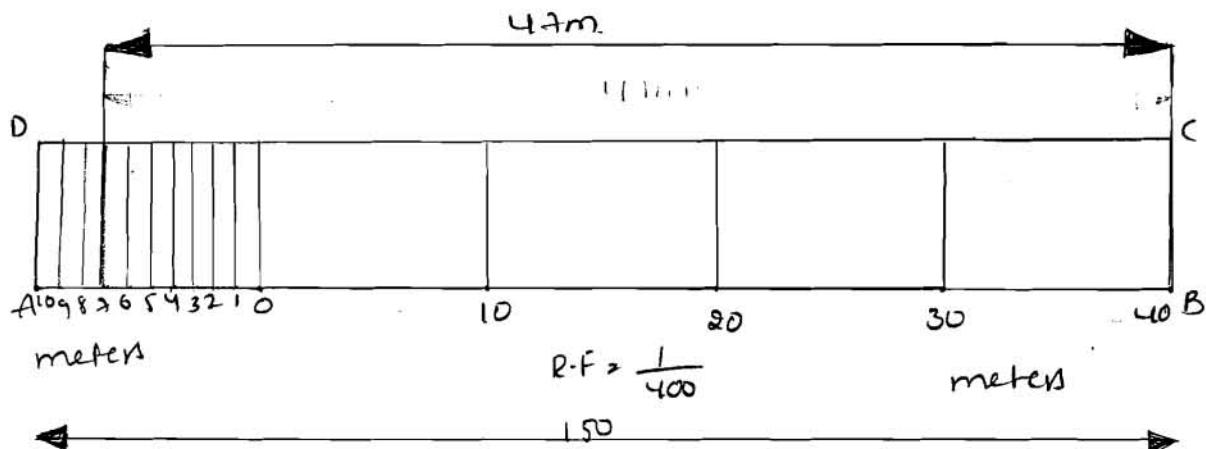
$$\frac{1}{400} = \frac{L \cdot O \cdot I \cdot D}{60m}$$

$$\frac{60m}{400} = L \cdot o \cdot I \cdot D$$

$$L \cdot O \cdot I \cdot D = \frac{15}{6000} \text{ cm}$$

$$L \cdot O \cdot I \cdot D = 15 \text{ cm} \\ = 150 \text{ mm}$$

$$\text{mating distance} = 4.7 \text{ m}$$



## Diagonal scale

1. A map is to be drawn with R.F 1:40. Construct a scale to read in meters, dm and cm and long enough to measure upto 6m. Show on it a distance of 3.84m.

A: Scale  $\rightarrow$  m, dm, cm

$$R.F = \frac{1}{40}$$

max length of object = 6m

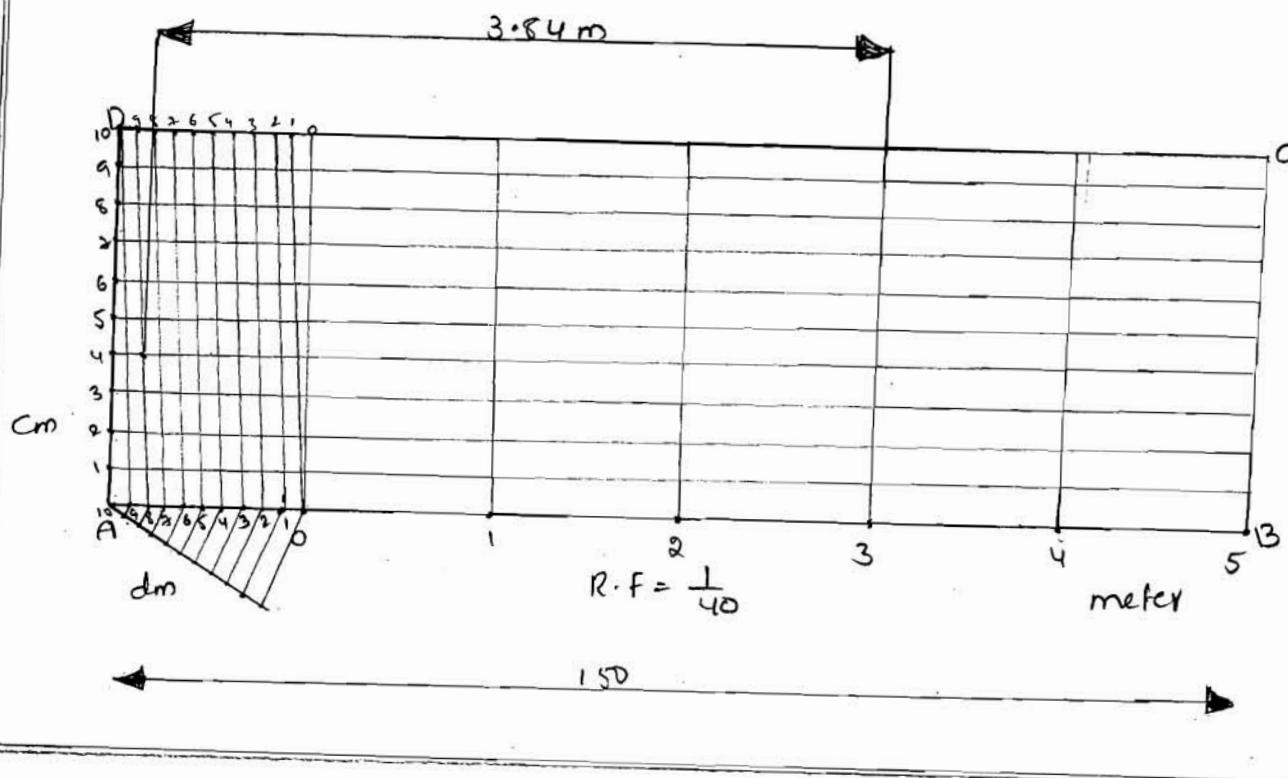
Marking distance = 3.84m

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual Length of object}}$$

$$\frac{1}{40} = \frac{L.O.I.D}{6m}$$

$$L.O.I.D = \frac{6m}{40} = \frac{3\frac{3}{5} \times 100cm}{40} = 15cm$$

$$L.O.I.D = 150mm$$



2. Construct a diagonal scale showing km, hm, dm in which 2cm long line represents 1km, and the scale is long enough to measure upto 7 km. Find the R.F and marking distance of 4.53 km on it.

A: Scale  $\rightarrow$  km, hm, dm

$$R.F = \frac{2\text{ cm}}{1 \times 10^5 \text{ cm}}$$

$$R.F = \frac{1}{5 \times 10^4}$$

$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$

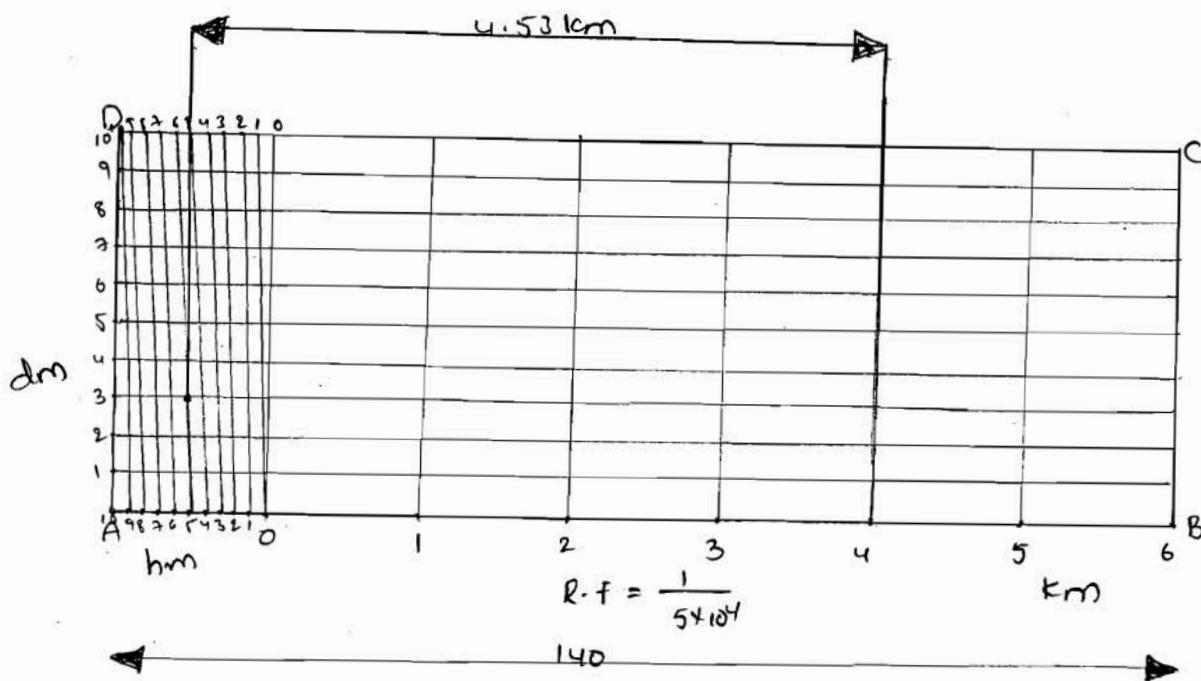
$$\frac{1}{5 \times 10^4} = \frac{L.O.I.D}{7\text{ km}}$$

$$\frac{1}{5 \times 10^4} = \frac{7 \times 10^8 \text{ cm}}{8 \times 10^4} = L.O.I.D$$

$$L.O.I.D = 14 \text{ cm } (or) 140 \text{ mm}$$

max length  $\rightarrow$  7 km

marking distance = 4.53 km.



3. Draw a diagonal scale of R.F 3:100 showing in meters, dm and cm and measure upto 5m. Mark a length of 3.69 m.

A:  $R.F = \frac{3}{100}$  Scale  $\rightarrow$  meters, dm, cm

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{3}{100} = \frac{L.O.I.D}{5m}$$

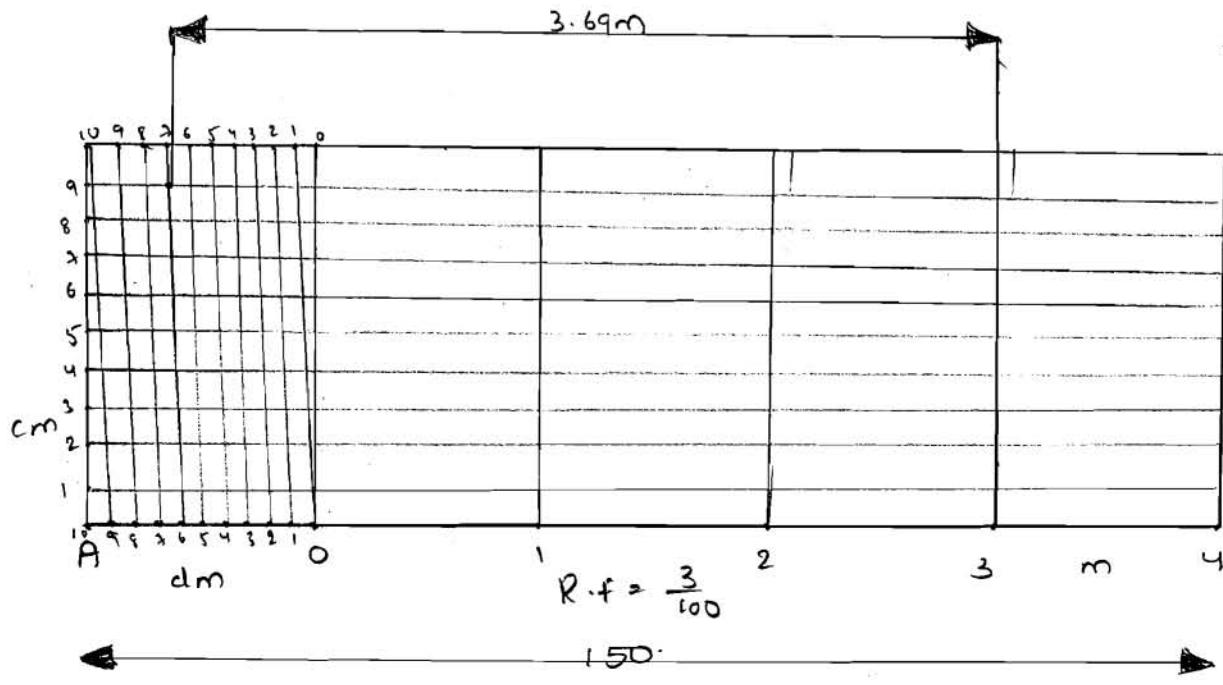
$$\frac{3 \times 5 \times 100 \text{ cm}}{100} = L.O.I.D$$

$$L.O.I.D = 15 \text{ cm.}$$

$$L.O.I.D = 150 \text{ mm.}$$

$$\text{max length} = 5 \text{ m}$$

marking distance = 3 m 6dm and 9cm (3.69m).



4. The distance between two cities 'A' and 'B' is 300 km. If its equivalent distance on the map measures only 6cm. what is R.F? Draw a diagonal scale show 100's of km, Ten's km and km indicate on the scale the following distances.

(i) 525 km, (ii) 313 km and 258 km.

A: Distance b/w two cities = 300 km (A.L)  
distance on the map = 6cm (L.O.I.D).

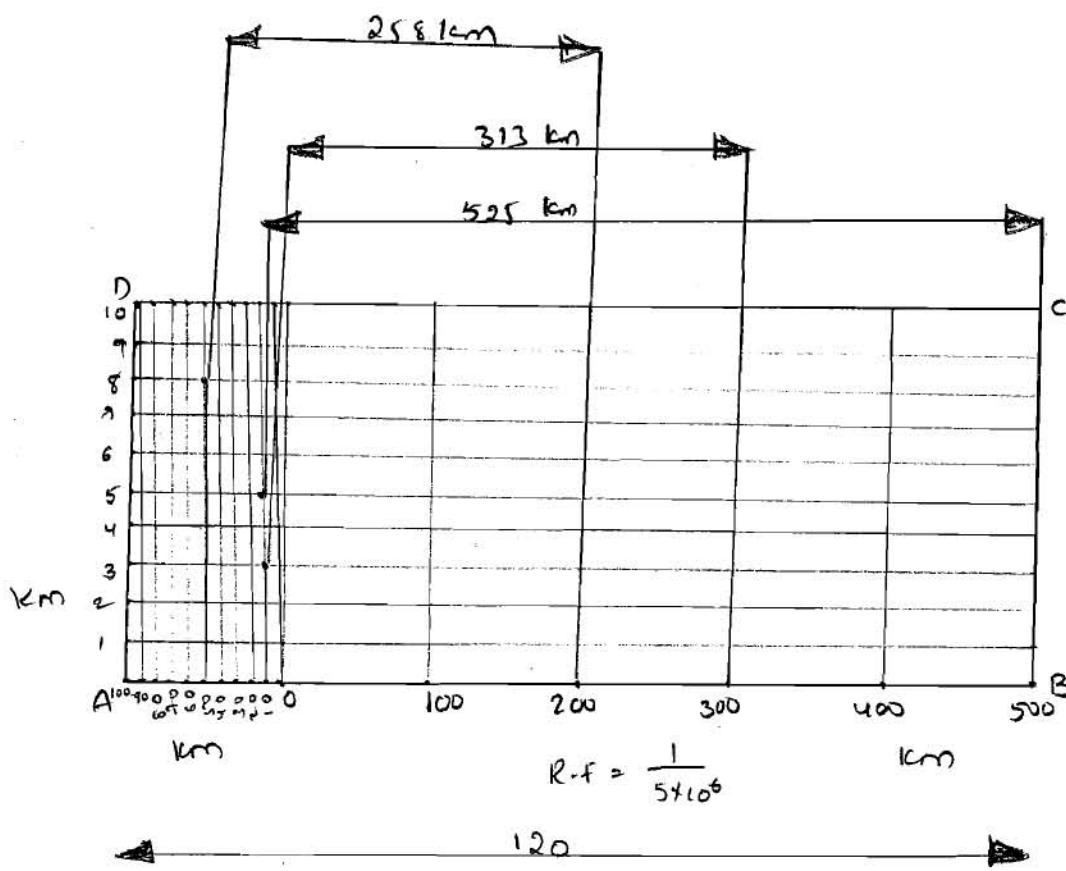
$$R.F = \frac{6\text{cm}}{300\text{km}} = \frac{6\text{cm}}{300 \times 10^5\text{cm}} = \frac{1}{5 \times 10^6}$$

max length = 600 km ( $\because$  max marking distance is 525 km)

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}} = \frac{1}{5 \times 10^6} = \frac{\text{L.O.I.D}}{600\text{km}}$$

$$\text{L.O.I.D} = \frac{600 \times 10^5\text{cm}}{5 \times 10^6} = 12\text{cm}$$

$$\text{L.O.I.D} = 120\text{ mm.}$$



5. On a map the actual distance of 5m is represented by a line of 25mm long. Calculate the R.F. Construct a diagonal scale long enough to measure upto 25m and make a distance of 19m and 11m.

A: Max length = 25m

$$R.F. = \frac{\text{Length of object in Drawing}}{\text{Actual Length of object}}$$

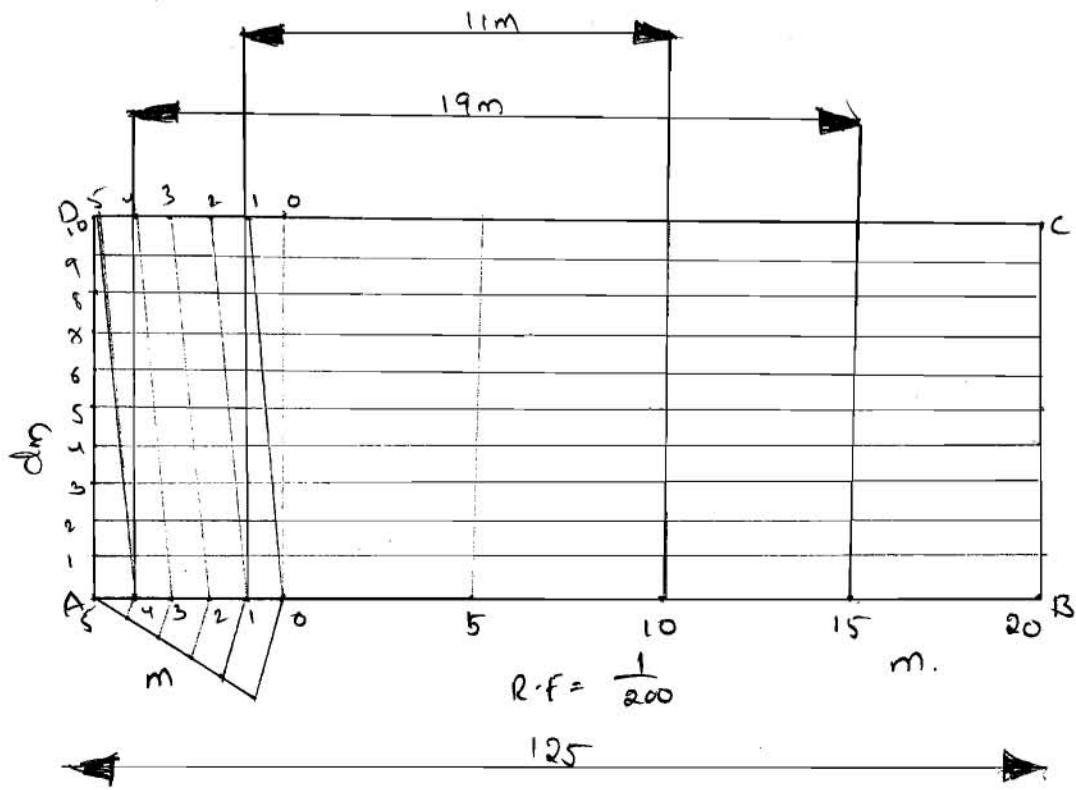
$$= \frac{25\text{ mm}}{5\text{ m}} = \frac{25\text{ mm}}{5 \times 10^3\text{ mm}} = \frac{1}{200}$$

$$R.F. = \frac{1}{200}$$

$$\frac{1}{200} = \frac{L.O.I.D.}{25\text{ m}}$$

$$\frac{25 \times 100\text{ cm}}{200} = L.O.I.D.$$

$$L.O.I.D. = 12.5\text{ cm or } 125\text{ mm.}$$



6. Construct a diagonal scale showing yards, feet and inches. In which 2 inches long line represents 1.25 yards and it is long enough to measure upto 5 yards, marking distance as 3 yards 2Feet and 10 inches.

Sol:

$$2 \text{ inches} = 1.25 \text{ yards}$$

$$R.F = \frac{2 \text{ inches}}{1.25 \text{ yards}} = \frac{2 \text{ inches}}{1.25 \times 3 \times 12 \text{ inches}}$$

$$R.F = \frac{106.2}{225} = \frac{2}{45}$$

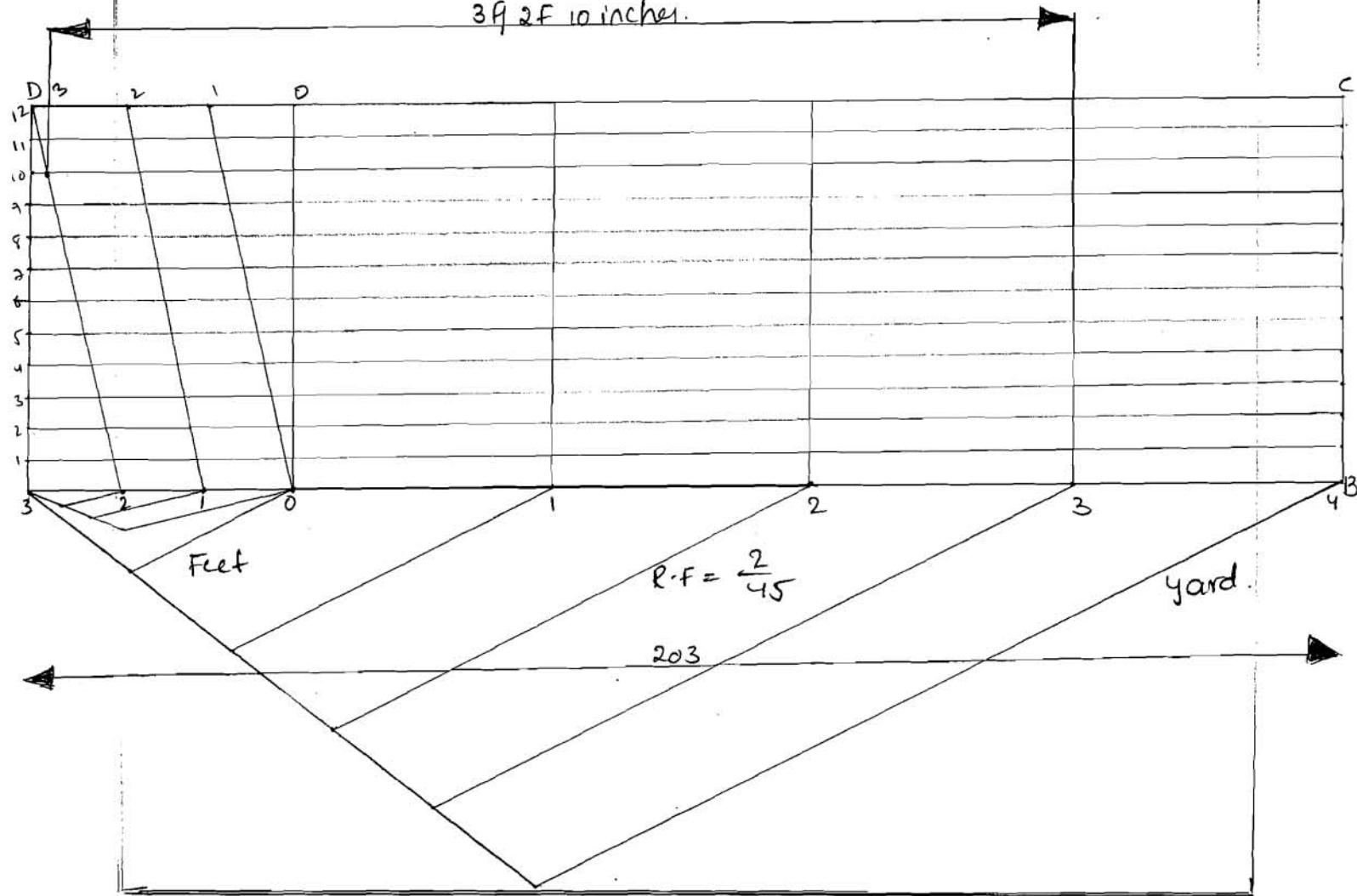
$$\text{max length} = 5 \text{ yards}$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{2}{45} = \frac{L.O.I.D}{5 \text{ yards}} = \frac{5 \times 3 \times 12 \times 2.54 \text{ cm}}{5 \text{ yards}} \times \frac{2}{45} = L.O.I.D.$$

$$L.O.I.D = 20.32 \text{ cm} \approx 20.3 \text{ cm (or) } 203 \text{ mm}$$

3Y 2F 10 inches.



7. A rectangular plots of land measuring 1.28 hectares is showing on a map by a similar rectangle of  $8\text{ cm}^2$  calculate R.F of the scale. Draw a diagonal scale two read 1m and long enough to measure 600m. show a distance of 438m on it.

$$\text{Sol: } \text{R.F} = \frac{8\text{ cm}^2}{1.28 \times 10^4 \text{ m}^2}$$

$$= \sqrt{\frac{8\text{ cm}^2}{1.28 \times 10^4 \text{ m}^2}} = \sqrt{\frac{18}{1128 \times 10^2}} \times \frac{\text{cm}}{\text{m}}$$

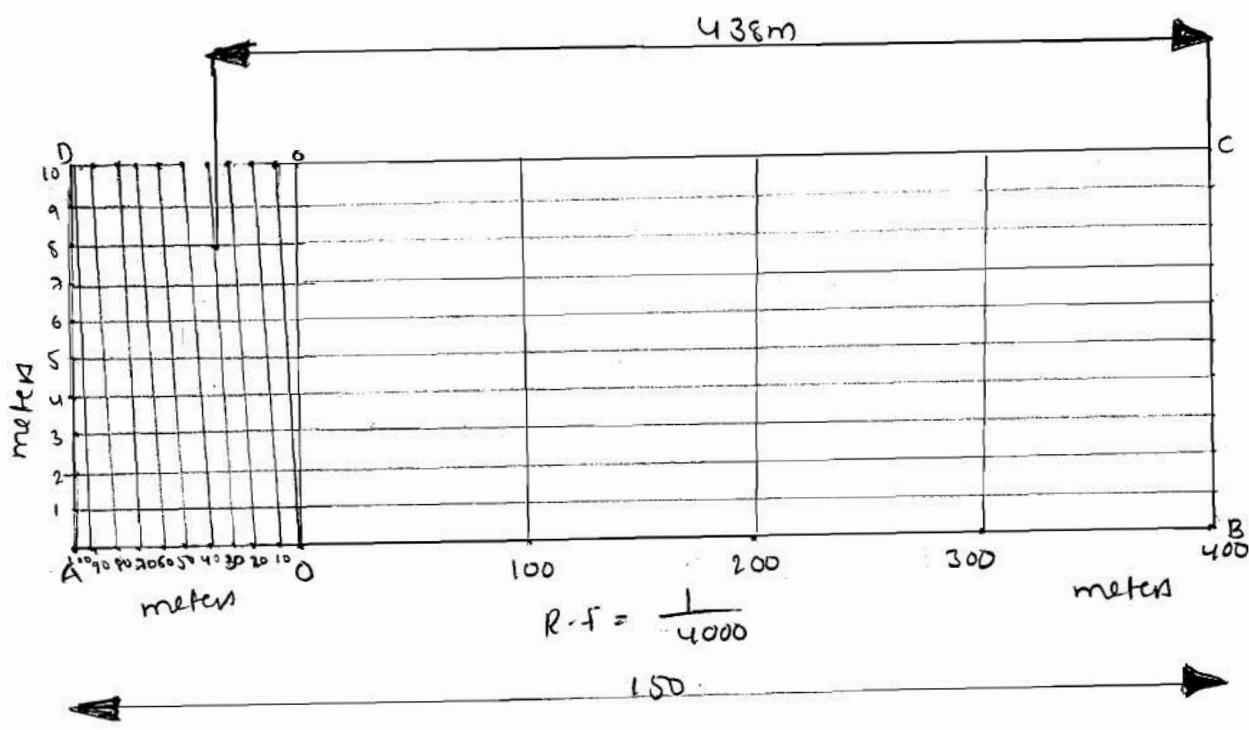
$$\therefore \text{R.F} = \frac{1}{4000} \times \frac{\text{cm}}{100\text{ m}} = \frac{1}{4000}$$

R.F =  $\frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$

$$\frac{1}{4000} = \frac{\text{L.O.I.D}}{600\text{ m}} = \frac{15}{\frac{600 \times 10^2}{4000}} = 15\text{ cm (or) } 150\text{ mm}$$

$\therefore$  max length = 600m

marking distance = 438m.



8. The distance between two stations is 100 km and on a map it is shown by 30 cm. Draw a diagonal scale and indicate 46.8 km and 32.4 km.

$$\text{Sol: } R.F = \frac{30 \text{ cm}}{100 \text{ km}} = \frac{30 \text{ cm}}{100 \times 10^5 \text{ cm}} = \frac{3}{10^6}$$

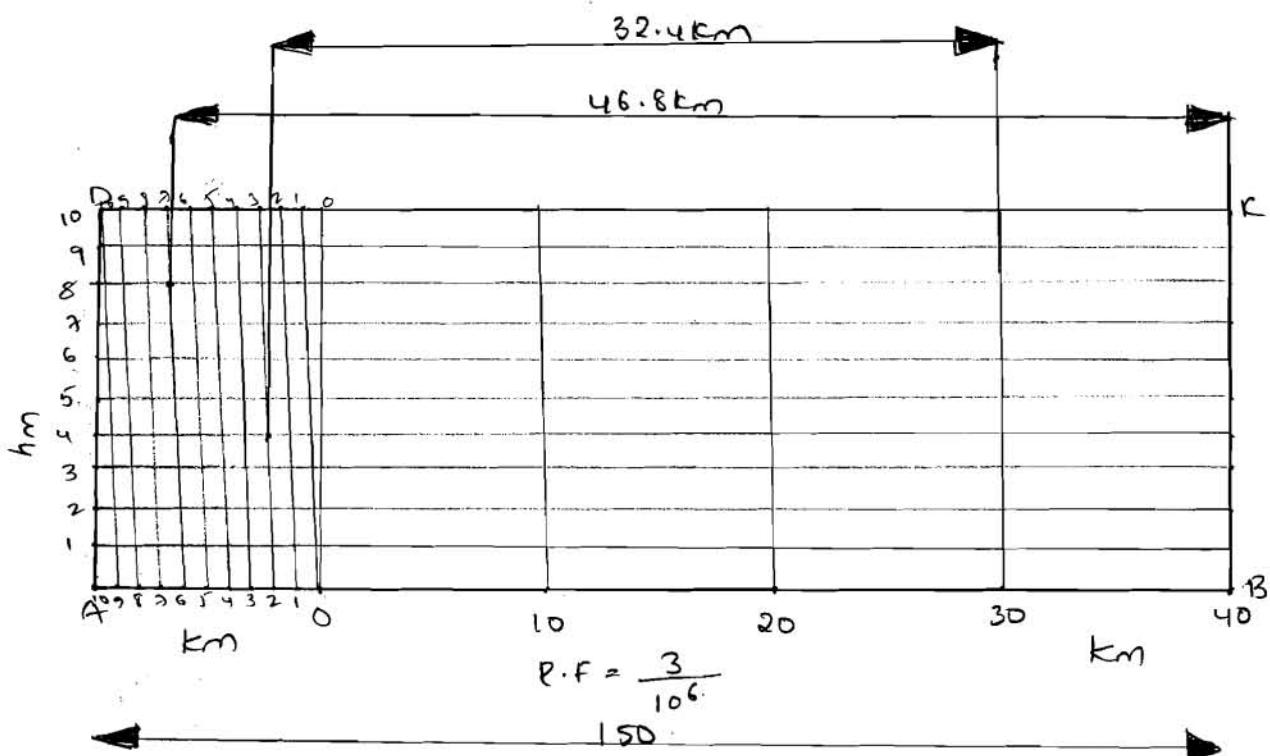
$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

Max length = 50 km ( $\because$  max marking is 46.8 km).

$$\frac{3}{10^6} = \frac{L.O.I.D}{50 \text{ km}}$$

$$L.O.I.D = \frac{50 \times 10^8 \times 3 \text{ cm}}{10^6} = 15 \text{ cm or } 150 \text{ mm}$$

marking distance = 46.8 km and 32.4 km



9. Construct a scale to measure km,  $\frac{1}{8}$  km and  $\frac{1}{40}$  km, in which 1 km is showing by 4 cm. Mark on the scale at a distance of 2.775 km.

$$\text{Sol. } R.F = \frac{4 \text{ cm}}{1 \text{ km}} = \frac{4 \text{ cm}}{1 \times 10^5 \text{ cm}} = \frac{1}{25 \times 10^3}$$

$$\therefore R.F = \frac{1}{25 \times 10^3}$$

$$R.F = \frac{\text{Length of the object in drawing}}{\text{Actual length of object}}$$

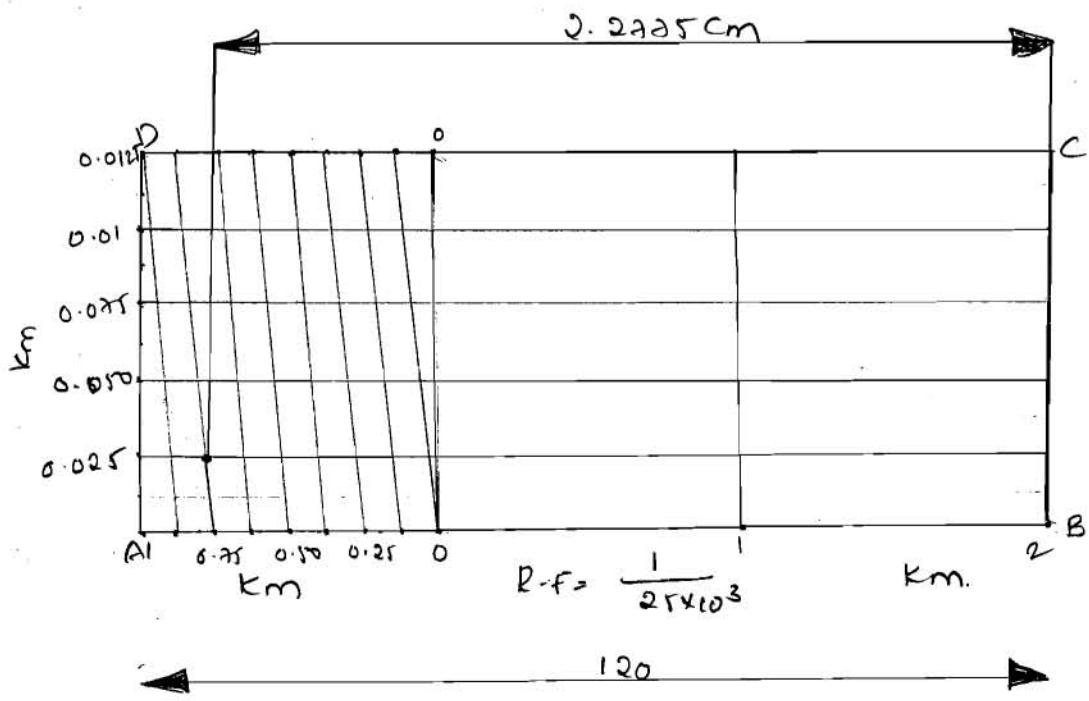
$\therefore$  Max length = 3 km ( $\because$  max marking is 2.775 km).

$$\frac{1}{25 \times 10^3} = \frac{\text{L.O.I.D}}{3 \text{ km}}$$

$$\text{L.O.I.D} = \frac{3 \times 10^5 \text{ cm}}{25 \times 10^3} = 34 \text{ cm} = 120 \text{ mm}$$

$$\therefore \text{L.O.I.D} = 120 \text{ mm}$$

Marking distance = 2.775 km.



1-Q:- Construct a scale of R.F = 2.5 to show m, dm, cm and long enough to measure upto 4m.

Sol:

$$R.F = 2.5$$

$$R.F = \frac{2.5}{10} = \frac{5}{2}$$

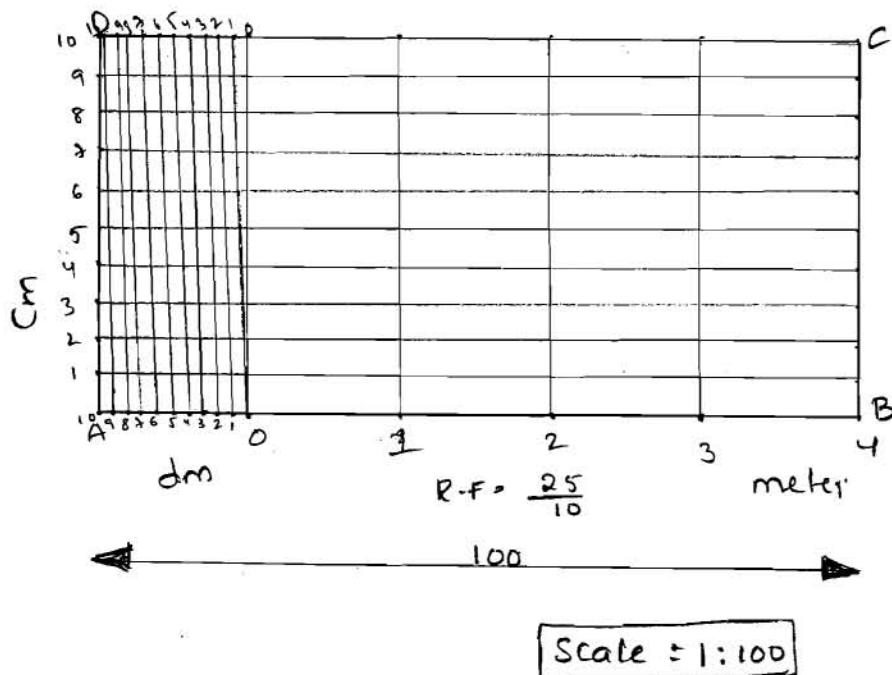
R.F =  $\frac{\text{Length of object in drawing}}{\text{Actual length of object}}$

$\therefore$  max length = 4m

$$\frac{5}{2} = \frac{L.O.I.D}{4m}$$

$$\frac{5}{2} \times 4 \times 100 = L.O.I.D$$

$$L.O.I.D = 1000\text{cm (or)} 10,000\text{mm.}$$



2. Q:- Draw a diagonal scale of R.F = 4 to read cm,  $\frac{1}{5}$  cm,  $\frac{1}{2}$  cm and to measure upto 5cm. Mark on the scale distance of 3.36 cm.

Sol:

$$R.F = 4$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\text{max length} = 5\text{cm}$$

$$\frac{4}{1} = \frac{L.O.I.D}{5\text{cm}}$$

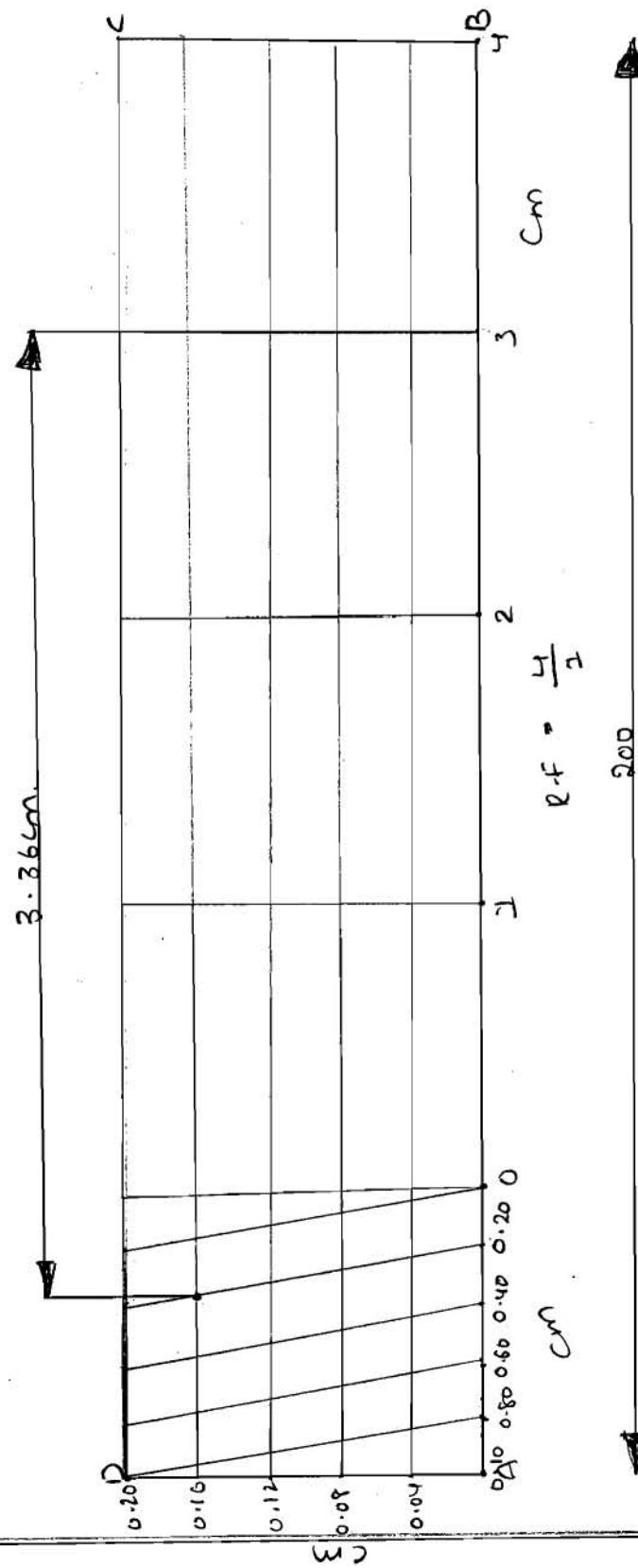
$$4 \times 5\text{cm} = L.O.I.D$$

$$L.O.I.D = 20\text{cm (or)}$$

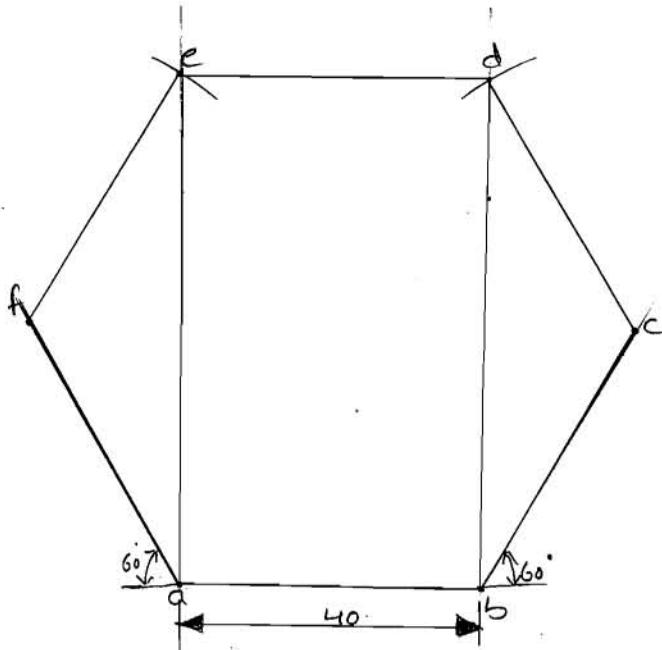
200 mm

Marking distance.

$$= 3.36\text{cm.}$$



- 3.Q:- a) Draw a regular hexagon of 40mm side using general method.



Hexagon

- b) The distance between two points on a map is 15cm. The real distance b/w them is 20 km. Draw a diagonal scale to measure upto 25 km and show a distance of 18.6 km on it.

Sol.

$$R.F = \frac{15\text{cm}}{20 \times 10^5 \text{cm}} = \frac{3}{4 \times 10^5}$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual Length of object}}$$

map length = 25 km

$$\frac{3}{4 \times 10^5} = \frac{L.O.I.D}{25 \text{km}}$$

$$L.O.I.D = \frac{25 \times 10^5 \times 3 \text{cm}}{4 \times 10^5}$$

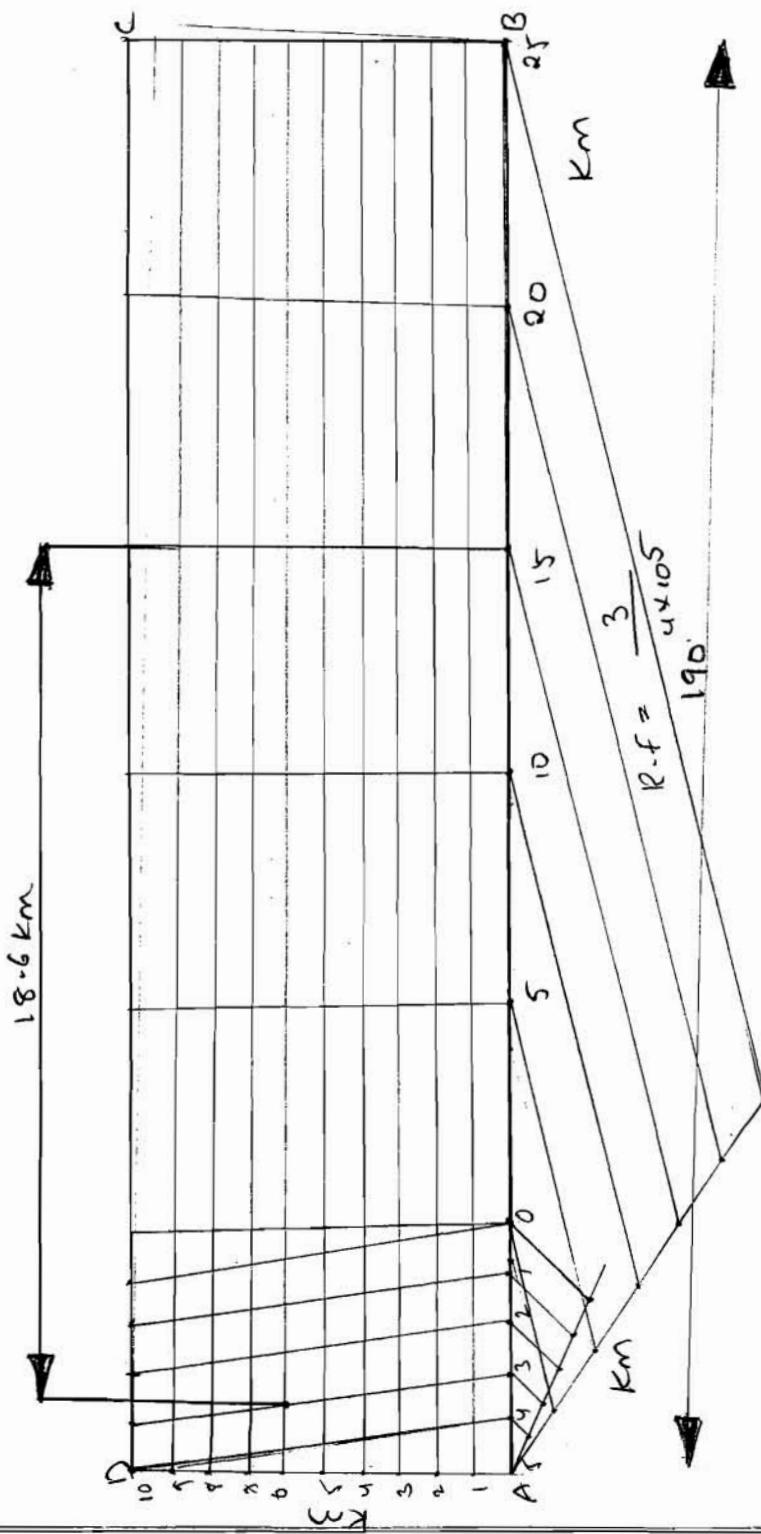
$$= \frac{75}{4} \text{ cm}$$

$$= 18.75 \text{ cm}$$

$$\approx 19 \text{ cm}$$

$$L.O.I.D = 19 \text{ cm} (0.19 \text{ m})$$

Walking distance is 18.6 km.



# Vernier scale

1. Construct a vernier scale of 1:40 to read meters, dm and cm and long enough to measure upto 6m and mark distance of 5.26m on it.

Sol:

$$R.F = \frac{1}{40}$$

$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$\therefore$  max length = 6m

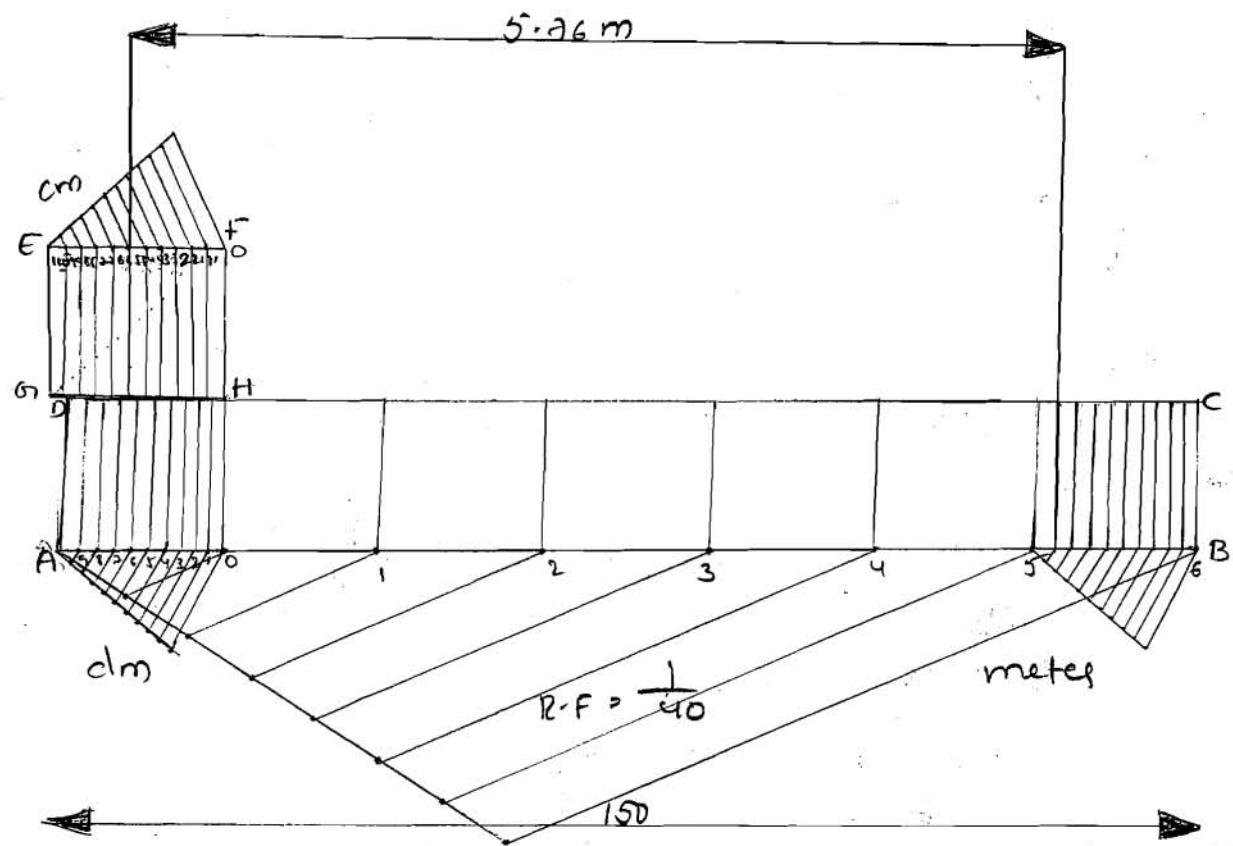
$$\frac{1}{40} = \frac{L.O.I.D}{A.L.O}$$

$$\frac{1}{40} = \frac{L.O.I.D}{6m}$$

$$\frac{6 \times 10 \text{ cm}}{40} = L.O.I.D$$

$$\therefore L.O.I.D = 15 \text{ cm (or) } 150 \text{ mm}$$

$\therefore$  Marking distance = 5.26m



2. If 1cm long line on a map represents a real distance of 4m. calculate the R.F. Draw a vernier scale long enough to measure upto 50m. show a distance of 44.5m on it.

$$\text{Sol: } R.F = \frac{1\text{cm}}{4\text{m}} = \frac{1\text{cm}}{4 \times 100\text{cm}}$$

$$R.F = \frac{1}{400}$$

$\therefore$  max length = 50m

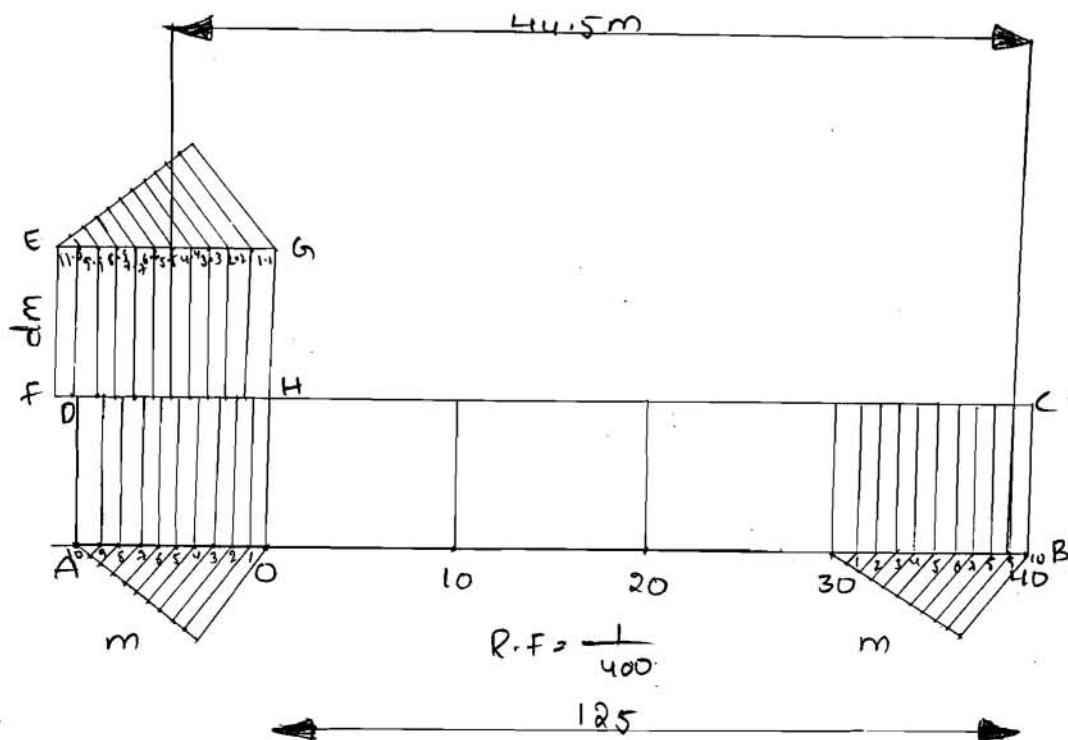
$$R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{1}{400} = \frac{\text{L.O.I.D}}{50\text{m}}$$

$$\frac{50 \times 100\text{cm}}{400} = \text{L.O.I.D}$$

$$\text{L.O.I.D} = 12.5\text{cm or } 125\text{mm}$$

marking distance = 44.5m.



3. A real length of 10m is represented by a line of 5cm on a drawing. Find the R.F and construct a vernier scale such that least count is 2dm and measure upto 25m mark a distance of 19.4m on it.

$$\text{R.F} = \frac{5\text{cm}}{10\text{m}}$$

$$\text{R.F} = \frac{5\text{cm}}{10 \times 100\text{cm}} = \frac{1}{200}$$

$$\text{max length} = 25\text{m}$$

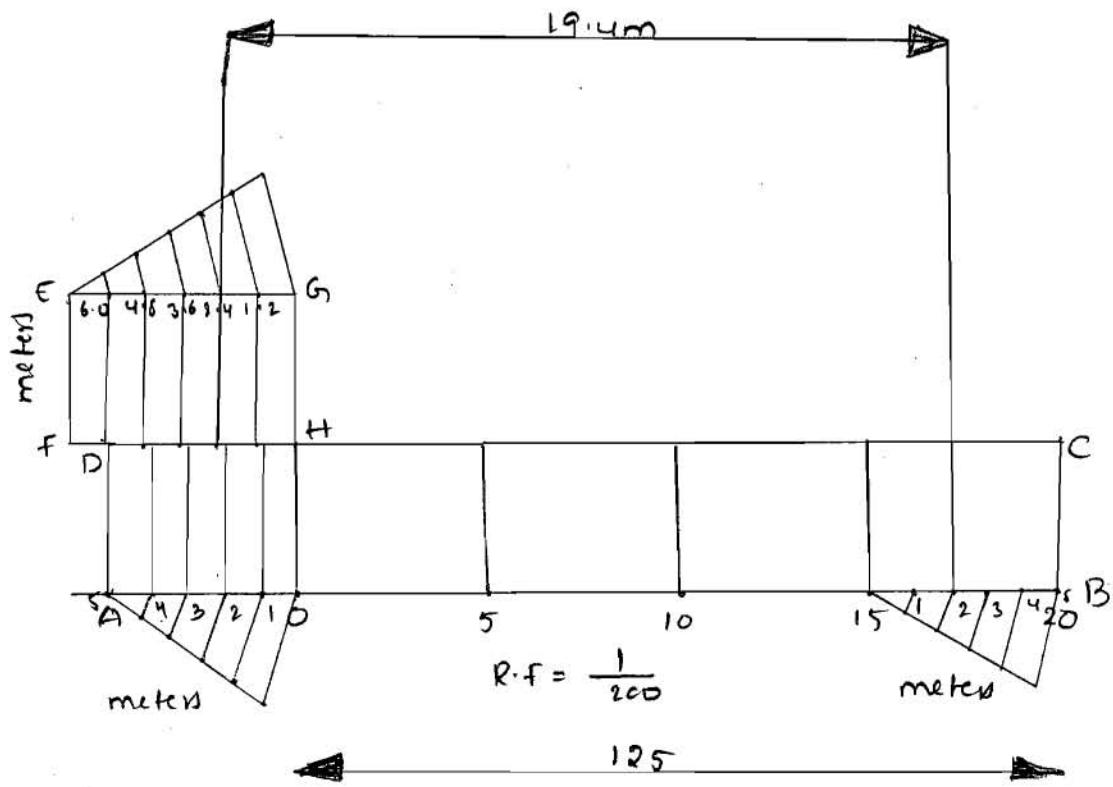
$$\text{R.F} = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{1}{200} \Rightarrow \frac{\text{L.O.I.D}}{25\text{m}}$$

$$\frac{25 \times 100 \text{ cm}}{200} = \text{L.O.I.D}$$

$$\text{L.O.I.D} = 12.5 \text{ cm or } 125 \text{ mm}$$

$$\therefore \text{marking distance} = 19.4\text{m.}$$



Vernier scale

4.

On a map rectangle of 125cm x 200cm represents area of 6250 km<sup>2</sup>. Draw a vernier scale to show Dm, and long enough to measure upto 7 km. show a distance of 6.43km on it.

Sol:

$$R.F = \sqrt{\frac{125 \times 200 \text{ cm}^2}{6250 \text{ km}^2}}$$

$$\Rightarrow \sqrt{\frac{25000}{6250} \times \frac{\text{cm}}{\text{km}}} = \sqrt{\frac{2500}{625} \times \frac{\text{cm}}{105 \text{ cm}}} \\ = \frac{50}{25 \times 10^5} = \frac{2}{105} = \frac{1}{5 \times 10^4}$$

$$\therefore R.F = \frac{1}{5 \times 10^4}$$

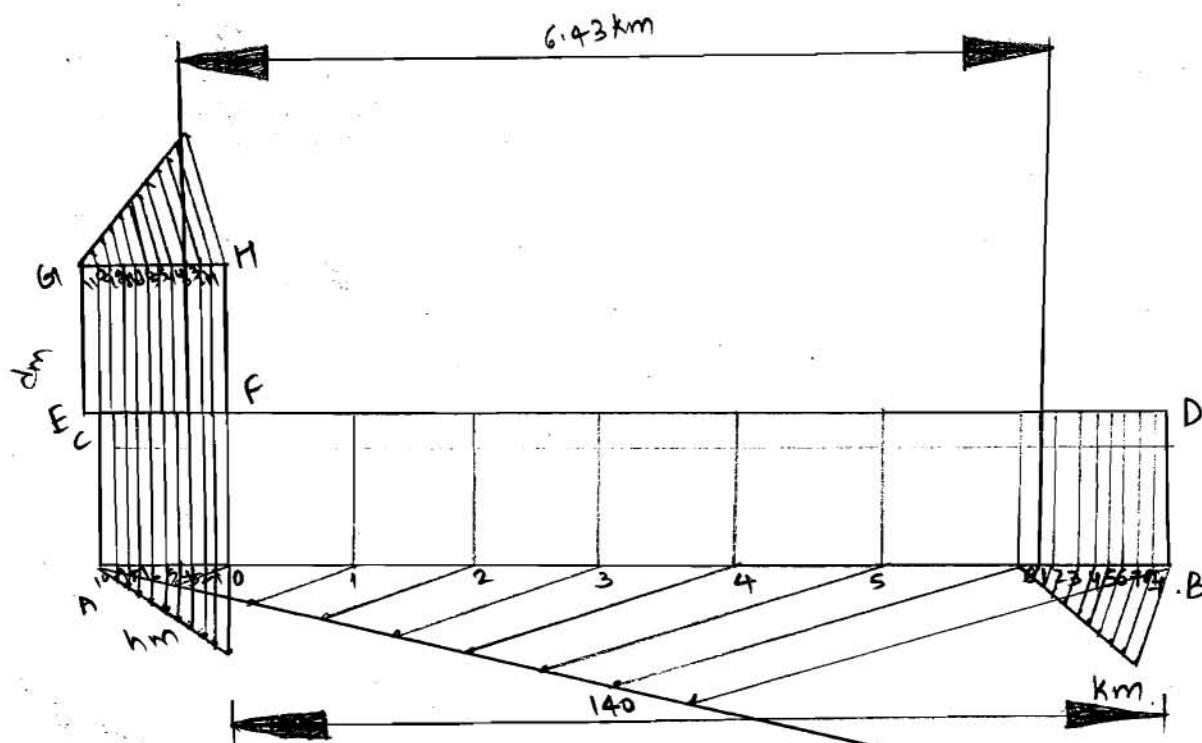
R.F max length = 7 km

$$\therefore R.F = \frac{\text{Length of object in drawing}}{\text{Actual length of object}}$$

$$\frac{1}{5 \times 10^4} = \frac{L.O.I.D}{7 \text{ km}}$$

$$L.O.I.D = \frac{7 \times 10^5 \text{ cm}}{5 \times 10^4} = 140 \text{ cm or } 140 \text{ mm}$$

mapping distance  $> 6.43 \text{ km}$



$$RF = \frac{1}{5 \times 10^4}$$

5. Construct a full size vernier scale of inches and show on it length of 4.67 inches.

full size scale ratio = 1:2

$$R.F. = \frac{1}{2}$$

mark length = 5 inches (mark marking is 1.67).

$$R.F. = \frac{\text{length of object in drawing}}{\text{actual length of object}}$$

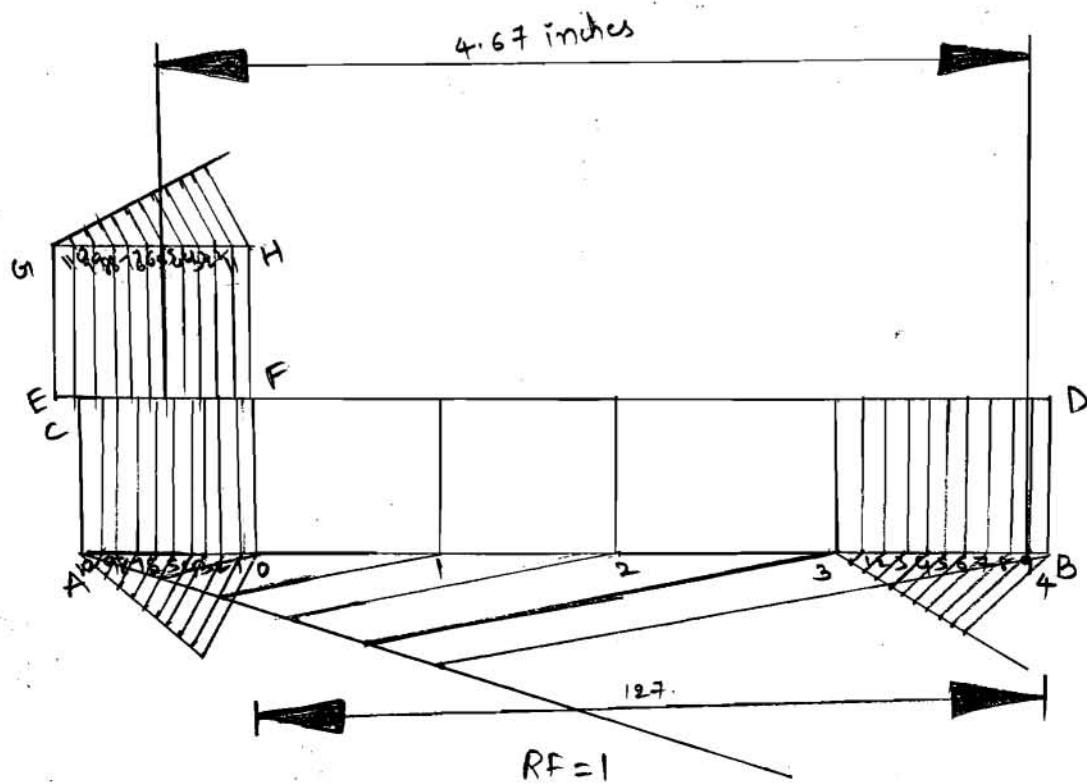
$$\frac{1}{1} = \frac{L.O.I.D}{5 \text{ inches}}$$

$$L.O.I.D = 5 \times 2.54 \text{ cm}$$

$$= 12.7 \text{ cm}$$

$$= 127 \text{ mm}$$

marking distance = 4.67 inches.



# **UNIT-II**

# **Content**

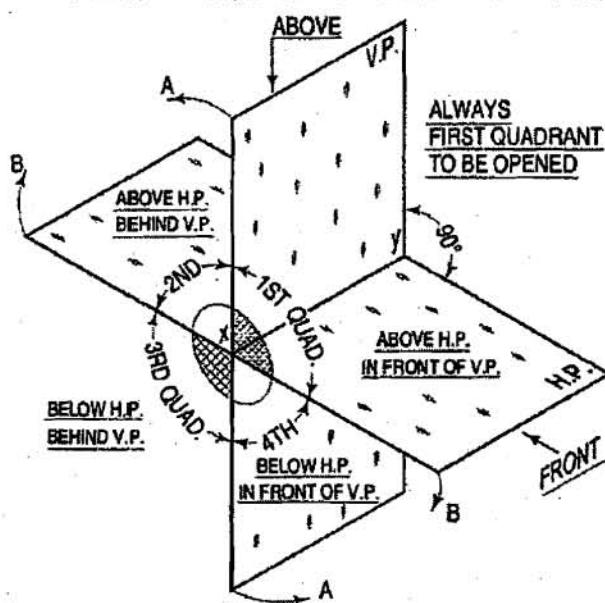
**Orthographic Projections:** Principles of Orthographic Projections — Conventions — Projections of Points and Lines, Projections of Plane regular geometric figures.—Auxiliary Planes.

## Unit-II

**Orthographic Projections:** When the projectors are parallel to each other and also perpendicular to the plane, the projection is called orthographic projection.

**Planes of Projection:** The two planes employed for the purpose of orthographic projections are called reference planes or principal planes of projection. They intersect each other at right angles. The vertical plane of projection (in front of the observer) is usually denoted by the letters V.P. It is often called the frontal plane and denoted by the letters F.P. The other plane is the horizontal plane of projection known as the H.P.

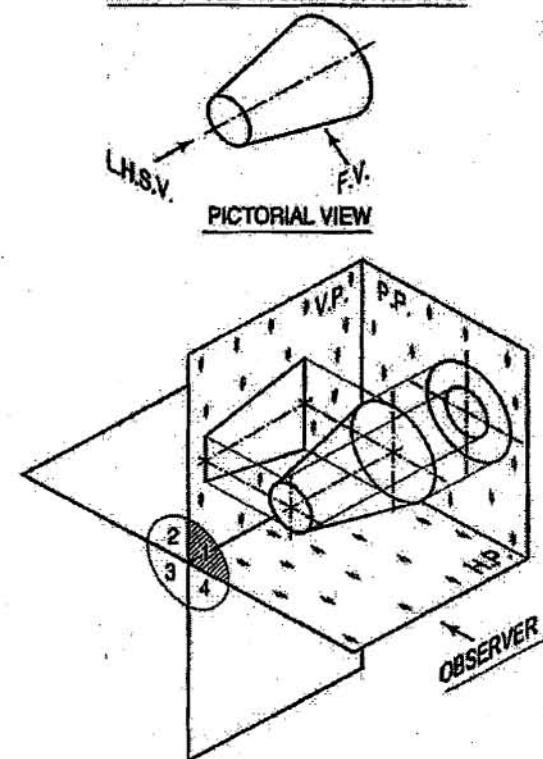
The line in which they intersect is termed the reference line and is denoted by the letters xy. The projection on the V.P. is called the front view or the elevation of the object. The projection on the H.P. is called the top view or the plan.



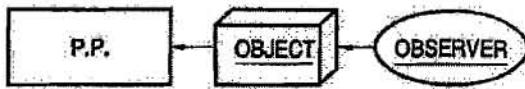
**First-Angle Projection:** We have assumed the object to be situated in front of the V.P. and above the H.P.i.e. in the first quadrant and then projected it on these planes. This method of projection is known as first-angle projection method. The object lies between the observer and the plane of projection.

In this method, when the views are drawn in their relative positions, the top view comes below the front view. In other words, the view seen from above is placed on the other side of (i.e. below) the front view. Each projection shows the view of that surface (of the object) which is remote from the plane on which it is projected and which is nearest to the observer.

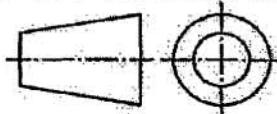
#### FIRST ANGLE PROJECTION METHOD



#### FIRST ANGLE PROJECTION



#### RELATION BETWEEN OBSERVER, OBJECT AND P.P.

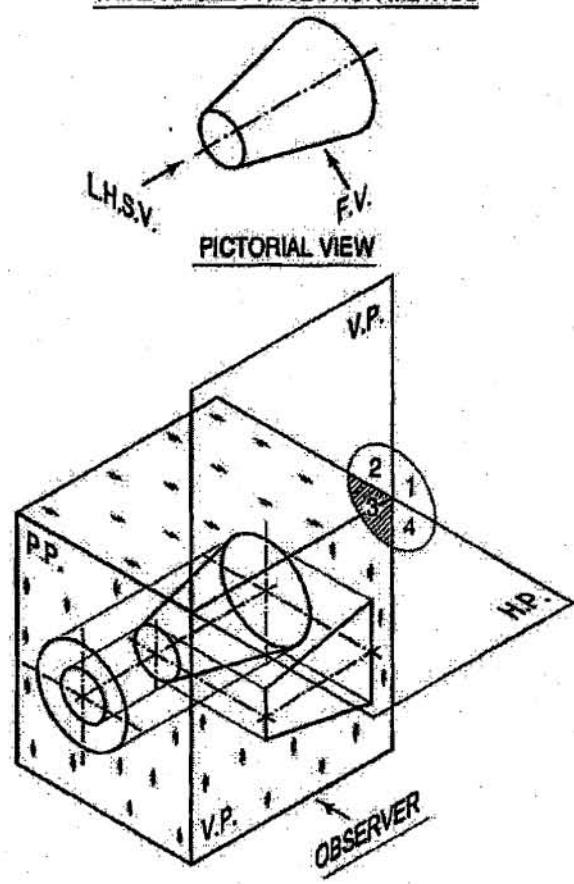


F.V.      L.H.S.V.  
IDENTIFYING GRAPHICAL SYMBOL OF  
FIRST ANGLE PROJECTION

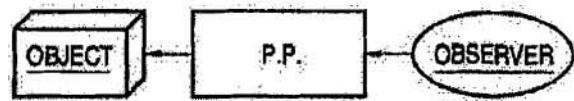
**Third-Angle Projection:** In this method of projection, the object is assumed to be situated in the third quadrant. The planes of projection are assumed to be transparent. They lie between the object and the observer. When the observer views the object from the front, the rays of sight intersect the V.P.

The figure formed by joining the points of intersection in correct sequence is the front view of the object. The topview is obtained in a similar manner by looking from above. When the two planes are brought in line with each other, the views will be seen as shown in fig. The top view in this case comes above the front view.

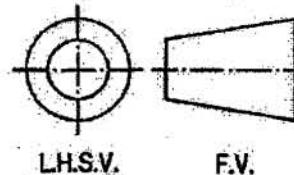
#### THIRD ANGLE PROJECTION METHOD



#### THIRD ANGLE PROJECTION



**RELATION BETWEEN OBSERVER, OBJECT AND P.P.**



**IDENTIFYING GRAPHICAL SYMBOL OF  
THIRD ANGLE PROJECTION**

### **Projections of Points:**

A point may be situated, in space, in any one of the four quadrants formed by the two principal planes of projection or may lie in any one or both of them. Its projections are obtained by extending projectors perpendicular to the planes.

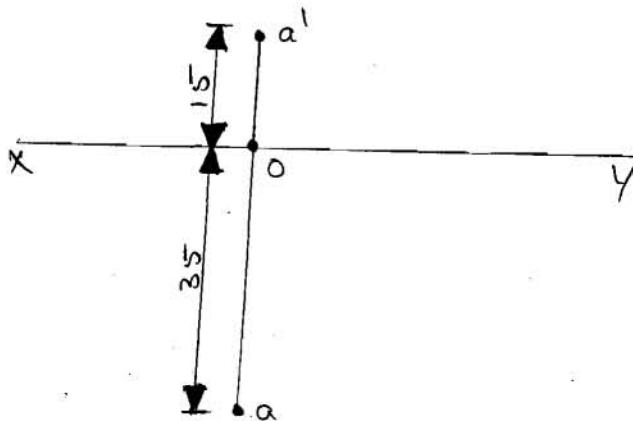
One of the planes is then rotated so that the first and third quadrants are opened out. The projections are shown on a flat surface in their respective positions either above or below or in xy.

# ORTHOGRAPHIC PROJECTIONS

## Projection of points:

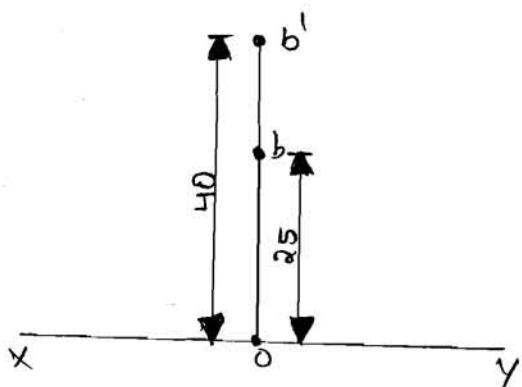
I) The Point A is 15mm above H.P, 35mm in front of V.P

A → 15mm above H.P  
35mm in front V.P



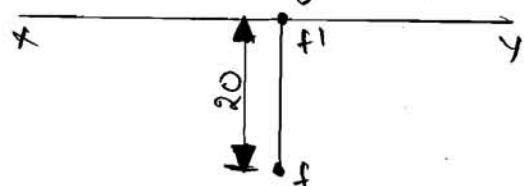
II) The point B is 40mm above H.P, 25mm behind V.P.

B → 40mm above H.P  
25mm behind V.P



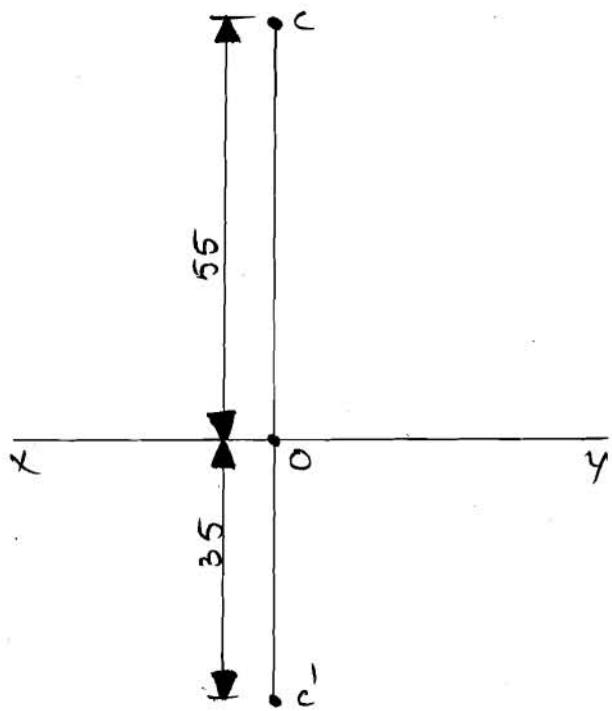
(III) The point F is on the H.P and 20 mm in front of V.P.

F → F on the H.P  
20mm in front V.P



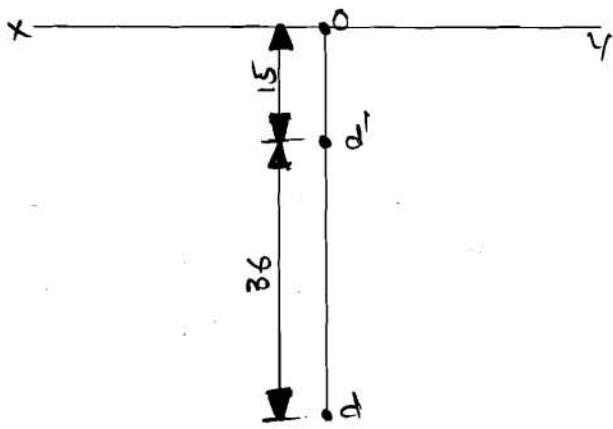
III) The point 'c' is 35mm below H.P, 55mm behind V.P.

c → 35mm below H.P  
55mm behind V.P



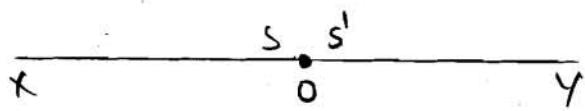
(IV) The point 'D' is 15mm below H.P, 36mm in front of V.P

D → 15mm below H.P  
36mm in front V.P.



(IX) The point 'S' both on the H.P and V.P.

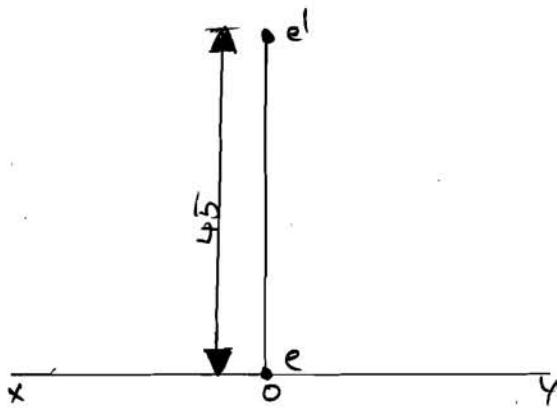
S → on the H.P  
on the V.P



V

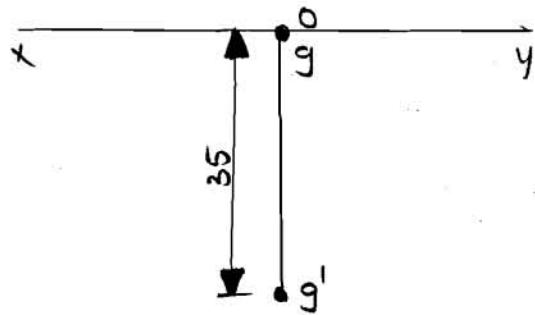
The Point E' on the V.P and 45mm above H.P

E → Point on the V.P  
45mm above H.P.



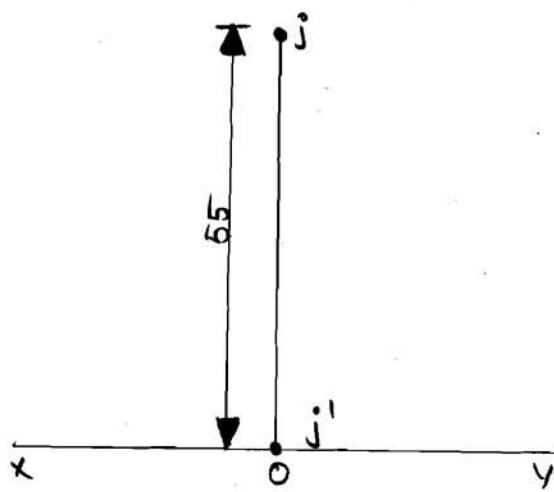
(VII) The point G' is on the V.P and 35mm below H.P

G → on the V.P  
35mm below H.P.



(VIII) The point J on the H.P and 55mm behind V.P.

J → point is on H.P  
55mm behind V.P



1. State the quadrants in which the following points are situated.

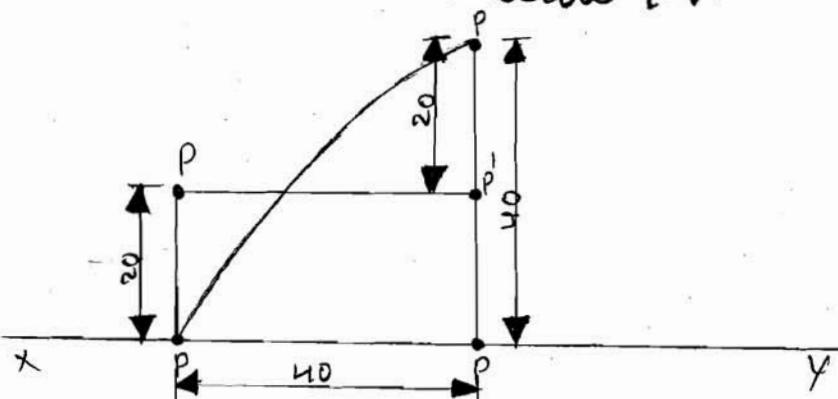
a) P' its top-view is 40mm above XY.

Frontview 20mm below the top-view.

b) The point Q' its projections coincide with each other  
40mm below XY.

Ans. a) P  $\rightarrow$  T.V 40mm above XY

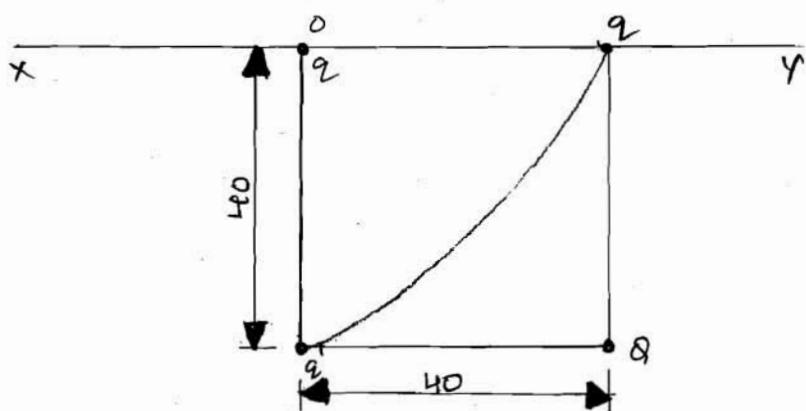
F.V 20mm below T.V.



'P lies in second quadrant.

b) Q  $\rightarrow$  coincide with each other

40mm below XY



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A point 'P' is 15mm above H.P and 20mm in front of V.P. Another point 'Q' is 25mm behind V.P and 40mm below H.P. Draw the projections of P and Q keeping the distance between their projectors equal to 90 mm draw st. lines joining.

(i) Their top-views

(ii) Their front views.

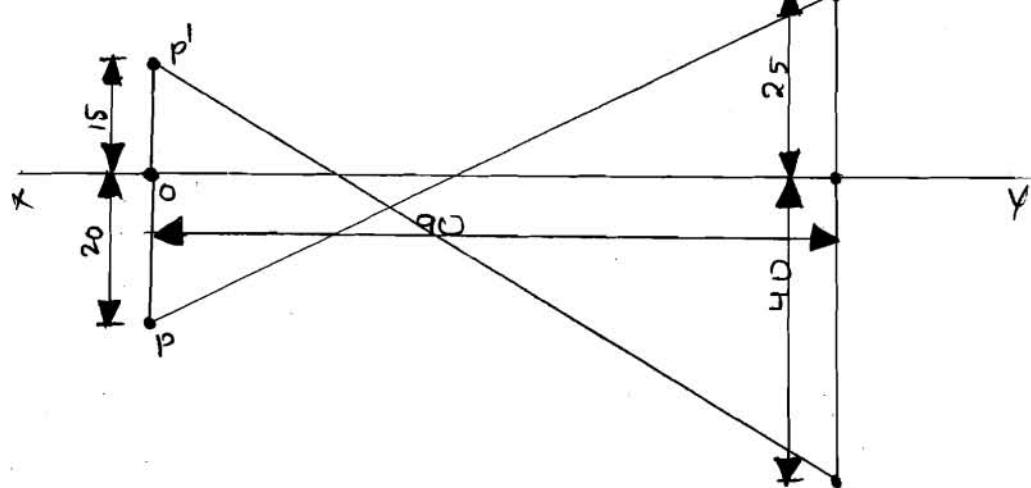
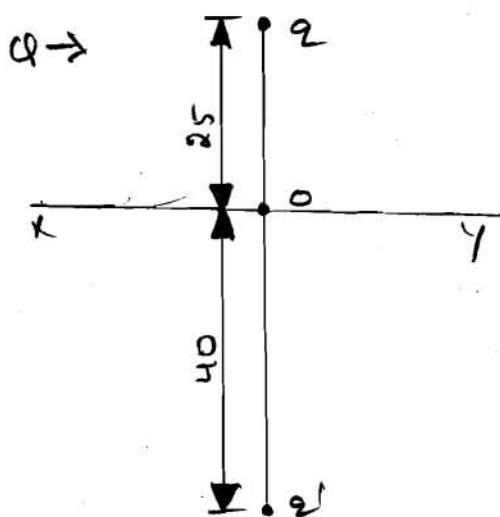
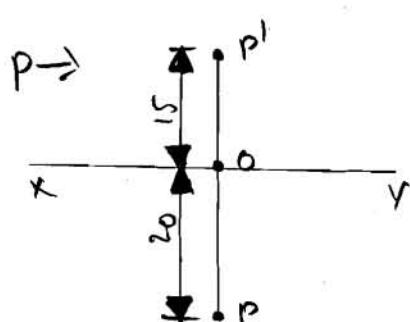
P  $\rightarrow$  15mm above H.P

20mm in front V.P

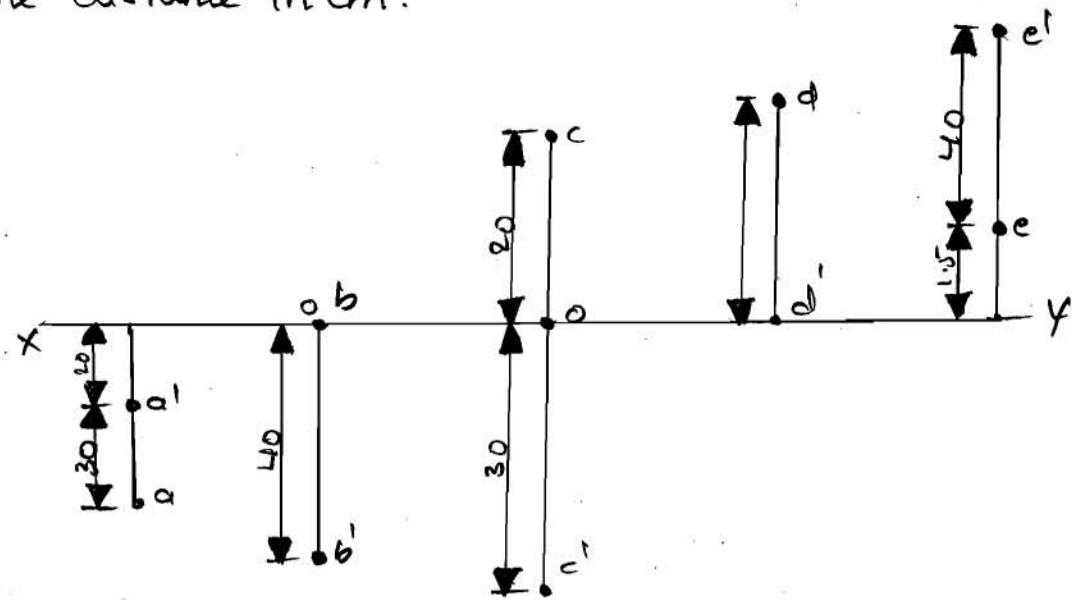
Q  $\rightarrow$  25mm behind V.P

40mm below H.P.

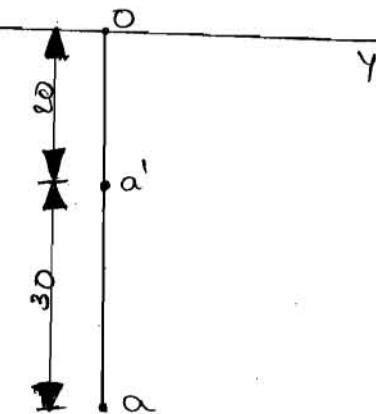
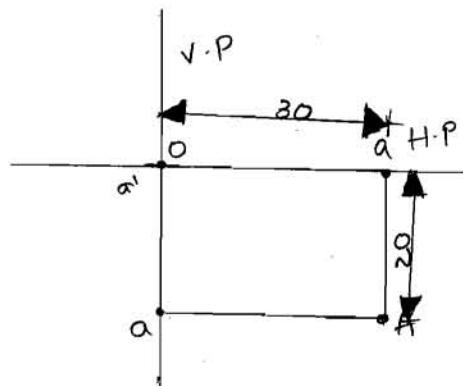
distance b/w their projectors is 90mm.



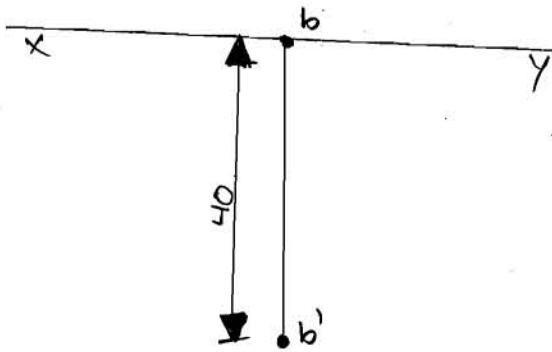
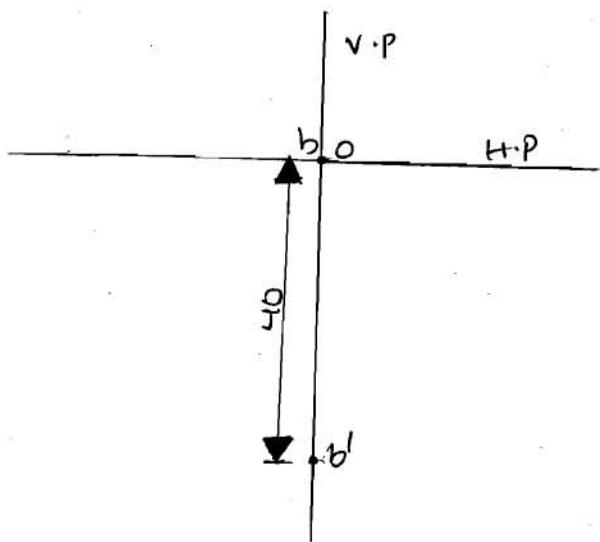
3. Projection of various points are given in the figure state the position of each point with respect to reference planes giving the distance in cm.



(i) A  $\rightarrow$  30mm  $\rightarrow$  V.P  
 20mm  $\downarrow$  H.P

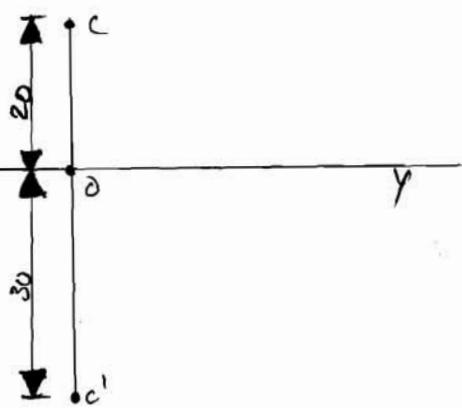
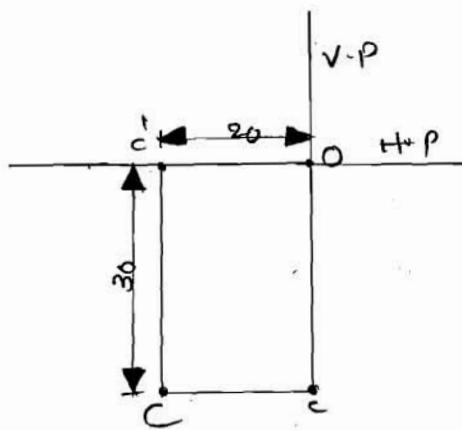


(ii) B  $\rightarrow$  on the V.P  
 40mm  $\downarrow$  H.P



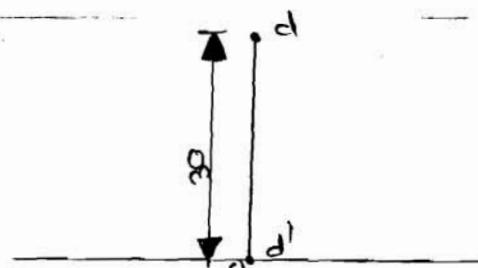
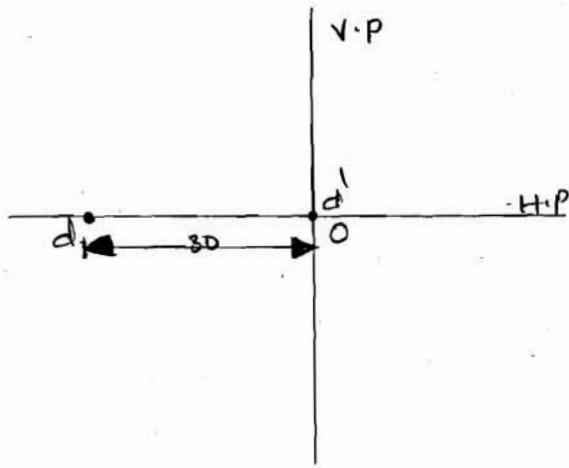
(iii)

C → 30 mm ↓ H.P.  
20 mm ← V.P.



(iv)

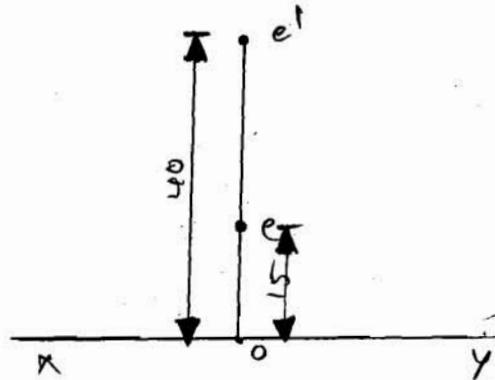
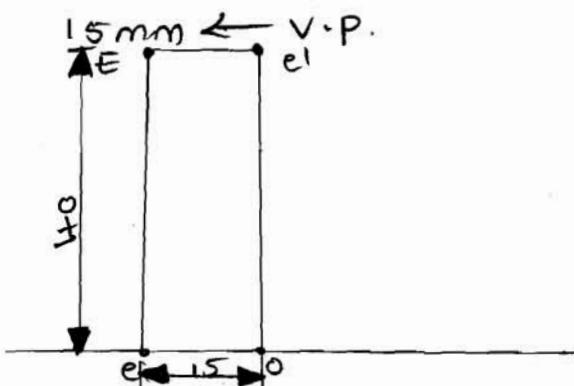
D → on the H.P.  
30 mm ← V.P.



(v)

E → 40 mm ↑ H.P.

15 mm ← V.P.

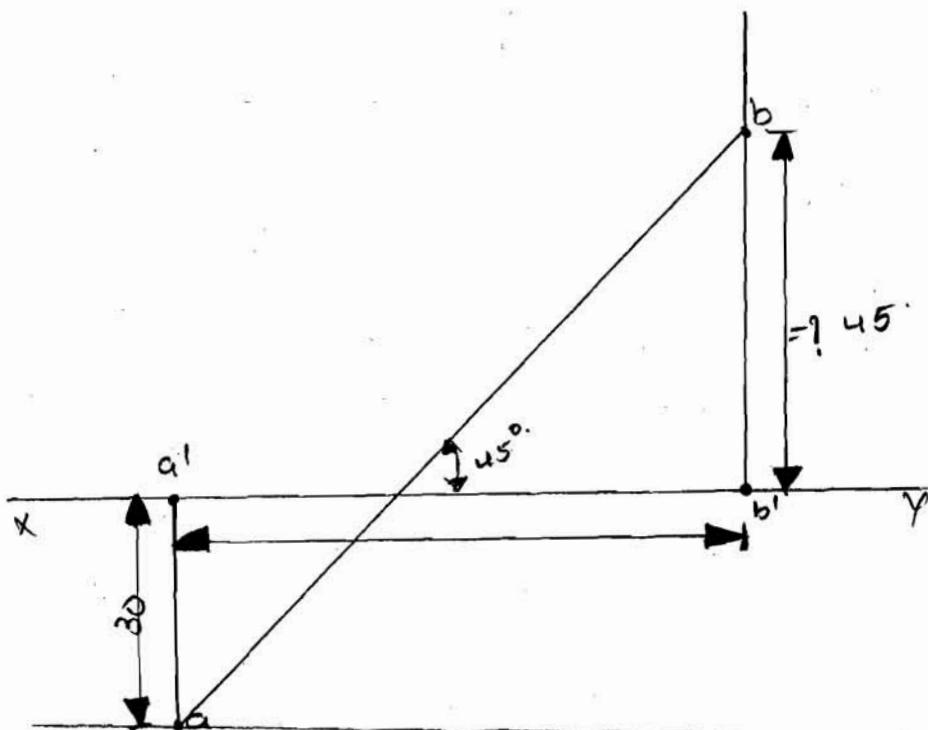


Q: Two points 'A' and 'B' are in the H.P. The Point 'A' is 30 mm in front of V.P, while 'B' is behind the V.P - The distance b/w their projectors is 75mm and their line joining their H.P views makes an angle of  $45^\circ$  with XY. Find the distance of the Point 'B' from V.P.

Ans: A  $\rightarrow$  30mm in front of V.P

B  $\rightarrow$  behind the V.P = ?

Distance b/w their projectors = 75mm.



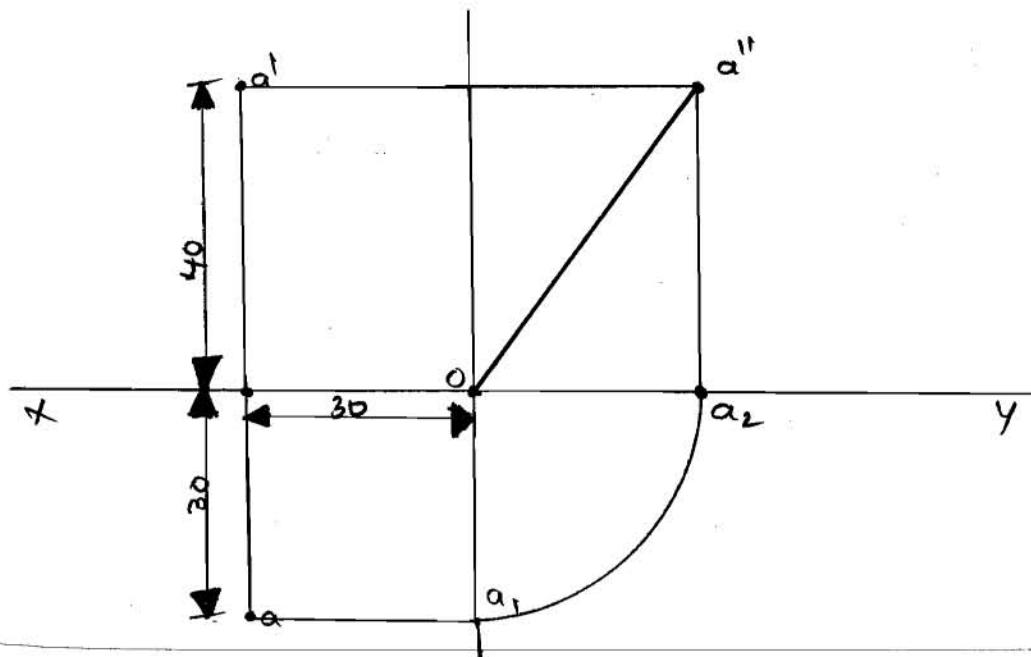
Q: The point 'Q' is situated in first quadrant. It is 40mm above H.P and 30 mm in front of V.P. Draw its projections and find its shortest distance from the intersection of H.P, V.P and auxiliary plane.

Ans: Q  $\rightarrow$  in first quadrant

40mm  $\uparrow$  H.P

30mm  $\rightarrow$  V.P

auxiliary plane = ?



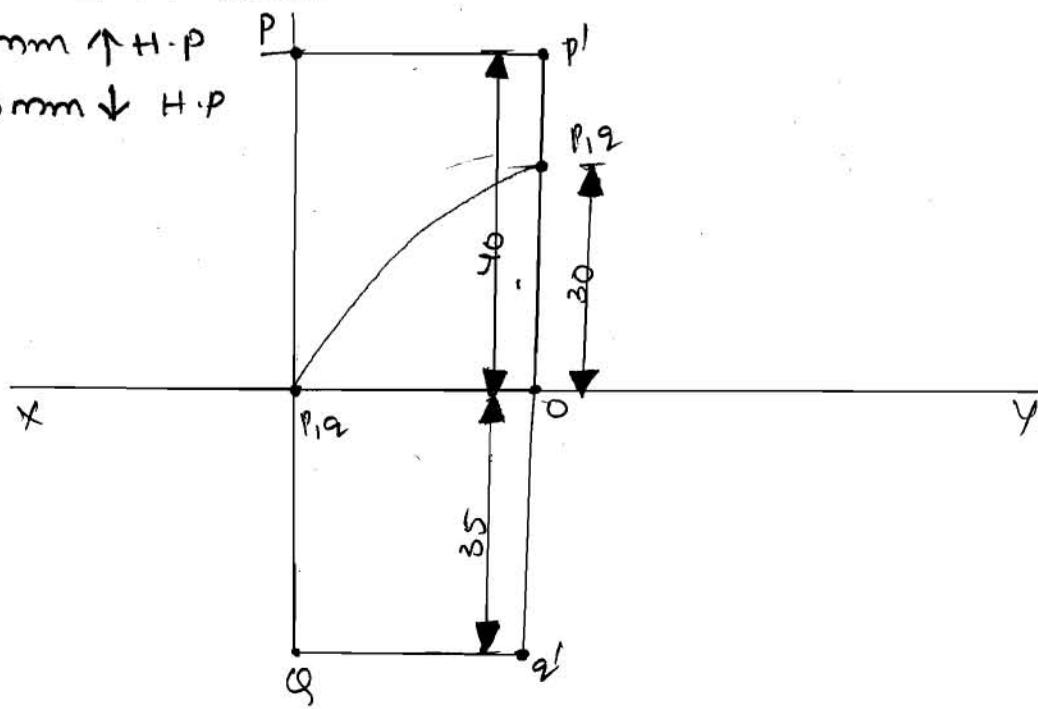
Q: A point 30 mm above XY line is the plan view (top view) of two points P and Q. The elevation of P' is 45 mm above H.P., while that of the point Q' is 35 mm below the H.P. Draw the projections of point and state their positions with reference to the Principle planes and the quadrant in which they lie.

Ans:

Both P and Q T.V = 30mm

P  $\rightarrow$  45mm  $\uparrow$  H.P

Q  $\rightarrow$  35mm  $\downarrow$  H.P

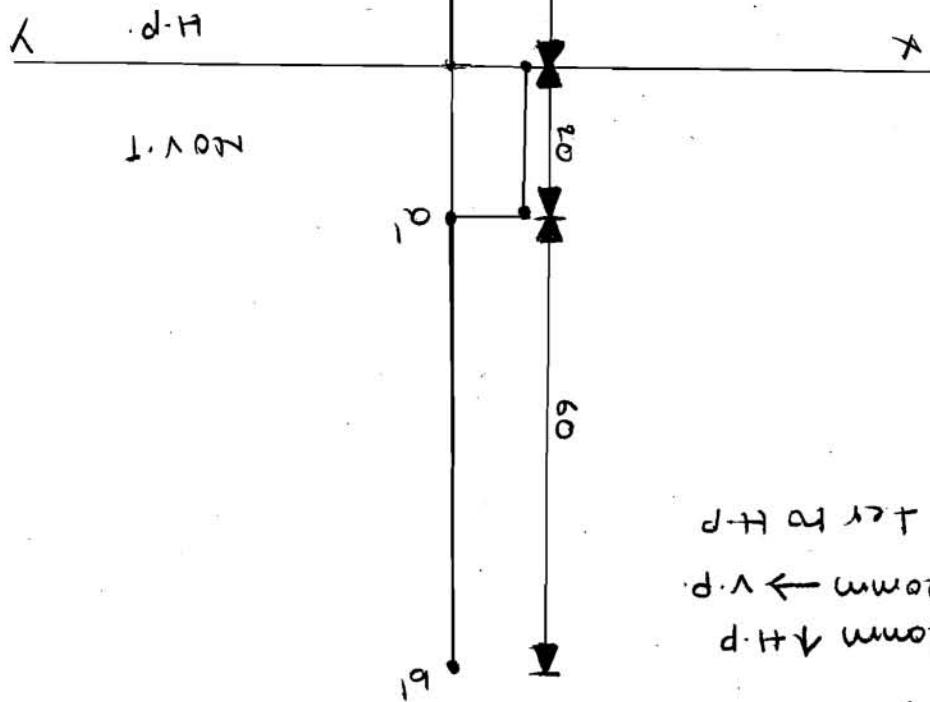


## **Projections of Straight Lines:**

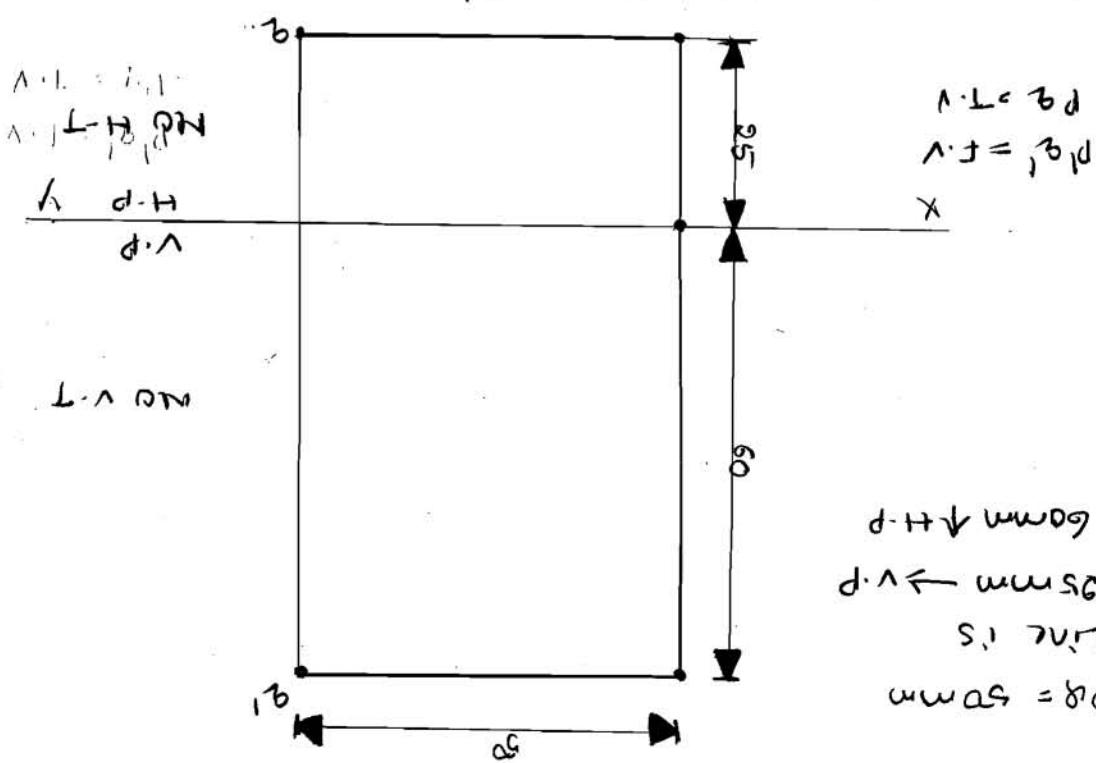
A straight line is the shortest distance between two points. Hence, the projections of a straight line may be drawn by joining the respective projections of its ends which are points.

The position of a straight line may also be described with respect to the two reference planes. It may be:

1. Parallel to one or both the planes.
2. Contained by one or both the planes.
3. Perpendicular to one of the planes.
4. Inclined to one plane and parallel to the other.
5. Inclined to both the planes.
6. Projections of lines inclined to both the planes.
7. Line contained by a plane perpendicular to both the reference planes.
8. True length of a straight line and its inclinations with the reference planes.
9. Traces of a line.
10. Methods of determining traces of a line.
11. Traces of a line, the projections of which are perpendicular to  $xy$ .
12. Positions of traces of a line.



A 60mm long line AB has its end A 20mm above H.P. - The line is 45° to H.P. and 40mm in front of V.P. Draw its projections and locate its traces?



A 50mm long line PQ is parallel to both H.P. and V.P. If its 25mm in front of V.P. and 60mm above H.P. Draw its projections and determine its traces.

3. A 60mm long line AB has its end A is 20 mm in front of V.P. The line is 40 mm above the H.P. - Draw its projections and locate its traces.  $v' b'(a')$

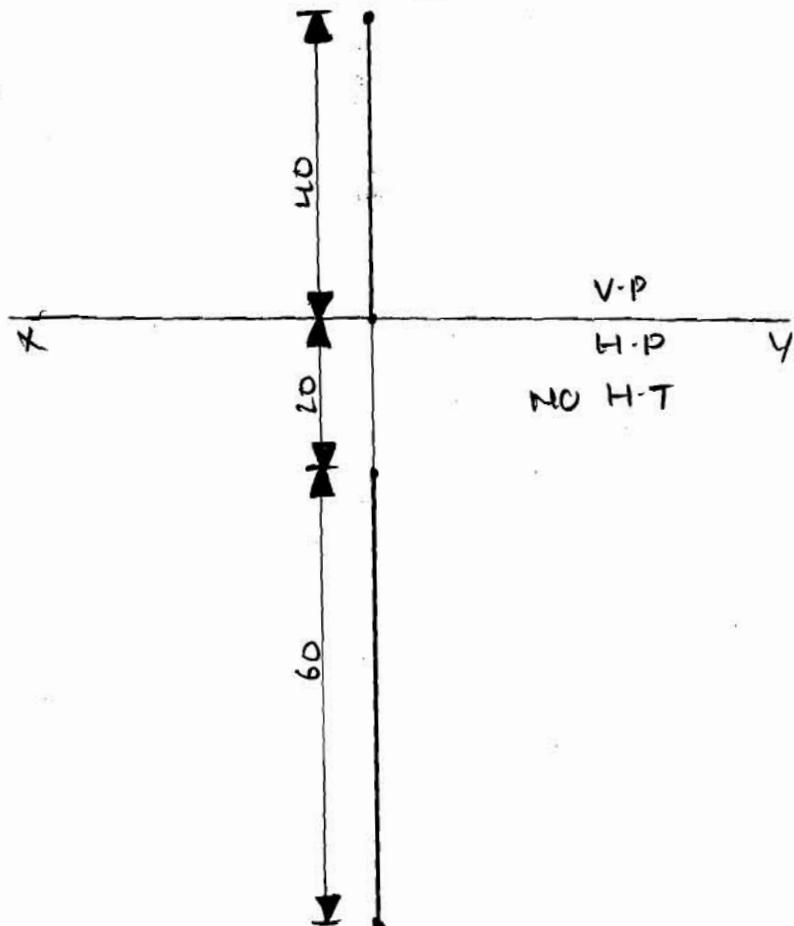
An!

$$AB = 60\text{mm}$$

$A \rightarrow$  20 mm in front V.P.

$$= 40\text{mm} \uparrow \text{H.P}$$

Line ter to v.p.



4. A 90mm long line AB has end A at distance of 20mm above H.P and 40mm in front of V.P. - The line is inclined at  $30^\circ$  to H.P and is parallel to V.P. Draw the projections of the line and determine its traces

An.

$$\Omega \rightarrow \text{H.P}$$

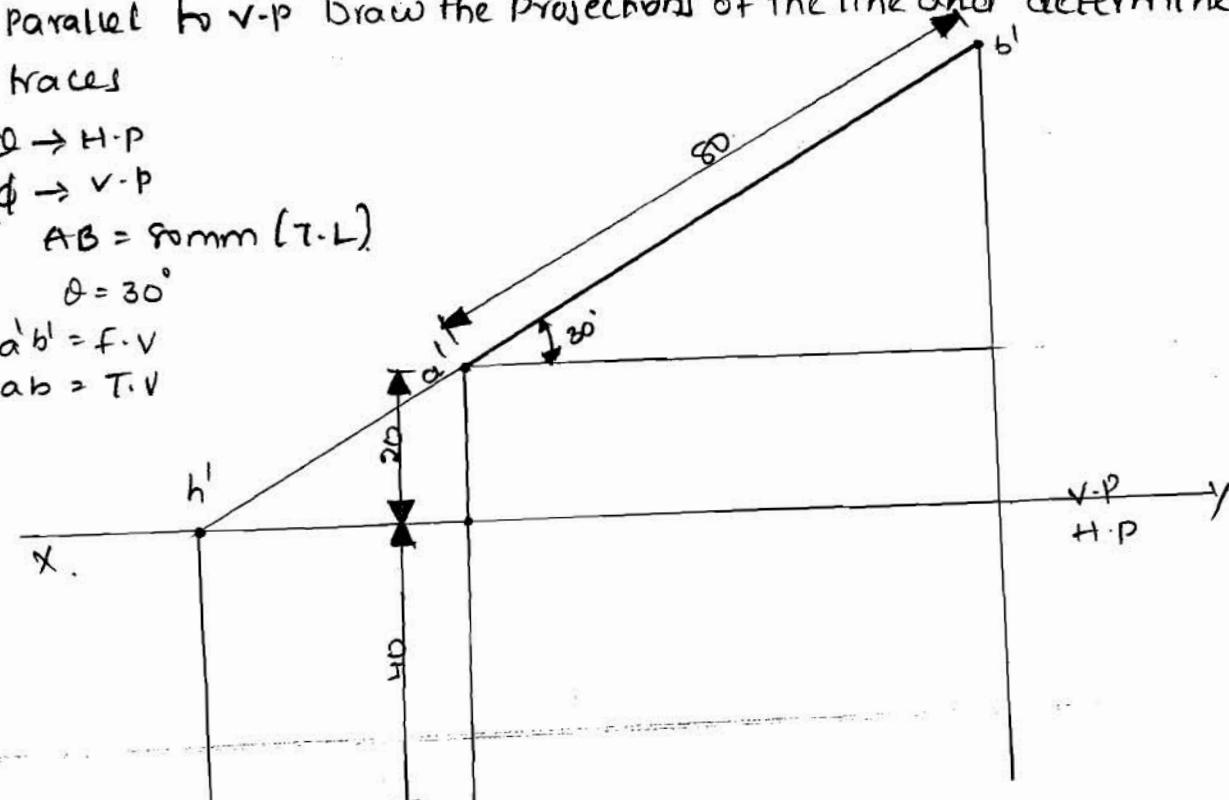
$$\phi \rightarrow \text{V.P}$$

$$AB = 90\text{mm} (\text{T.L})$$

$$\theta = 30^\circ$$

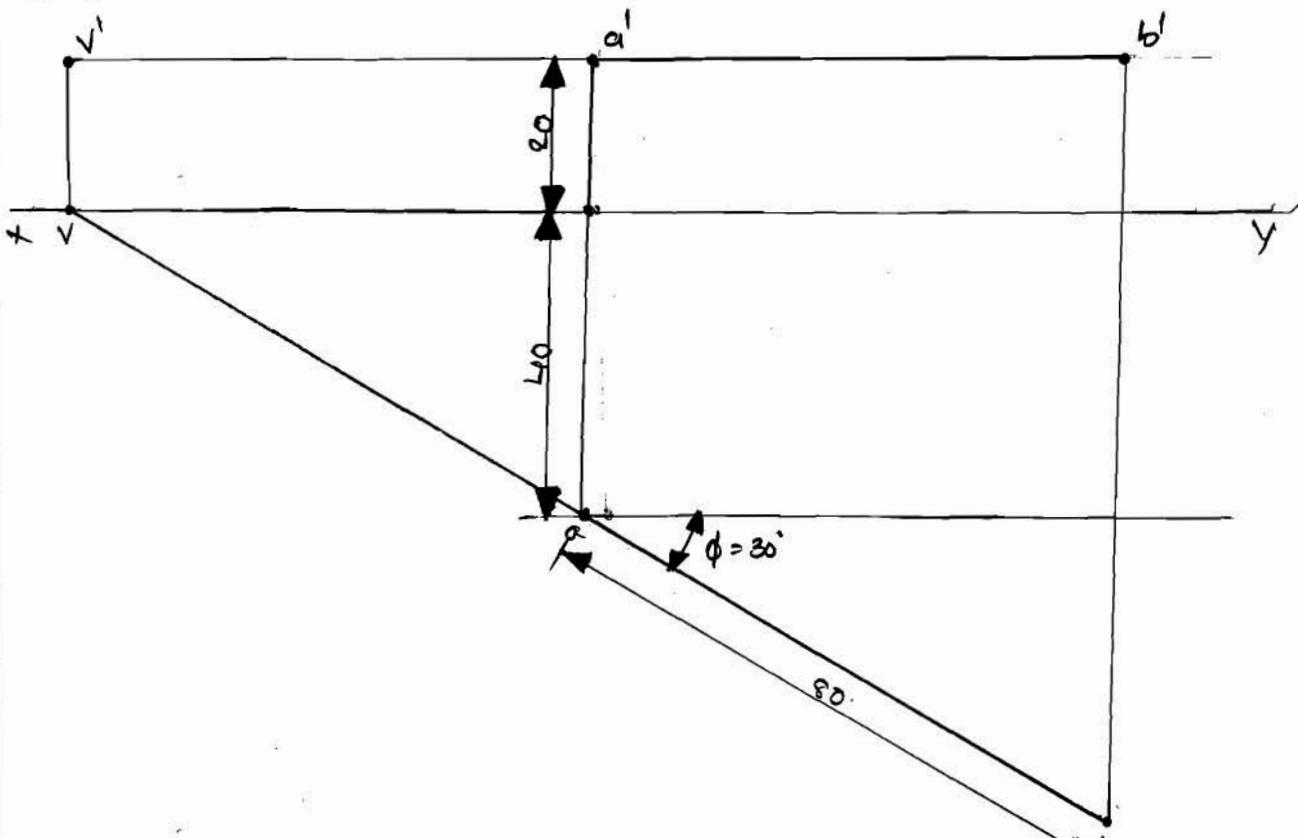
$$a'b' = f \cdot V$$

$$ab = T \cdot V$$

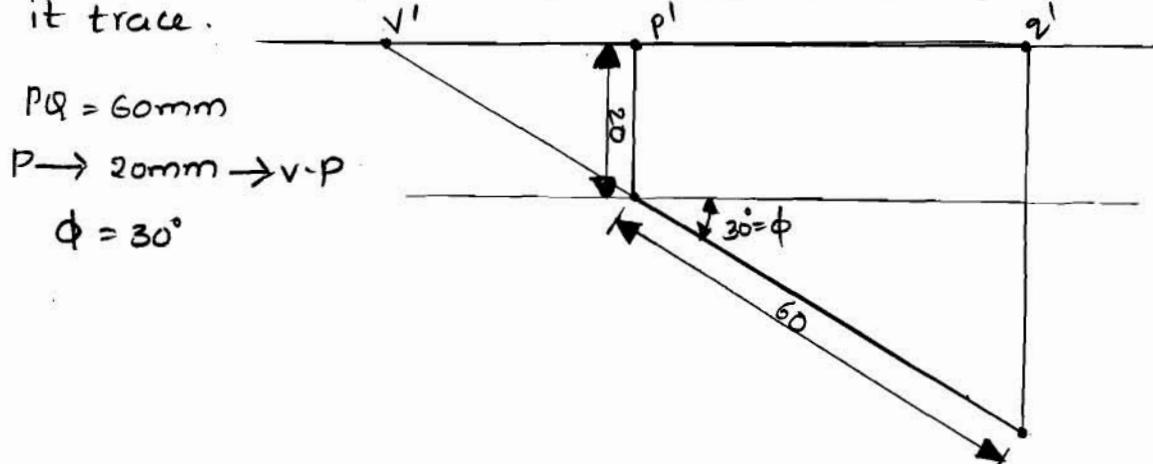


5. A 80mm long line AB is inclined at  $30^\circ$  to V.P and parallel to H.P - The end 'A' of the line is 20mm above the H.P and 40mm in front of the V.P. Draw the projections of the line and determine its traces.

$$AB = 80 \text{ mm} \\ A \rightarrow 20 \text{ mm} \rightarrow \text{H.P} \quad B \rightarrow 40 \rightarrow \text{V.P} \quad \phi = 30^\circ$$

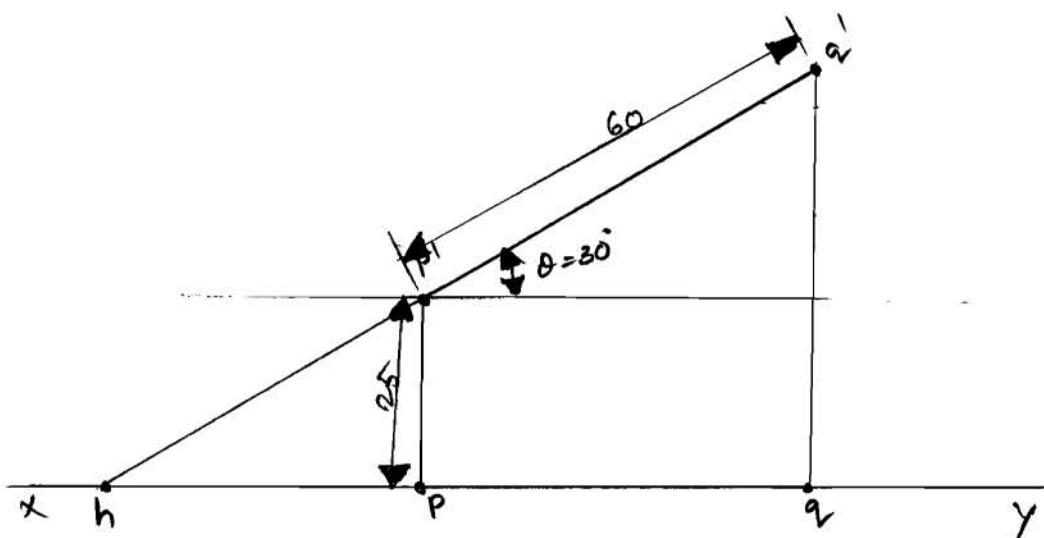


6. A 60mm long line PQ is situated in H.P and is inclined at  $30^\circ$  to V.P. The end 'P' of the line is situated 20mm in front of V.P. Draw the projections of the line and determine its trace.



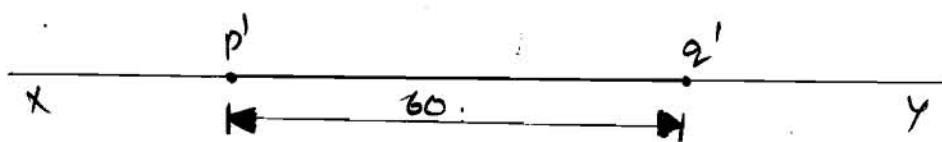
7. Draw the projections of a 60mm long line  $p'q'$  is in the V.P and inclined at  $30^\circ$  to H.P. The end  $p'$  of the line is 25mm above the H.P. Also determine the traces of the line.

Ans  
 $p'q' = 60 \text{ mm}$   
 $P \rightarrow 25 \text{ mm } \uparrow \text{H.P}$   
 $\theta = 30^\circ$



8. Draw the projections of a 60mm Long Line  $PQ$ , which is situated in H.P and V.P both. Also determine the traces of the line.

Ans  
 $PQ = 60 \text{ mm}$



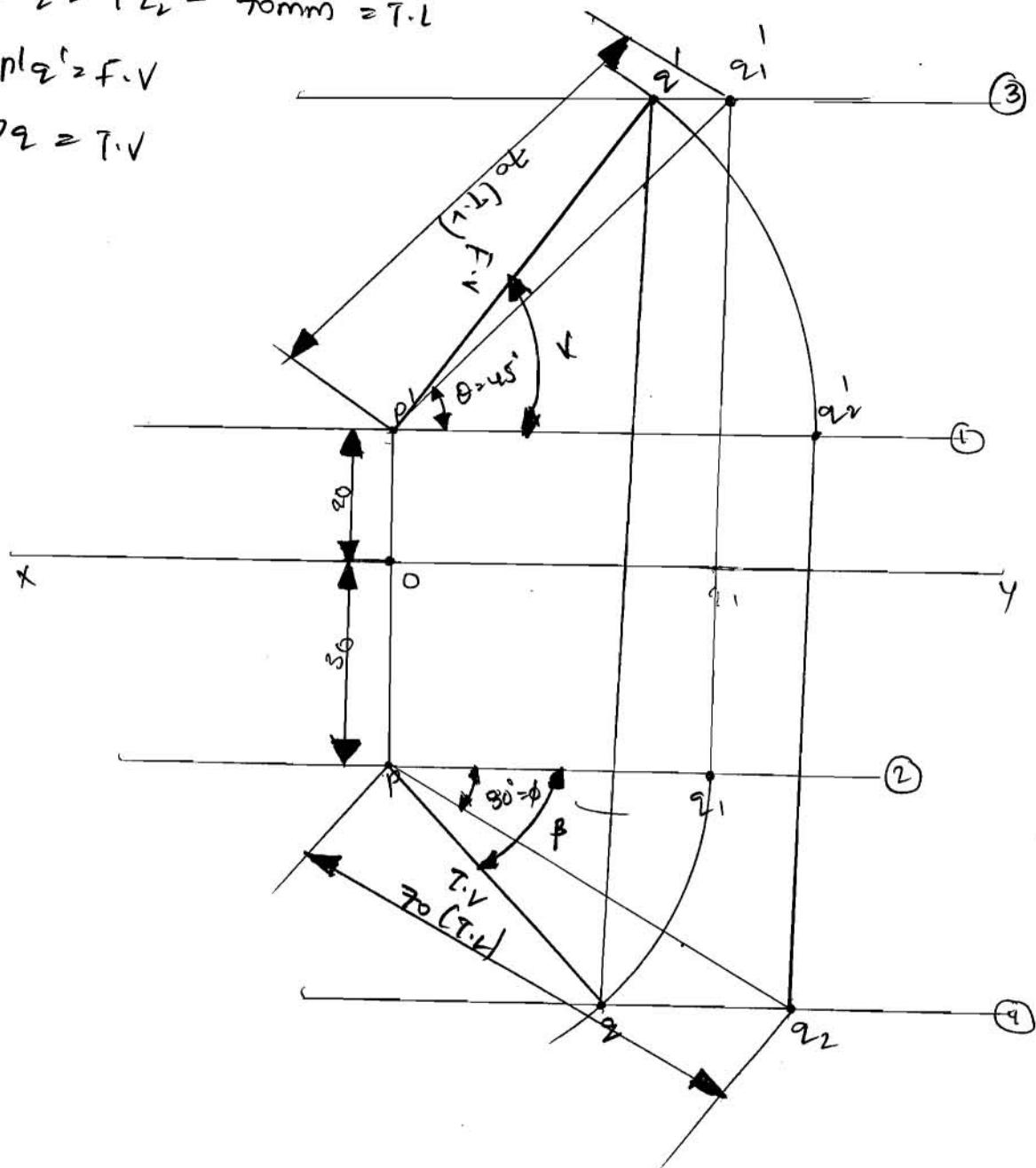
9. A 70mm long line PQ has its end 'P' is 20mm above H.P and 30mm in front of V.P - The line is inclined at  $45^\circ$  to H.P and  $30^\circ$  to V.P. Draw its projections.

Ans:-

$$P'Q' = PQ = 70\text{mm} = 7.1$$

$$PQ = f.v$$

$$PQ = 7.v$$



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A straight Line 'PQ' as its end 'P' is 20mm above H.P and 30 mm in front of V.P and the end 'Q' is 80mm above H.P and 70 mm in front of V.P. If the end projectors are 60mm apart draw the projections of the line determine the true length ( $T.L$ ) and True inclinations with reference planes.

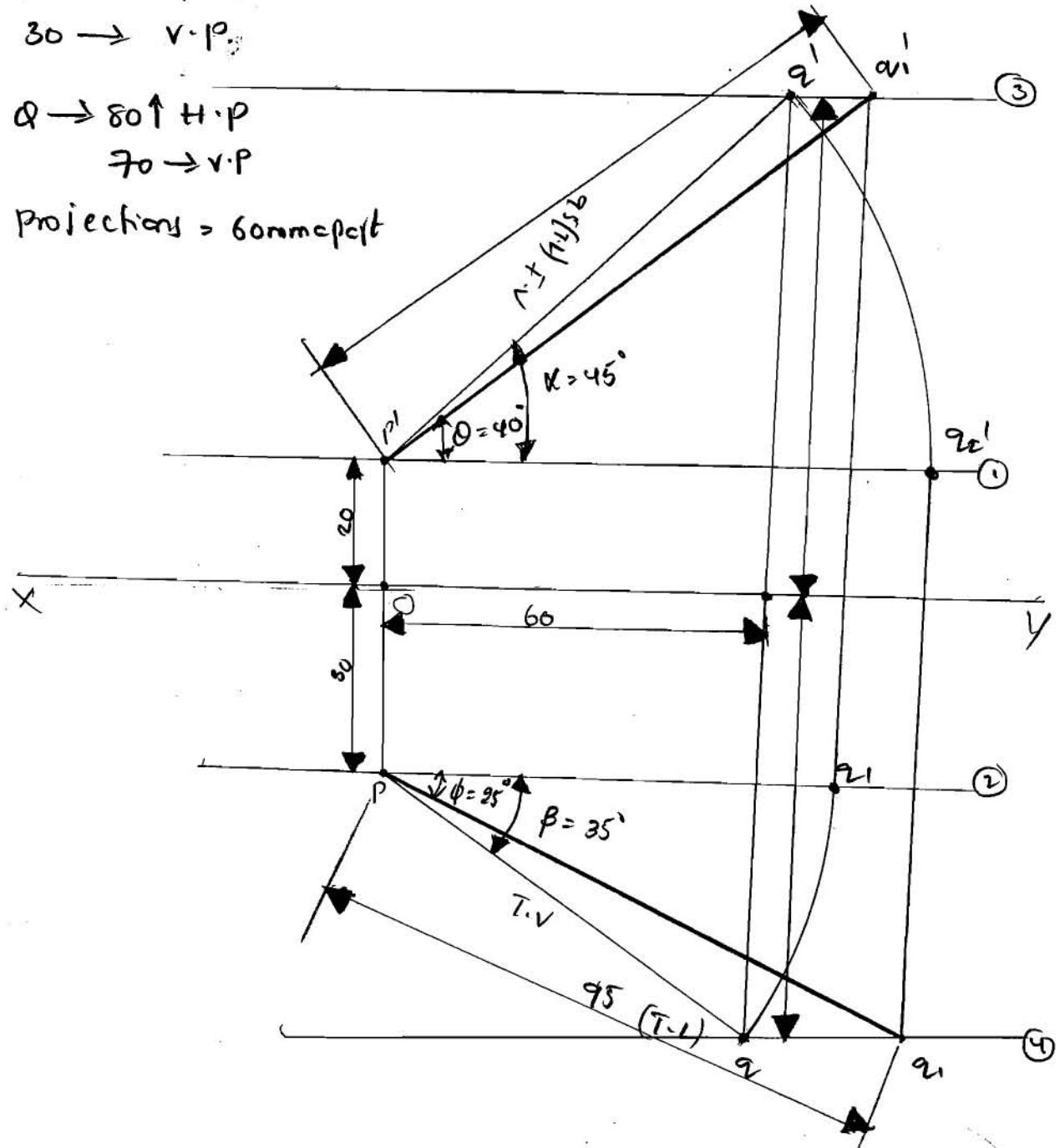
$P \rightarrow 20 \uparrow H.P$

$30 \rightarrow V.P$

$Q \rightarrow 80 \uparrow H.P$

$70 \rightarrow V.P$

Projections = 60mm each

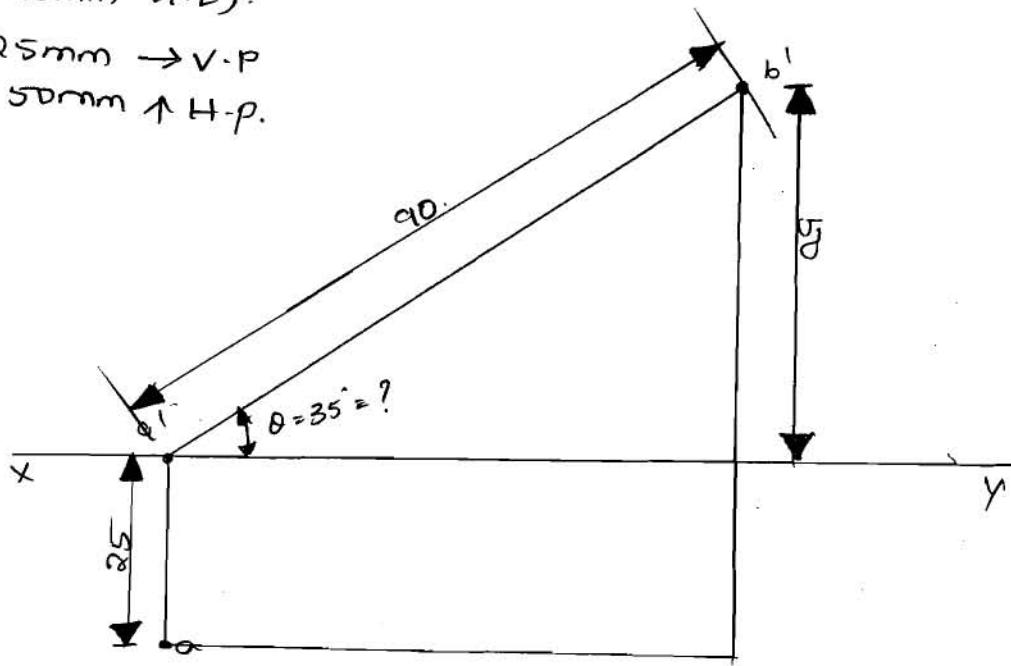


1. A 90mm long line is parallel to and 25mm in front of v.p. Its one end is in the H.P. while the other is 50mm above the H.P. Draw its projections and finds its inclination with the H.P.

Ans -  $AB = 90\text{mm}$  (T.L.).

25mm  $\rightarrow$  V.P

50mm  $\uparrow$  H.P.

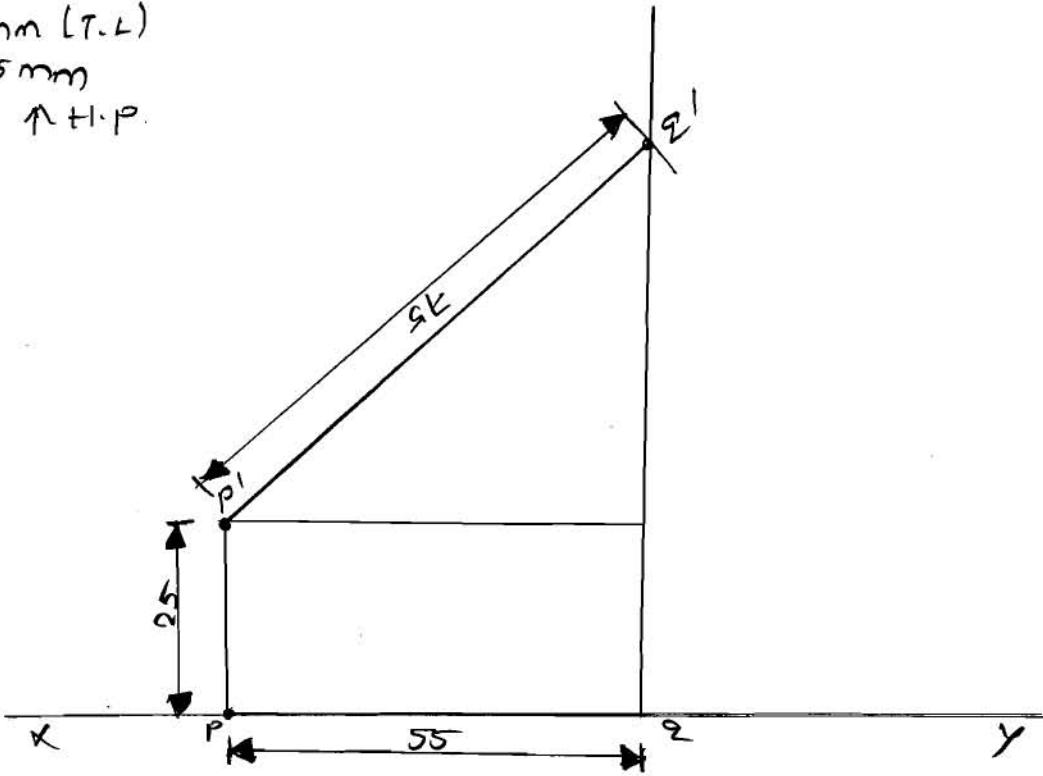


2. The topview of 75mm Long line measures 55mm. The line is in the v.p. Its one end is being 25mm above H.P. Draw its projections.

Ans  $PQ = 75\text{mm}$  (T.L.)

T.V = 55 mm

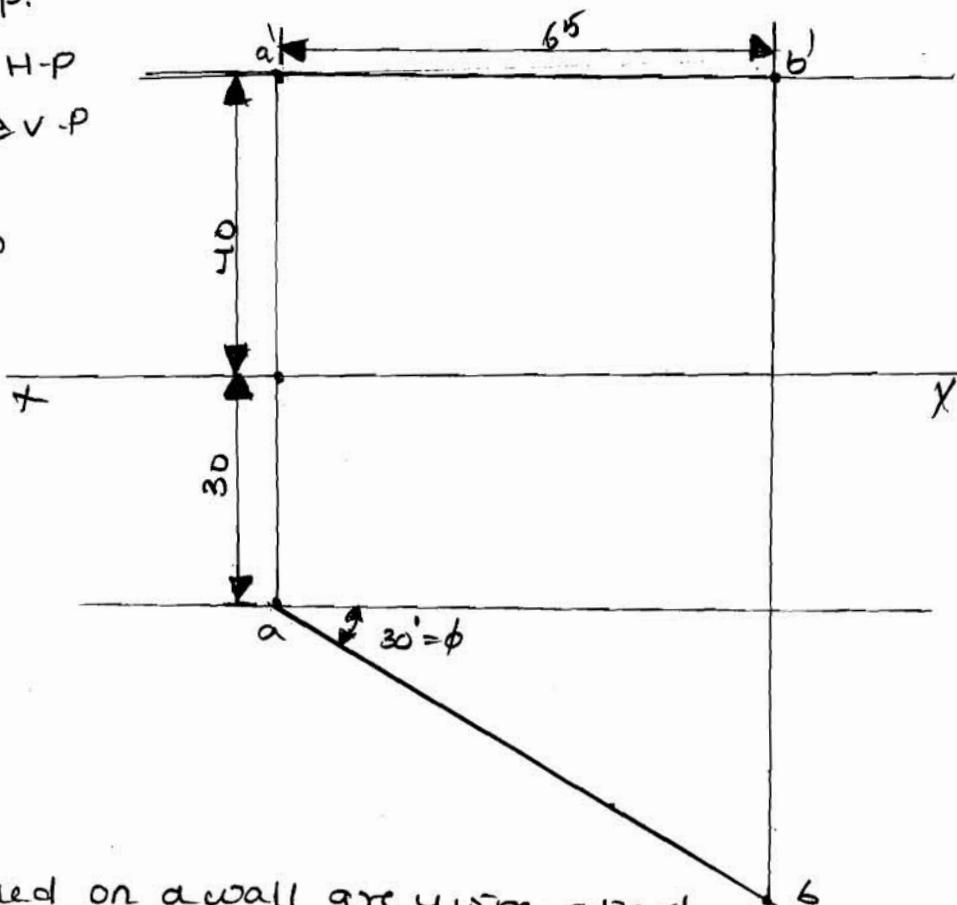
25mm  $\uparrow$  H.P.



3. The front view of a long line inclined at  $30^\circ$  to v.p. is 60 mm long. Draw the projections of the line when it is parallel to and 40 mm above the H.P. its one end being 30 mm in front of V.P.

Ans:

$$\begin{aligned} A \rightarrow 40 \text{ mm} &\uparrow \text{H.P} \\ 30 \text{ mm} &\rightarrow \text{V.P} \\ \phi = 30^\circ & \\ AB = 60 \text{ mm} & \end{aligned}$$



5. Two pegs fixed on a wall are 4.5m apart. The distance b/w the pegs measured parallel to the floor is 3.6m. If one peg is 1.5m above the floor, find the height of second peg and the inclination of the line joining the two pegs with the floor,

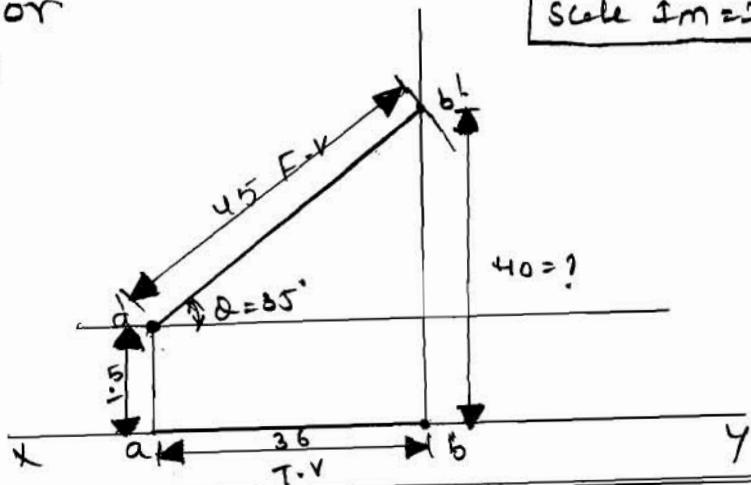
$$\text{Distance b/w the two pegs} = 3.6 \text{ m} = T.V.$$

with respect to floor

Actual distance b/w

$$\text{them} = 4.5 \text{ m}$$

Scale 1m = 5cm



4. A vertical line AB, 75mm long has its end A in the H.P and 25mm in front of V.P. A line AC, 100mm long is in the H.P and parallel to the V.P. Draw the projections of the line joining B and C, determine inclination with the H.P

Ans.

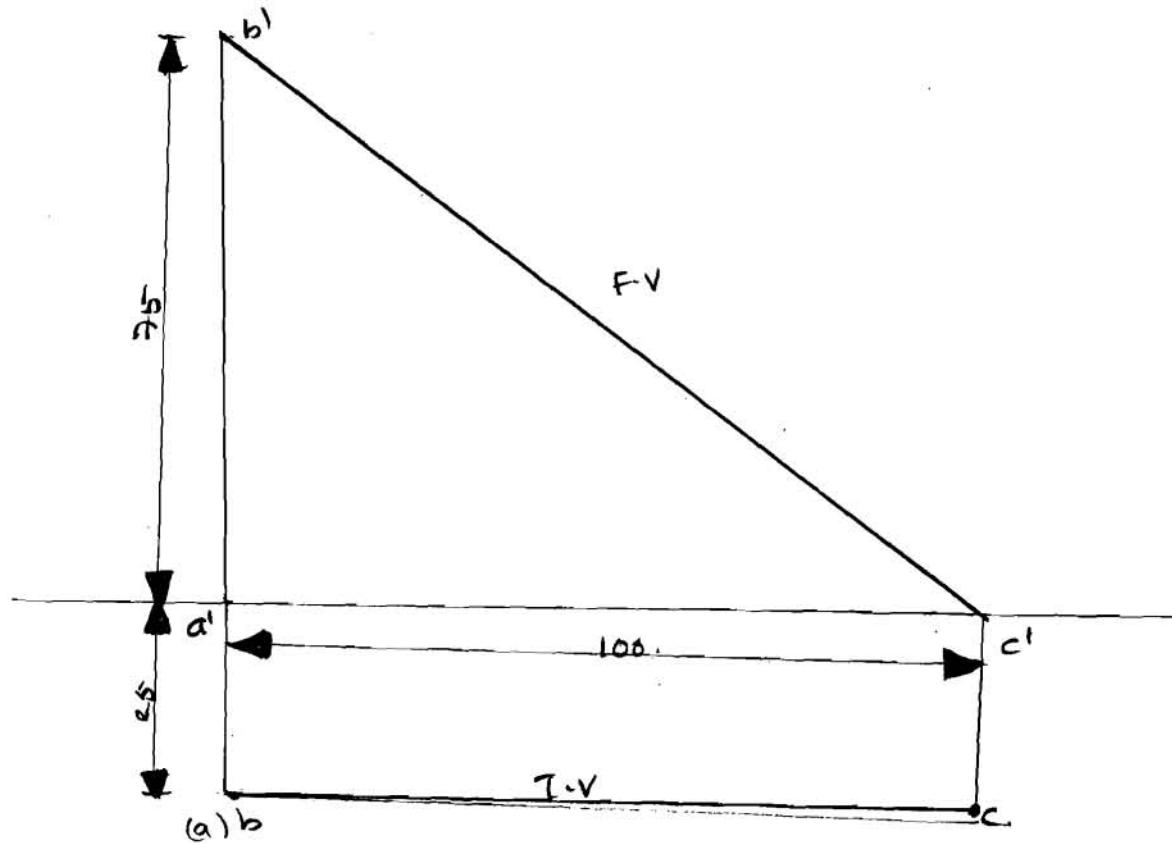
AB → Vertical line.

A → in the H.P

25mm → V.P

AC → 100mm → in the H.P but not in V.P.

BC length = ?



1. A line CD 80mm long is inclined at  $45^\circ$  to H.P and  $30^\circ$  to V.P. Its end C is in the H.P and 40mm in front of V.P. Draw the projections. Locate Traces.

Ans:

$$CD = T.L = 80\text{mm}$$

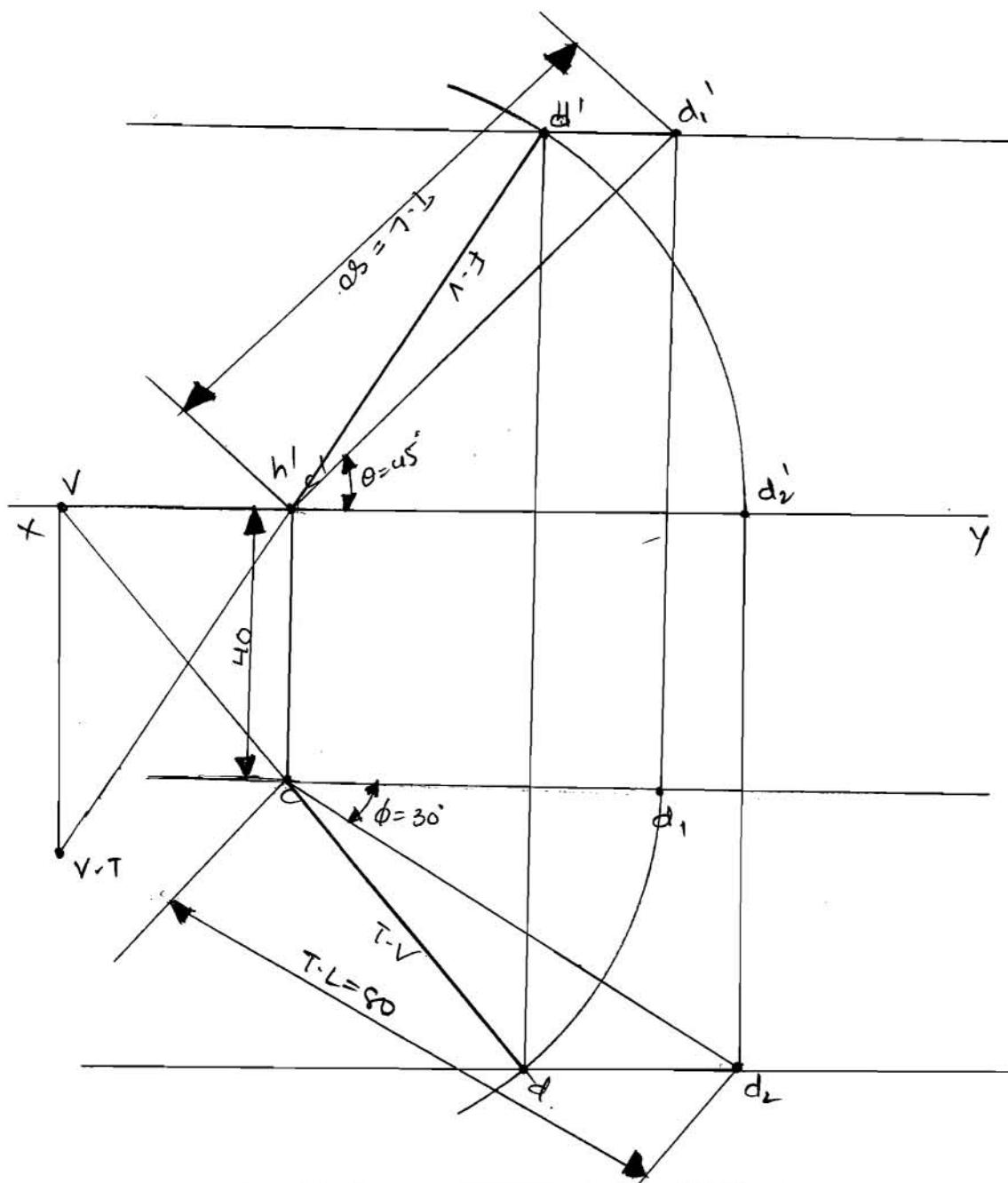
$$\theta = 45^\circ$$

$$\phi = 30^\circ$$

on the H.P and 40mm  $\rightarrow$  V.P

$$c'd' = F.V \quad cd = T.V$$

$$c'd'_1 = T.L = cd_2$$



2. A 100mm long line PQ is inclined at  $30^\circ$  to H.P and  $45^\circ$  to V.P its mid-point is 35mm above H.P and 50mm in front of V.P. Draw its projections locate traces.

Ans

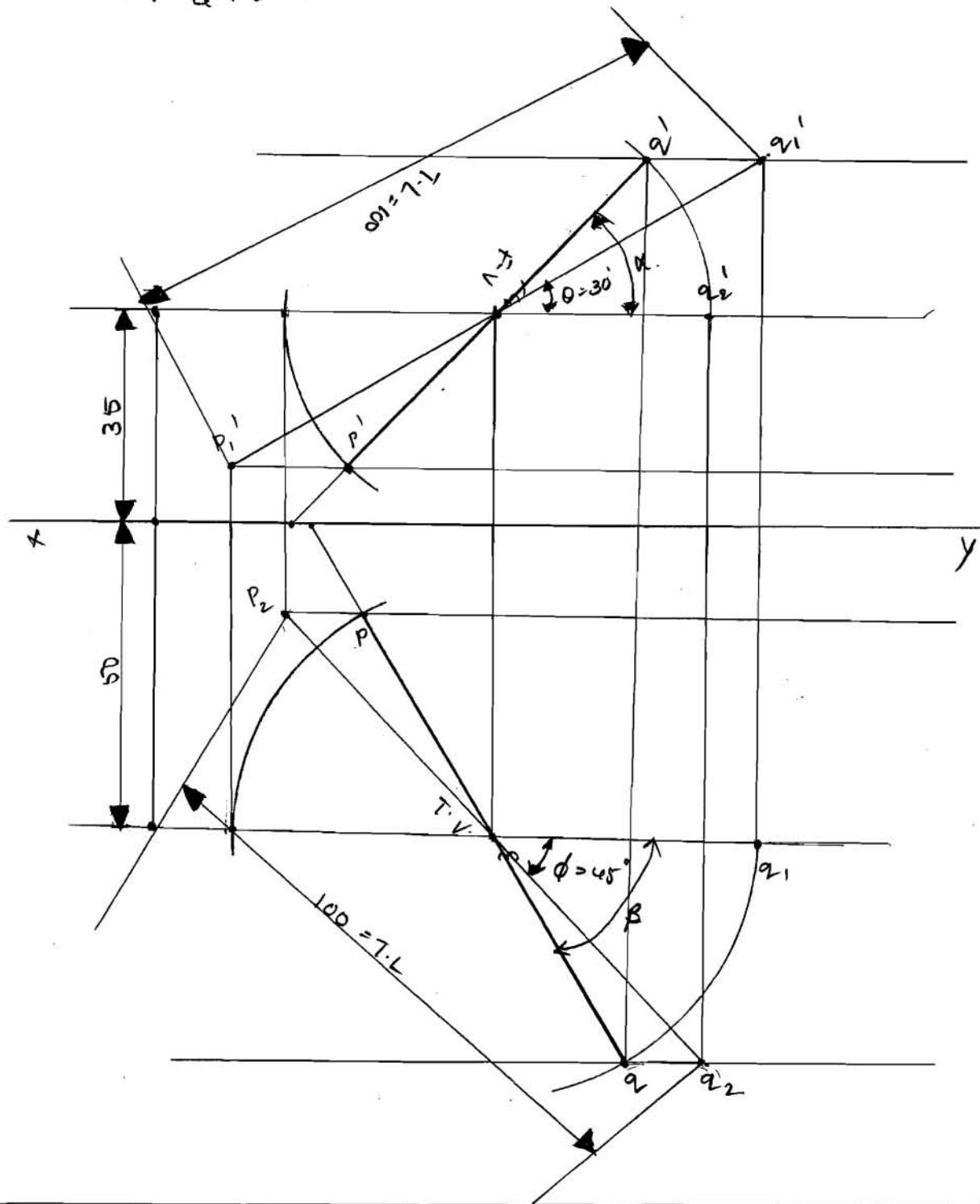
$$PQ = T.L = 100\text{mm}$$

$$\theta = 30^\circ$$

$$\phi = 45^\circ$$

35mm  $\uparrow$  H.P and 50mm  $\rightarrow$  V.P

$$PQ^T = F.V \quad \& \quad PQ = T.V$$



3. Draw the projections and find out true length of a Line AB with end B' on the H.P and 40mm in front of V.P. AB is inclined at  $30^\circ$  to H.P and  $45^\circ$  to V.P and its plan view measures 50 mm. Locate Traces.

Ans:

$$T.L = ?$$

B → in the H.P

$$40\text{mm} \rightarrow V.P$$

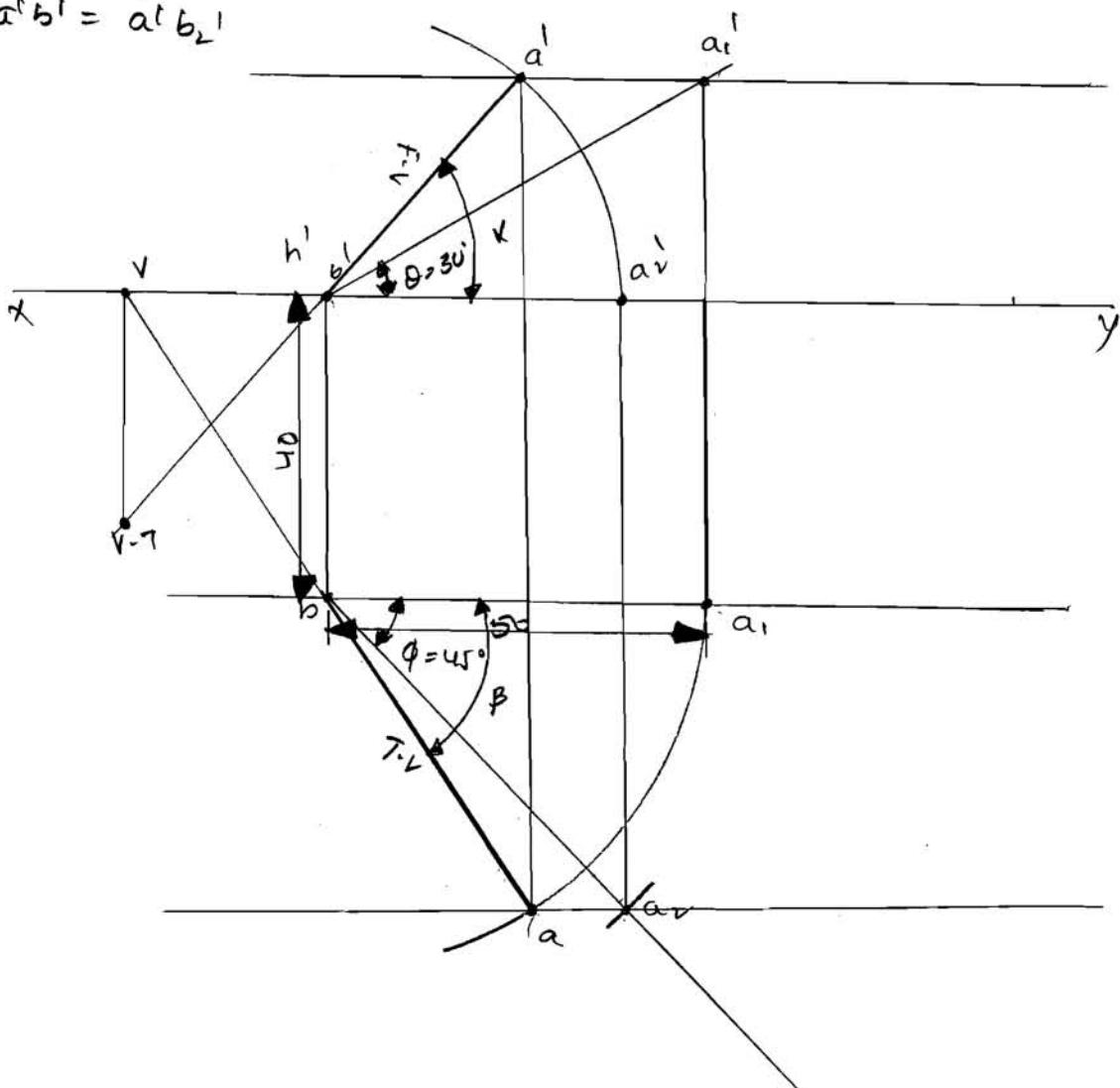
$$\theta = 30^\circ \text{ & } \phi = 45^\circ$$

$$T.V = 50\text{mm}$$

$$a'b_1' = T.L = ab_L$$

$$a'b_1' = F.V, ab = T.V$$

$$a'b_1' = a'b_2'$$



4. The top view of a 80mm long line PQ measured 65mm while the length of its frontview is 55mm its end A' is in the H.P and 12mm in front of V.P. Draw the projections of AB and determine its inclination with the H.P and V.P  
Locate Traces.

$$T.V = 65 \text{ mm}$$

$$F.V = 55 \text{ mm}$$

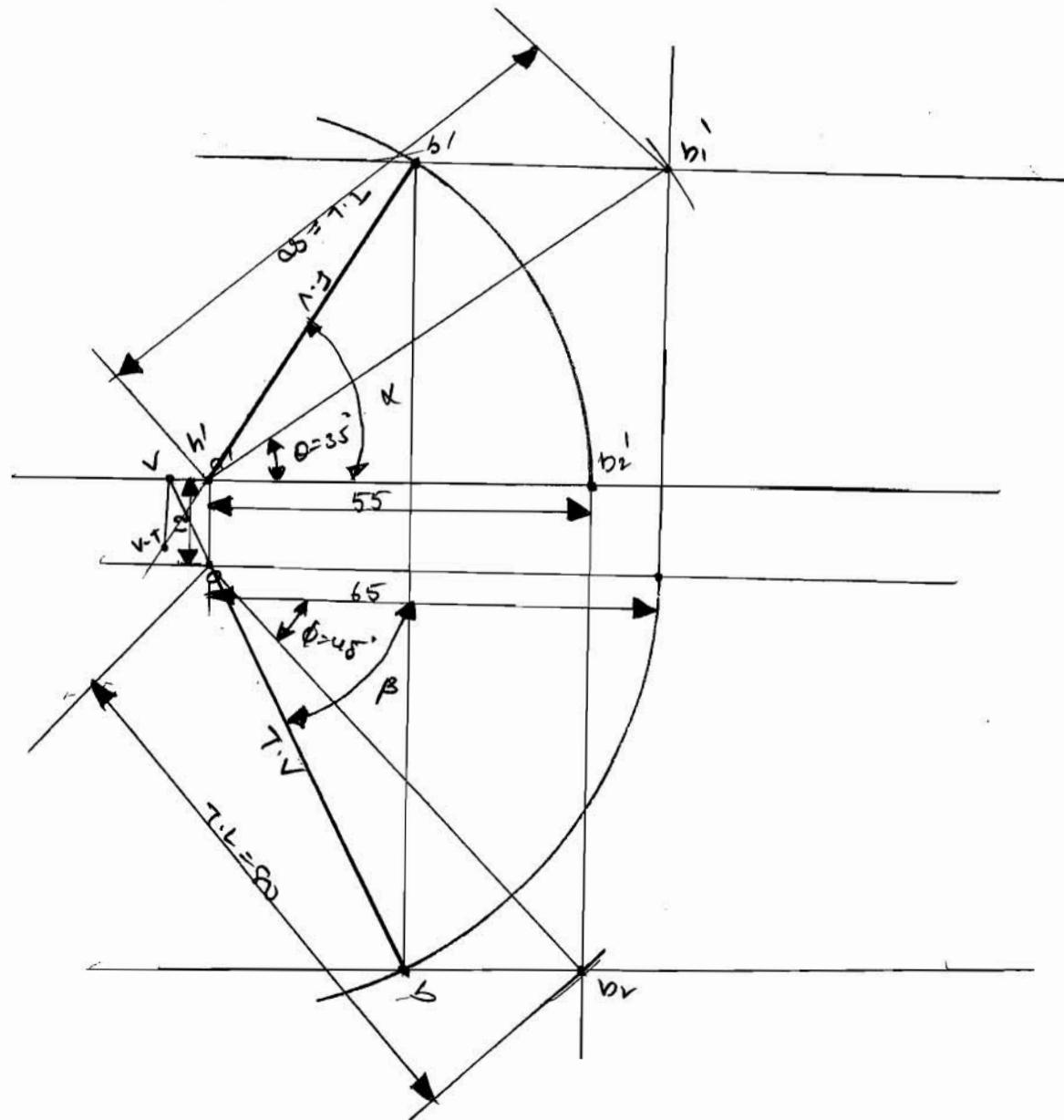
$$T.L = 80 \text{ mm}$$

A → in the H.P & 12mm → V.P

$$PQ_1' = T.L = PQ_2$$

$$PQ_1' = F.V, PQ_2 > T.V$$

$$PQ_1' = PQ_2'$$



5. A line AB 90mm long is inclined at  $45^\circ$  to H.P and its topview makes an angle of  $60^\circ$  with the V.P - The end A is in the H.P and 12 mm in front of V.P draw its f.v and find its true inclination with V.P - also locate traces.

Ans:

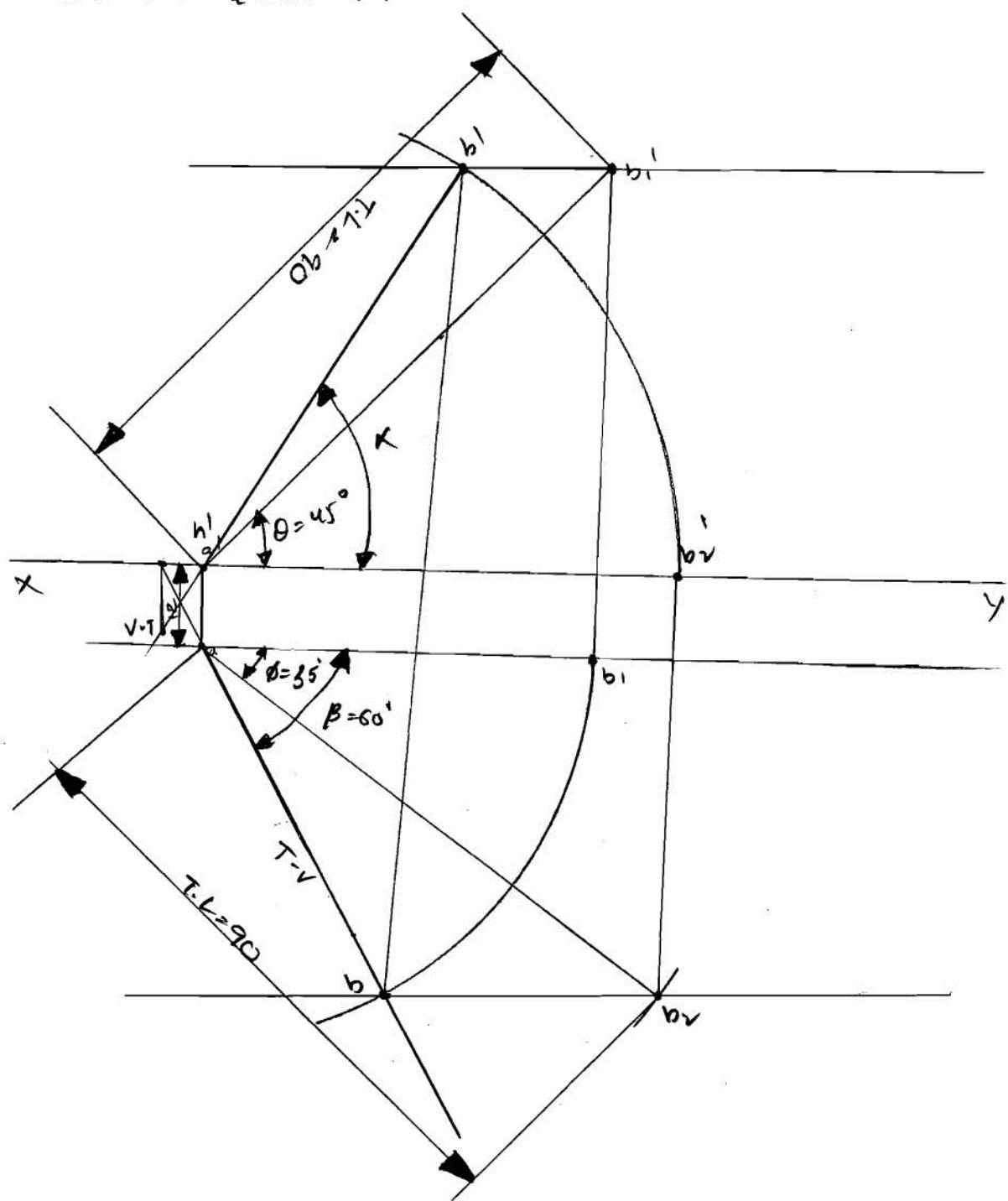
$$AB = 90\text{mm c.t.l}$$

$$\theta = 45^\circ \quad \phi = ?$$

$$\beta = 60^\circ$$

A → on the H.P and 12mm → V.P

$$a'b' = f.v \quad \& \quad ab = t.v$$



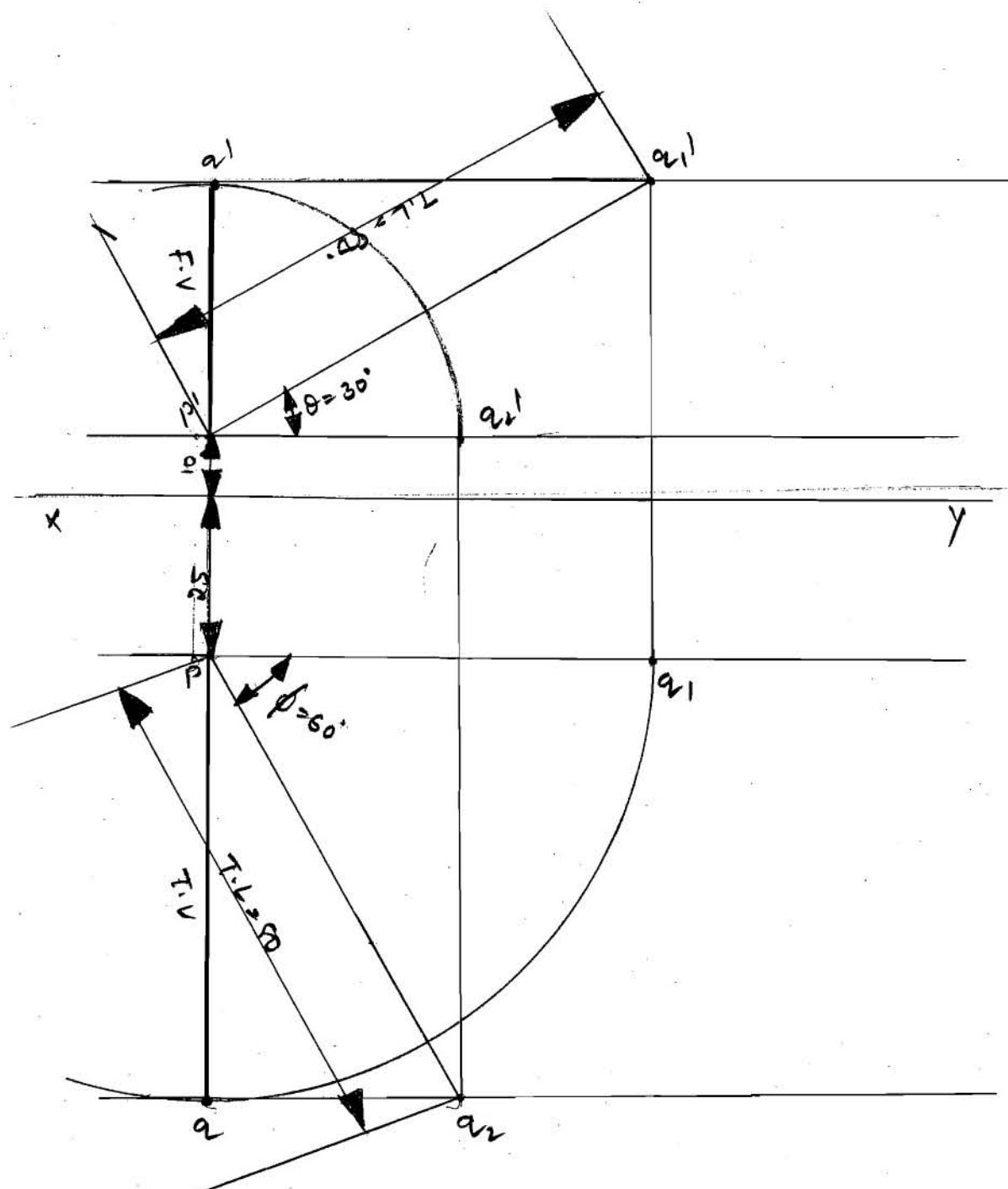
6. A 80 mm long line PQ as its end 'P' 10mm above H.P and 25 mm in front of V.P the line inclined at 30° to H.P and 60° to V.P . Draw its projections.

Ans:-  
 $l = 80 \text{ mm}$

$P \rightarrow 10 \text{ mm } \uparrow \text{H.P}$

$25 \text{ mm } \rightarrow \text{V.P}$

$\theta = 30^\circ, \phi = 60^\circ$



8. The front view of line  $\bar{A}\bar{B}'$  makes an angle of  $30^\circ$  with XY line. The H.T of the line is 45mm in front of V.P, while its V.T is 30mm below the H.P. The end  $\bar{A}'$  is 12mm above the H.P and end  $\bar{B}'$  is 105mm in front of V.P. Draw the projections of line and find its true length, inclination with H.P and V.P.

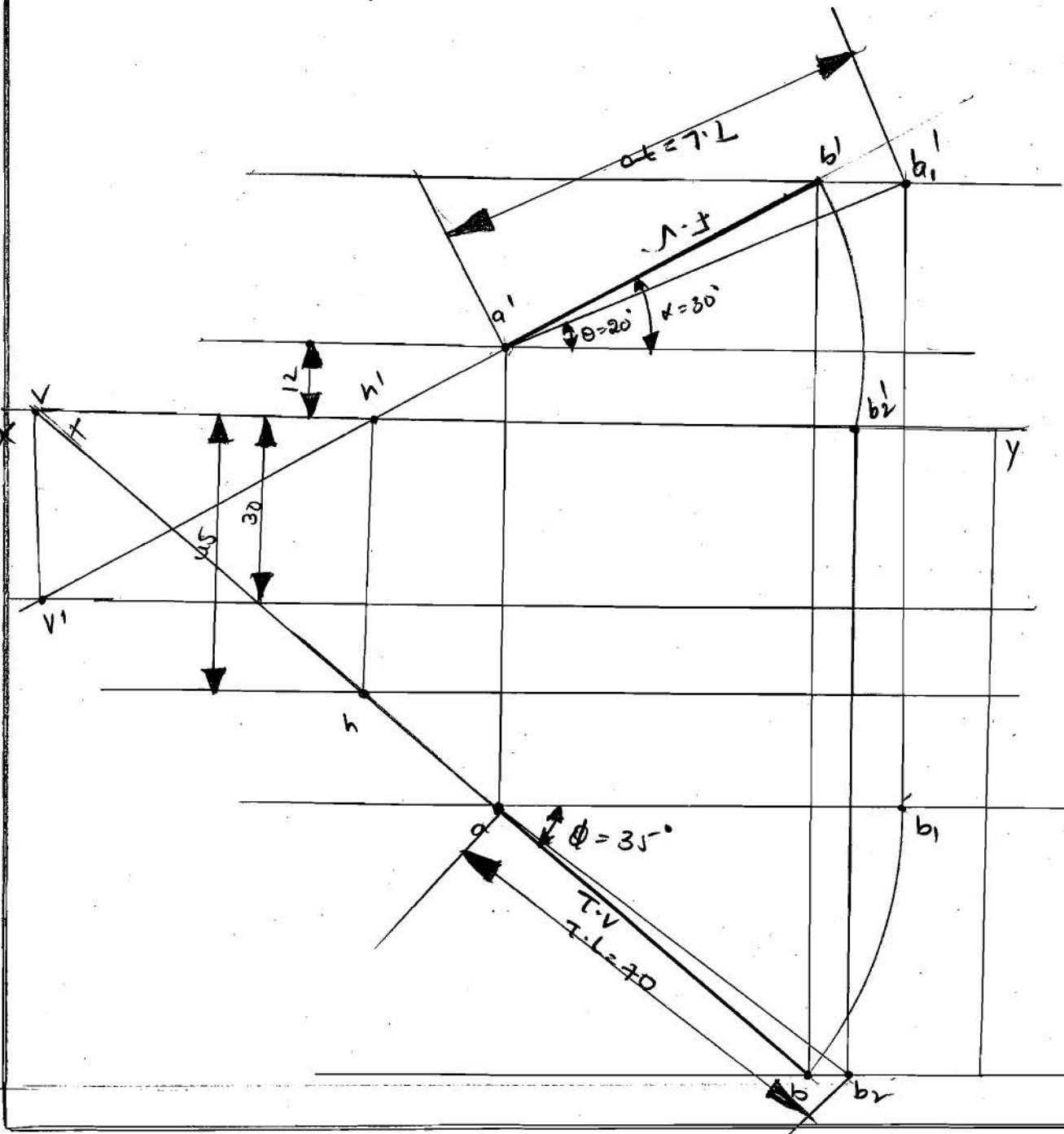
Ans:

$$a'b' = 30^\circ \text{ with } XY$$

$$H.T = 45\text{mm} \rightarrow \text{of V.P}$$

$$V.T = 30\text{mm} \downarrow \text{H.P}$$

$$A \rightarrow 12\text{mm} \uparrow \text{H.P.}$$



A 70mm long line PQ has its end P 20mm above the H.P  
 and 40mm in front of the V.P. The other end Q is 60mm above the H.P  
 and 10mm in front of the V.P. Draw the projections of PQ  
 and determine its inclinations with the reference planes.

P - 7.24

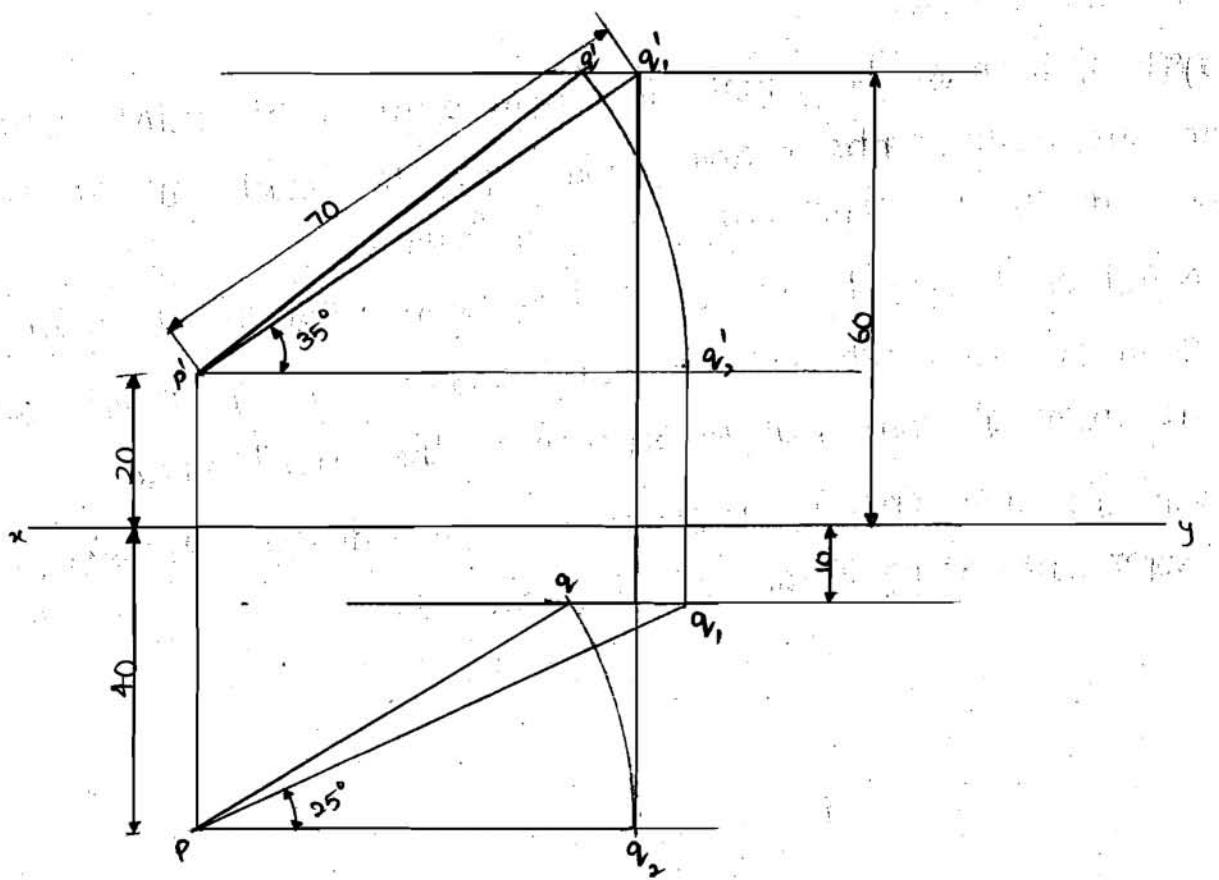
PQ = 70mm line

End P is 40mm in front of V.P

and 20mm above H.P

End Q is 60mm above the H.P

and 10mm in front of V.P



1. On a projector, mark point  $p'$  20mm above  $xy$  and  $p$  40mm below  $xy$ .
2. Draw a line  $ab$  parallel to and 60mm above  $xy$  as the locus of  $q'$ .
3. Draw another line  $cd$  parallel to and 10mm below  $xy$  as locus of  $q$ .
4. Draw an arc with centre  $p'$  and radius 70mm to meet  $ab$  at point  $q_1'$ . Join  $p'q_1'$  to represent true inclination of line with the H.P. Here  $\Theta = 35^\circ$ .
5. Draw an arc with centre  $p$  and radius 70 mm to meet  $cd$  at point  $q_2$ . Join  $pq_2$  to represent true inclination of line with the V.P. Here  $\phi = 25^\circ$ .
6. Project  $q_1'$  to meet horizontal line from point  $p$  at point  $q_1$ . Draw an arc with centre  $p$  and radius  $pq_1$  to meet  $cd$  at point  $q_1$ . Join  $pq_1$  to represent the top view.
7. Project  $q_2$  to meet horizontal line from point  $p'$  at point  $q_2'$ . Draw an arc with centre  $p'$  and radius  $p'q_2'$  to meet  $ab$  at point  $q'$ . Join  $p'q'$  to represent the front view.
8. Join  $q_1q_1$  and ensure that it is perpendicular to  $xy$ , representing projector of the end  $\Phi$ .

The front and top views of 75mm long line PQ measures 50mm and 60mm, respectively. If the end P of the line is 35mm above the H.P. and 15mm in front of the V.P. draw its projections and locate the traces. Determine the true inclinations of the line PQ with the H.P. and the V.P.

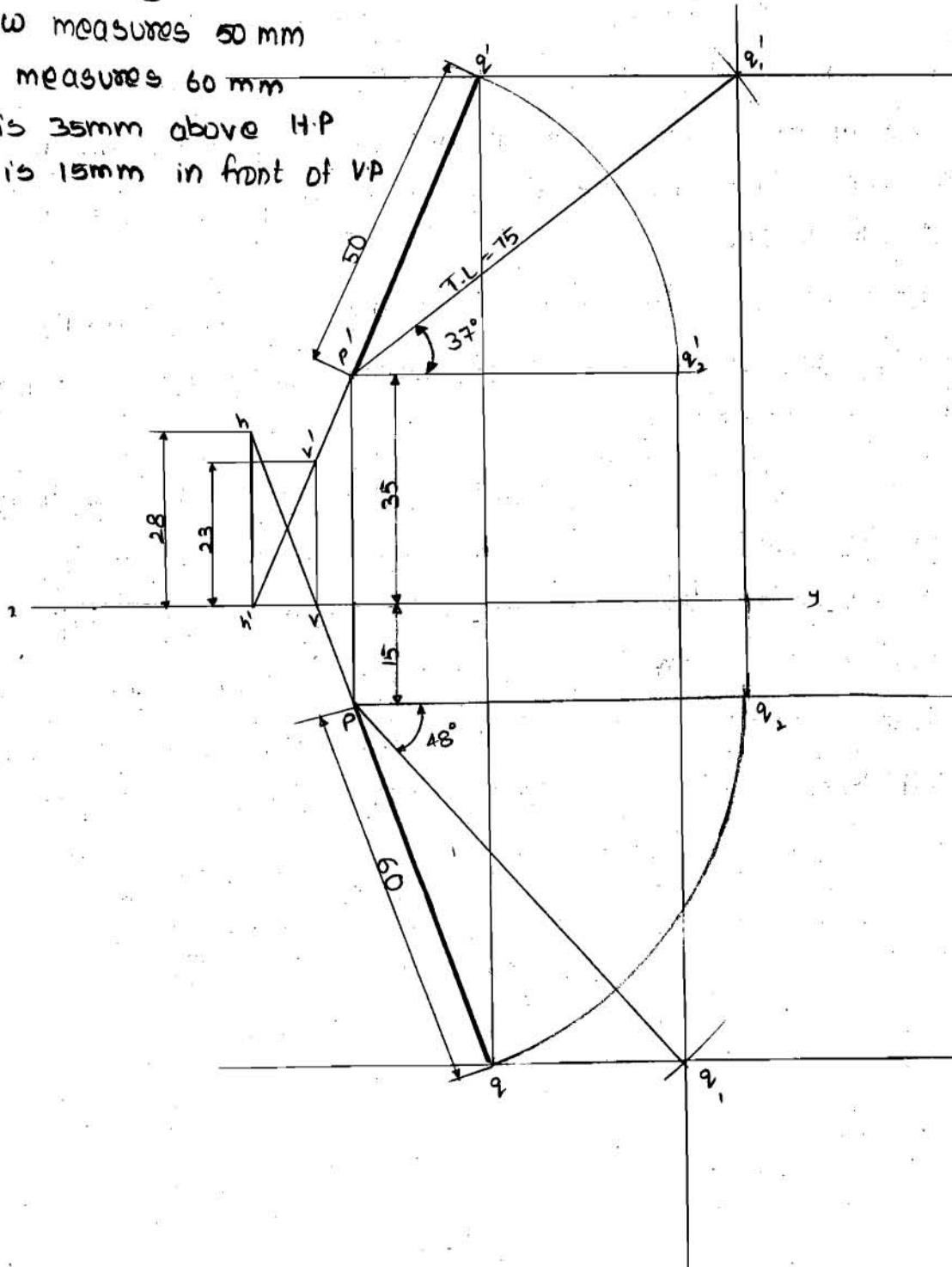
PQ is 75 mm long

front view measures 50 mm

Top view measures 60 mm

End P is 35mm above H.P

End P is 15mm in front of V.P



1. Draw reference line, mark  $p'$  35mm above and 15mm below it is  $P$ .
2. Draw a 50mm long line  $p'q_2'$  parallel to  $xy$ . Draw another 60mm long line  $pq_1$ , parallel to  $xy$ .
3. Draw an arc with centre  $p'$  and radius 75mm to meet projector of  $q_1$  at point  $q_1'$ . Join  $p'q_1'$  to represent true inclination of line with the H.P. Here  $\theta = 37^\circ$ .
4. Repeat above step same with V.P. Here  $\phi = 48^\circ$ .
5. Draw an arc with centre  $p'$  and radius  $p'q_2'$  (50mm) to meet horizontal line from point  $q_1'$  at point  $q_2'$ . Join  $p'q_2'$  to represent the front view.
6. Repeat above with centre  $P$  and radius 60mm. Join  $pq_2$  it is top view.
7. Join  $q_2q_1$  and ensure that it is perpendicular to  $xy$ , representing projector of end Q.
8. Produce  $p'q_1'$  to meet  $xy$  at a point  $h'$ . Draw vertical projector through point  $h'$  to meet the  $pq$  produced at point  $h$ . The point  $h$  represents the H.T. Here  $h$  is 28mm above  $xy$ .
9. Produce  $pq_2$  to meet  $xy$  at a point  $v$ . Draw a vertical projector through point  $v$  to meet  $pq_2'$ , produced at point  $v'$ . Point  $v'$  represents the V.T. Here, point  $v'$  is 23mm above  $xy$ .

Its mid-point is 35 above the H.P and 50mm in front of V.P  
Draw its projects.

PQ = 100 mm line

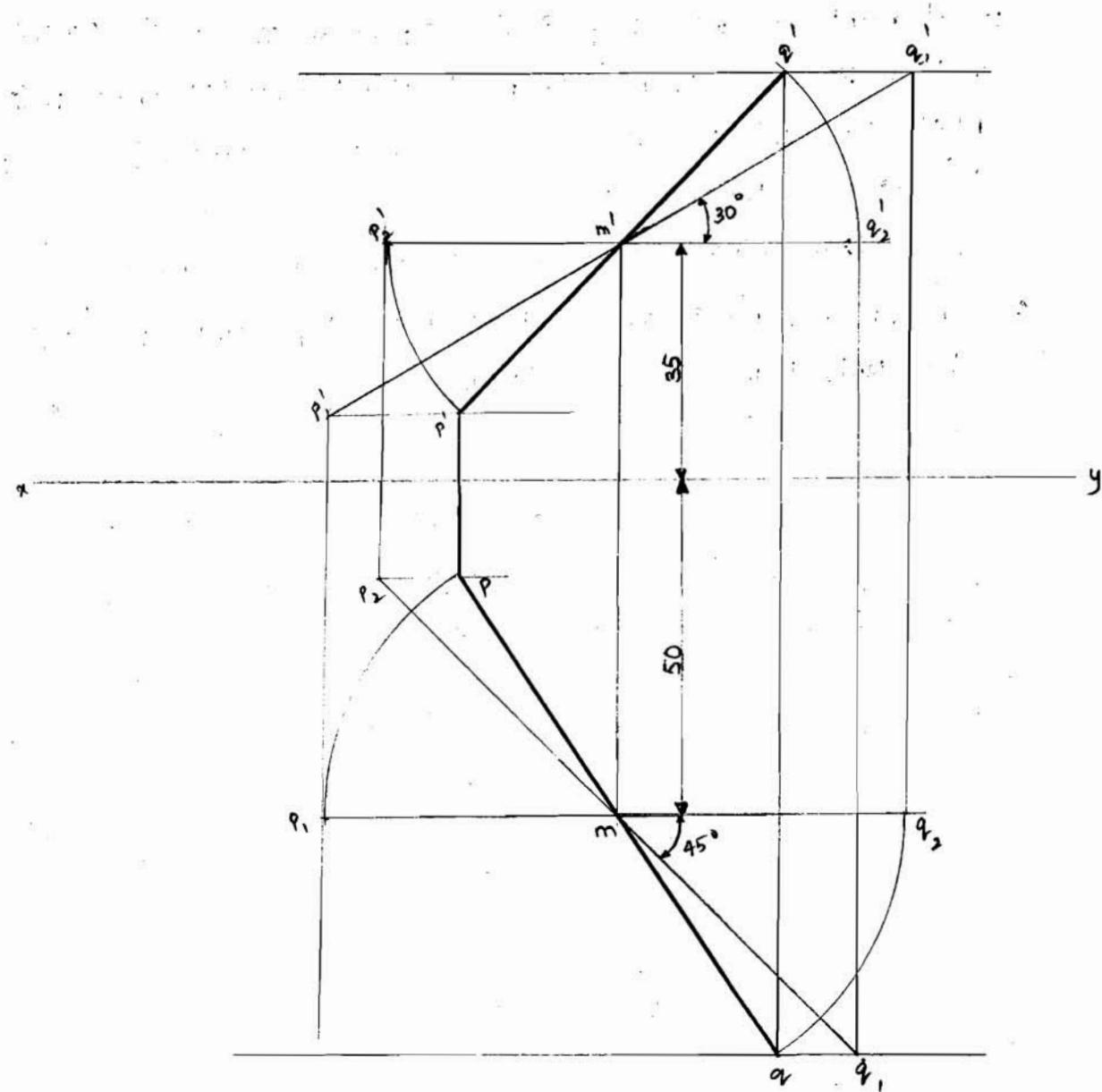
M is midpoint

M is 35 above H.P

and 50 in front of V.P

Line inclined  $30^\circ$  to H.P

$45^\circ$  to V.P



1. Draw a reference line  $xy$ . On a vertical projector mark point  $m'$  35mm above  $xy$  and point  $m$  50 mm below  $xy$ .
2. Draw a 50mm long line  $m'q'$  inclined at  $30^\circ$  to  $xy$ . Produce it such that  $P_1q'_1 = 100\text{mm}$ .
3. Draw another 50mm line  $m_1q_1$  inclined at  $45^\circ$  to  $xy$ . Produce it such that  $P_2q_2 = 100\text{mm}$ .
4. Project points  $p'_1$  and  $q'_1$  to meet horizontal line through point  $m$  at points  $P_1$  and  $q_1$ , respectively. Draw an arc with centre  $m$  and radius  $mp_1$  or  $mq_1$  to meet the horizontal lines from points  $P_2$  and  $q_2$  at points  $p$  and  $q$ , respectively. Join  $p_1q_1$  to represent the top view.
5. Project remaining to represent front view ( $p'm'q'$ )
6. Join  $p_1p$  and  $q'_1q$  to ensure that they represent projector of the ends  $P$  and  $Q$  respectively.

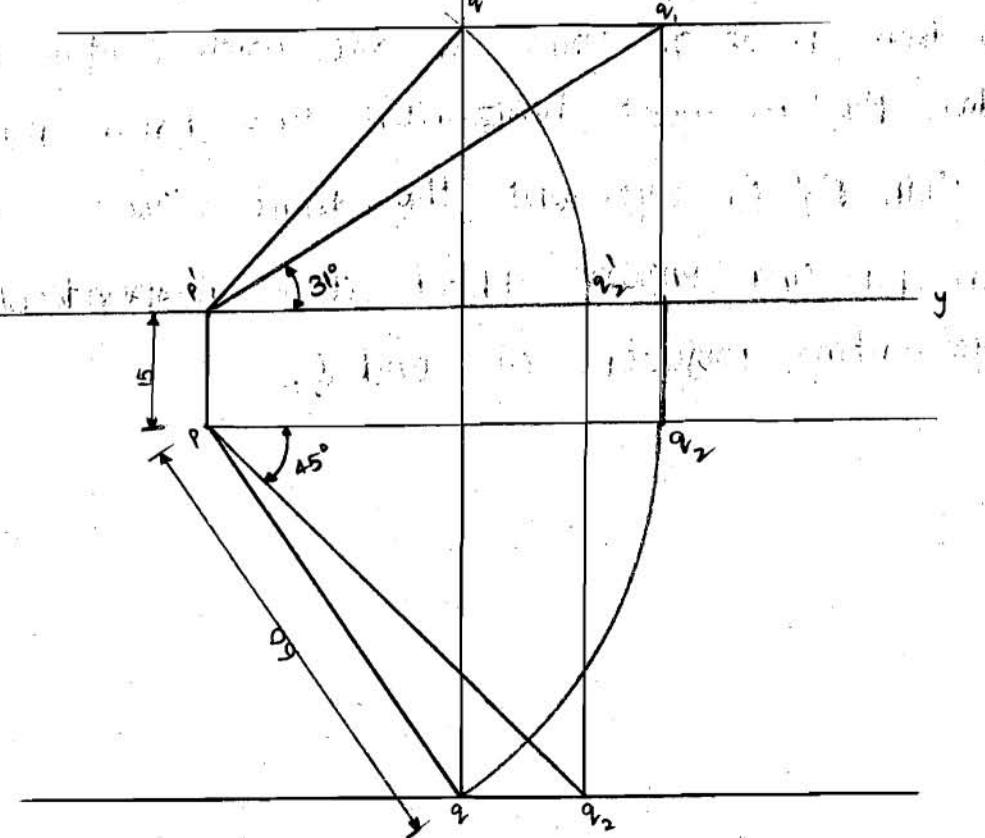
PQ is 70mm long line

line inclined at  $45^\circ$  to the V.P.

End P is on H.P.

End Q is 15mm in front of V.P.

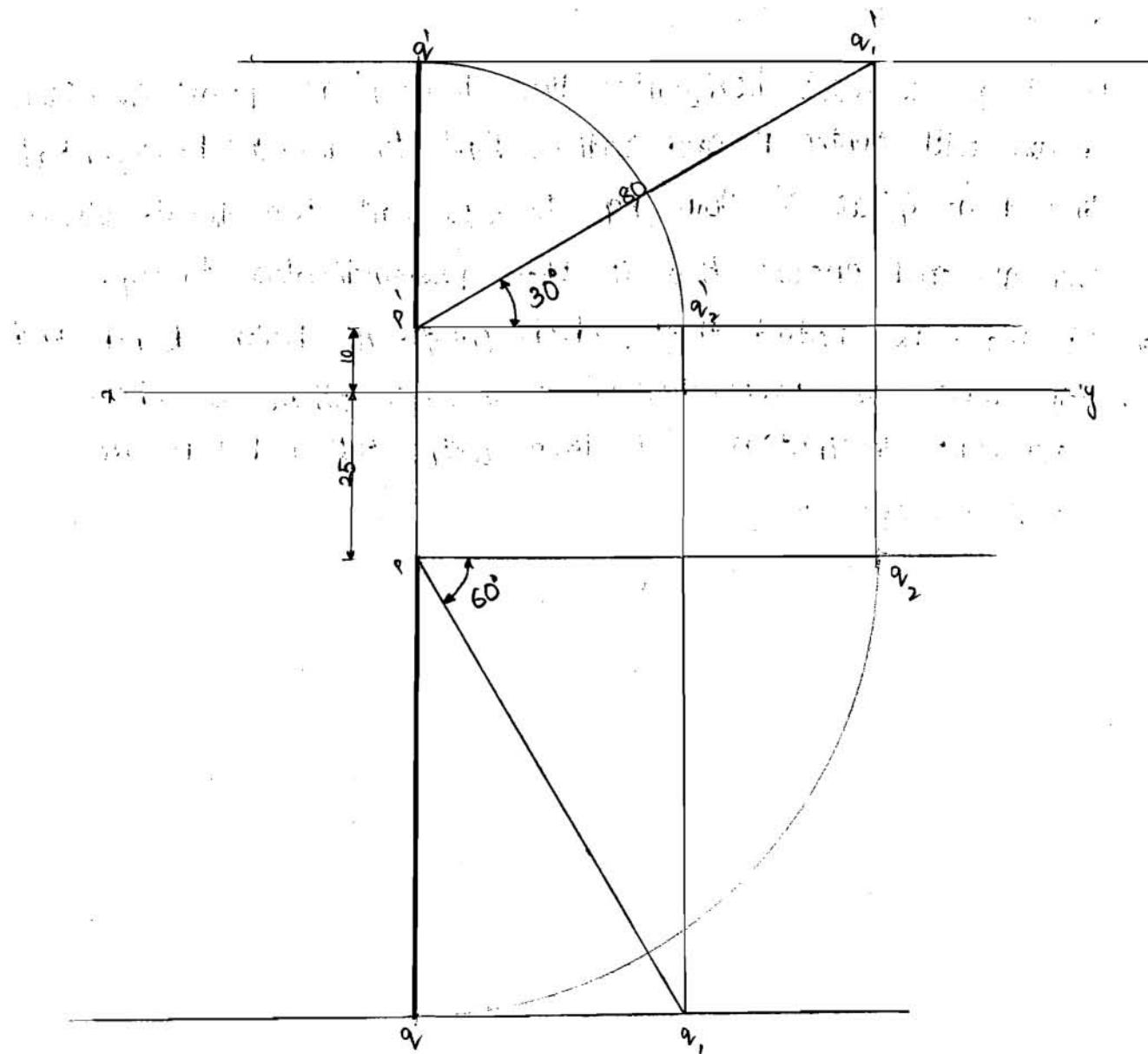
Top View measures 60mm



1. Draw the reference line  $xy$ . Make  $P'$  on  $xy$  and  $P$  10mm below  $xy$ .
2. Draw a 70mm long line  $PQ_2$  inclined at  $\theta = 45^\circ$  to  $xy$ .
3. Draw an arc with centre  $P$  and radius 60mm to meet the horizontal line through point  $Q_2$  at point  $Q$ . Join  $PQ$  to represent top view.
4. Draw an arc with centre  $P$  and radius  $PQ$  to meet the horizontal line from point  $P$  at point  $q_1$ . Draw another arc with  $P'$  and radius 70mm to meet projector of  $q_1$  at  $q'_1$ . Join  $P'q'_1$  to represent the true inclination of line with H.P. Here  $\theta = 31^\circ$ .
5. Draw a vertical line from point  $Q_2$  to meet horizontal line from  $P'$  at  $q_2'$ . Draw an arc with centre  $P'$  and radius  $P'q_2'$  to meet horizontal line from point  $q'_1$  at  $q'$ . Join  $P'q'$  to represent the front view.
6. Join  $q'q$  and ensure that it is perpendicular to  $xy$ , representing projector of end  $Q$ .

Projections of Line where  $\theta + \phi = 90^\circ$

P. 9.35



1. Draw a reference line  $xy$ . Mark  $p'$  10mm above  $xy$  and  $p$  25mm below  $xy$ .
2. Draw an 80mm long line  $p'q_1'$  inclined at  $30^\circ$  to  $xy$ .
3. Draw another 80mm long line  $pq_2$  inclined at  $60^\circ$  to  $xy$ .
4. Project  $q_1'$  to meet horizontal line from  $q$  at  $q_1$ . Draw an arc with centre  $p$  and radius  $pq_1$ , to meet horizontal line from  $q_2$  at  $q$ . Join  $pq_1$  to represent top view.
5. Project  $q_2$  to meet horizontal line from  $p'$  at point  $q_2'$ . Draw an arc with centre  $p'$  and radius  $p'q_2'$  to meet horizontal line from  $q_1'$  at  $q'$ . Join  $p'q_2'$  to represent the front view.
6. Join  $q_1q_2$  and ensure that it is perpendicular to  $xy$ .
7. It may be noted that when  $\theta + \phi = 90^\circ$ , both front and top views are perpendicular to  $xy$ . In other words, apparent inclinations of line with H.P and V.P are  $90^\circ$ , i.e.,  $\alpha = \beta = 90^\circ$ .

Line inclined to both reference planes where  $\theta + \phi < 90^\circ$

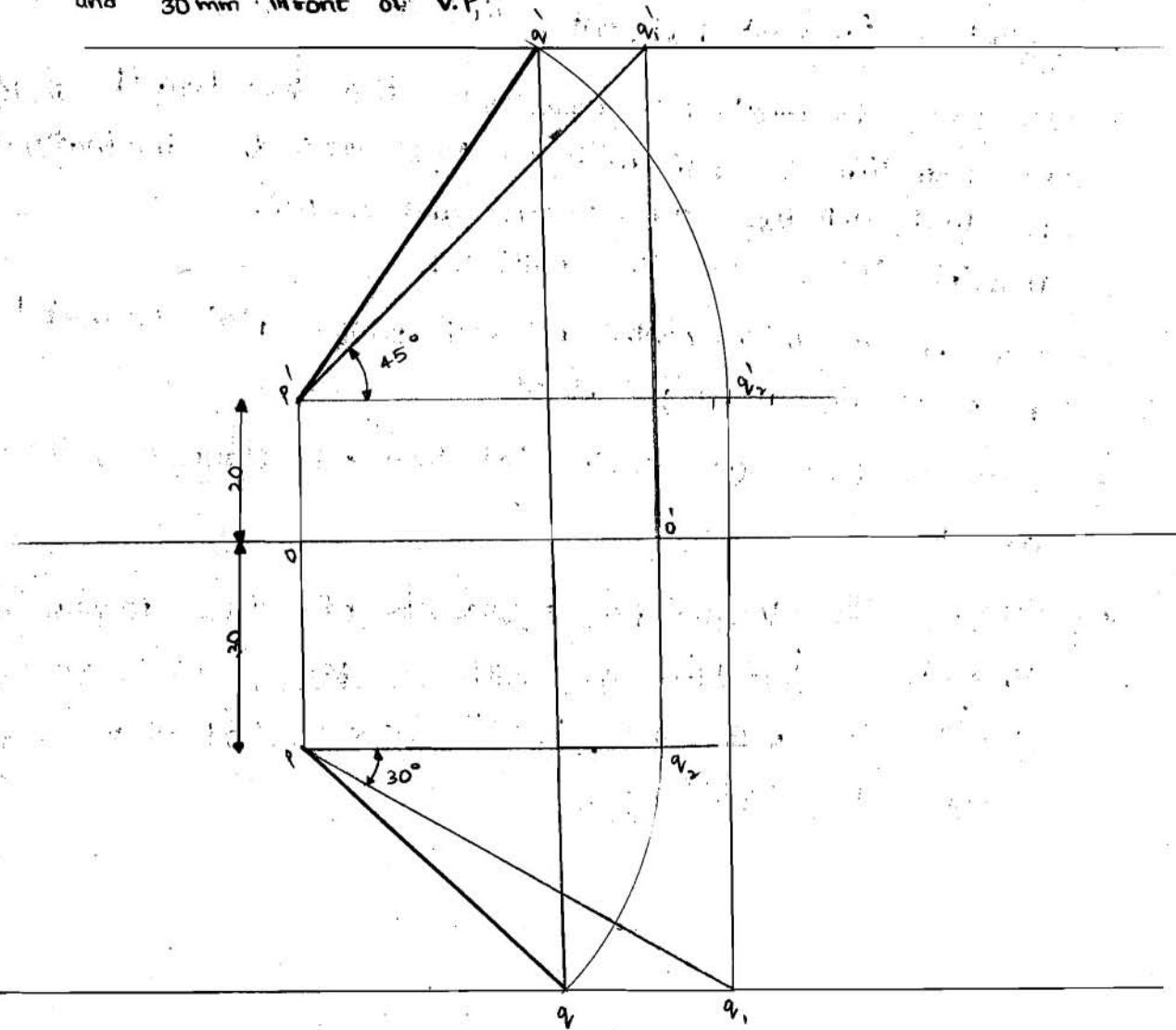
Line PQ = 70 mm

$$\theta = 45^\circ$$

$$\phi = 30^\circ$$

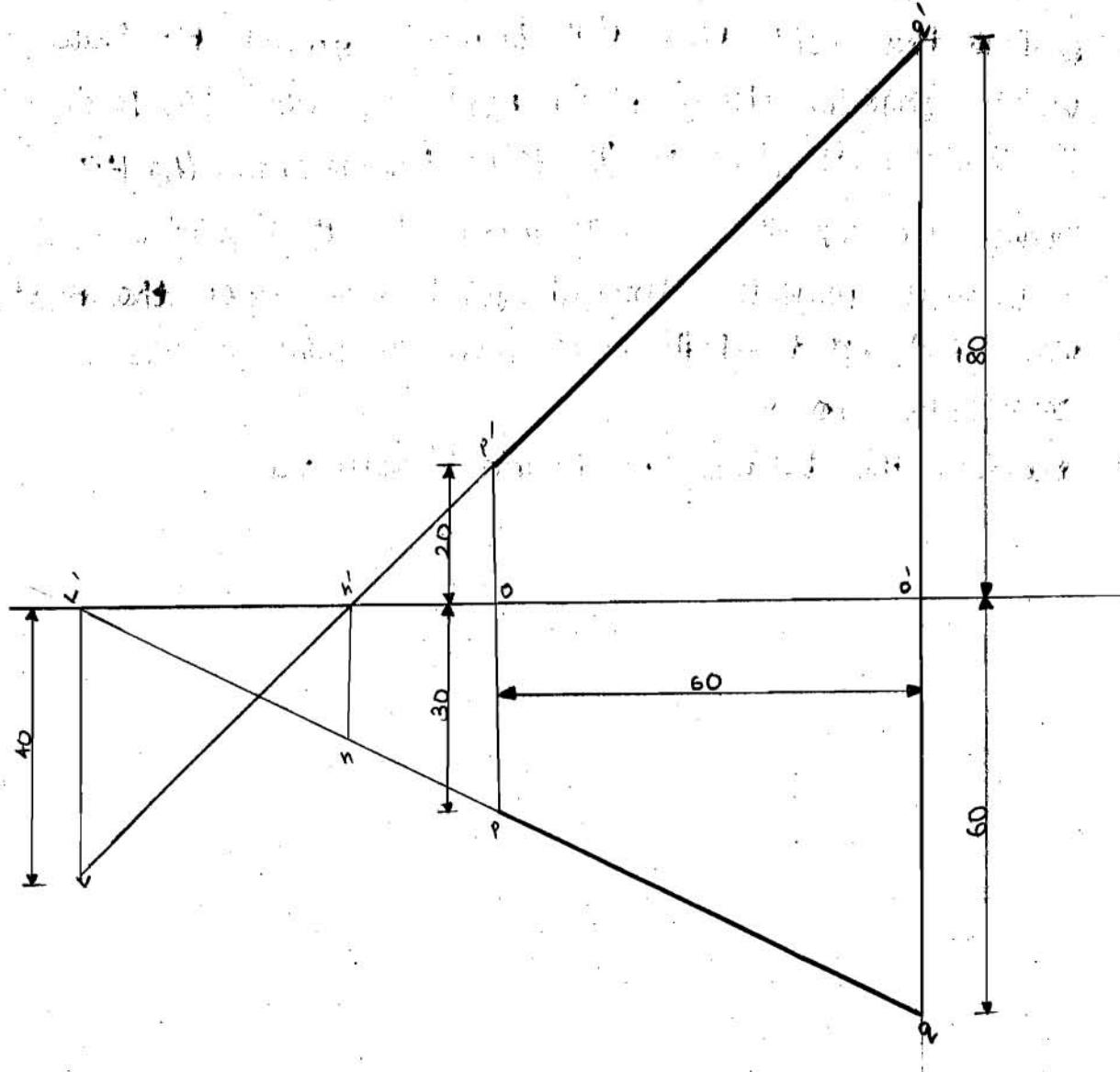
P end 20mm above the H.P

and 30 mm in front of V.P.



1. Mark O and O<sub>1</sub> on line such that they are 60mm apart
2. On vertical projector through O, mark P' 20mm above xy and P 30 below xy.
3. On the vertical projector through O<sub>1</sub>, mark Q' 80mm above xy and Q 70mm below xy.
4. Join Pq<sub>1</sub>' and pq<sub>1</sub> to represent front and top view of line respectively. Find the T.L and C.O. of line with H.P
5. Draw an arc with centre P and radius pq<sub>1</sub> to meet horizontal line from P at q<sub>1</sub>.
6. Project q<sub>1</sub> to meet horizontal line ab through q<sub>1</sub>' at q<sub>1</sub>'.
7. Join p'q<sub>1</sub>'. The length p'q<sub>1</sub>' represents the true length of pq. The inclination of p'q<sub>1</sub>' with xy represents true inclination of PQ with H.P. Here, T.L = 44 mm and  $\theta = 40^\circ$ . Find E.L and  $\phi$  of line with V.P.
8. Draw an arc with centre P' and radius p'q<sub>1</sub>' to meet the horizontal line from P' at q<sub>2</sub>'.
9. Project q<sub>2</sub>' to meet horizontal line cd through point q at q<sub>2</sub>.
10. Join pq<sub>2</sub>. The length pq<sub>2</sub> represents the true length of pq. The inclination of pq<sub>2</sub> with xy represents true inclination of PQ with V.P. Here,  $\phi = 25^\circ$ . Ensure that the length pq<sub>2</sub> is equal to length p'q<sub>1</sub>'.

Traces of line  $\theta + \phi < 90^\circ$



1. Draw a reference line  $xy$ . Mark  $O$  and  $O_1$  on  $xy$  such that they are 60 mm apart.
2. On vertical projector through  $O$ , mark  $p'$  and  $p$  as the front and top views of  $p$ .
3. similarly, on vertical projector through  $O_1$ , mark  $q'$  and  $q$  as the front and the top views of  $Q$ .
4. Join  $p'q'$  and  $pq$  to represent the front and top views of the line  $PQ$ .
5. Produce the front view  $p'q'$  to meet  $xy$  at  $h'$ . Draw a vertical projector through  $h'$  to meet top view  $pq$ , produced if required, at point  $v$ . The point  $h$  represents the H.T
6. Produce the top view  $pq$  to meet  $xy$  at a point  $v$ . Draw a vertical projector through point  $v$  to meet the front view  $p'q'$ , produced if necessary, at point  $v'$ . The  $v'$  represents the V.T
7. Measure the distance of  $h$  and  $v'$  from  $xy$ .

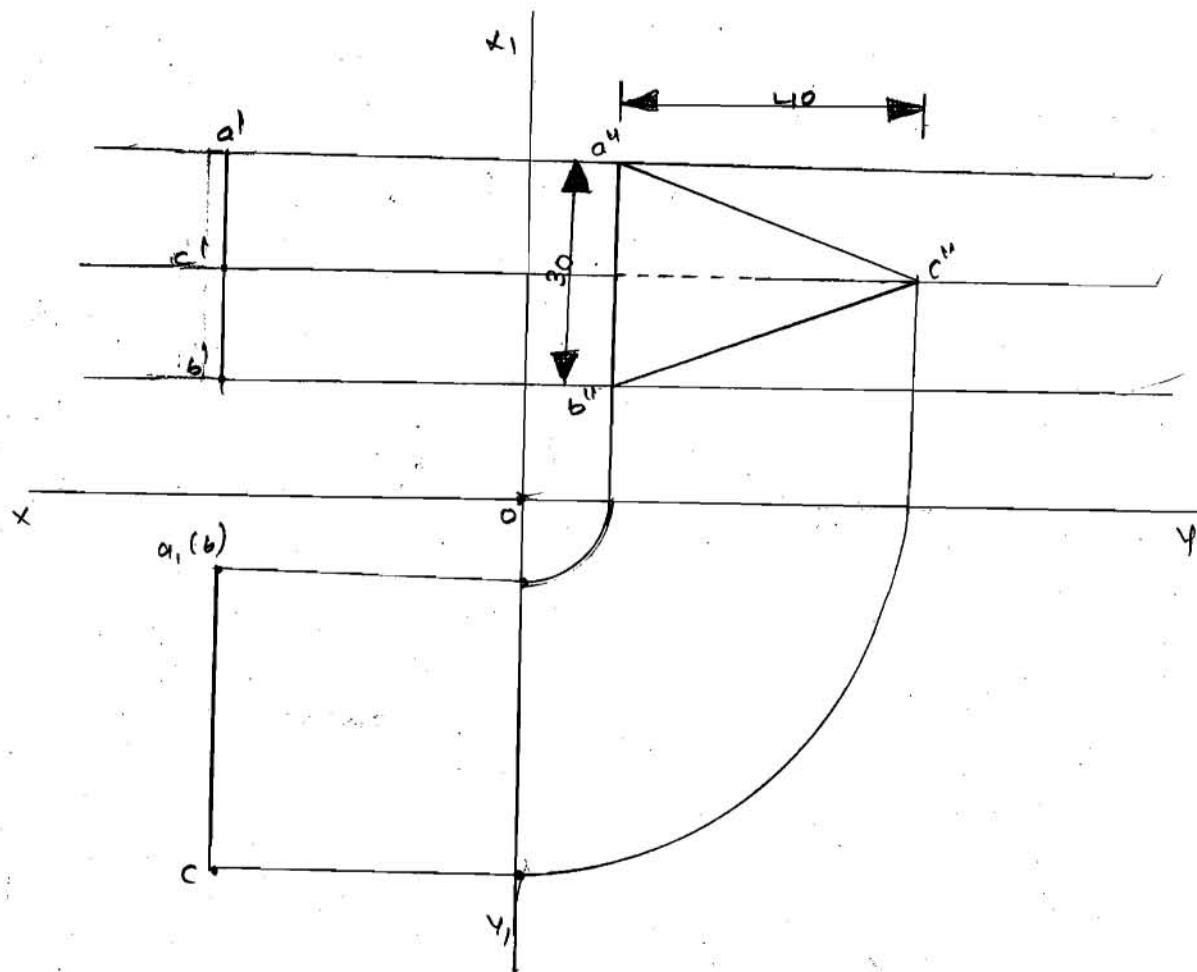
## **Projections of Planes:**

Plane figures or surfaces have only two dimensions, viz. length and breadth. They do not have thickness. A plane figure may be assumed to be contained by a plane, and its projections can be drawn, if the position of that plane with respect to the principal planes of projection is known.

1. A triangular plane is in the form of Isosceles triangle of 30mm side base and 40mm long altitude. It is kept in the first quadrant such that the surface is perpendicular to both H.P. and V.P. Draw its projections when the base is parallel to V.P.

Sol: Base = 30mm

altitude = 40mm.

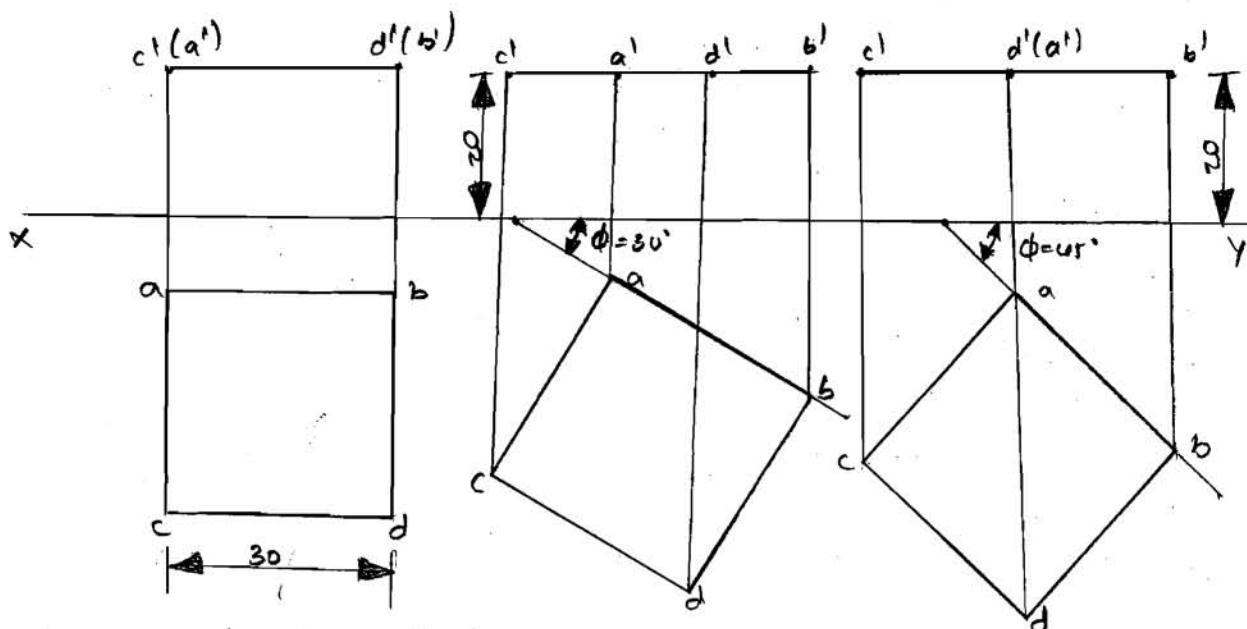


- ② A square plane A<sub>1</sub>B<sub>1</sub>C<sub>1</sub>D 30mm side as its surface parallel to H.P. and 20mm away from it. Draw its projections of the plane when two of its sides are
- parallel to v.p
  - inclined at 30° to v.p
  - all sides are equally inclined to v.p

Sol:

side = 30mm

20mm away from it at 30°  
and  $\phi = 45^\circ$



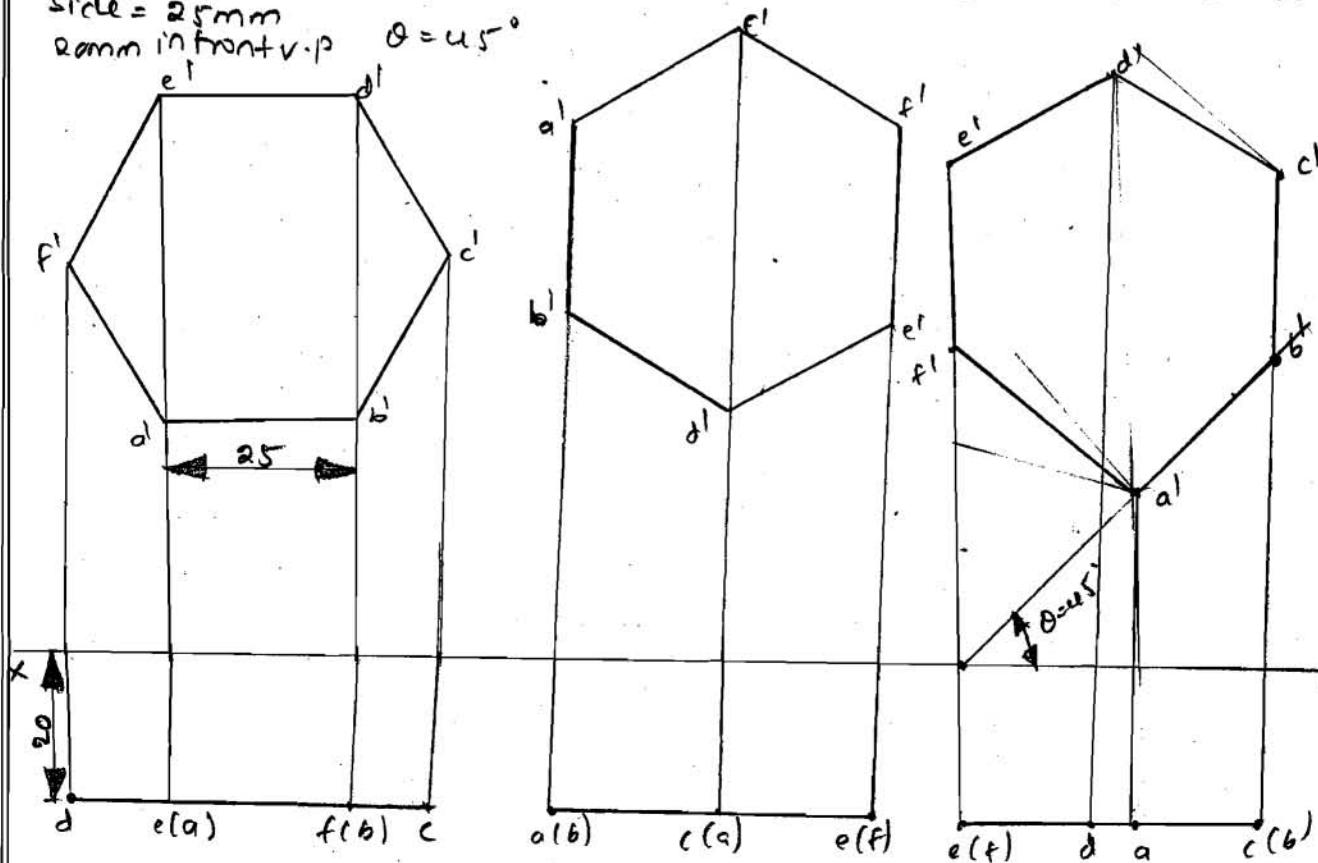
3.

A hexagonal plane of 25mm side as its surface lies 20 mm in front of V.P. Draw the projections of the plane when a side (i) Parallel to H.P (ii) Perp to H.P (iii) Inclined  $\theta = 45^\circ$

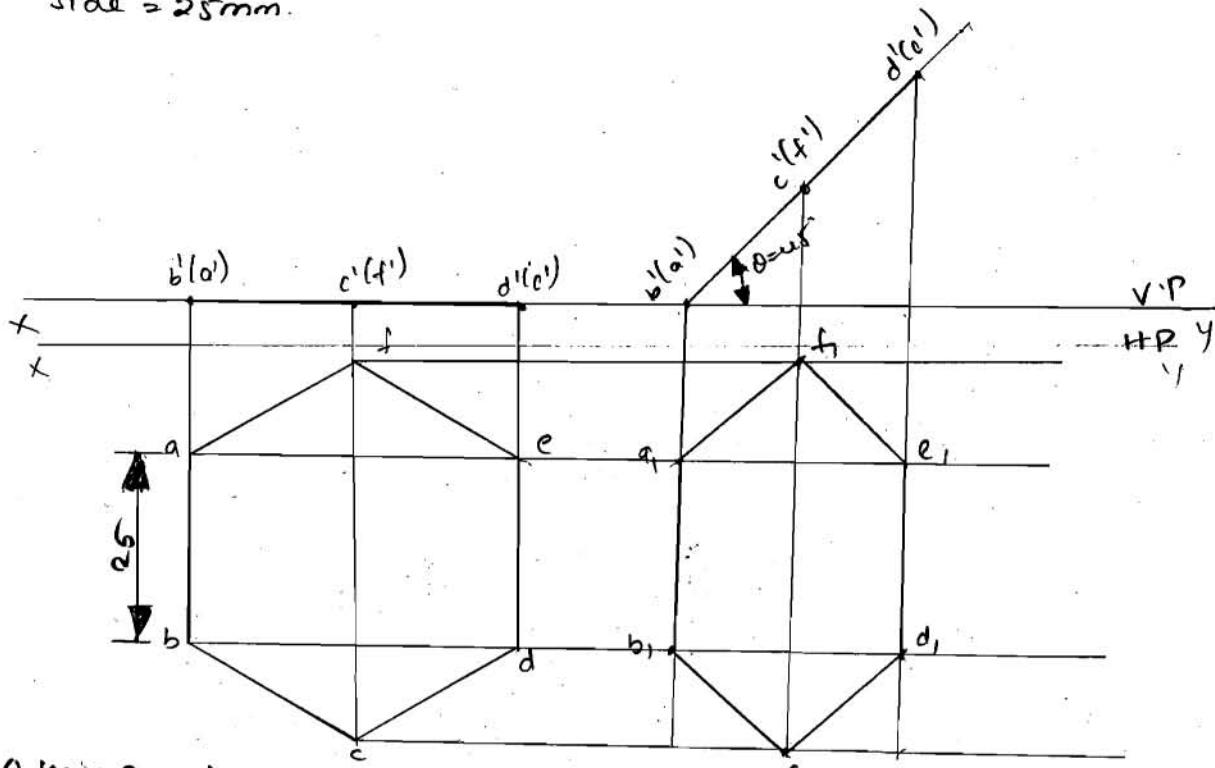
Sol:

Side = 25mm

20mm in front v.p.  $\theta = 45^\circ$



4. A hexagonal Plane of 25mm side as one side on the ground. The surface of the Plane is inclined at  $45^\circ$  to H.P and  $45^\circ$  to V.P - Draw its Projections  
 $\theta = 45^\circ$   
 one of the side on the ground  
 side = 25mm.

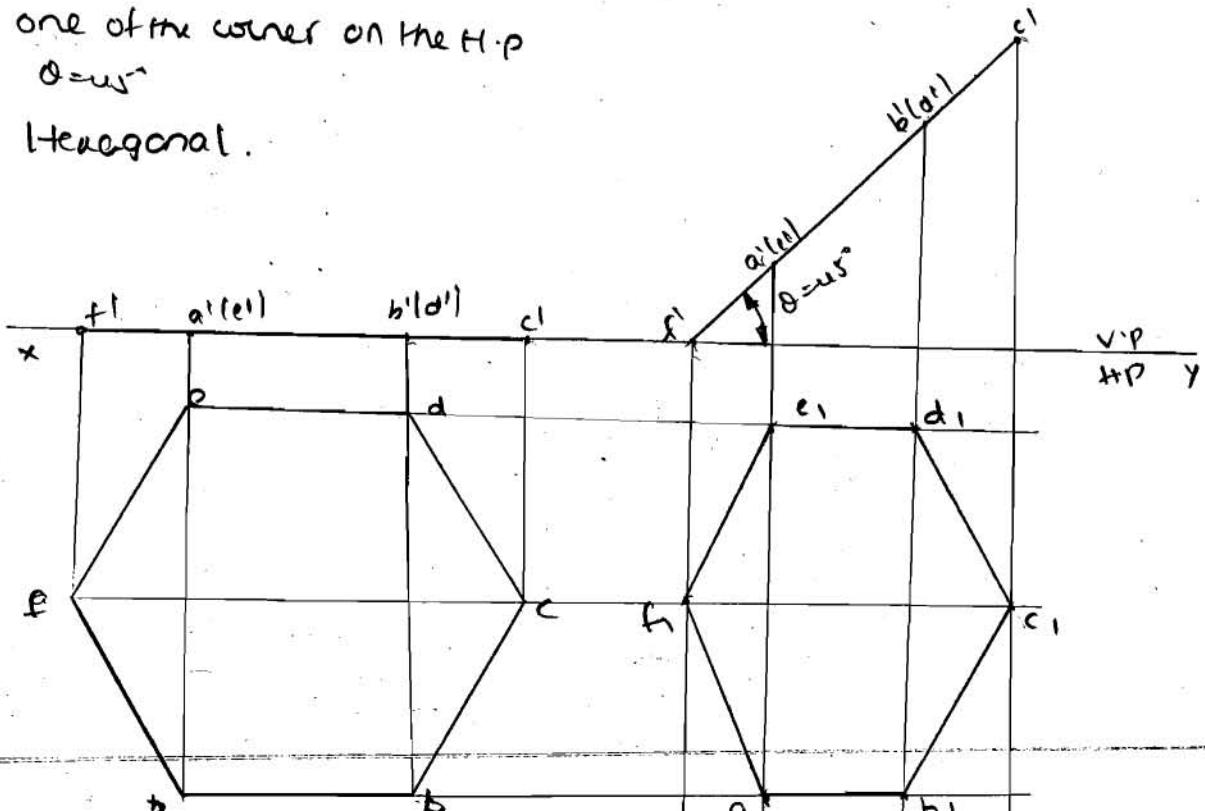


5. A hexagonal plate of 30mm side resting on one of its corners on the H.P. The plate is  $45^\circ$  to V.P and inclined at  $45^\circ$  to H.P - Draw its projections.  
 side = 30mm

one of the corner on the H.P

$$\theta = 45^\circ$$

Hexagonal.

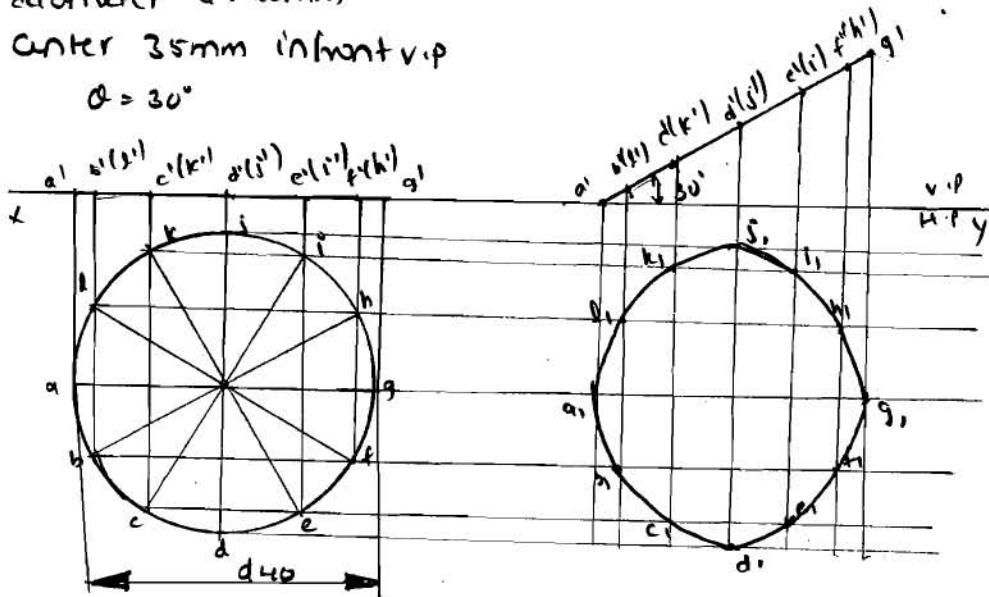


Q: Draw the projections of a circle of 40mm diameter resting on the H.P. on a point on the circumference. Its plane is inclined at  $30^\circ$  to H.P and lies to V.P. Its center is 35mm in front of V.P.

Diameter  $\phi = 40\text{mm}$

Center 35mm in front V.P.

$\theta = 30^\circ$

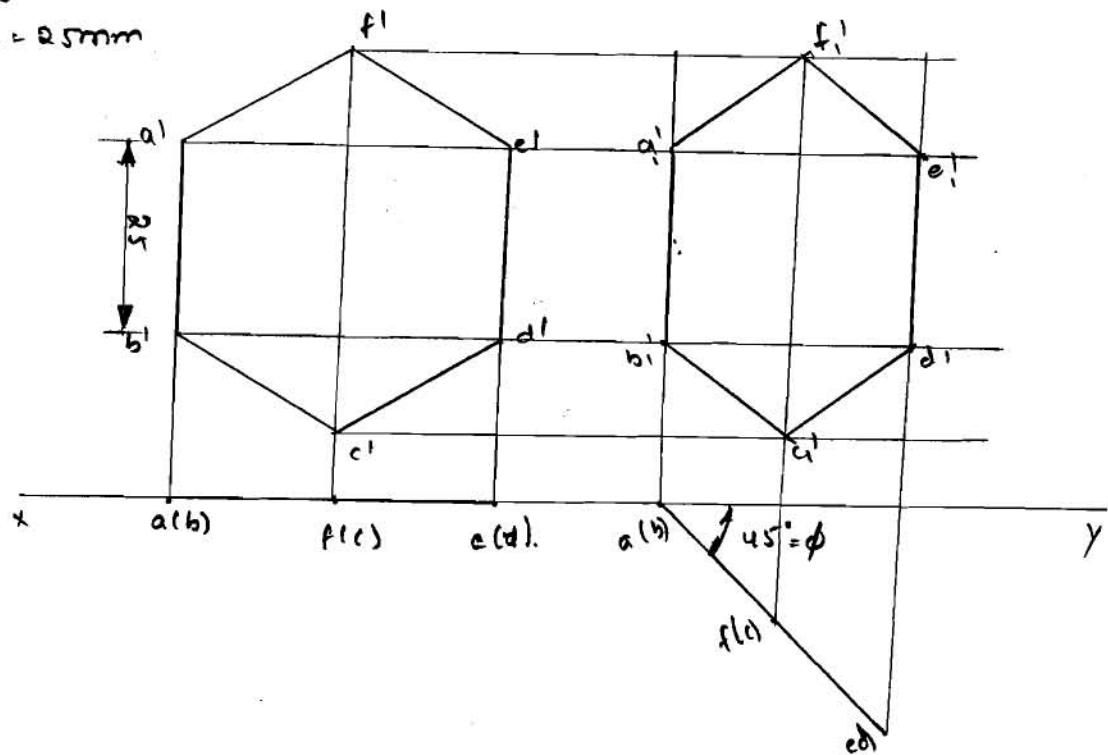


Q: A hexagonal plate of 25mm side and negligible thickness has one of its edges in the V.P. The surface of the plate is ten to H.P and inclined at  $45^\circ$  to V.P. Draw its projections.

Hexagonal

$\phi = 45^\circ$

Side = 25mm

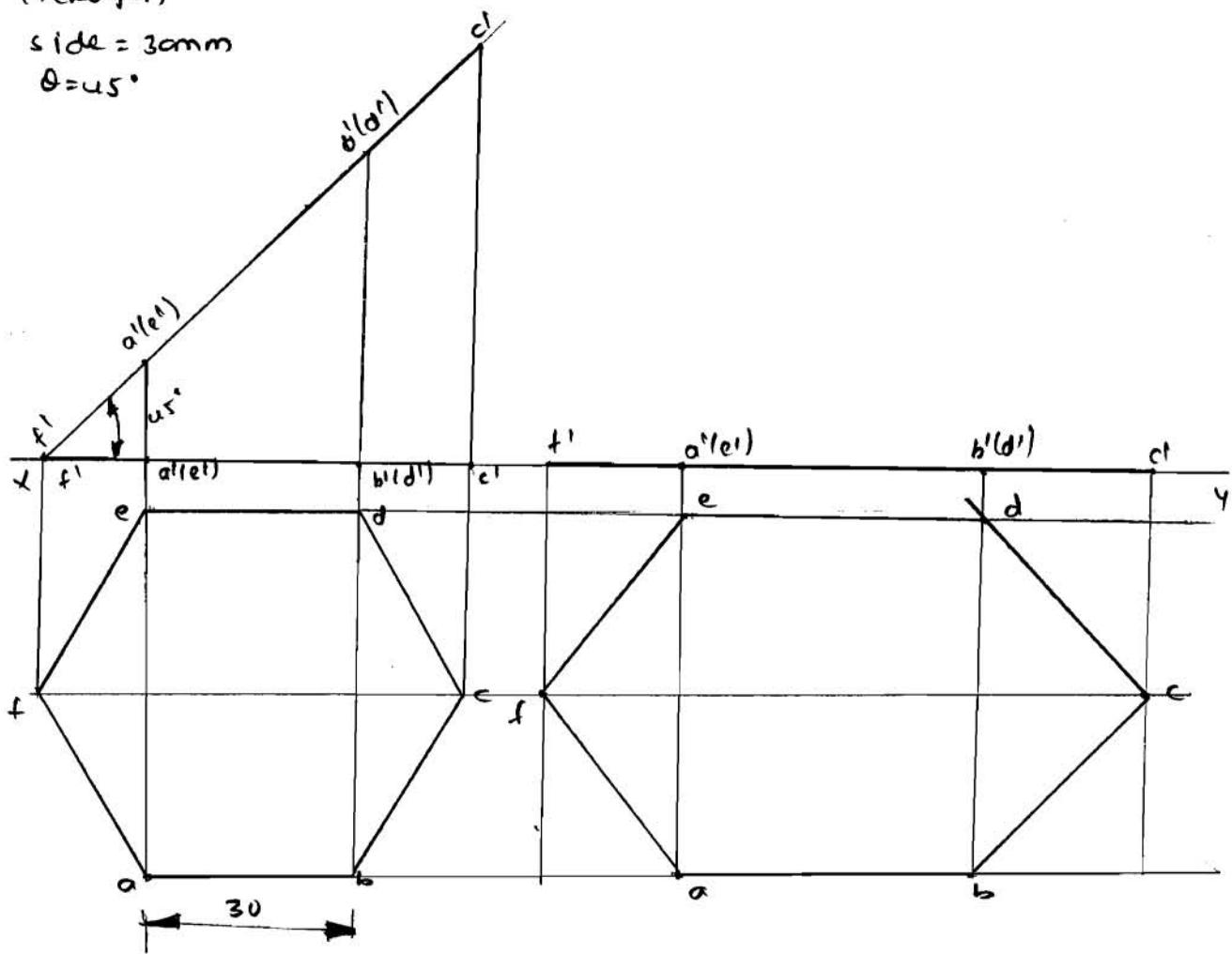


Q: The top view of a lamina whose surface is true to v.p. and inclined at  $45^\circ$  to h.p. appears as a regular hexagon of 30mm side, having a side parallel to the reference line. Draw the projections of the plane and obtain its true shape.

Hexagon

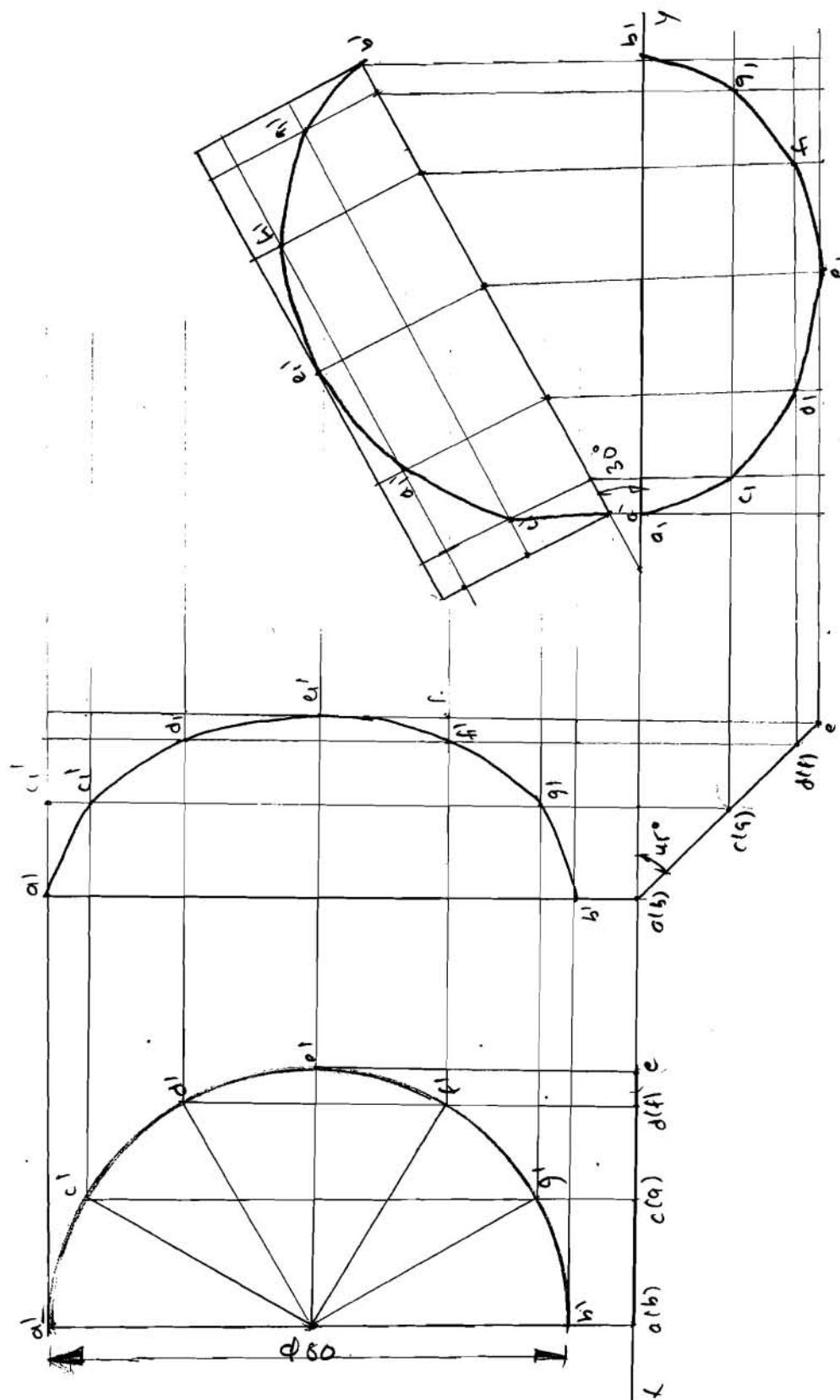
side = 30mm

$\theta = 45^\circ$



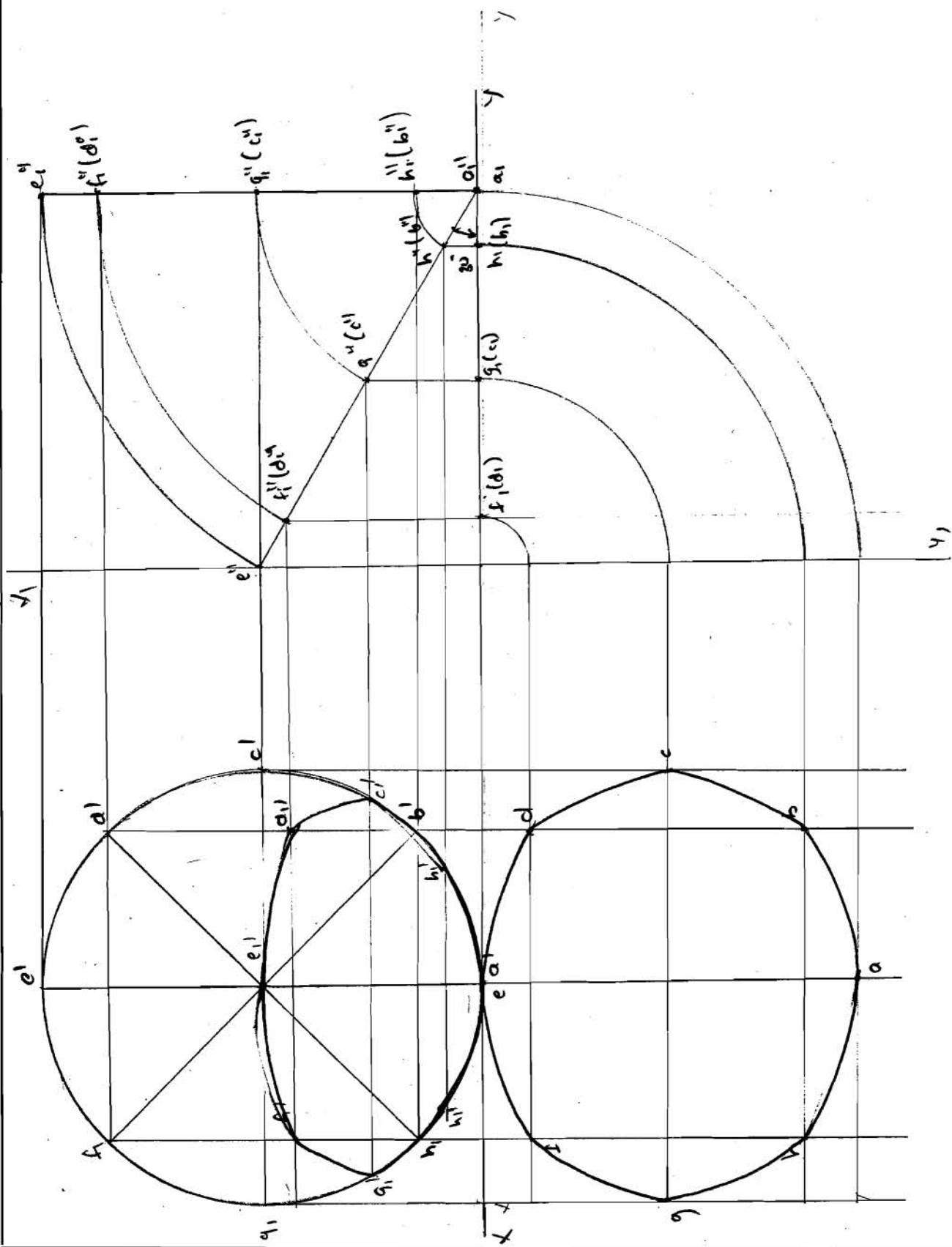
d:

A semi-circular plate of 80mm diameter has its straight edge on the V.P and inclined at 30° to H.P. while the surface of the plate is inclined at 45° to V.P. Draw the projections of the plate.



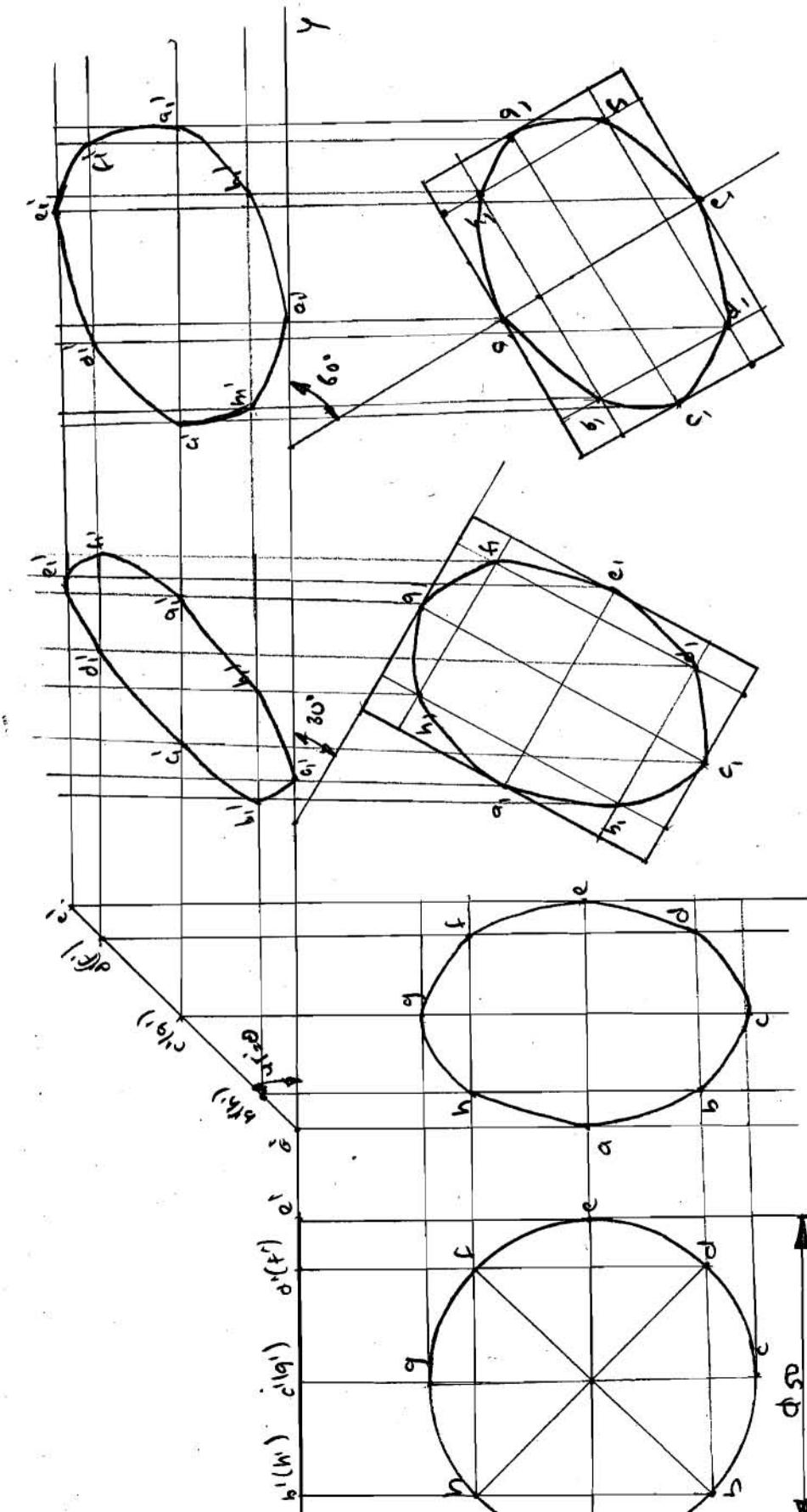
Q:

A circular plane of 80mm diameter has one of the ends of the diameter in the H.P., while the other end is in the V.P. The plane is inclined 30° to the H.P and 60° to V.P draw its projections.



Q:

- Draw the projections of a circle of 50mm diameter resting in the H.P. on a point A' on the circumference its plane is inclined at  $45^\circ$  to H.P. and
- The top-view of the diameter A'G' making  $30^\circ$  angle with the V.P.
  - The diameter A'G' making  $30^\circ$  angle with the V.P.



Q:

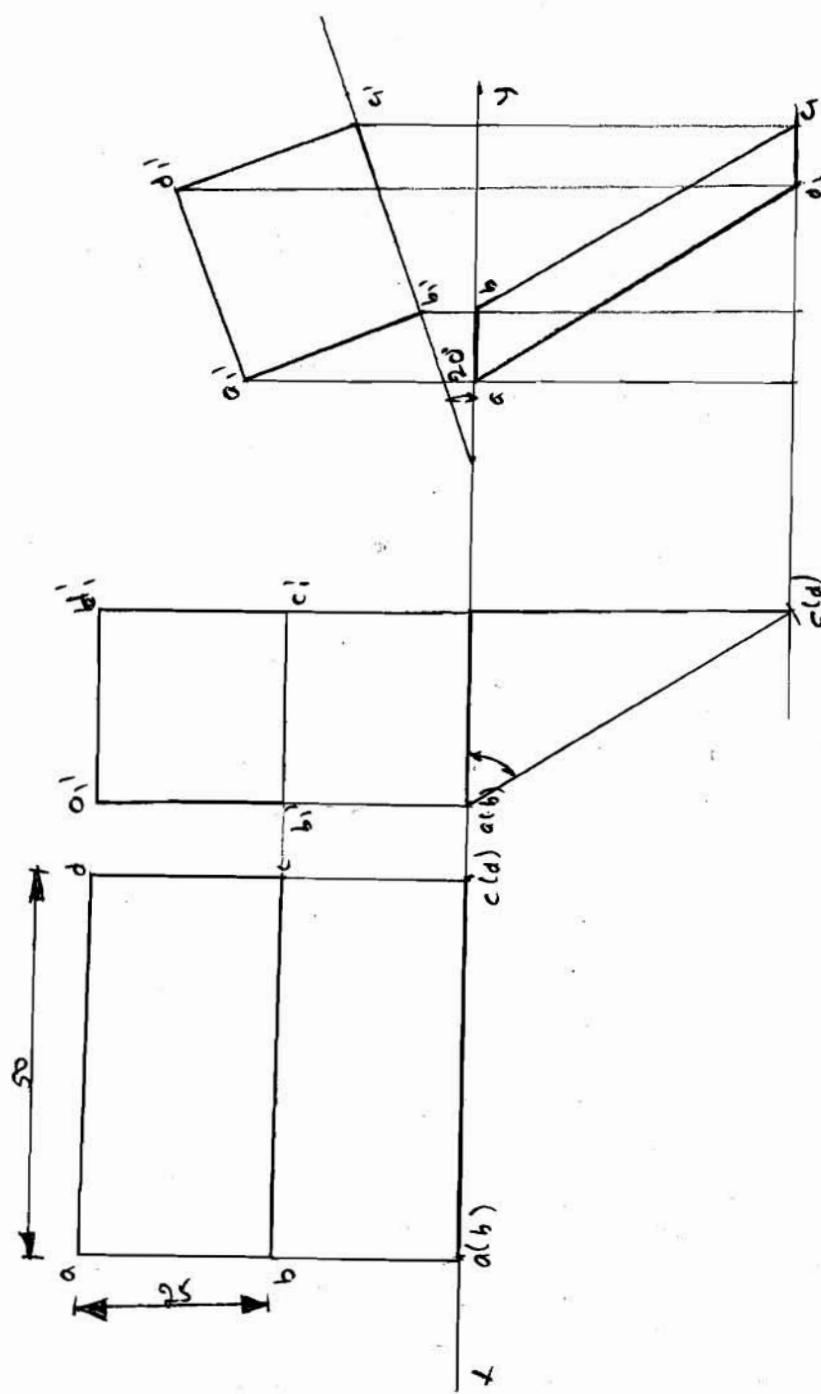
An elevation of a rectangular lamina ABCD at 25mm x 50mm sides of is a square of 25mm when its side AB is in the V.P and the side AD is making an angle of  $30^\circ$  to the H.P

Rectangular ABCD

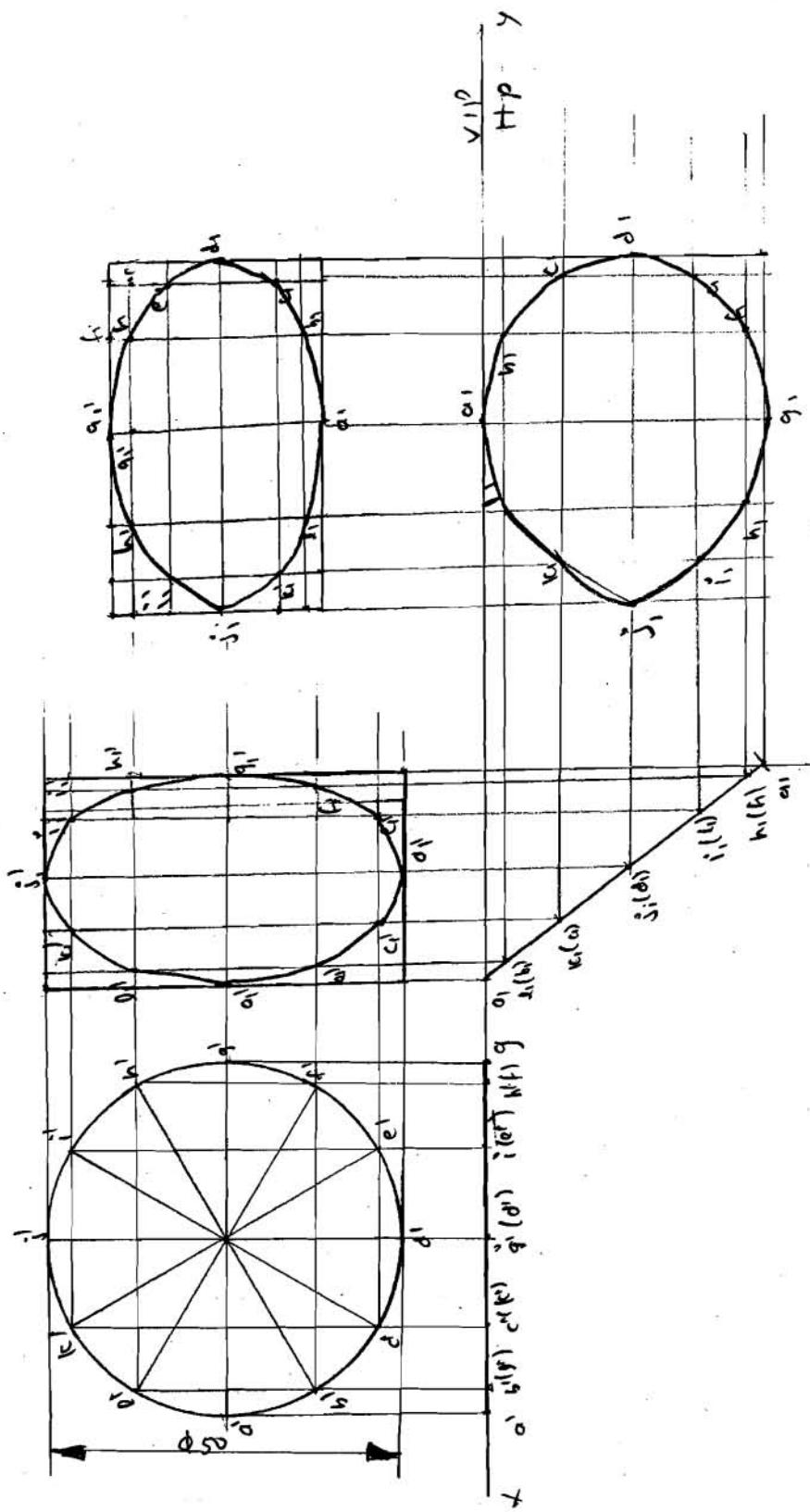
side = 25 x 50 mm

square = 25 mm

$\theta = 20^\circ$



a: A circular plate of negligible thickness and 50mm diameter appears as an ellipse in the front view, having major axis 50mm and minor axis 30mm long. Draw its Top view when the major axis of the ellipse is horizontal.



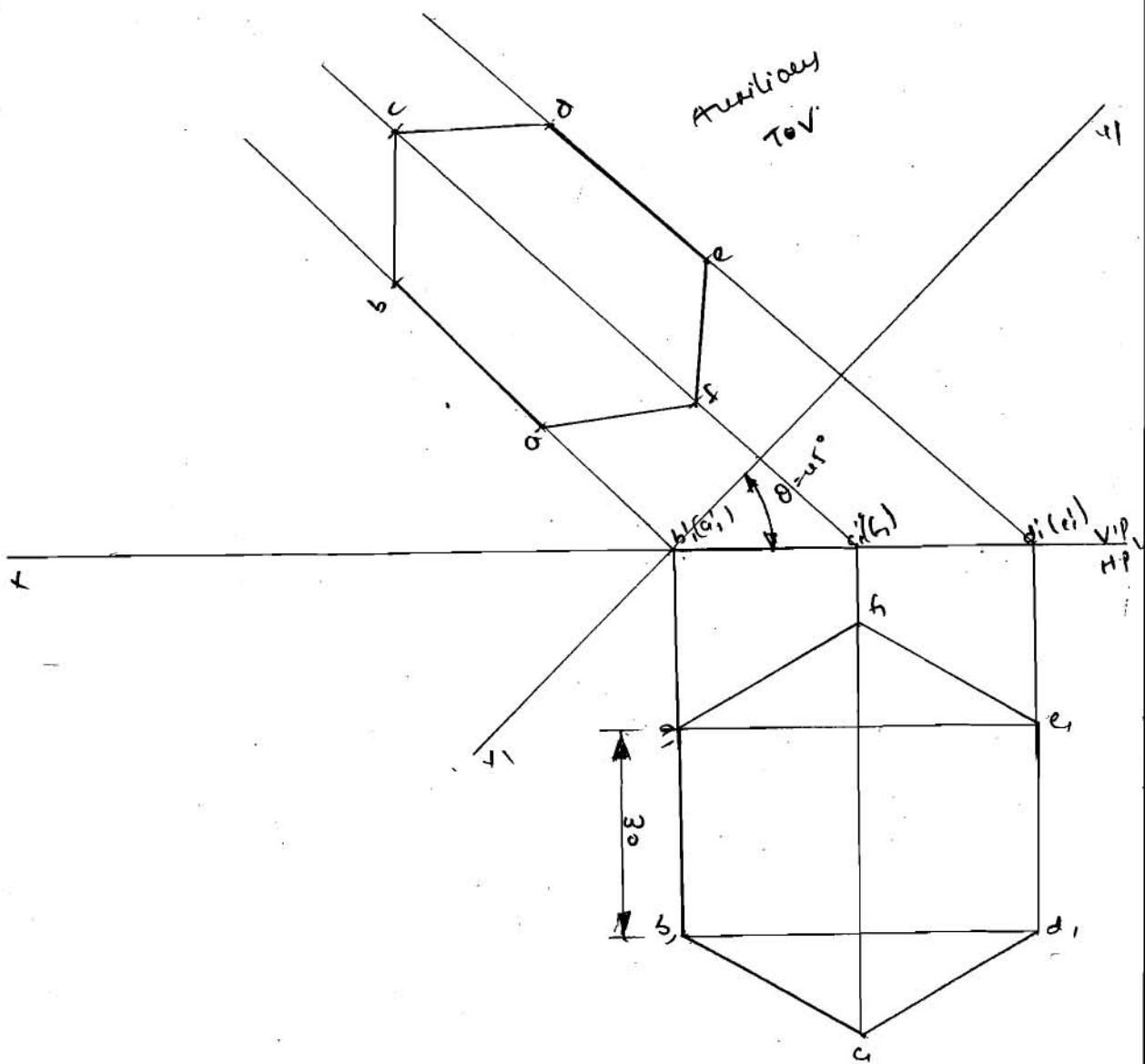
## Auxiliary Plane method

1. A hexagonal Plane side 30mm has an edge on H.P. The surface is inclined at  $45^\circ$  to H.P and  $60^\circ$  to V.P. Draw its projections.

Hexagonal Plane.

Side = 30mm

$\theta = 45^\circ$

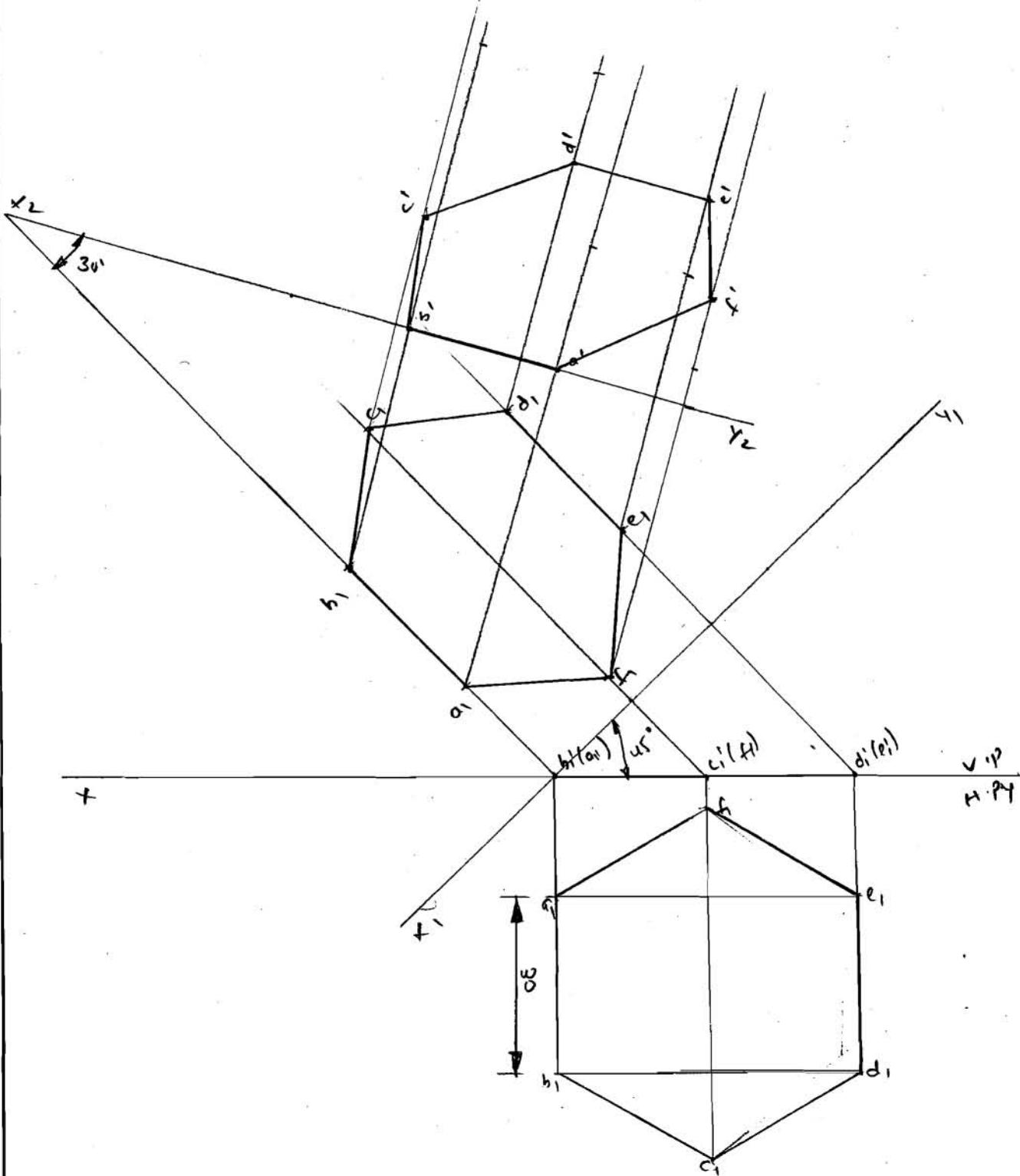


2. A hexagonal Plane of side 30mm has an edge on the H.P. It's surface is inclined at  $45^\circ$  to H.P and the edge on which the plane rests is inclined at  $30^\circ$  to V.P. Draw its projections.

Hexagonal Plane.

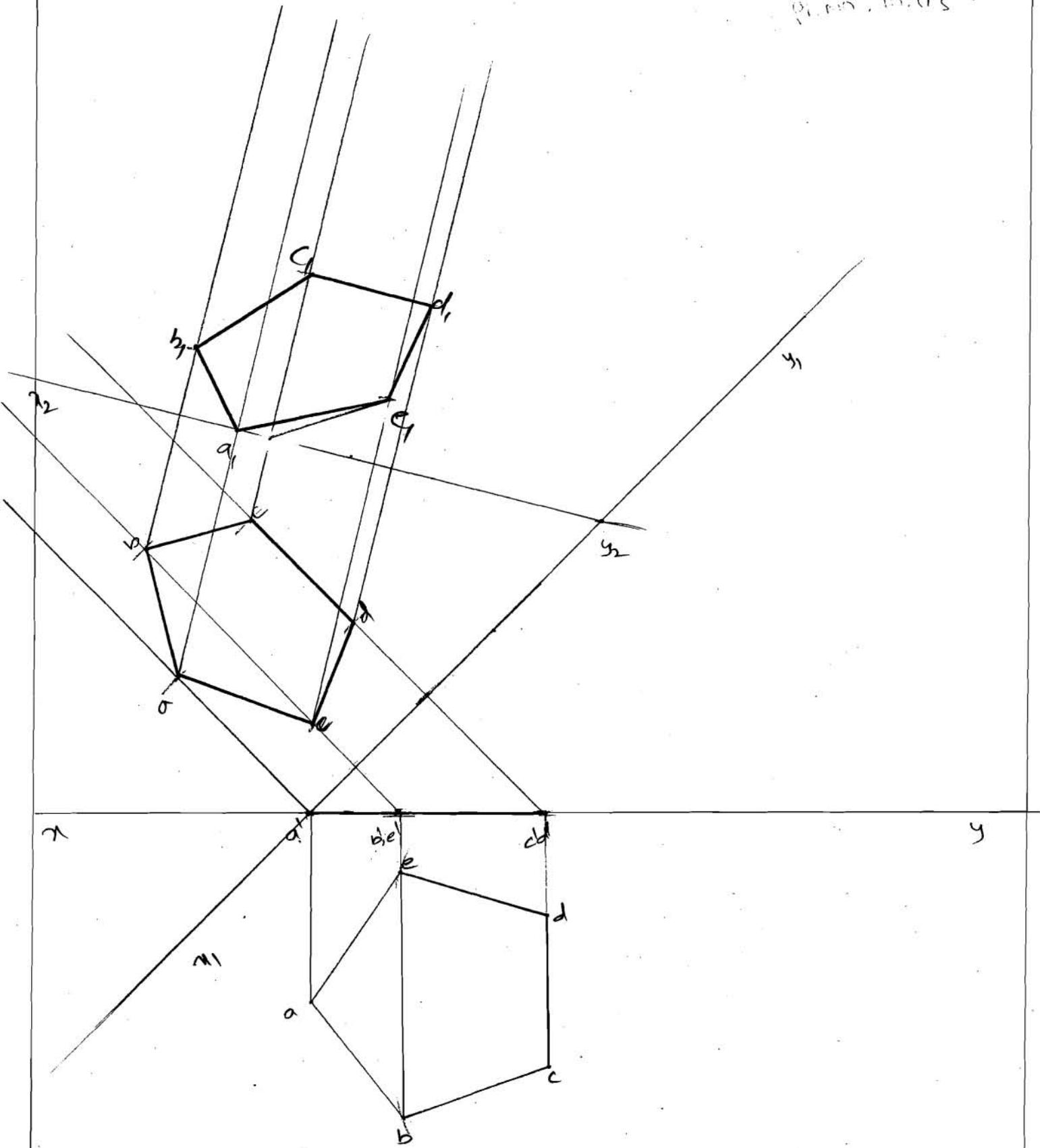
Side = 30mm.

$\phi = 30^\circ$ ,  $\theta = 45^\circ$



\* Pentagonal Plane Auxiliary Views Inclined both the planes

Ques. No. 113

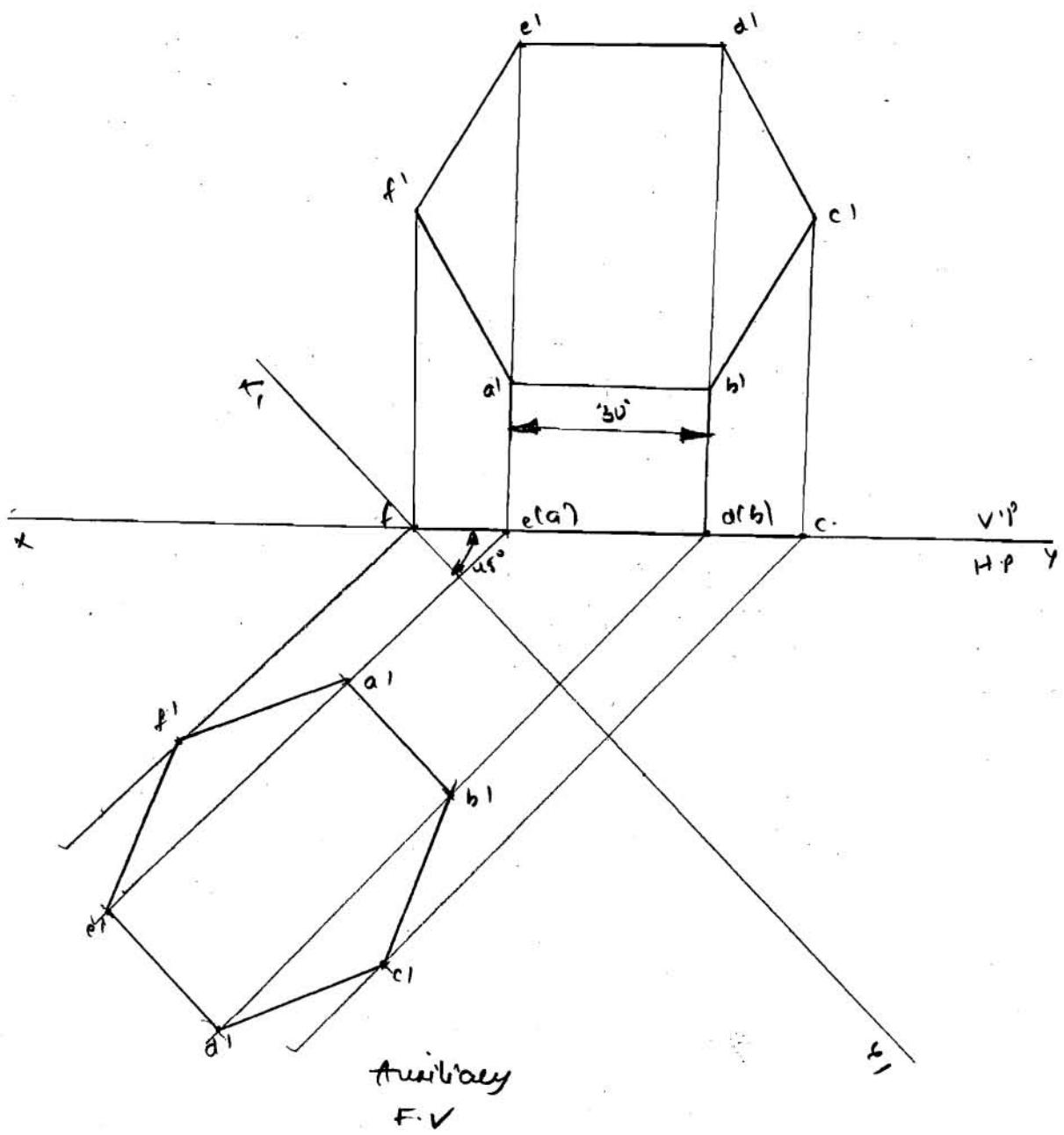


3. A hexagonal plane of side 30mm has a corner in the v.p. The surface of the plane is inclined at  $45^\circ$  to V.P and true to H.P. Draw its projections.

Hexagonal Plane

Side = 30mm

$$\theta = 45^\circ$$



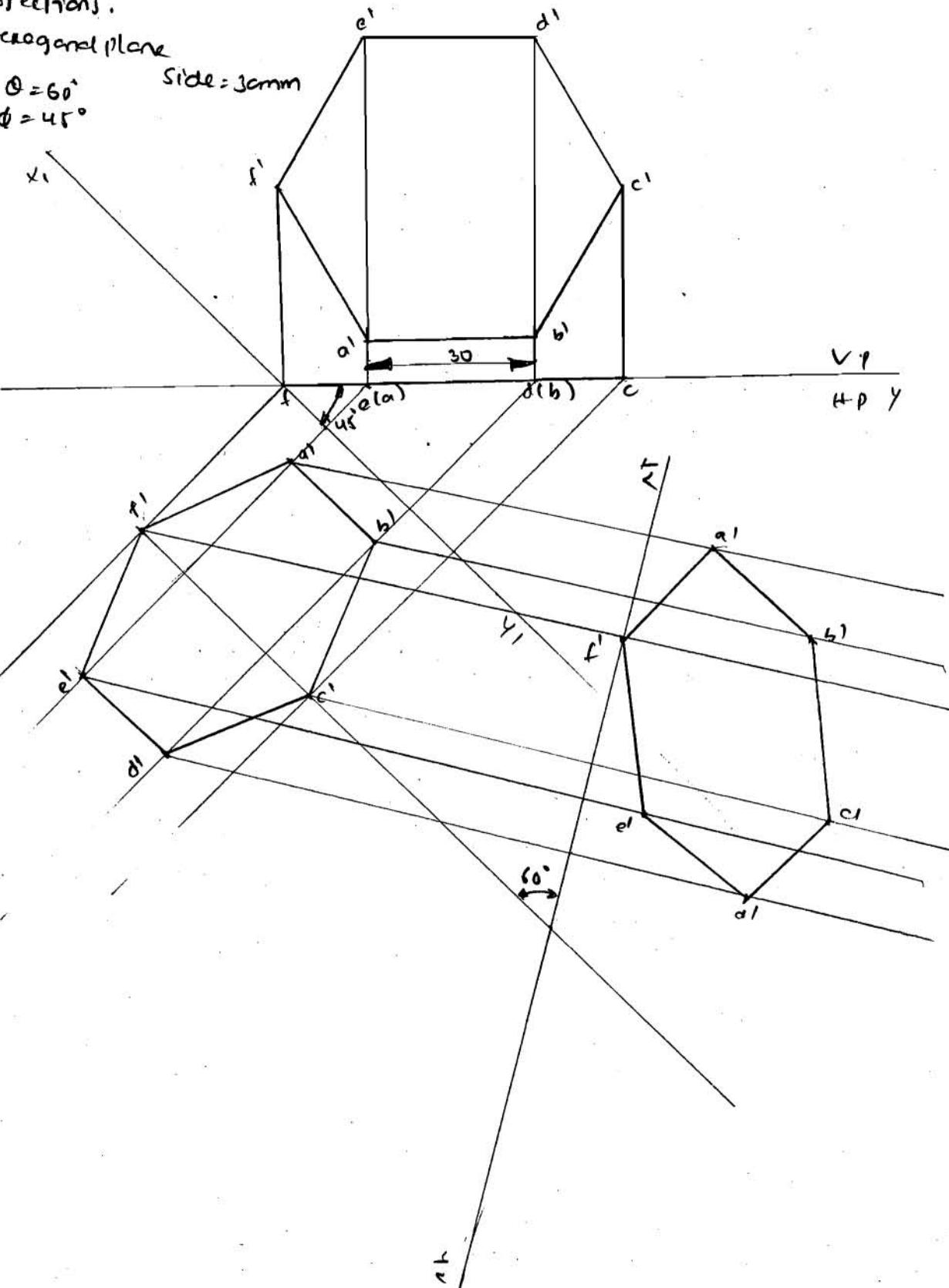
4. A hexagonal plane of side 30mm has a corner in the V.P. The surface of the plane is inclined at  $45^\circ$  to V.P and  $60^\circ$  to H.P. The F.V. of the diagonal passing through that corner is inclined at  $60^\circ$  to H.P. Draw its projections.

Hexagonal plane

$$\theta = 60^\circ$$

Side = 30mm

$$\phi = 45^\circ$$



# **UNIT-III**

## **Content**

**Projections of Regular Solids – Auxiliary Views -**  
**Sections or Sectional views of Right Regular Solids**  
**– Prism, Cylinder, Pyramid, Cone – Auxiliary views**  
**– Sections of Sphere**

# **Unit-III**

## **Projections of Solids:**

A solid has three dimensions, viz. length, breadth and thickness. To represent a solid on a flat surface having only length and breadth, at least two orthographic views are necessary. Sometimes, additional views projected on auxiliary planes become necessary to make the description of a solid complete.

## **This chapter deals with the following topics:**

1. Types of solids.
2. Projections of solids in simple positions.
  - (a) Axis perpendicular to the H.P.
  - (b) Axis perpendicular to the V.P.
  - (c) Axis parallel to both the H.P. and the V.P.
3. Projections of solids with axes inclined to one of the reference planes and parallel to the other.
  - (a) Axis inclined to the V.P. and parallel to the H.P.
  - (b) Axis inclined to the H.P. and parallel to the V.P.
4. Projections of solids with axes inclined to both the H.P. and the V.P.
5. Projections of spheres.

### 3. PROJECTION OF SOLIDS

1. A square pyramid side of base 40mm and axis 60mm is resting on its base on the H.P. Draw its projections when
- Aside of the base is parallel to V.P.
  - Aside of the base is inclined at  $30^\circ$  to V.P.
  - All sides of the base are equally inclined to V.P.

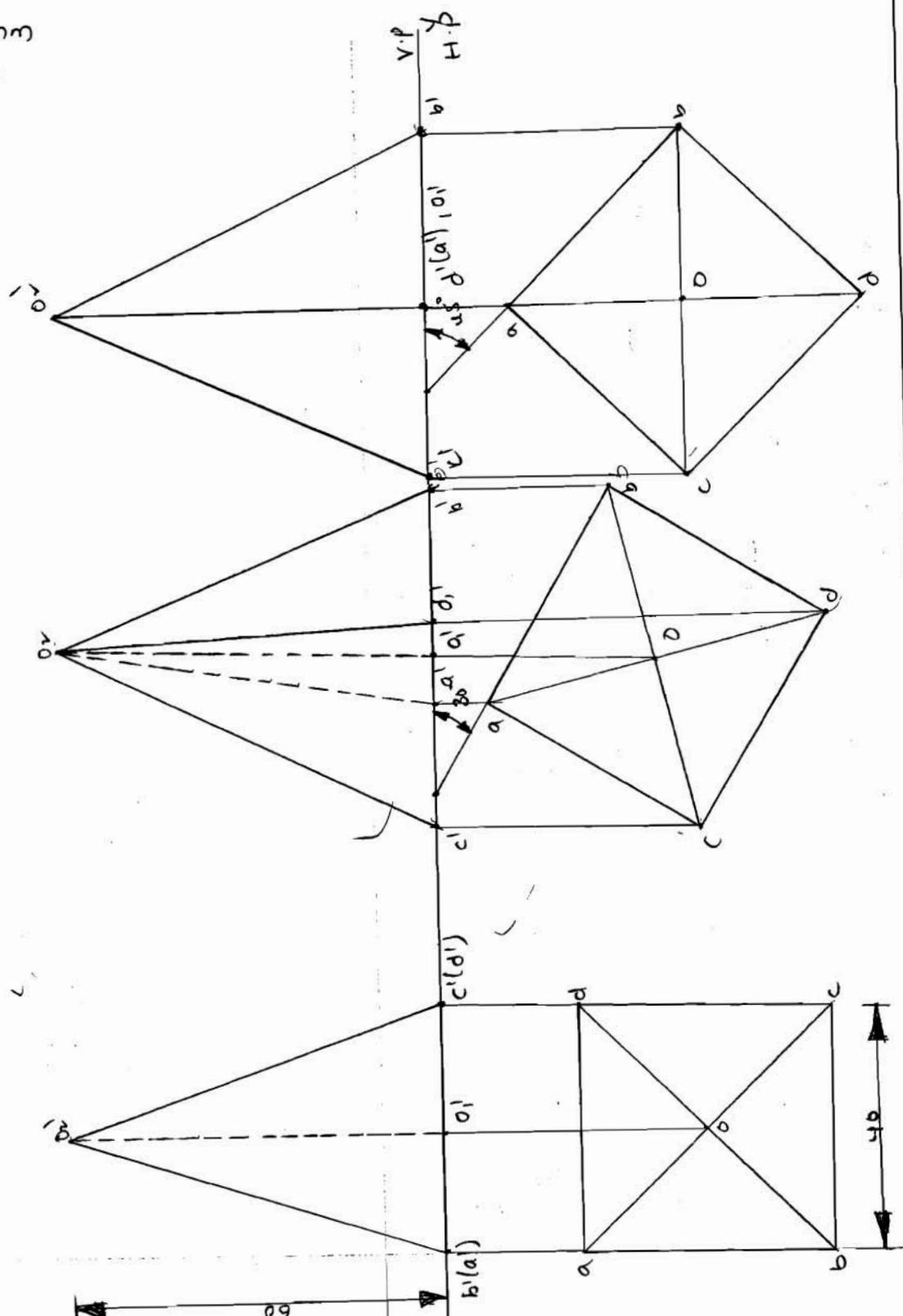
Sol:

Square Pyramide

Base = 40mm

Axis = 60mm

$\phi = 30^\circ$



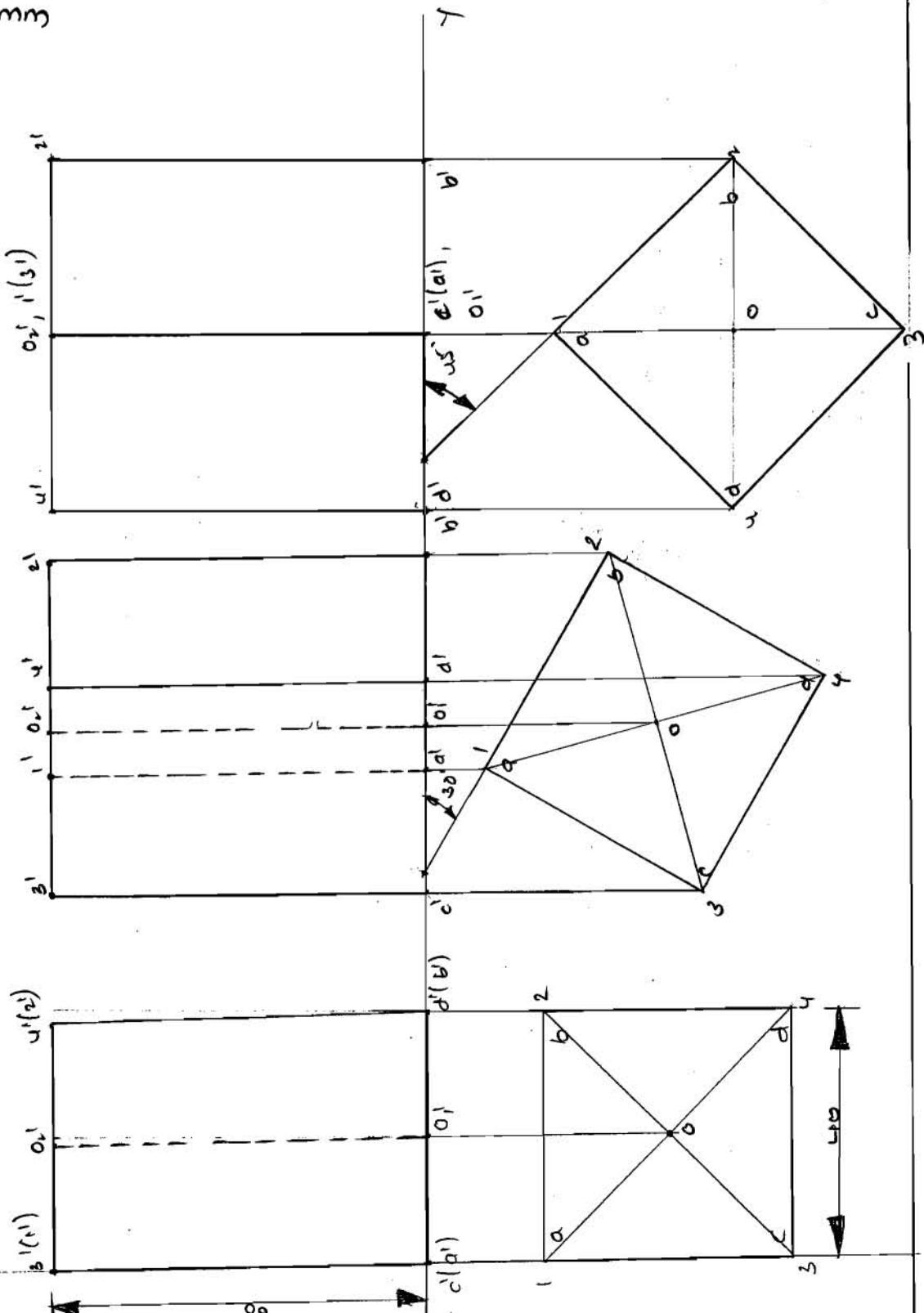
- Q. A square prism of 40mm above edges and 60mm long axis is resting on its base on the ground. Draw its projections when
- A face is perpendicular to V.P
  - A face is inclined at  $30^\circ$  to V.P
  - All the faces are equally inclined.

Ans: square prism.

$$\text{Base} = 40\text{mm}$$

$$\text{Axis} = 60\text{mm}$$

$$\phi = 30^\circ$$



3. A Pentagonal Prism of 30mm base edges and 60mm long axis has one of its bases in the V.P. Draw its projections when
- A rectangular face is parallel to and 15mm above H.P.
  - A face is perp to H.P.
  - A face is inclined at  $45^\circ$  to H.P.

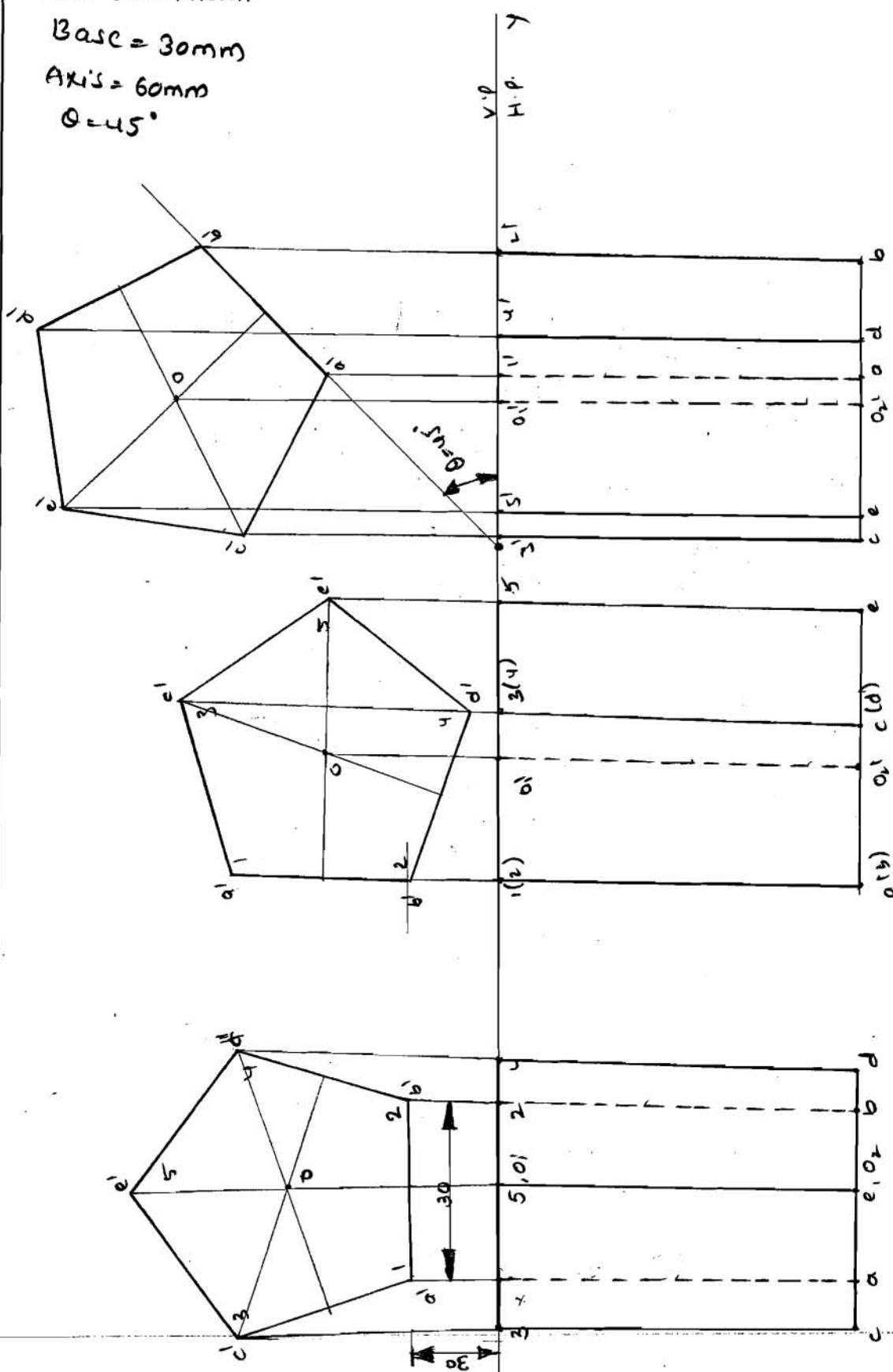
Sol:-

Pentagonal Prism.

Base = 30mm

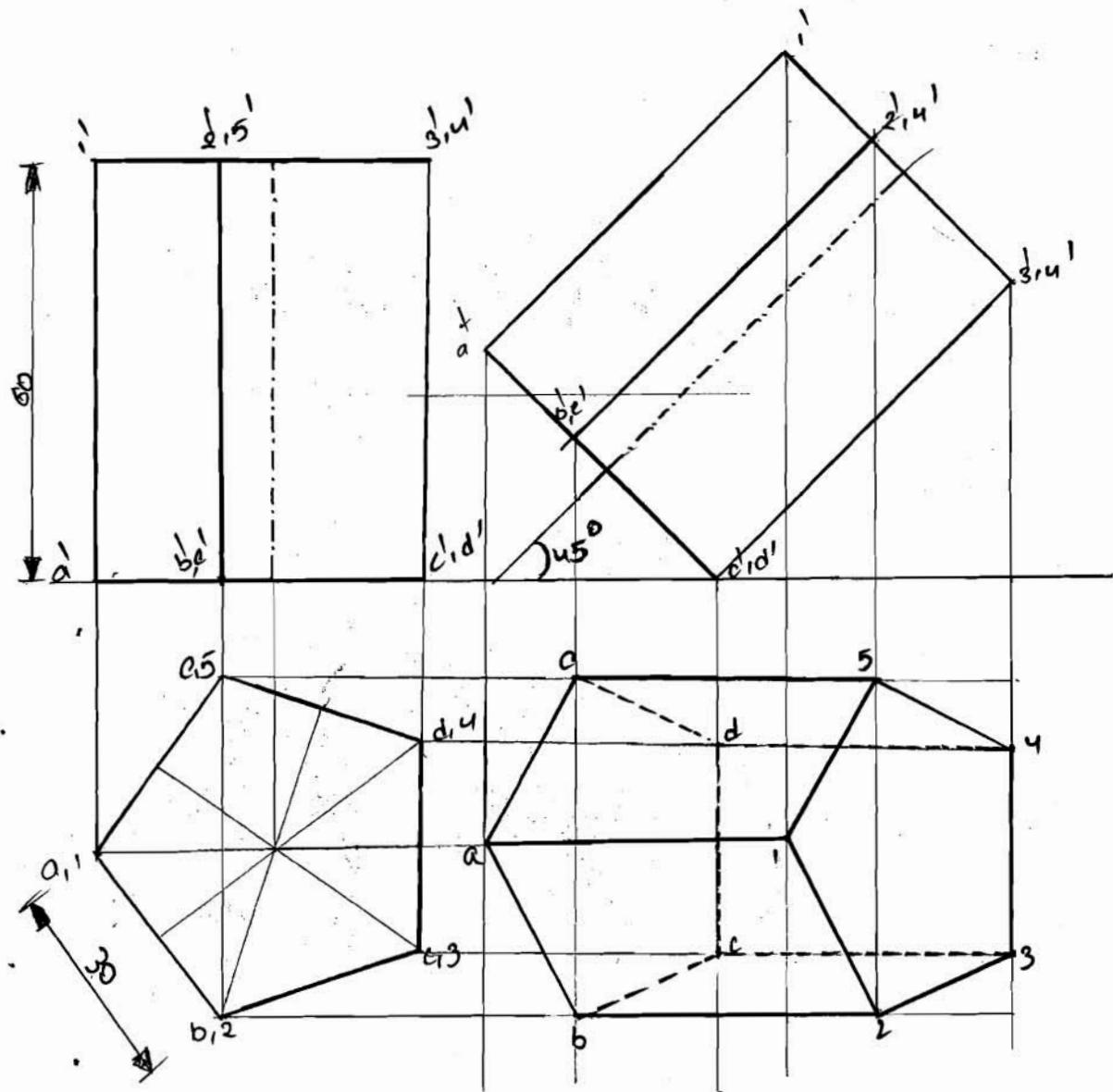
Axis = 60mm

$\theta = 45^\circ$

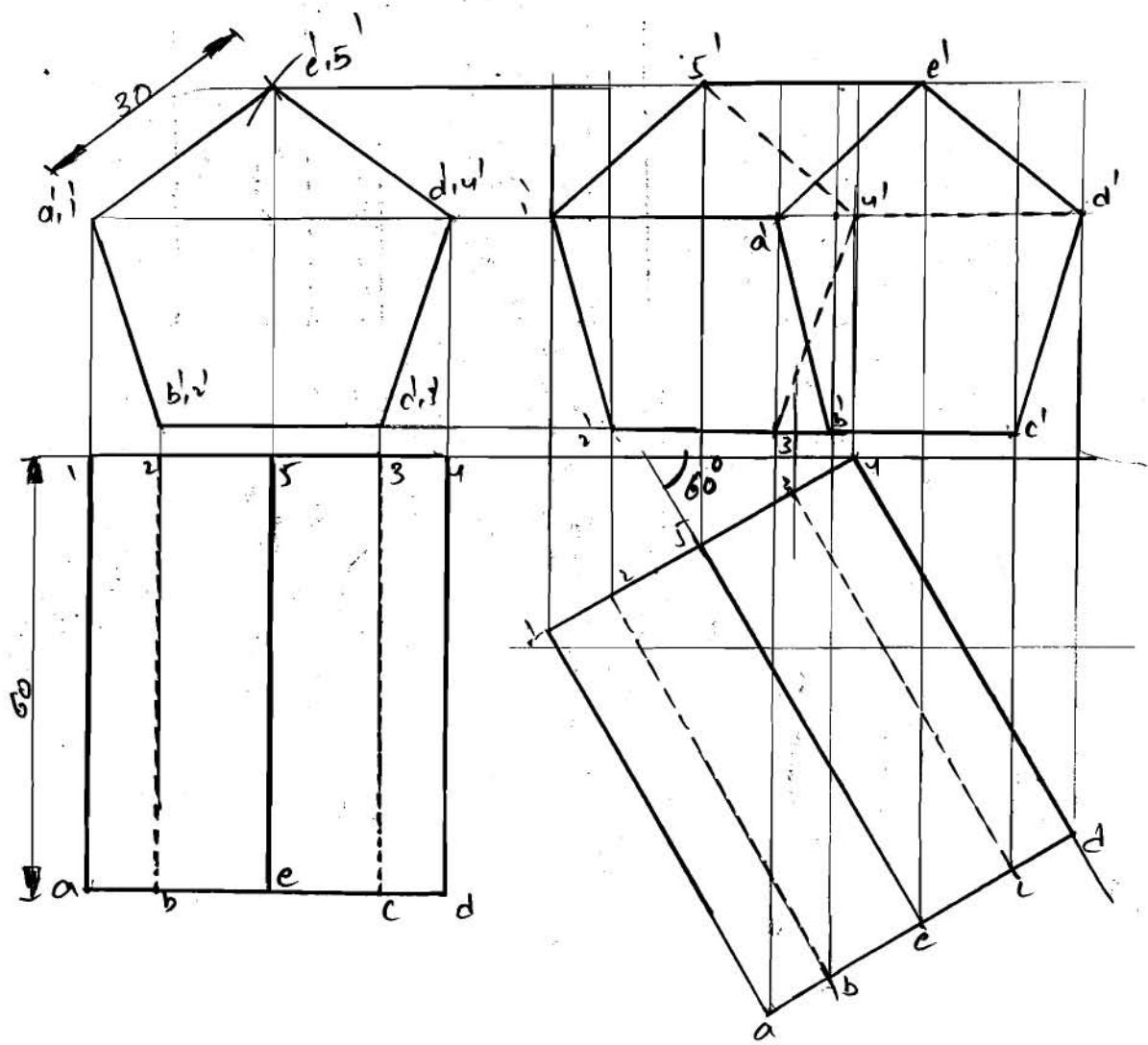


Pentagonal Prism

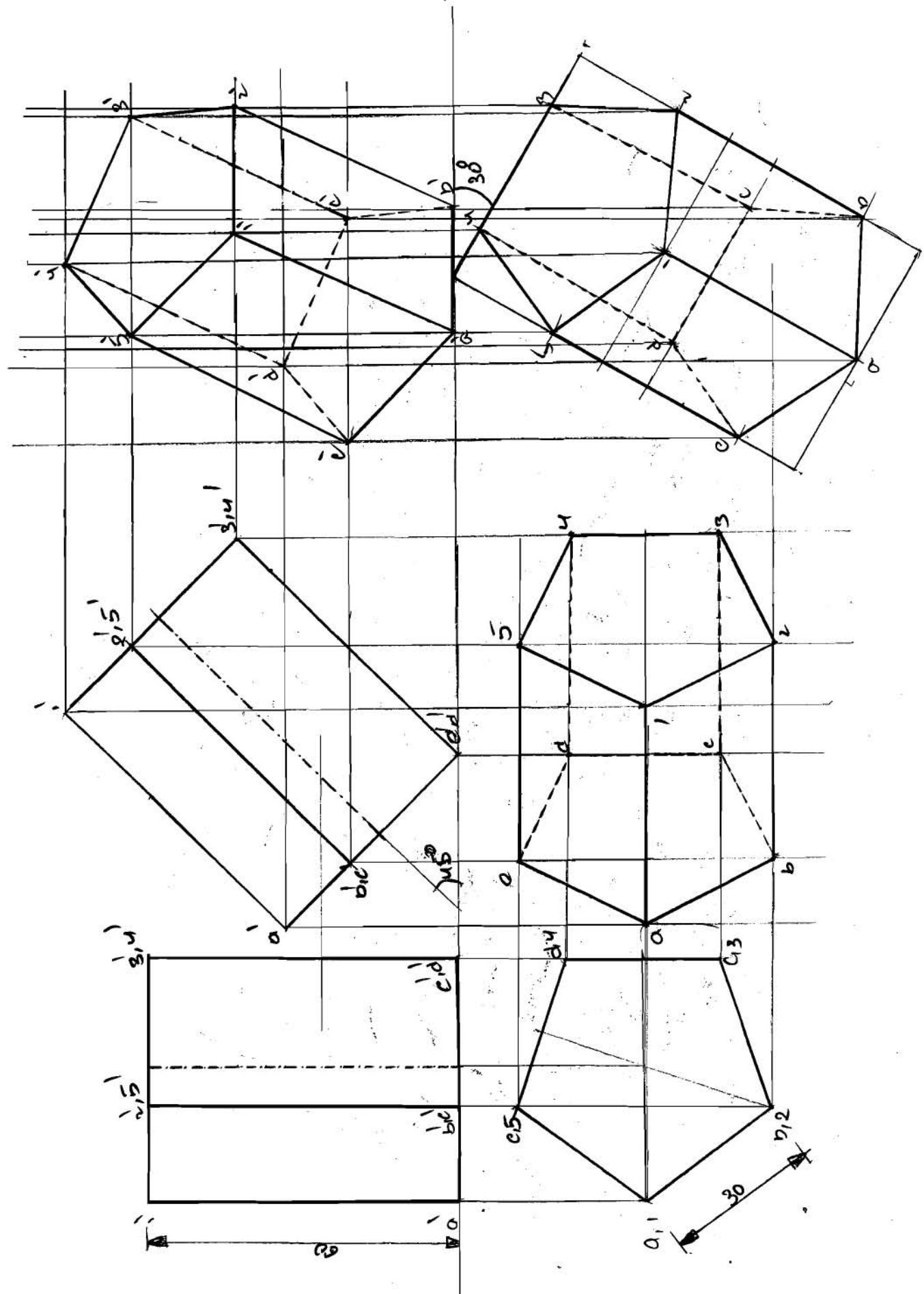
\* Pentagonal Prism Inclined to H.P



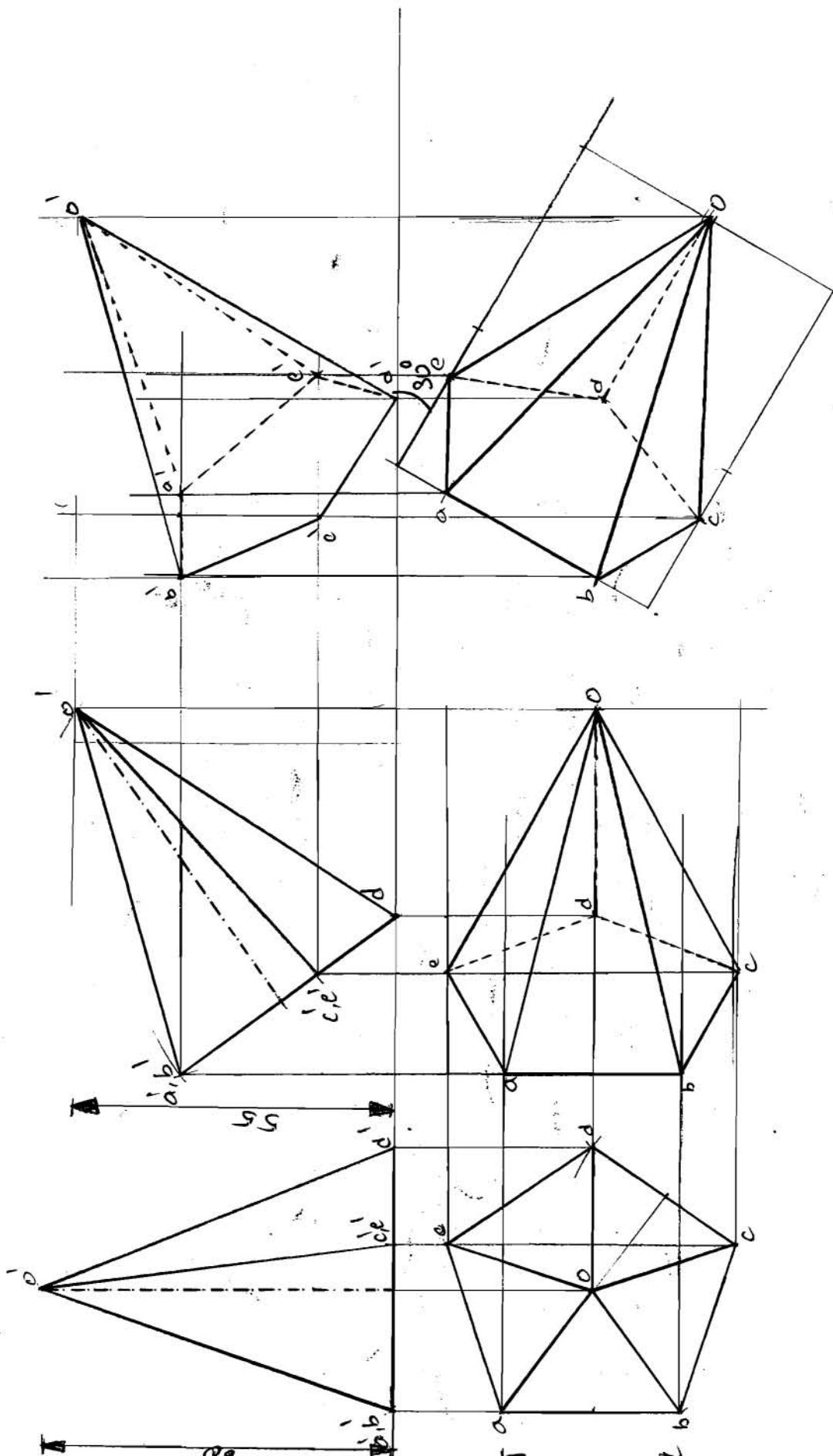
\* Pentagonal Prism Reflected to V.P



\* Pentagonal Prism Axis inclined from the plane V.P & H.P



\* Pentagonal Pyramid Axis inclined both the plane H.P & V.P

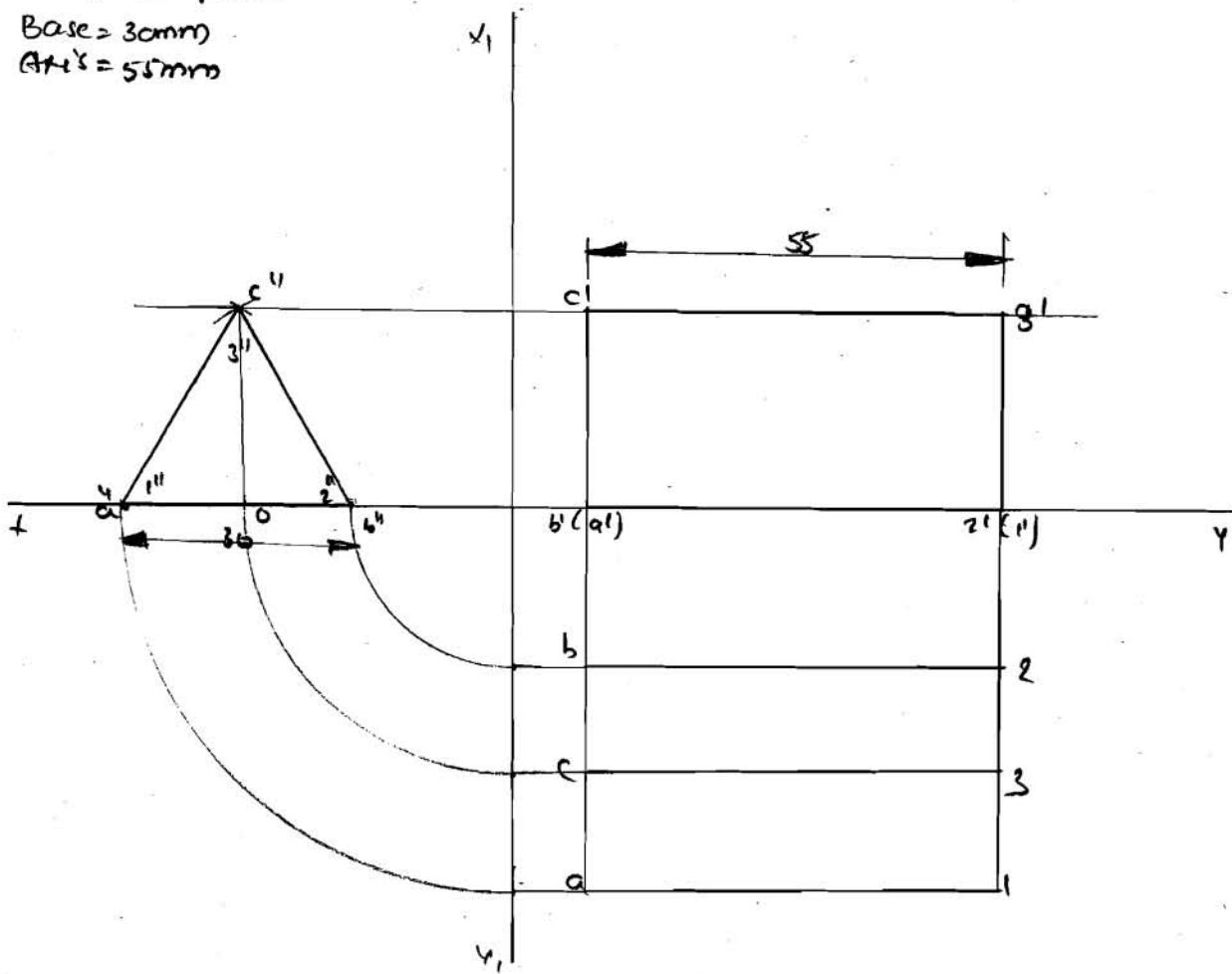


2. A triangular prism of base 30mm and axis 55mm long lies on its rectangular face in H.P. with its axis parallel to V.P. Draw the three views of the prism.

Triangular prism

Base = 30mm

Axis = 55mm

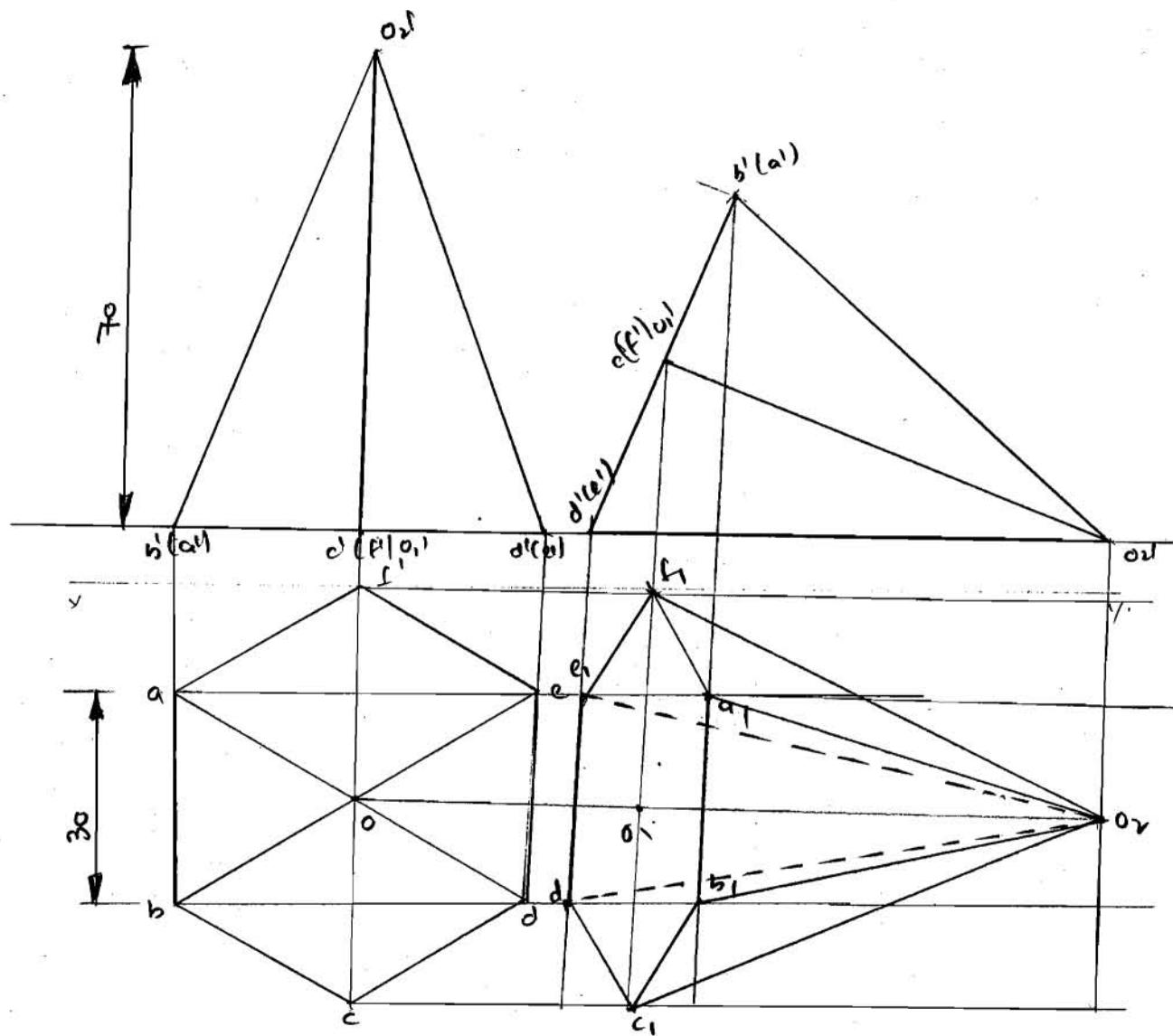


Q:- A Hexagonal pyramid with 30mm base edge and 70mm long axis as a triangular face on the ground, and the axis parallel to the V.P. Draw its projections.

### Hexagonal Pyramid

Base = 30mm

Axis = 70mm.



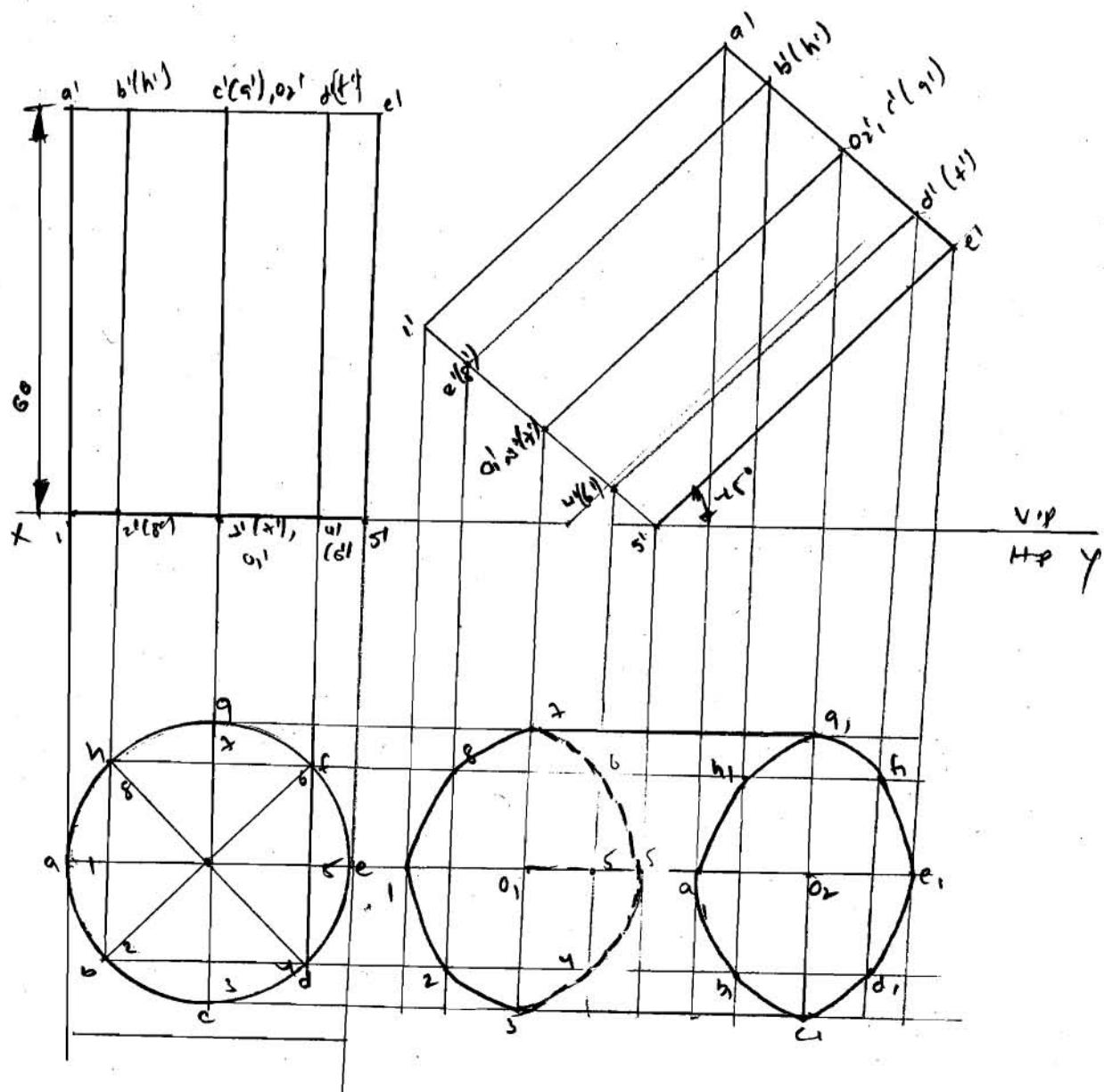
Q: Draw the projections of a cylinder of 40mm diameter and 60mm long axis when it is lying on the H.P. with axis inclined at  $45^\circ$  to H.P. and parallel to V.P.

Cylinder

Diameter ( $\phi$ ) = 40mm

Axis = 60mm

$\theta = 45^\circ$  / parallel to V.P.

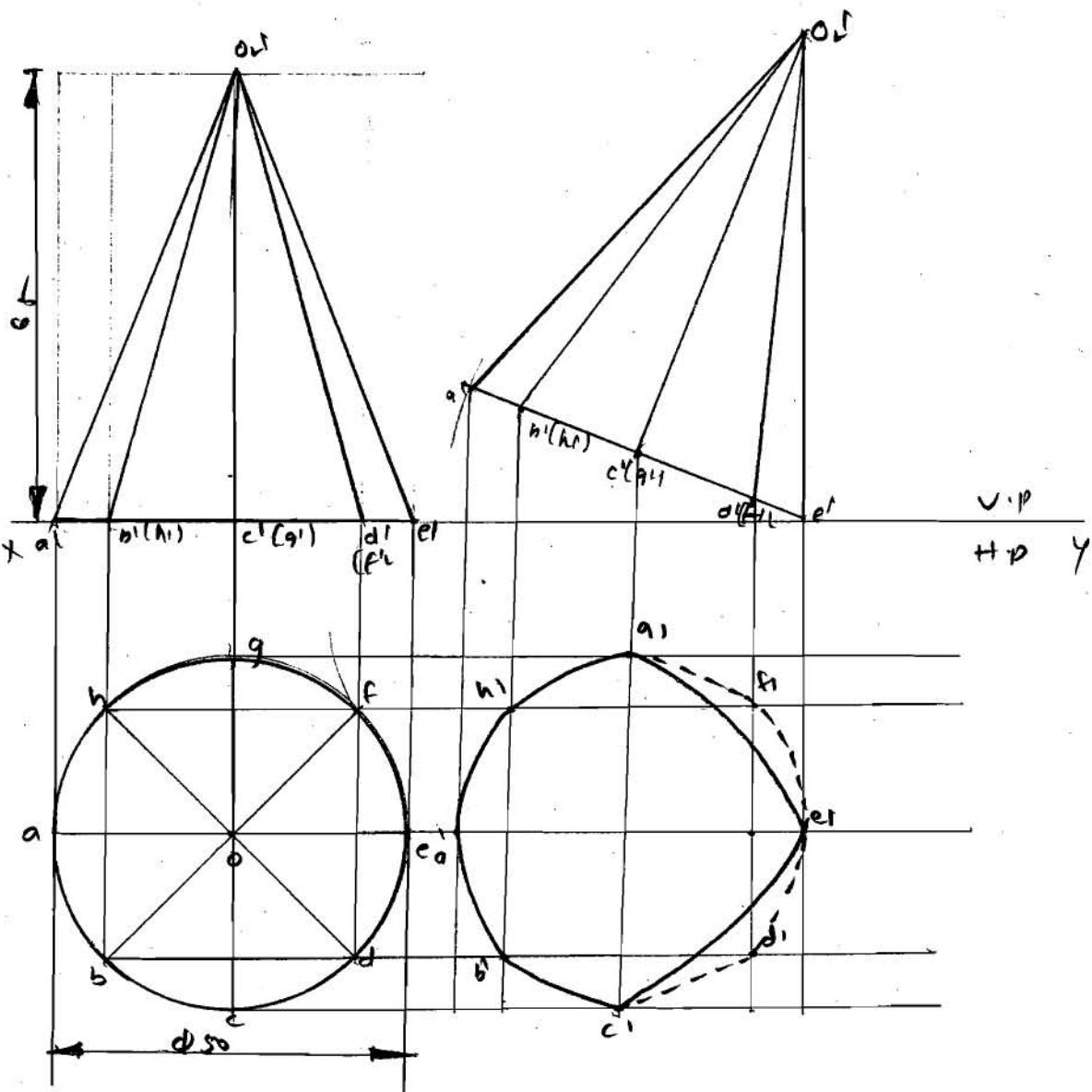


a: A right circular cone with 50mm diameter base and 65mm long axis rest on its base rim on the H.P. with its axis parallel to V.P and one of the generator perpendicular to H.P. Draw the projections of the cone.

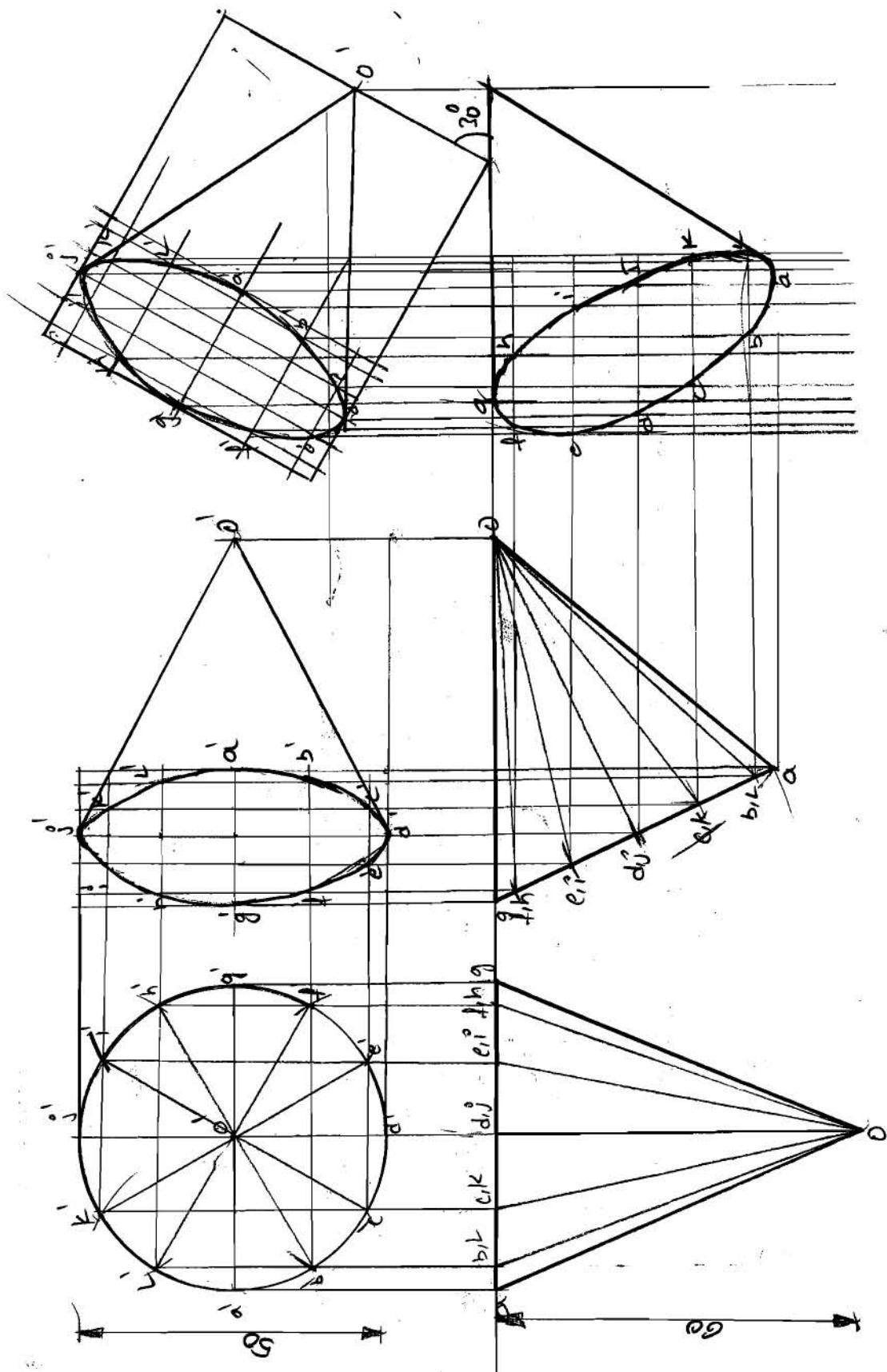
Cone

Diameter =  $\phi 50\text{mm}$

Axis = 65mm.



\* cone Ans Reckined the both plane V.P & H.P

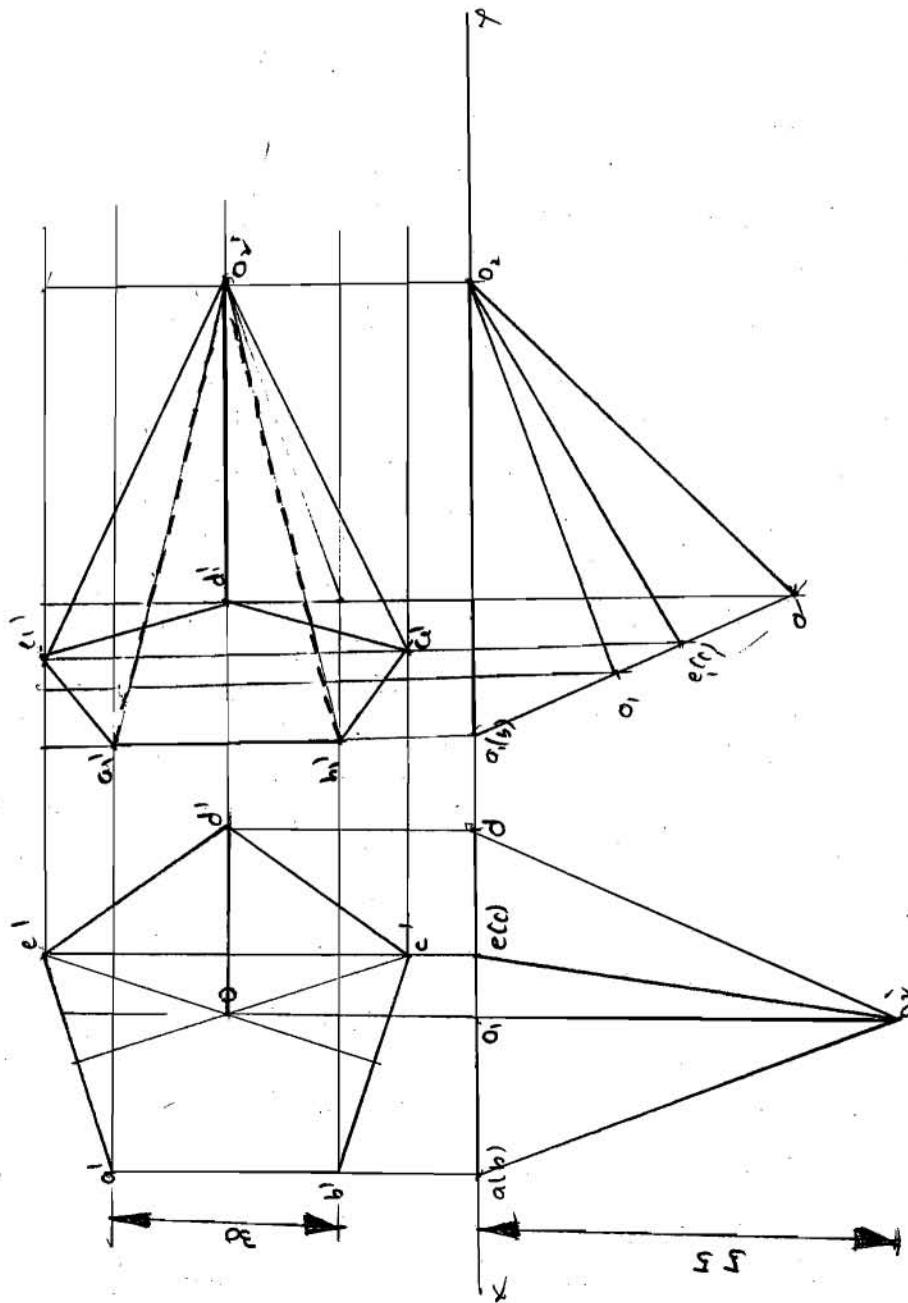


Q: A Pentagonal Pyramid base side 30mm and axis 55mm long, has a triangular face in the V.P. and axis parallel to H.P. Draw its projections.

### Pentagonal Pyramid

Base = 30mm

Axis = 55mm



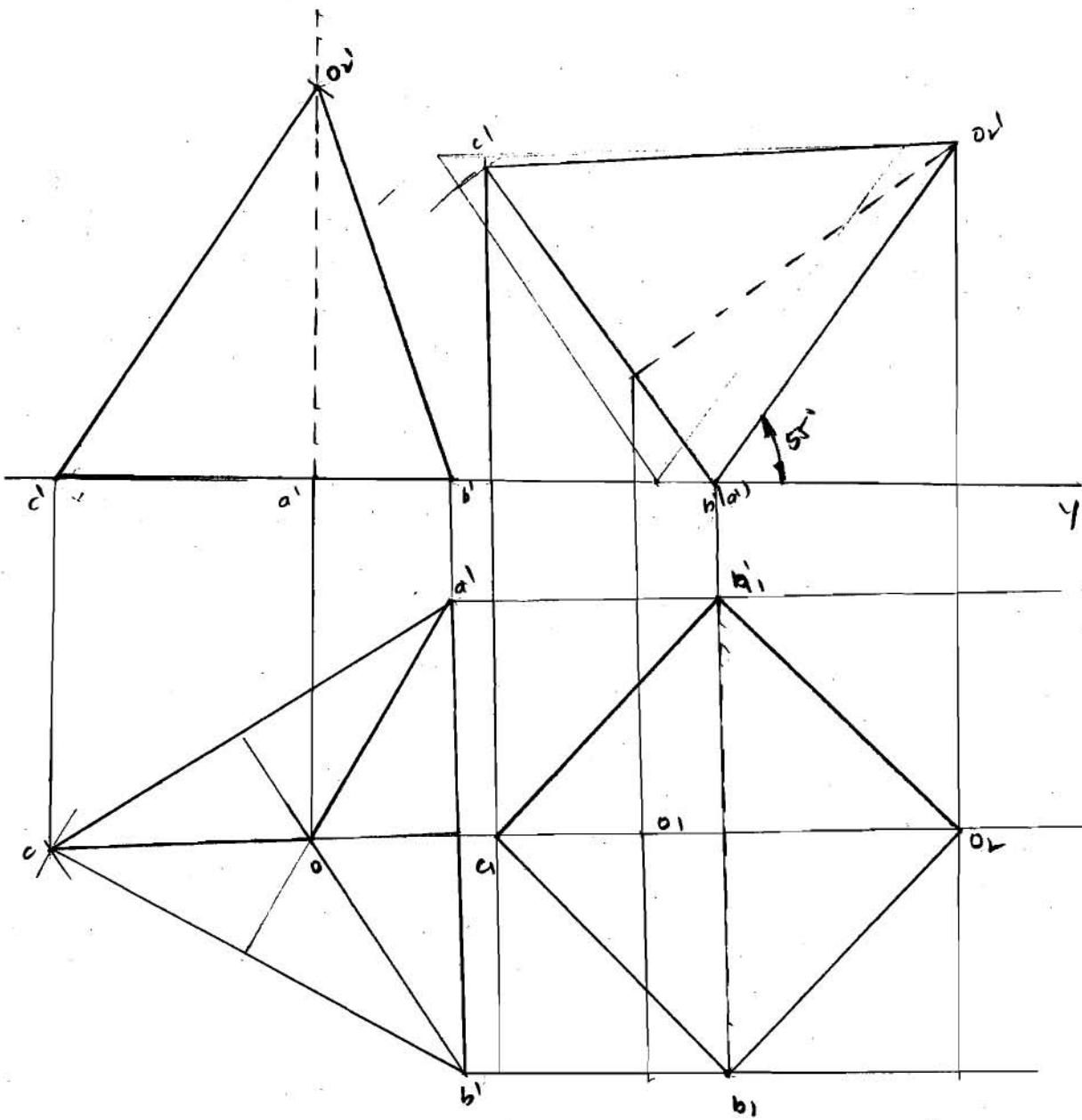
d:- A tetrahedron of 70mm long edge on the ground and the faces containing that edge are equally inclined to the H.P. Draw its projections when the edge lying on the ground lies H.V.P.

Tetrahedrons

Side = 70mm

Long edge on H.P.

$\theta = 45^\circ$



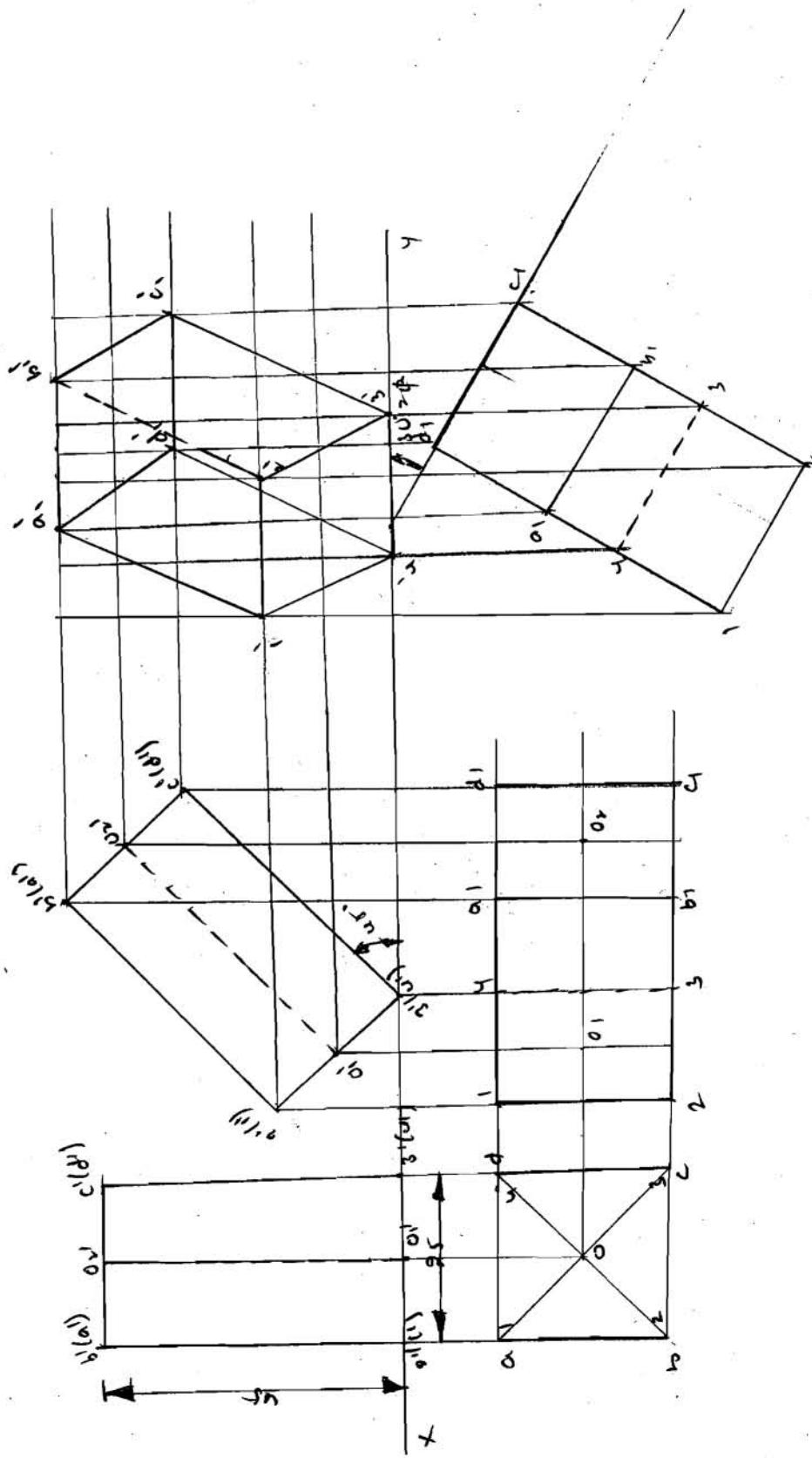
- Q: A square prism 25mm edge base and 45mm long axis has its axis inclined at  $45^\circ$  to H.P and edge of its base on which the prism rests is inclined at  $30^\circ$  to V.P. Draw its projections.

Square Prism

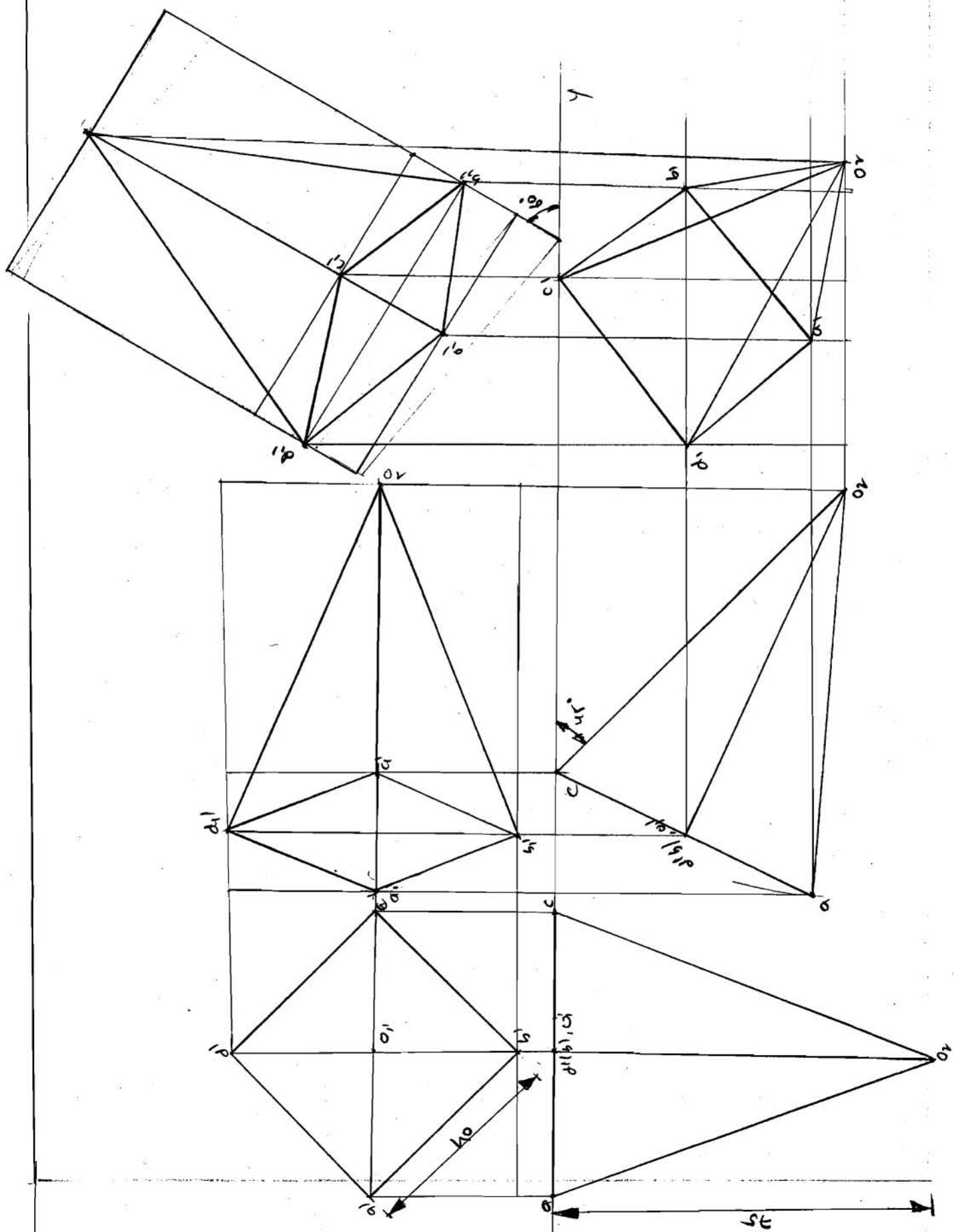
$$\text{Base} = 25\text{mm}$$

$$\text{Axis} = 45\text{mm}$$

$$\phi = 30^\circ, \theta = 45^\circ$$



Q: A square pyramid of 40mm base side and 75mm long axis has a corner of its base on the V.P. The slant edge contained by that corner is inclined at  $45^\circ$  to V.P. and the plane containing the slant edge and the axis is inclined at  $60^\circ$  to H.P. - Draw its projections.



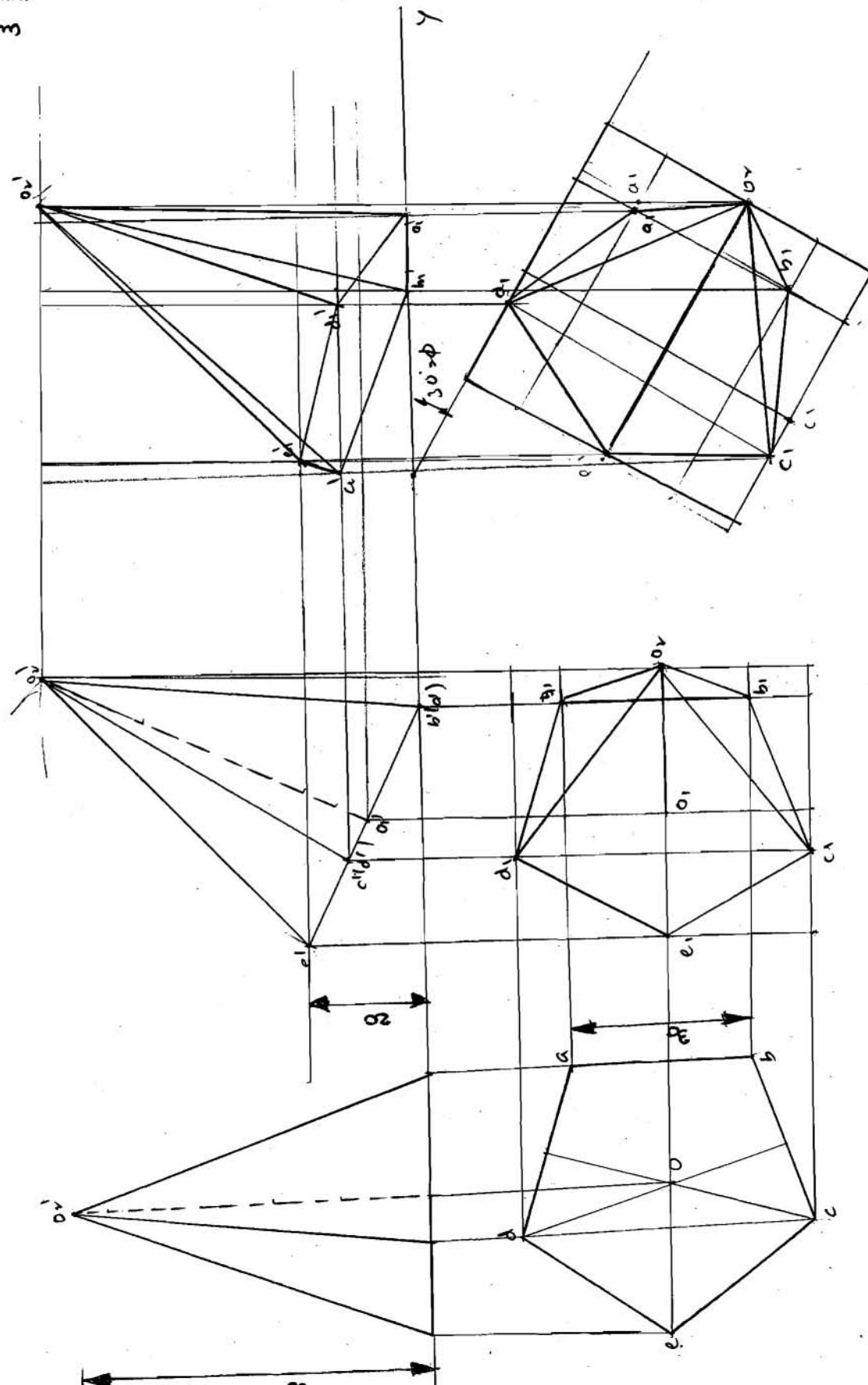
2. A Pentagonal pyramid of 30mm base side and 60mm long axis resting on an edge of its base on the ground so that the highest point on the base is 20mm above the ground. Draw its projections if the vertical plane containing the axis is inclined at  $30^\circ$  to V.P.

Pentagonal Pyramid

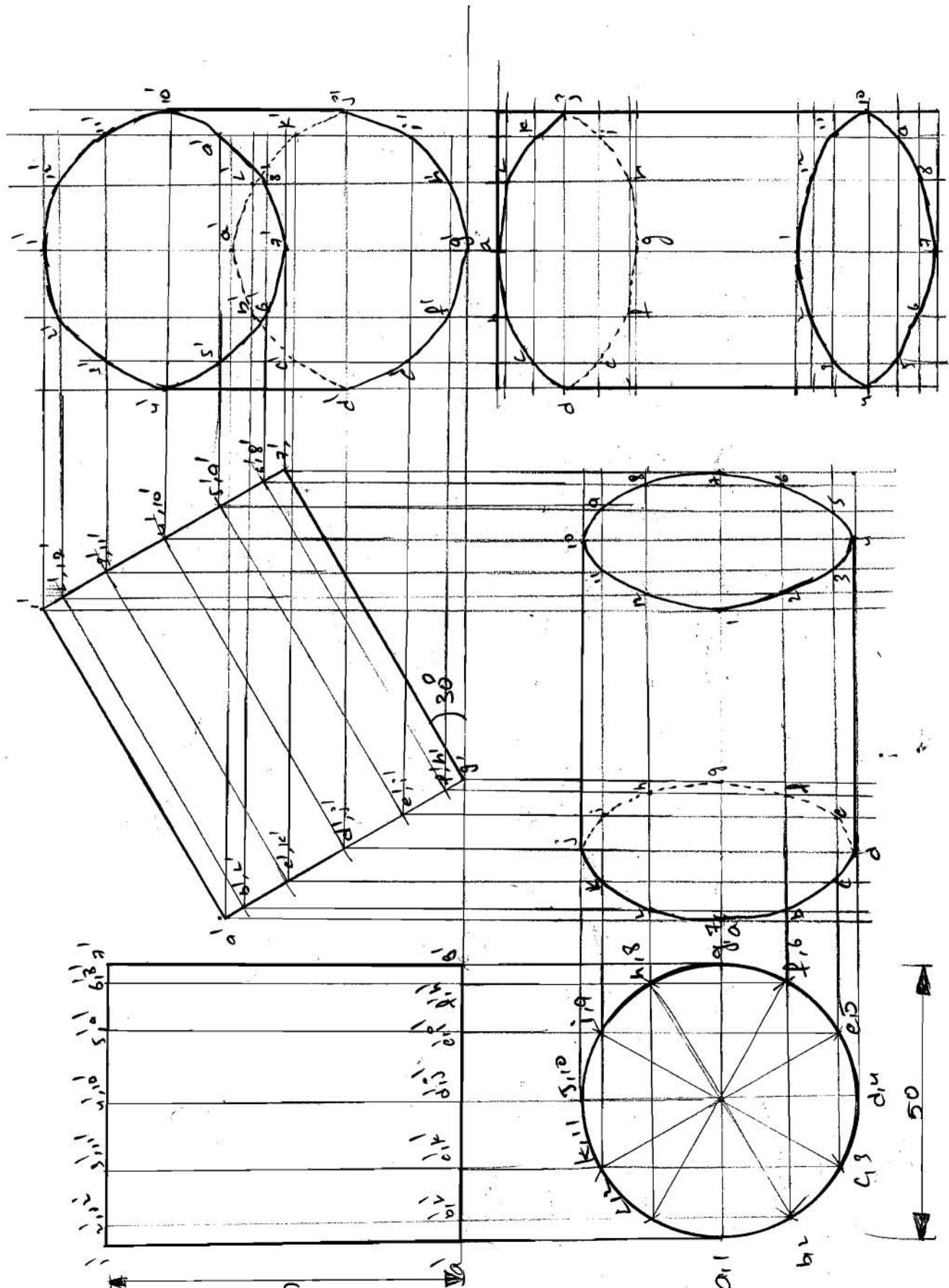
$$B = 30\text{mm}$$

$$A = 60\text{mm}$$

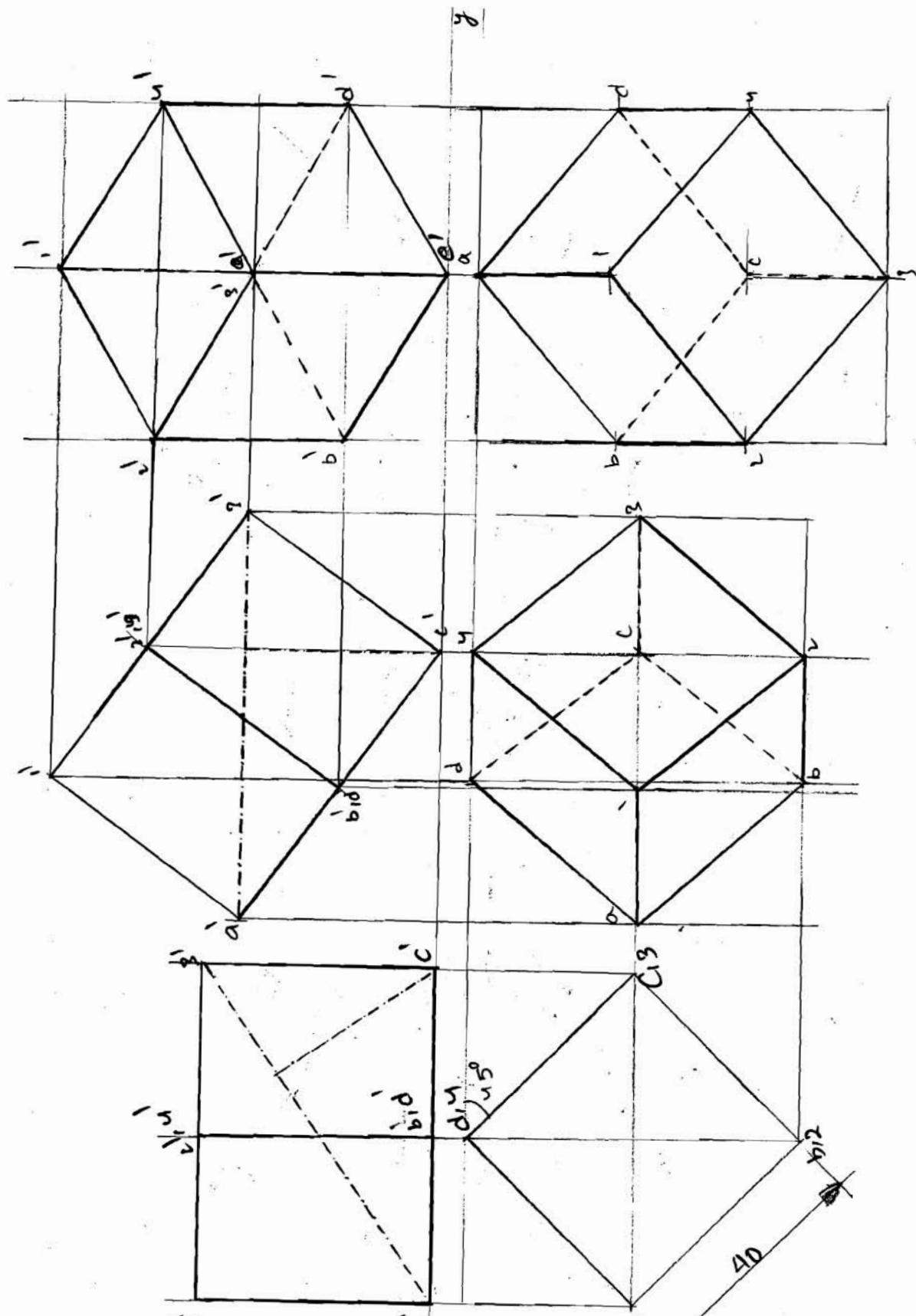
$$d = 30^\circ$$



\* Cylinder inclined both the plane V.P & H.P

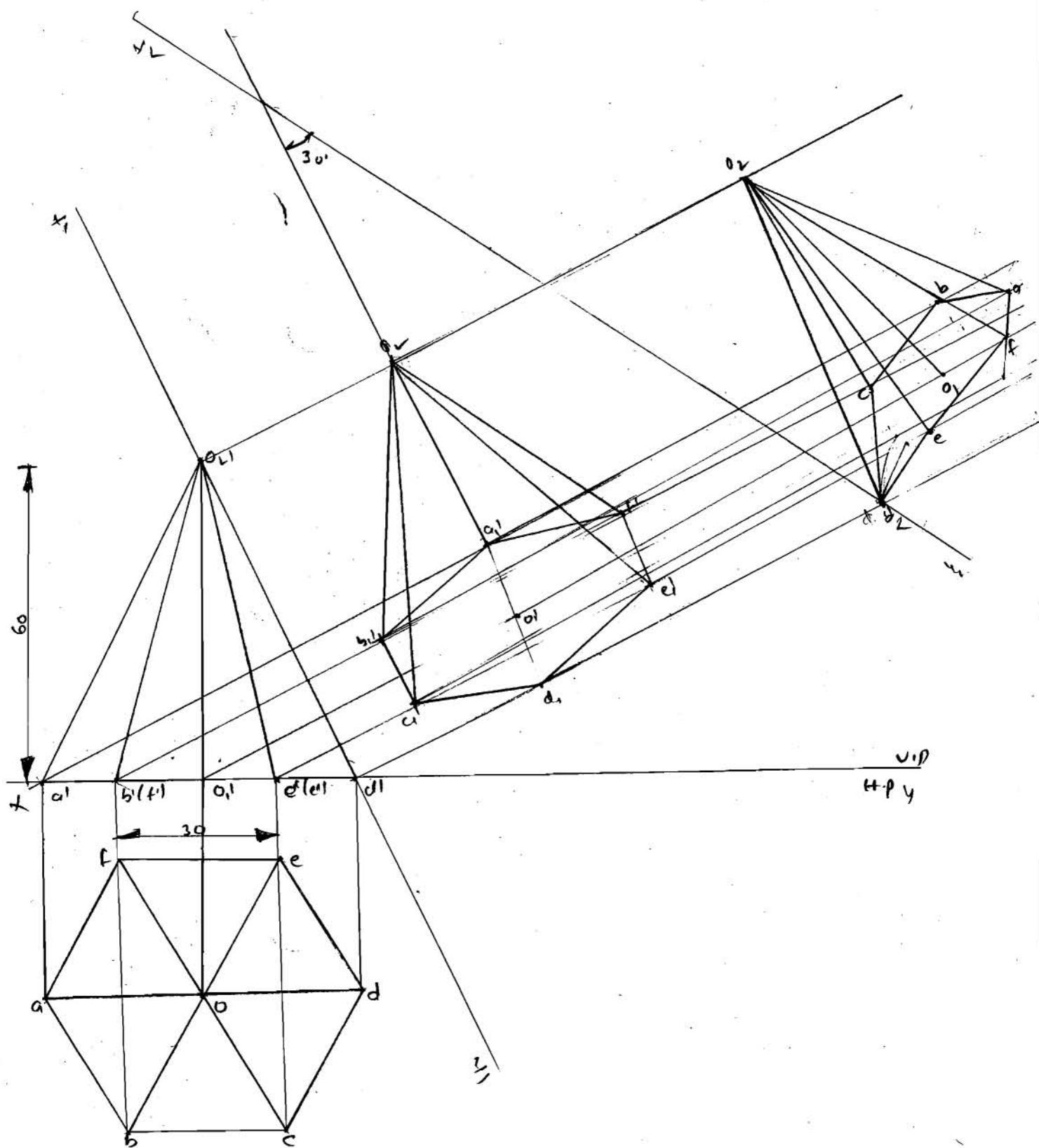


\* Cube Diagonal Parallel to the H.P. (Included both A.P.E, V.P)



A Hexagonal Pyramid of base side 30mm and axis 60mm has one of its slant edges on the H.P. and inclined at  $30^\circ$  to the V.P. Draw its projections when the base is visible.

$B = 30\text{mm}$  Hexagonal Pyramid.  
 $\text{Axis} = 60\text{mm}$

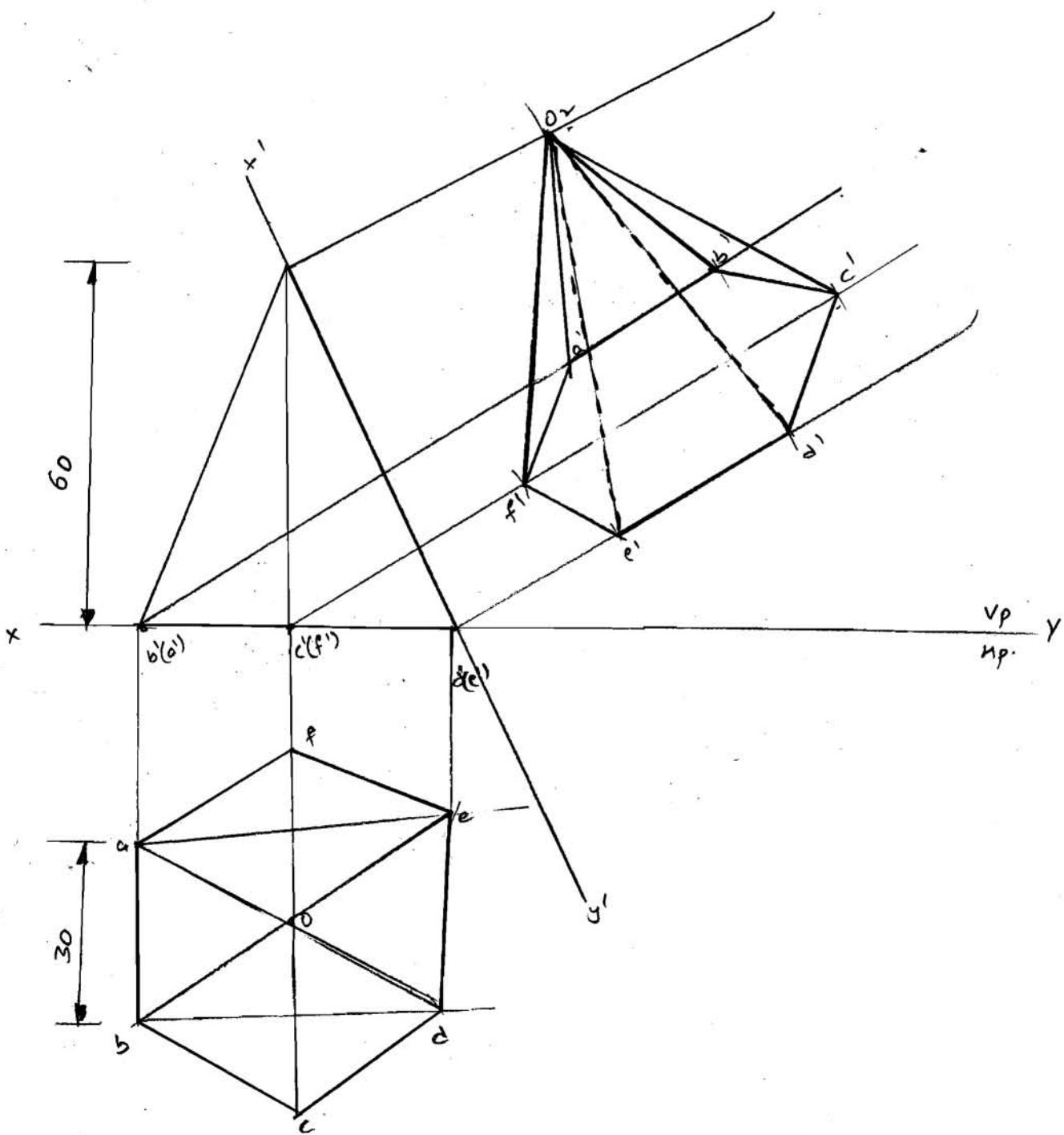


1. A Hexagonal Pyramid base side 30mm and axis 60mm as a triangular face on the ground and the axis parallel to V.P. Draw its projections

Pyramid

$$B = 30\text{mm}$$

$$A = 60\text{mm}$$



## **Sections of solids:**

Invisible features of an object are shown by dotted lines in their projected views. But when such features are too many, these lines make the views more complicated and difficult to interpret. In such cases, it is customary to imagine the object as being cut through or sectioned by planes. The part of the object between the cutting plane and the observer is assumed to be removed and the view is then shown in section.

The imaginary plane is called a section plane or a cutting plane. The surface produced by cutting the object by the section plane is called the section. It is indicated by thin section lines uniformly spaced and inclined at  $45^\circ$ .

The projection of the section along with the remaining portion of the object is called a sectional view. Sometimes, only the word section is also used to denote a sectional view.

**Section planes:** Section planes are generally perpendicular planes. They may be perpendicular to one of the reference planes and either perpendicular, parallel or inclined to the other plane. They are usually described by their traces. It is important to remember that the projection of a section plane, on the plane to which it is perpendicular, is a straight line. This line will be parallel, perpendicular or inclined to xy, depending upon the section plane being parallel, perpendicular or inclined respectively to the other reference plane.

**Sections:** The projection of the section on the reference plane to which the section plane is perpendicular, will be a straight line coinciding with the trace of the section plane on it. Its projection on the other plane to which it is inclined is called apparent section. This is obtained by

- (i) Projecting on the other plane, the points at which the trace of the section plane intersects the edges of the solid and
- (ii) Drawing lines joining these points in proper sequence.

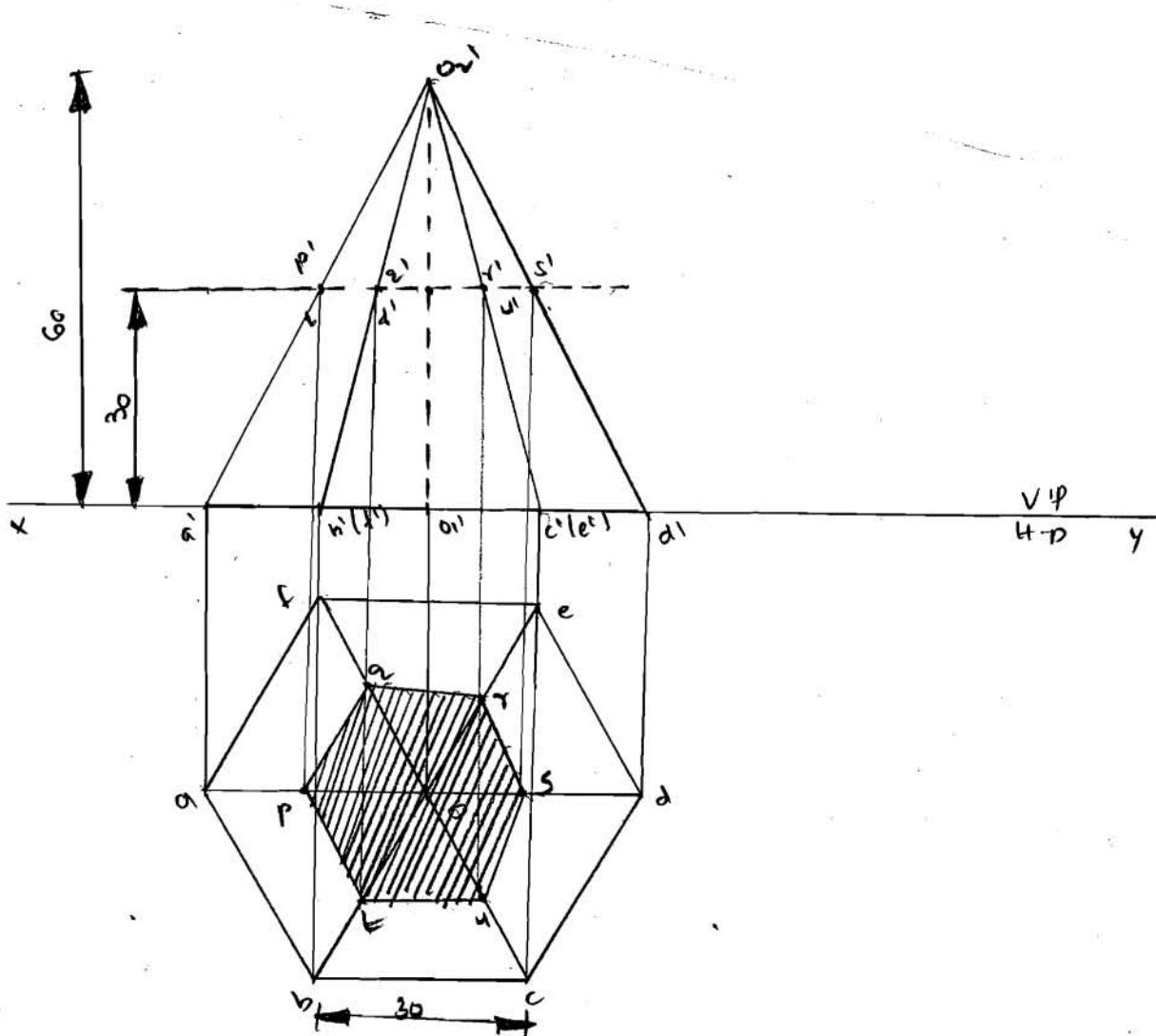
**True shape of a section:** The projection of the section on a plane parallel to the section plane will show the true shape of the section. Thus, when the section plane is parallel to the H.P. or the ground, the true shape of the section will be seen in sectional top view. When it is parallel to the V.P., the true shape will be visible in the sectional front view. But when the section plane is inclined, the section has to be projected on an auxiliary plane parallel to the section plane, to obtain its true shape. When the section plane is perpendicular to both the reference planes, the sectional side view will show the true shape of the section.

## Section of solids.

1. A hexagonal Pyramid of 30mm base side and 60mm long axis's rest with its base on H.P. and one of the edges of the base is parallel to V.P. It is cut by a horizontal section plane at a distance of 30mm above the base. Draw the F.V and sectional T.V
- Hexagonal Pyramid.**

$$B = 30\text{mm}$$

$$A = 60\text{mm}$$

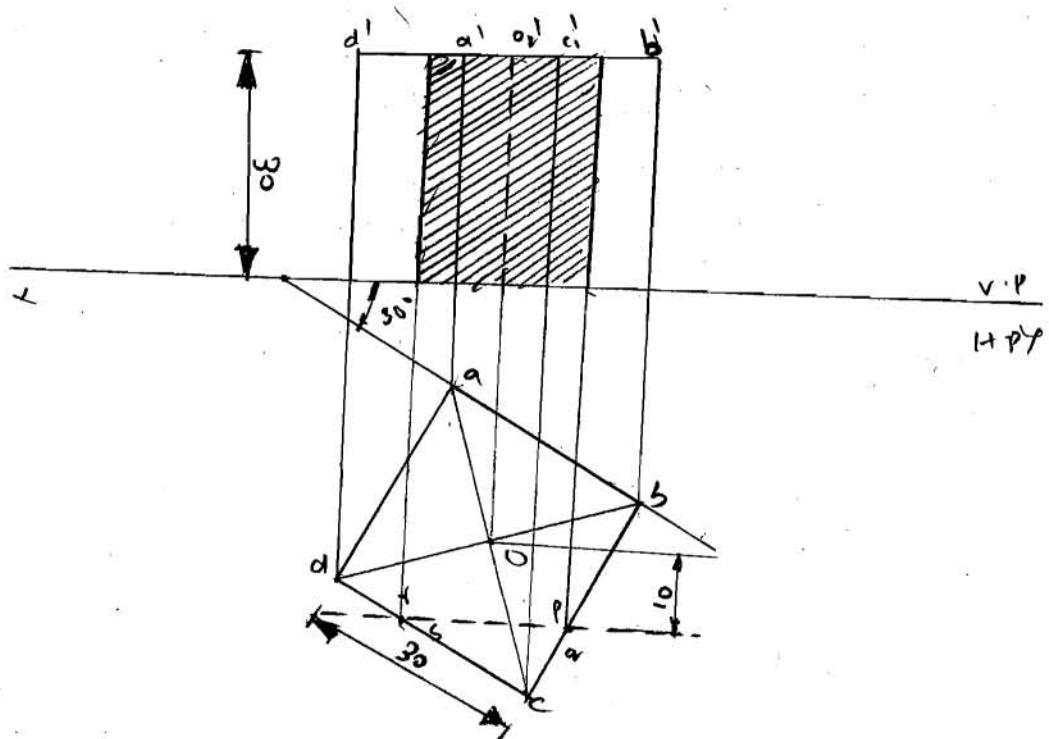


A cube of 30mm long edges is resting on the H.P. on one of its faces with a vertical face inclined at  $30^\circ$  to the V.P. It is cut by a sectional plane parallel to the V.P. and 10mm away from the axis and further away from the V.P. Draw the sectional front view and top-view of the cube.

Cube

$$b = 30\text{mm}$$

$$\phi = 30^\circ$$



3. A triangular prism of 30mm base side and 50mm long axis is lying on the H.P on one of its rectangular faces - with its axis inclined at  $30^\circ$  to V.P. It is cut by a horizontal section plane at a distance of 12mm above the ground. Draw its frontal sectional top view.

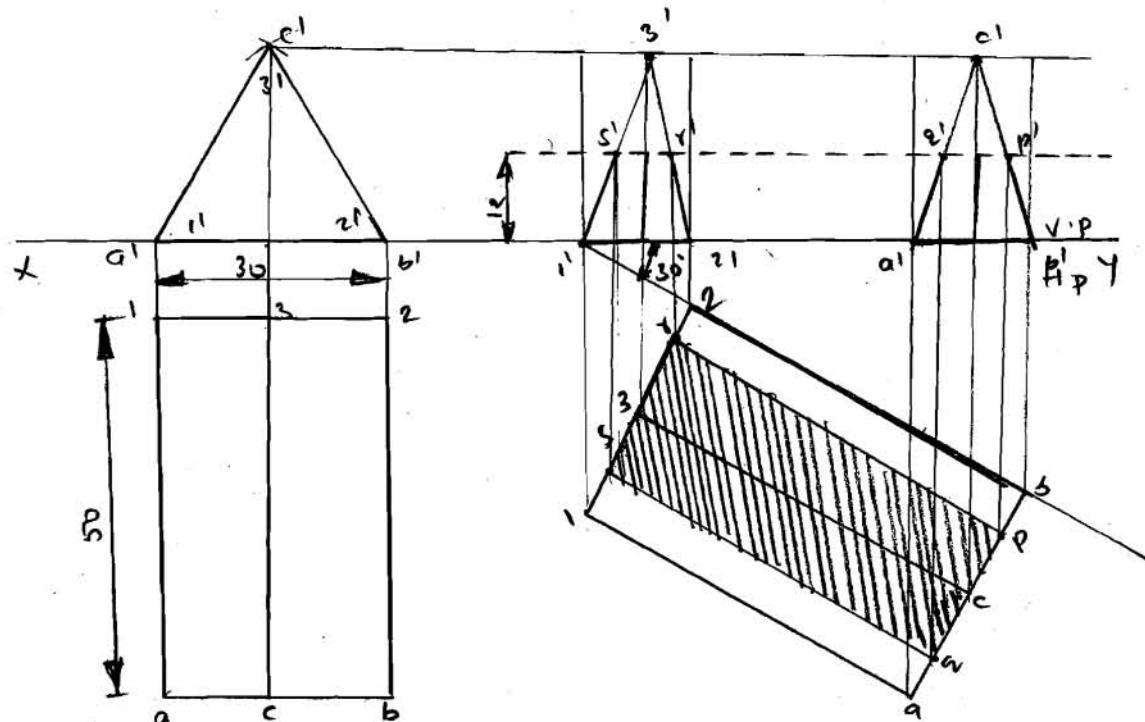
Triangular prism

$$\text{Base} = 30\text{mm}$$

$$\text{Axis} = 50\text{mm}$$

$$\theta = 30^\circ$$

Horizontal sectional plane = 12mm ↑ ground.



Q: A Hexagonal Prism of 20mm base and 60mm height is resting on one of its corners on the ground. with the base making 60° with the ground. The axis is parallel to V.P. A sectional plane parallel to H.P and perp to V.P cuts the object such that it is 15mm from the base as measured along the axis. Draw I.B. sectional view from the above and the view from the front.

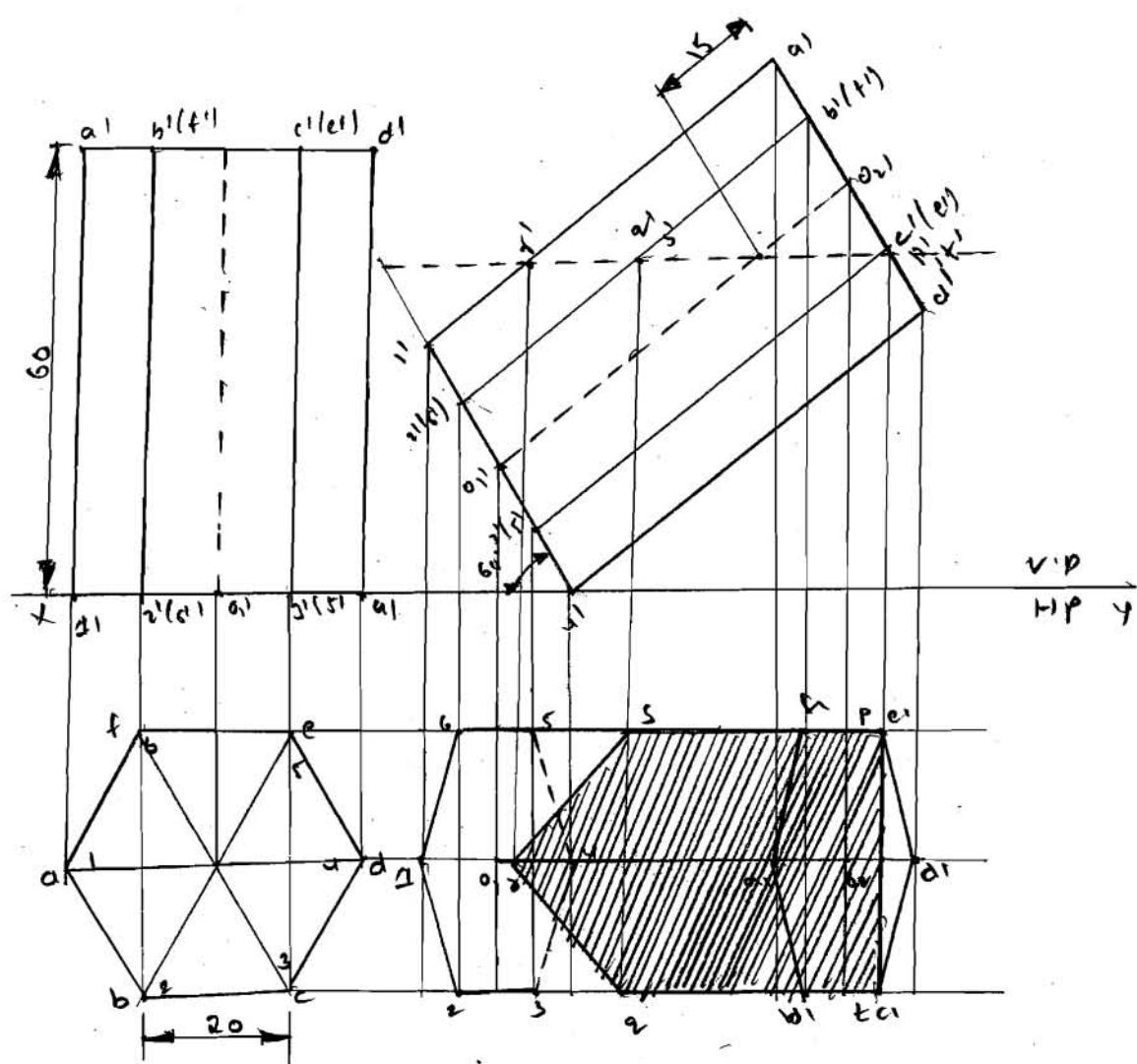
Hexagonal Prism

$$\theta = 60^\circ$$

$$\text{Height} = 60\text{mm}$$

$$\text{Base} = 20\text{mm}$$

$$\text{A.O.S.P} = 15\text{mm}$$



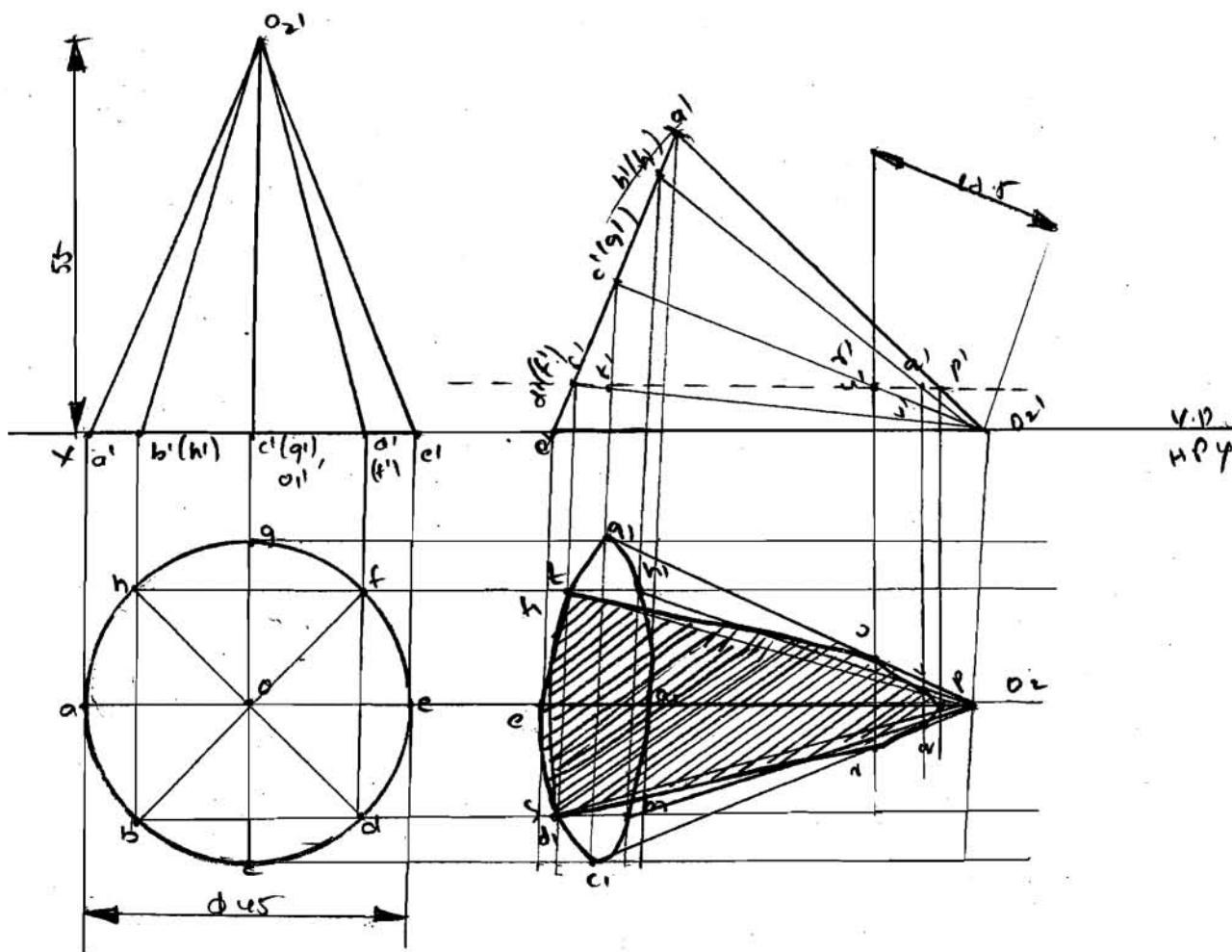
5. A right circular cone of the 45mm base diameter and 55mm axis long is lying on the one of its generator on the H.P. - It is cut by a horizontal sectional plane passing through the midpoint of axis. Draw the projections of the cone and its true section.

Cone

$$d = 45\text{mm}$$

$$elevation = 55\text{mm}$$

H.U.S.P. passing through mid-point



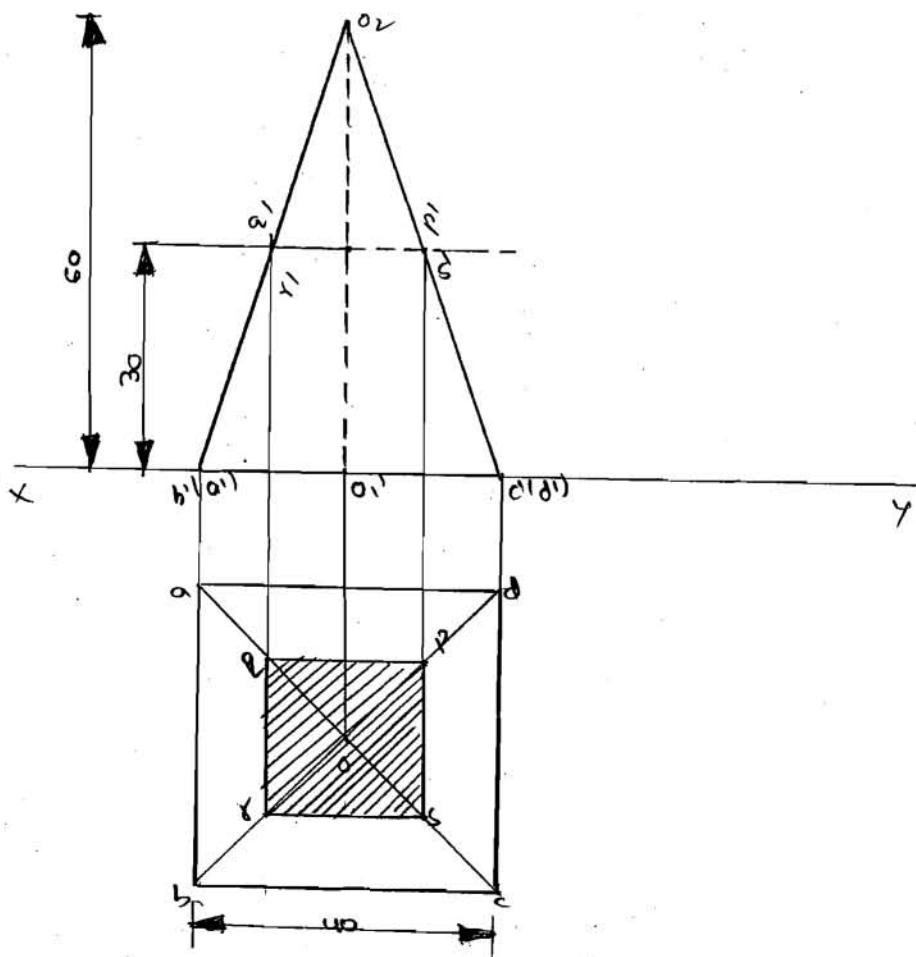
Q; A square pyramid base side 40mm and axis 60mm is resting on the base on the H.P with a side of base parallel to V.P. Draw its sectional view and the sphere of the section, if it is cut by a sectional plane perpendicular to V.P, bisecting the axis

- a) perpendicular to H.P
- b) inclined at  $45^\circ$  to H.P
- c) inclined at  $60^\circ$  to H.P
- (d) Parallel to H.P

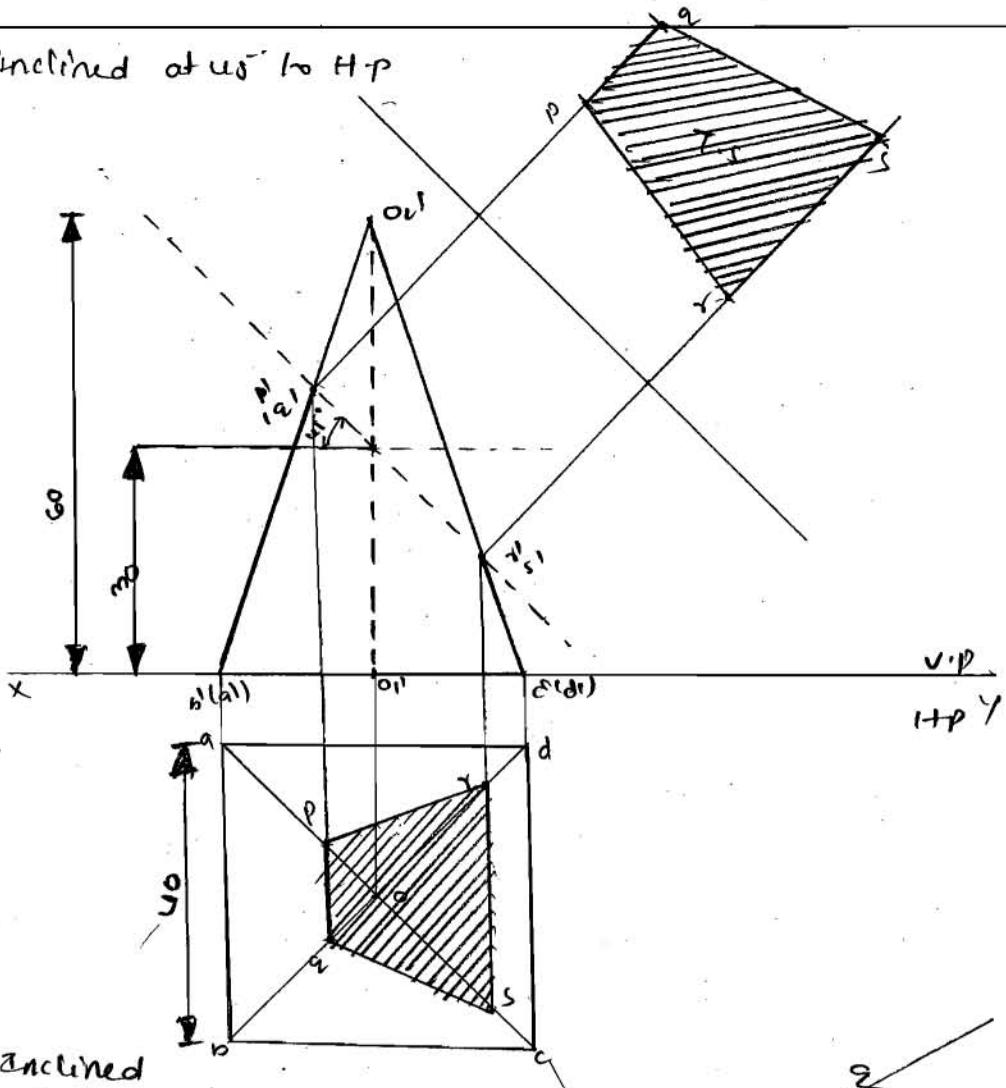
Square Pyramid

Base = 40mm

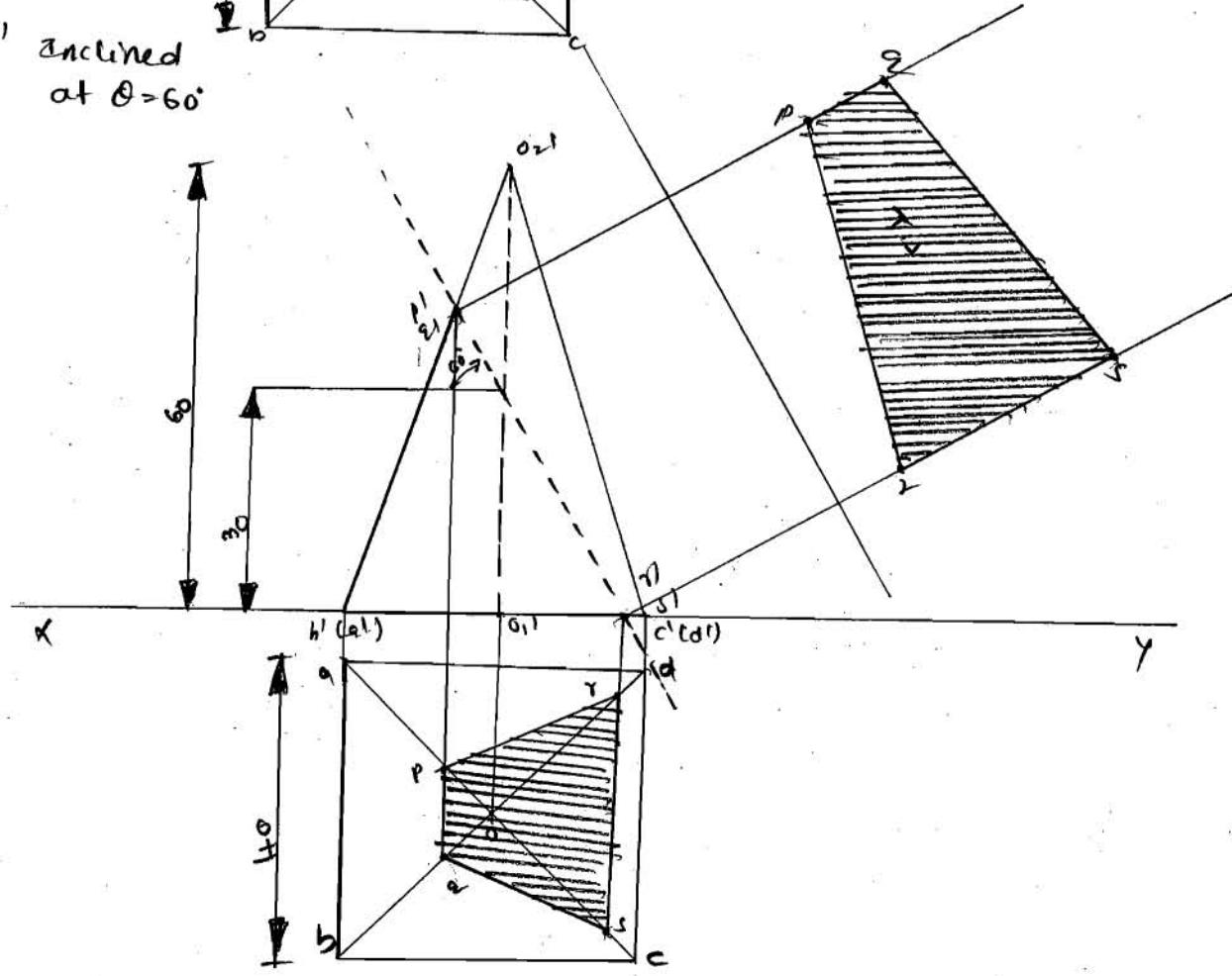
Axis = 60mm



(b) Inclined at  $45^\circ$  to H.P.



(c) Inclined  
at  $\theta = 60^\circ$



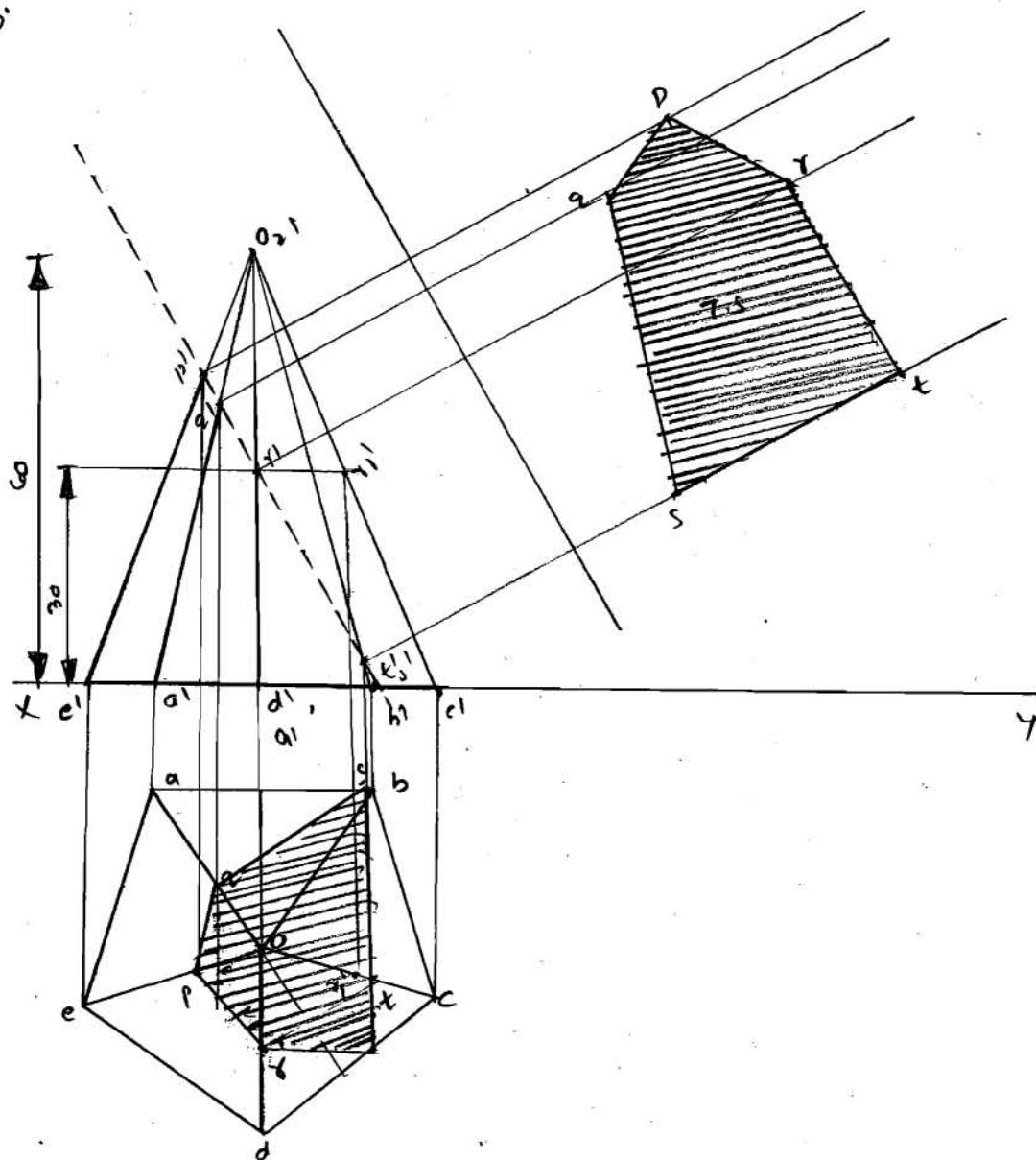
2. A Pentagonal Pyramid base side 30mm and axis 60mm is resting on its base on the H.P. with an edge of its base parallel to V.P. It is cut by a sectional plane perpendicular to V.P., inclined at 60° to H.P. and bisecting the axis. Draw its front view and sectional T.V. and True shape of the section.

### Pentagonal Pyramid

Base = 30mm

Axis = 60mm

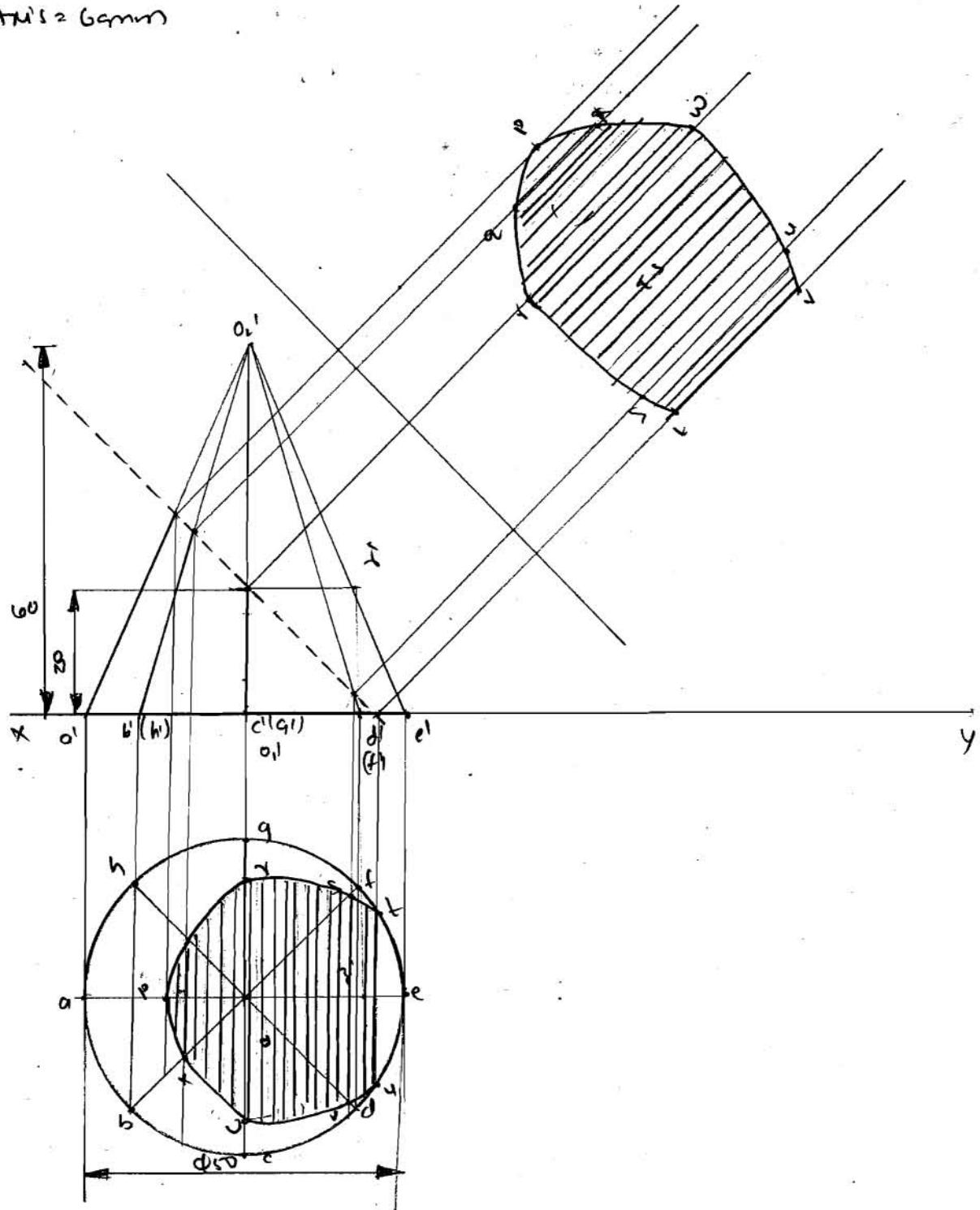
$\theta = 60^\circ$



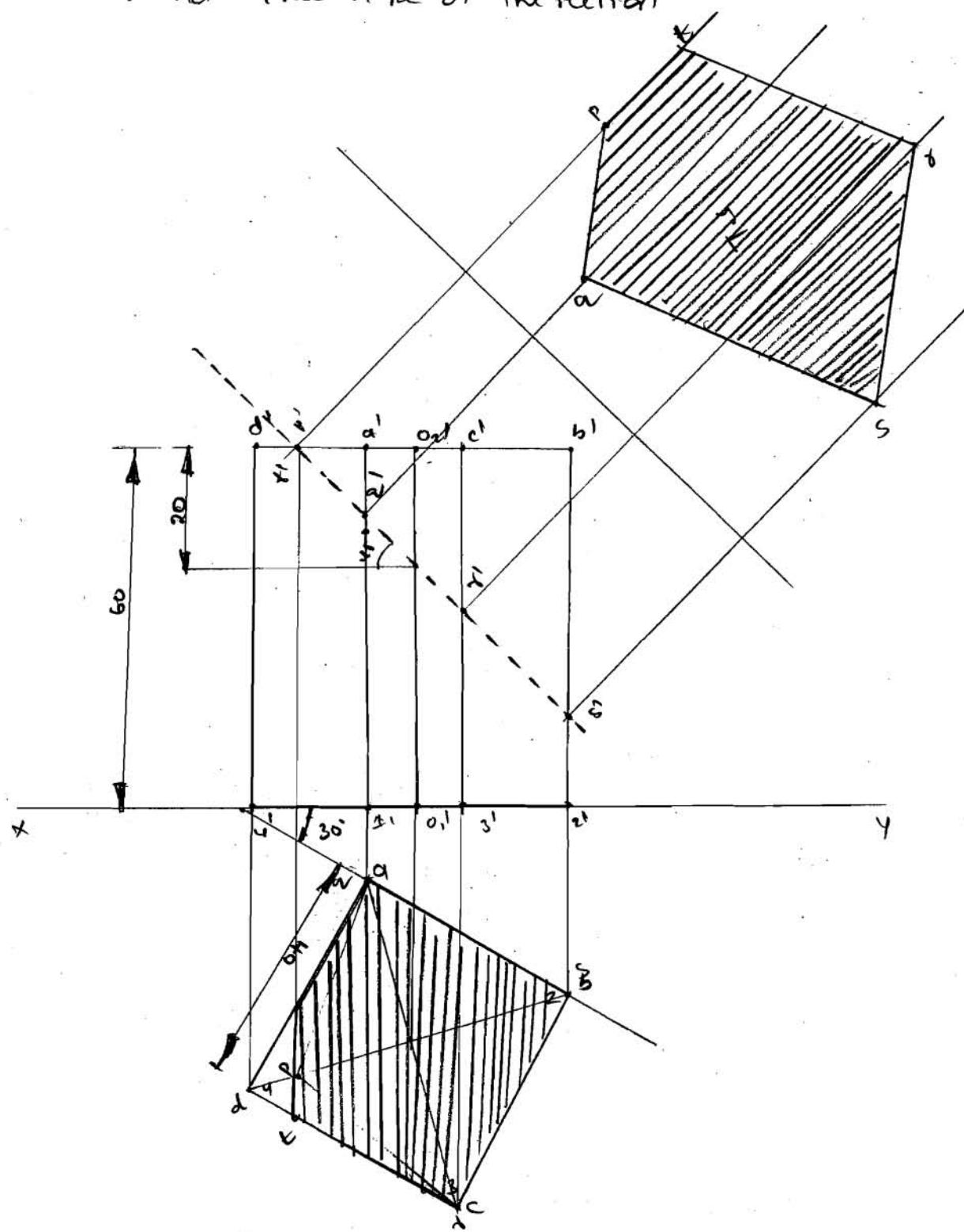
A cone of base diameter 50mm and axis 60mm is resting on its base on the H.P. It is cut by an A.I.P. inclined at  $45^\circ$  to H.P. and passing through a point on the axis, 20mm above the base. Draw its sectional T.V. and obtain the true shape of the section.

diameter  $d = 50\text{mm}$

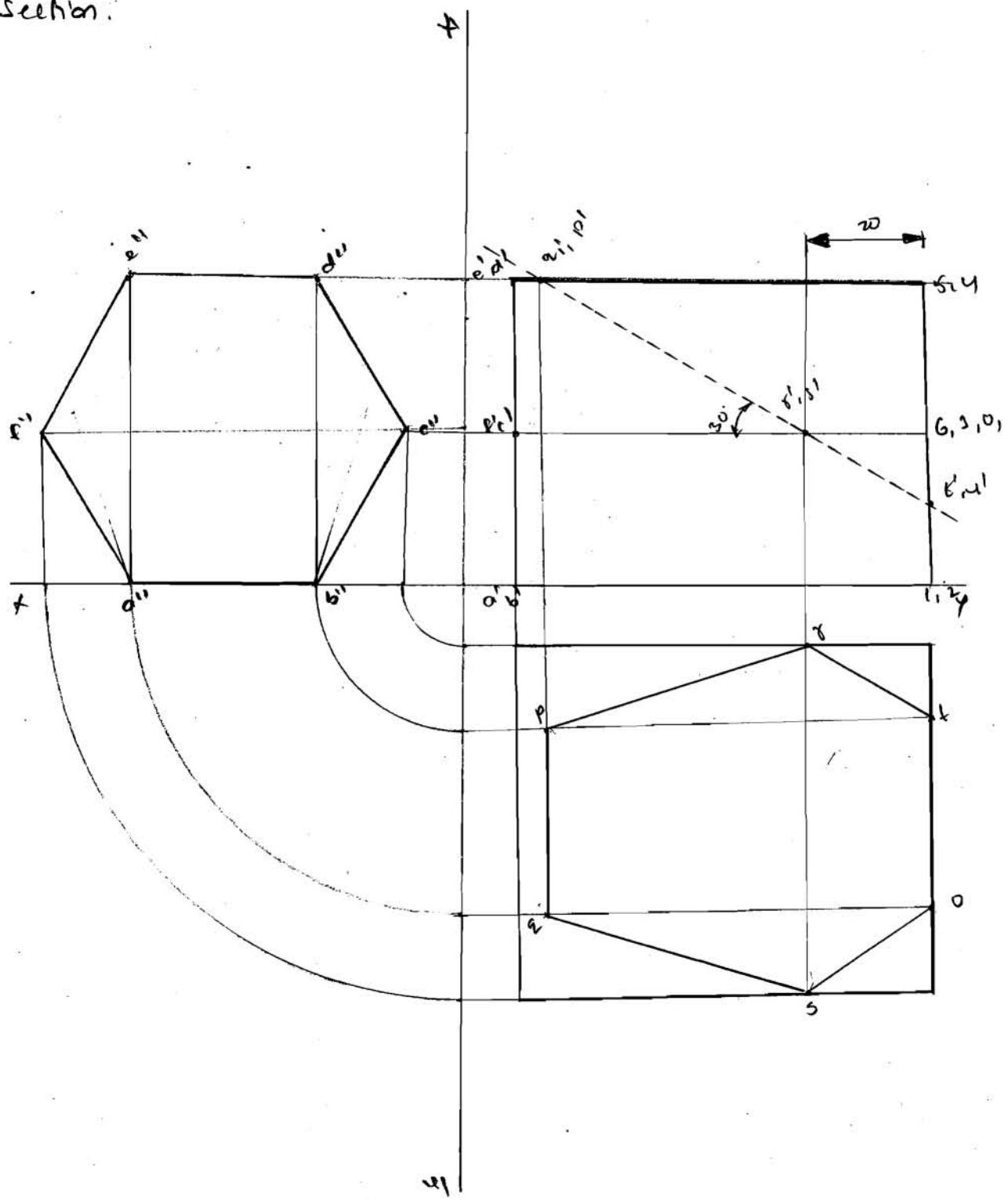
Axis = 60mm



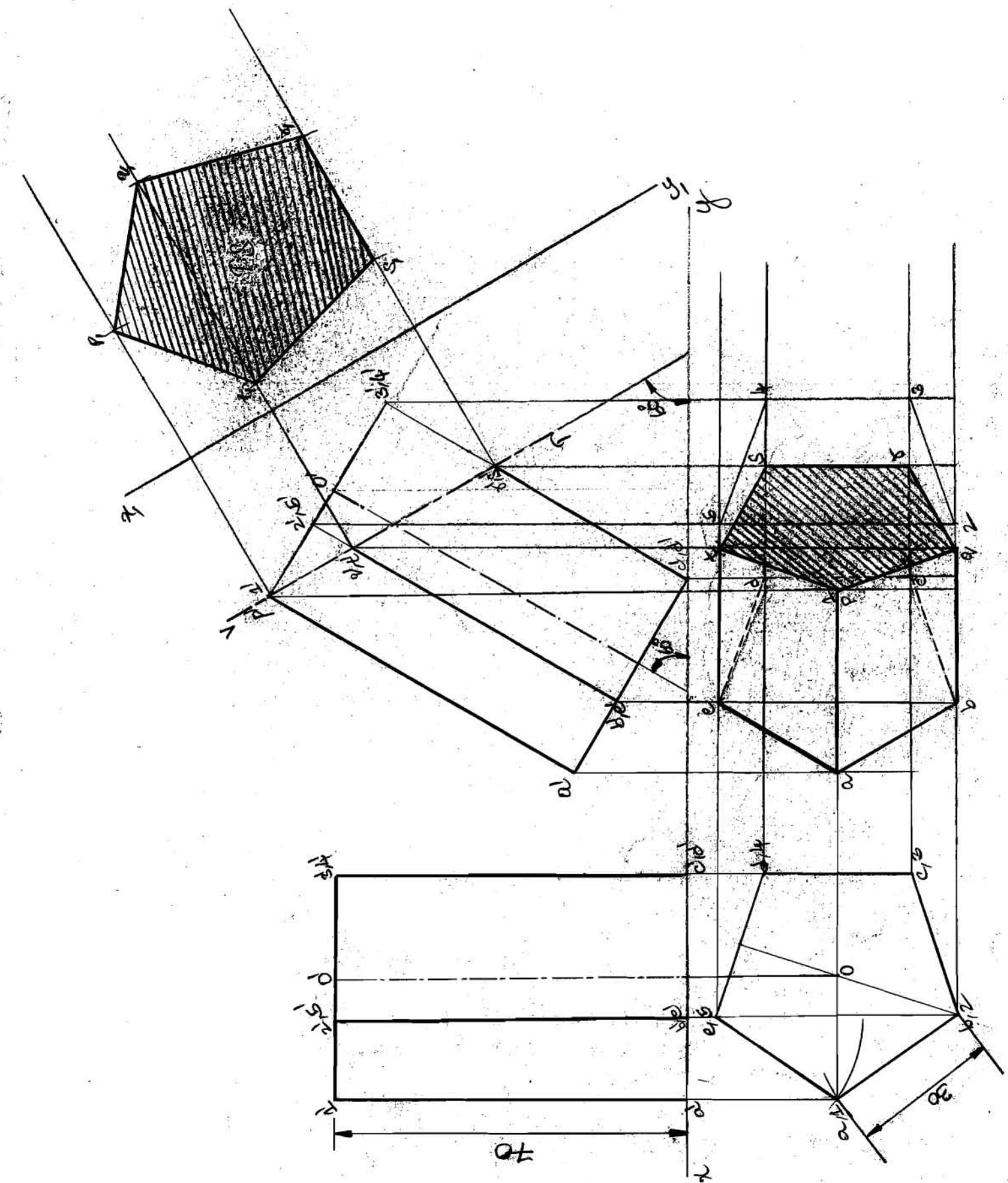
A square Prism of base side 10mm and axis 60mm rest on its base on the H.P. such that one of the V.T. inclined at  $30^\circ$  to V.P. A sectional Plane lies to V.P., inclined at  $45^\circ$  to H.P. passing through the axis at a point 20mm from its top end cut the Prism draw its F.V. sectional T.V. and True shape of the section.



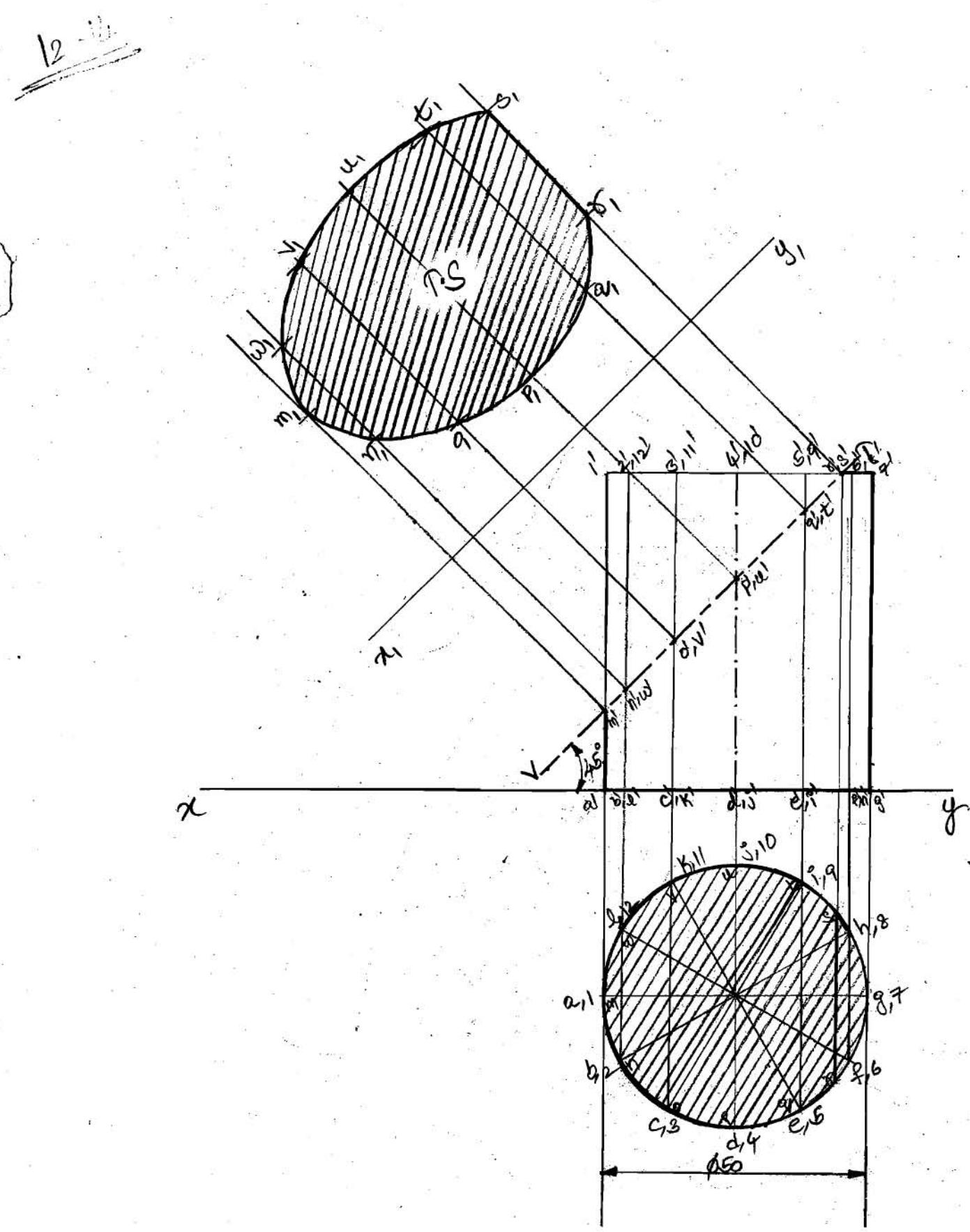
A Hexagonal Prism of base side 30mm and axis 70mm is resting on a face on the H.P. with the axis vertical to the V.P. It is cut by a Plane whose V.T. is inclined at  $30^\circ$  to the reference line and passes through a point on the axis 20mm from one of its ends. Draw its sectional Top view and obtain the true shape of the section.



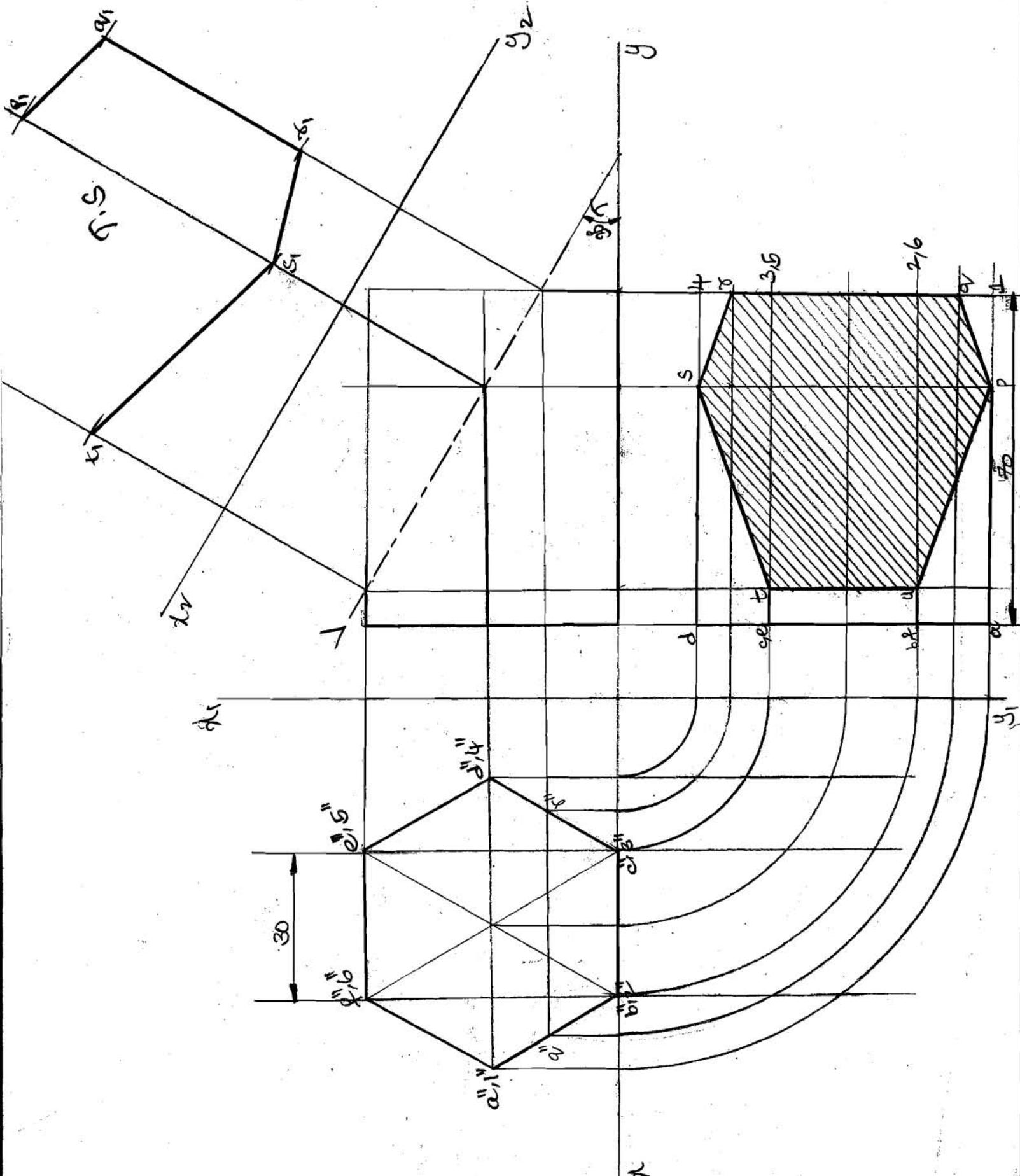
\* Pentagonal Prism inclined to the plane of projection



# \* Cylinder Sectional View



\* Hexagonal Prism sectional view



# **UNIT-IV**

# **Content**

**Development of Surfaces of Right Regular Solids**

– Prism, Cylinder, Pyramid and Cone

**Intersection of Solids:** Intersection of – Prism vs  
Prism- Cylinder Vs Cylinder

## **Unit-IV**

### **Development of Surfaces of Right Regular Solids:**

Imagine that a solid is enclosed in a wrapper of thin material, such as paper. If this covering is opened out and laid on a flat plane, the flattened-out paper is the development of the solid. Thus, when surfaces of a solid are laid out on a plane, the figure obtained is called its development.

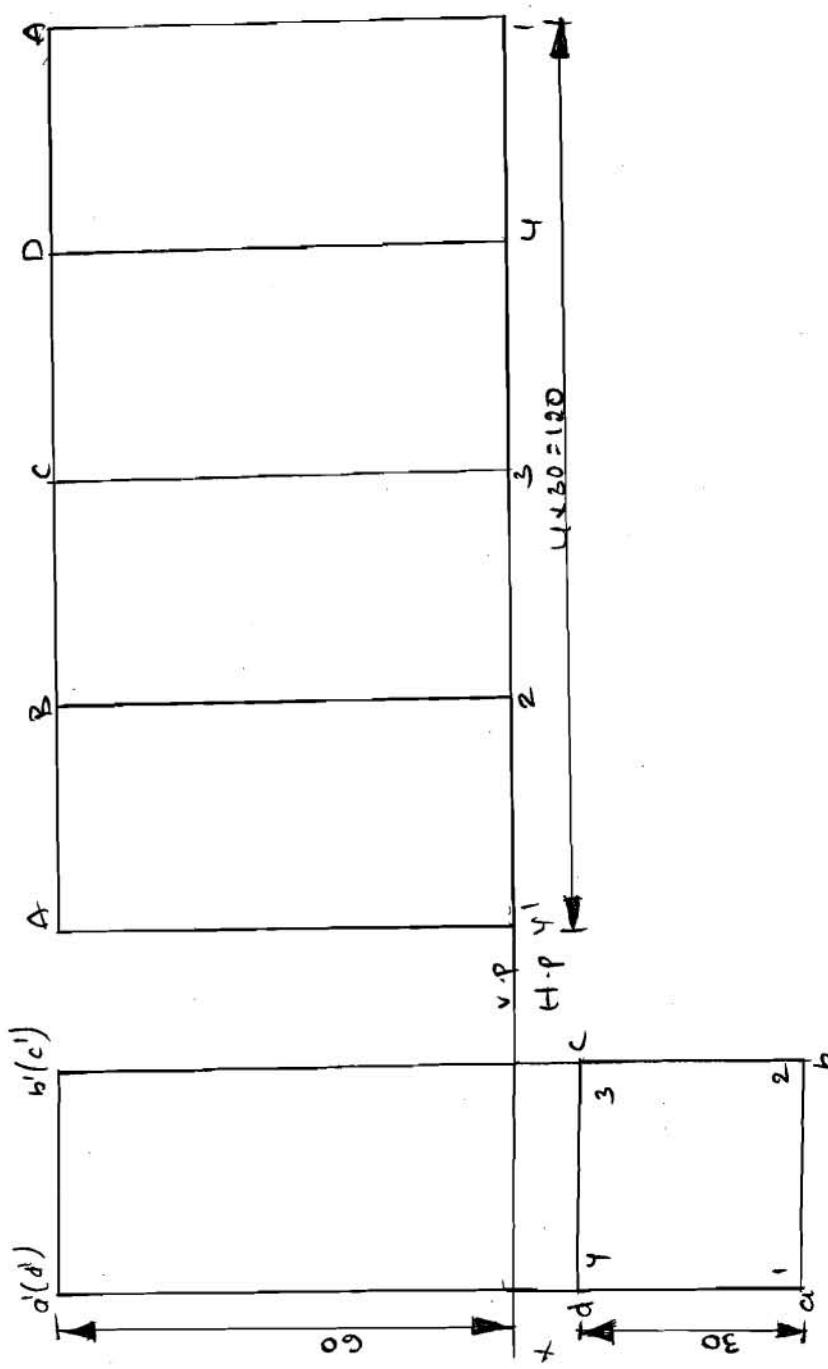
### **Intersection of Solids:**

The intersecting surfaces may be two plane surfaces or two curved surfaces of solids. The lateral surface of every solid taken as a whole is a curved surface. This surface may be made of only curved surface as in case of cylinders, cones etc. or of plane surfaces as in case of prisms, pyramids etc. In the former case, the problem is said to be on the intersection of surfaces and in the latter case, it is commonly known as the problem on interpenetration of solids. It may, however, be noted that when two solids meet or join or interpenetrate, it is the curved surfaces of the two that intersect each other. The latter problem also is, therefore, on the intersection of surfaces.

1. A square Prism of base side 30mm and axis 60mm is resting on its base on the H.P. with a rectangular face parallel to V.P. develop the surface of the Prism.

Base = 30mm, Square prism

Axis = 60mm.

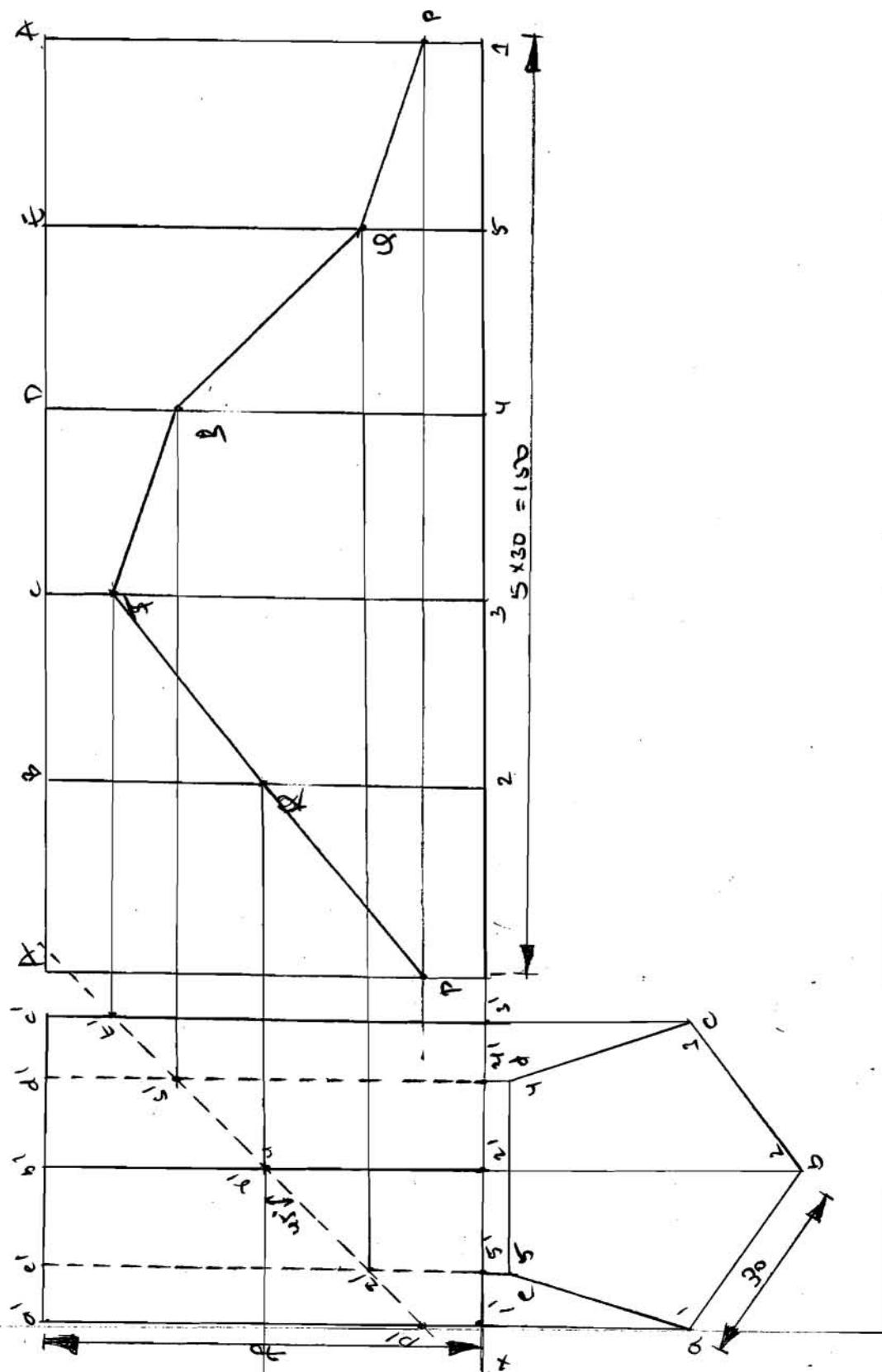


a: A Pentagonal Prism base side 30mm and axis 70mm is resting on its base on the H.P. with rectangular face (ref) to the V.P. if it is cut by a A.I.P. whose V.T is inclined at  $45^\circ$  to the reference line and passes through the midpoint of the axis. Draw the development of lateral surface of truncated prism.

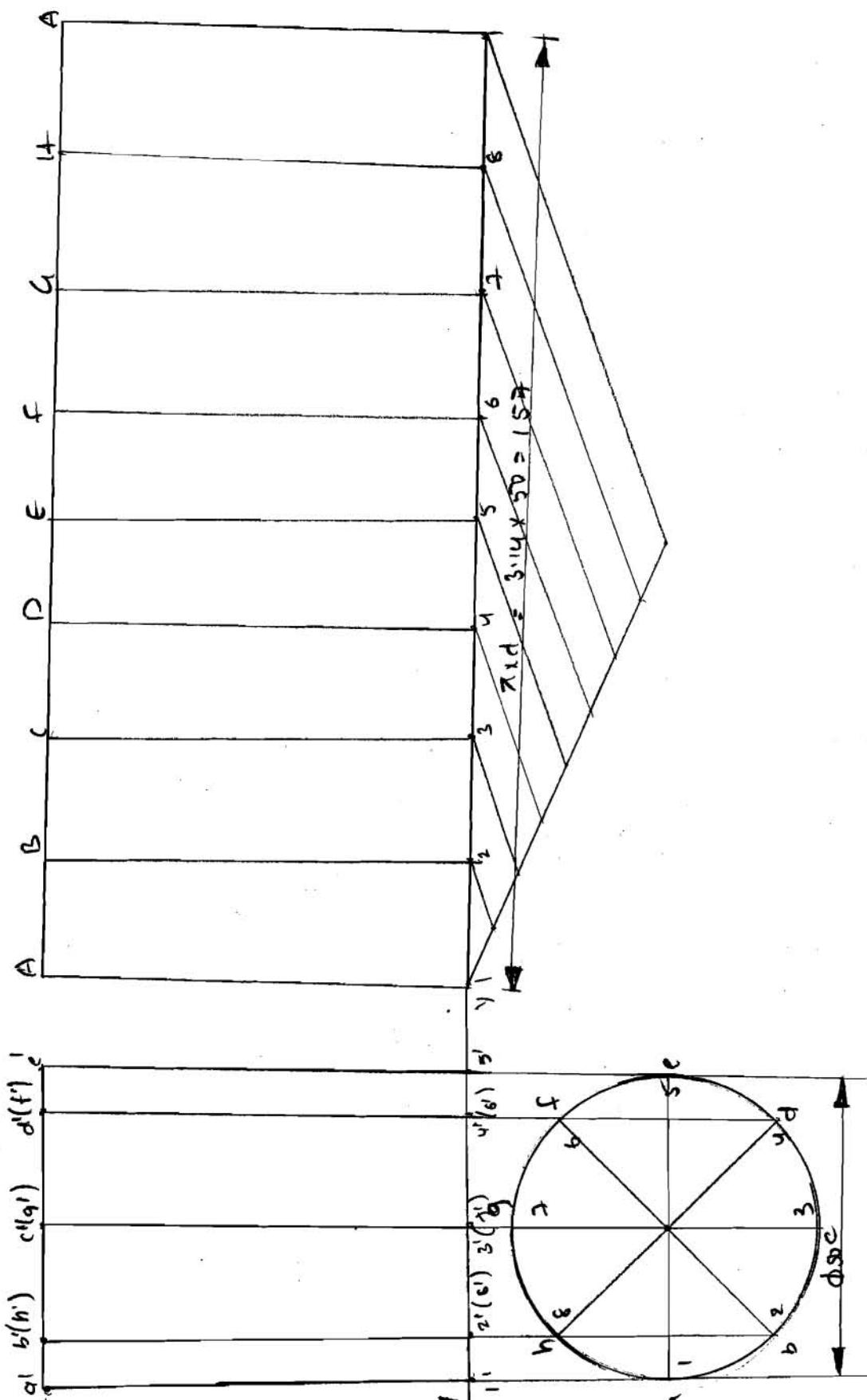
Pentagonal Prism

Base = 30mm

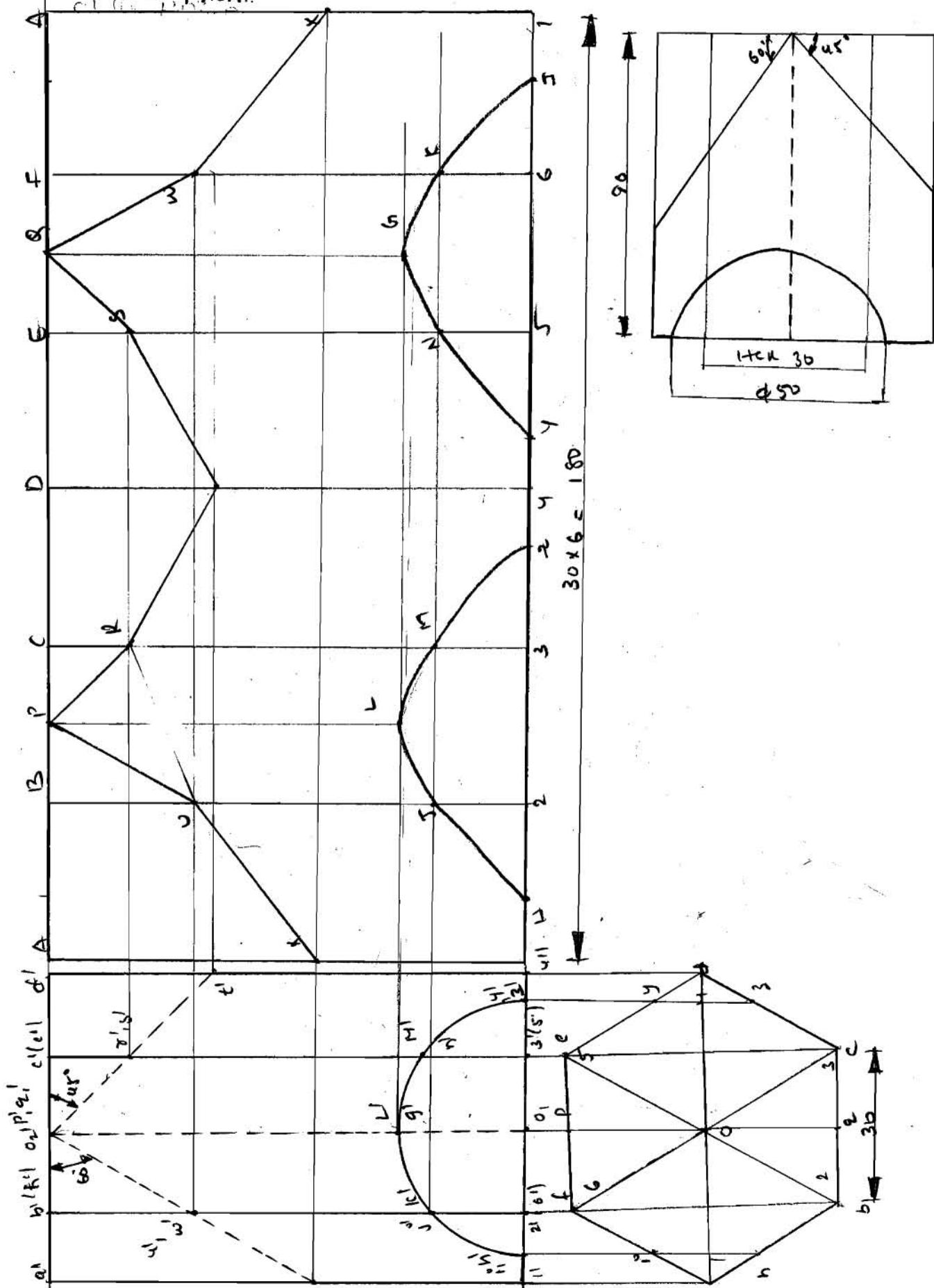
Axis = 70mm

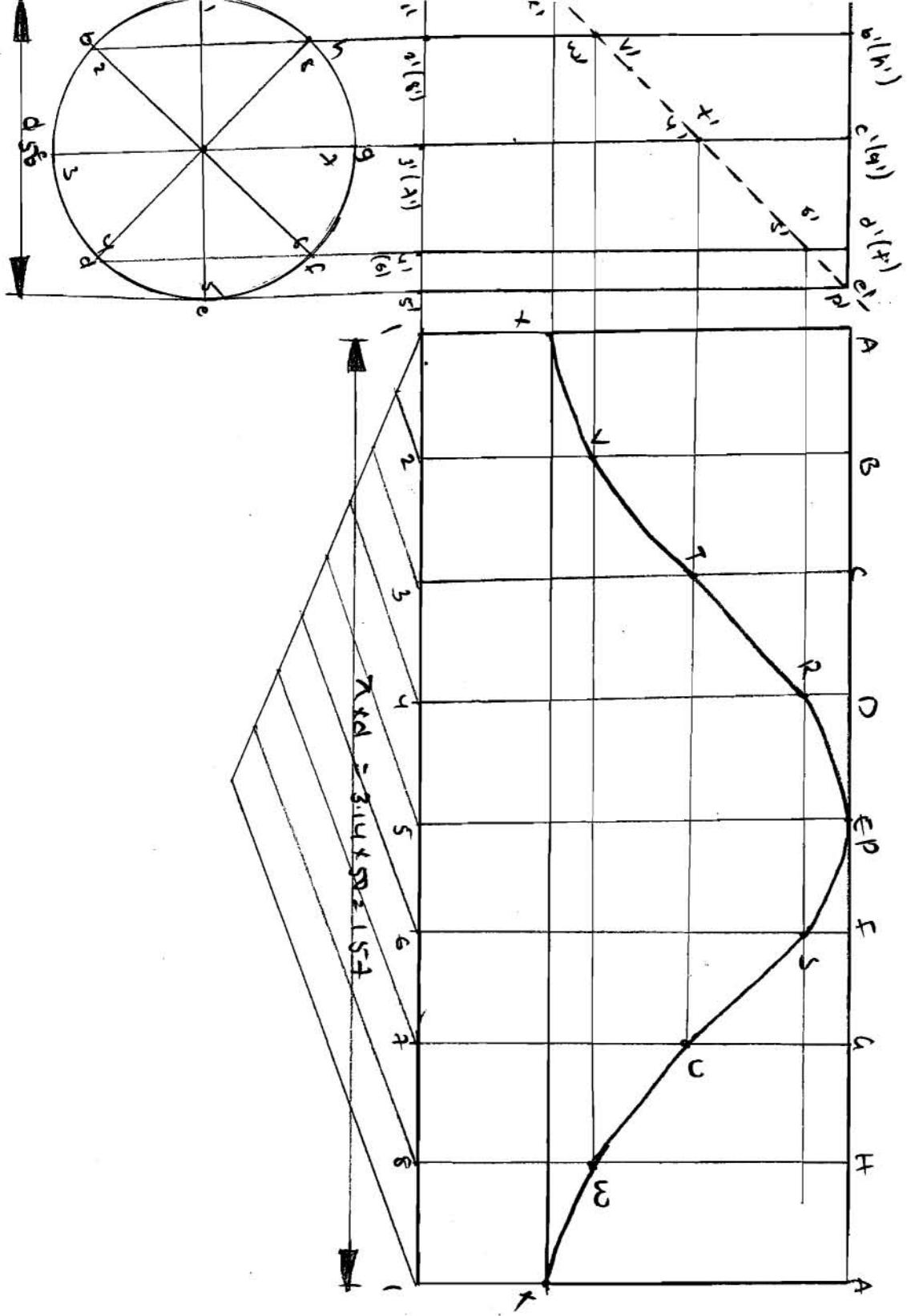


3. A cylinder of base diameter 50mm and axis 70mm is resting on the ground with its axis vertical. Draw the development of lateral surface of cylinder.



Q:- The figure shows the F.V. of a truncated hexagonal prism of base side 30mm and axis 90mm. The Prism is resting on the H.P with the basic side parallel to V.P. Develop the Lateral Surface of the Prism.

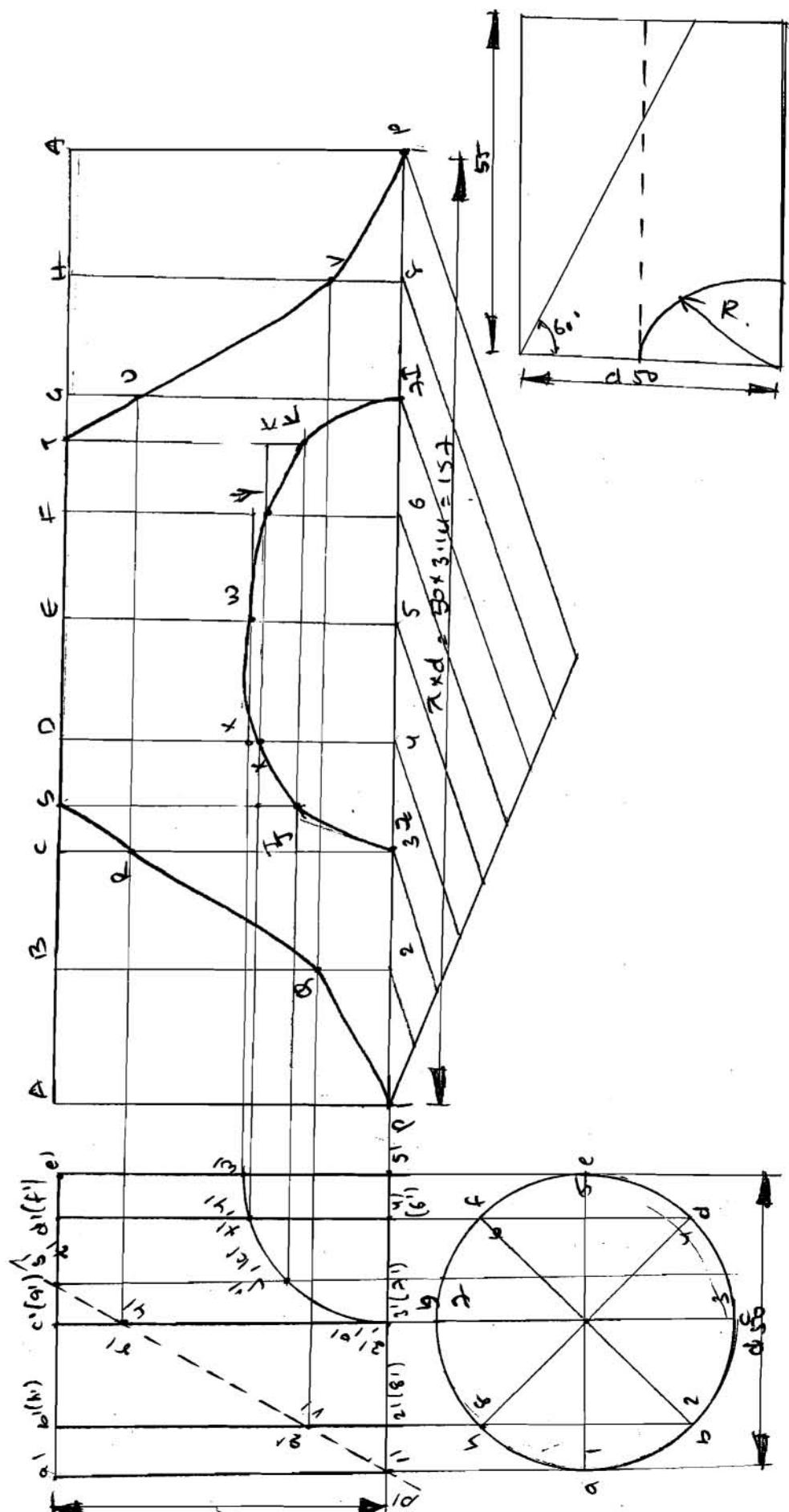




A cylinder of base diameter 5 mm and axis length 30 mm is resting on the ground with its axis vertical. It is cut by a section plane V.P. inclined at 45° to the H.P., passing through the top of a generatrix and cutting all the other generatrices. Draw the development of the lateral surface.

Q:

Q:- Figure shows the F.V. of a truncated cylinder of diameter 50 mm resting on its base on the H.P. Draw the development of its lateral surfaces.

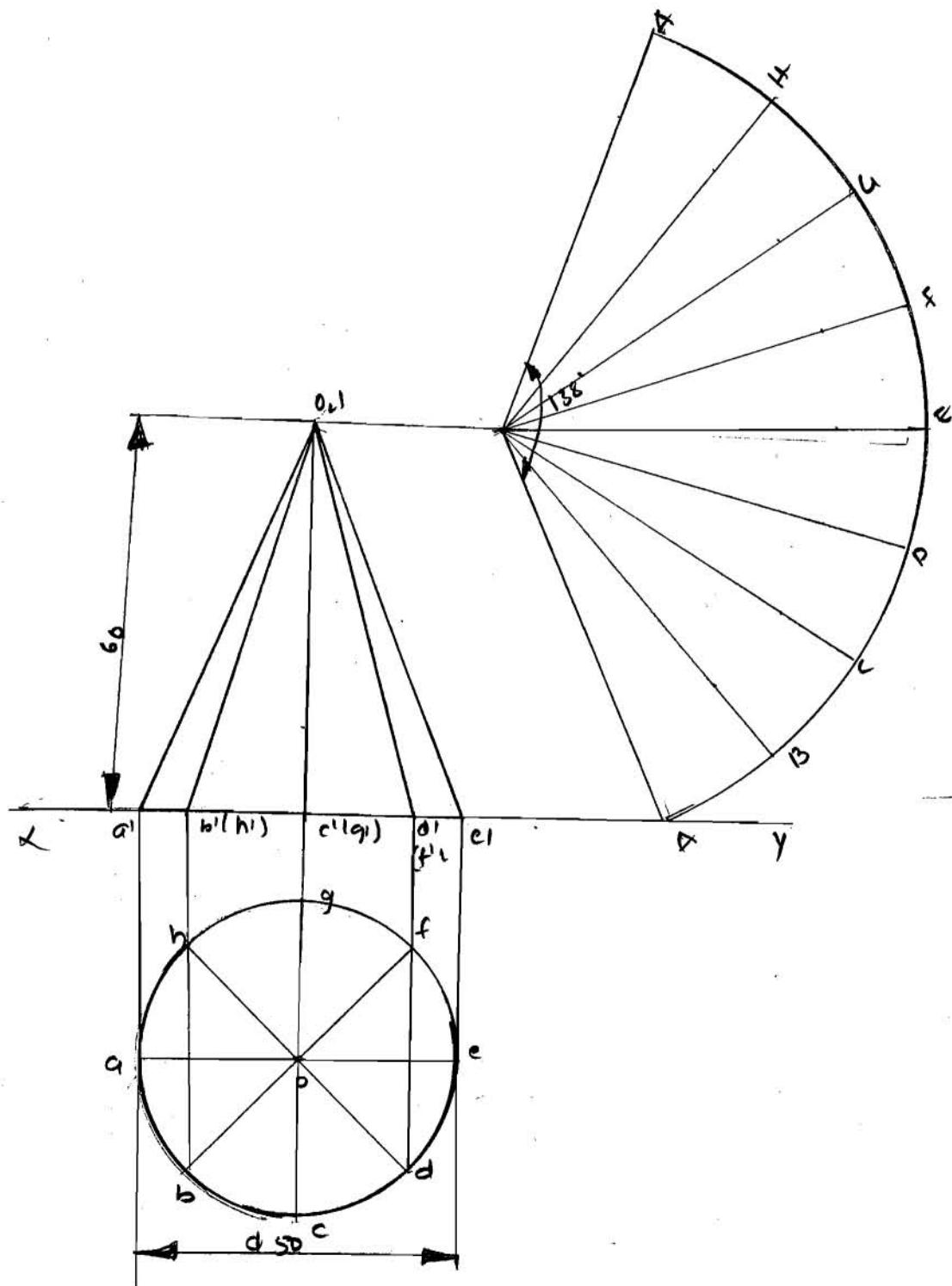


Q. A cone of base diameter 50mm and axis 60mm is resting on its base on the H.P. Draw the development of its lateral surface.

Base diameter  $\phi = 50\text{mm}$

Axis = 60mm

$\theta = 138^\circ$



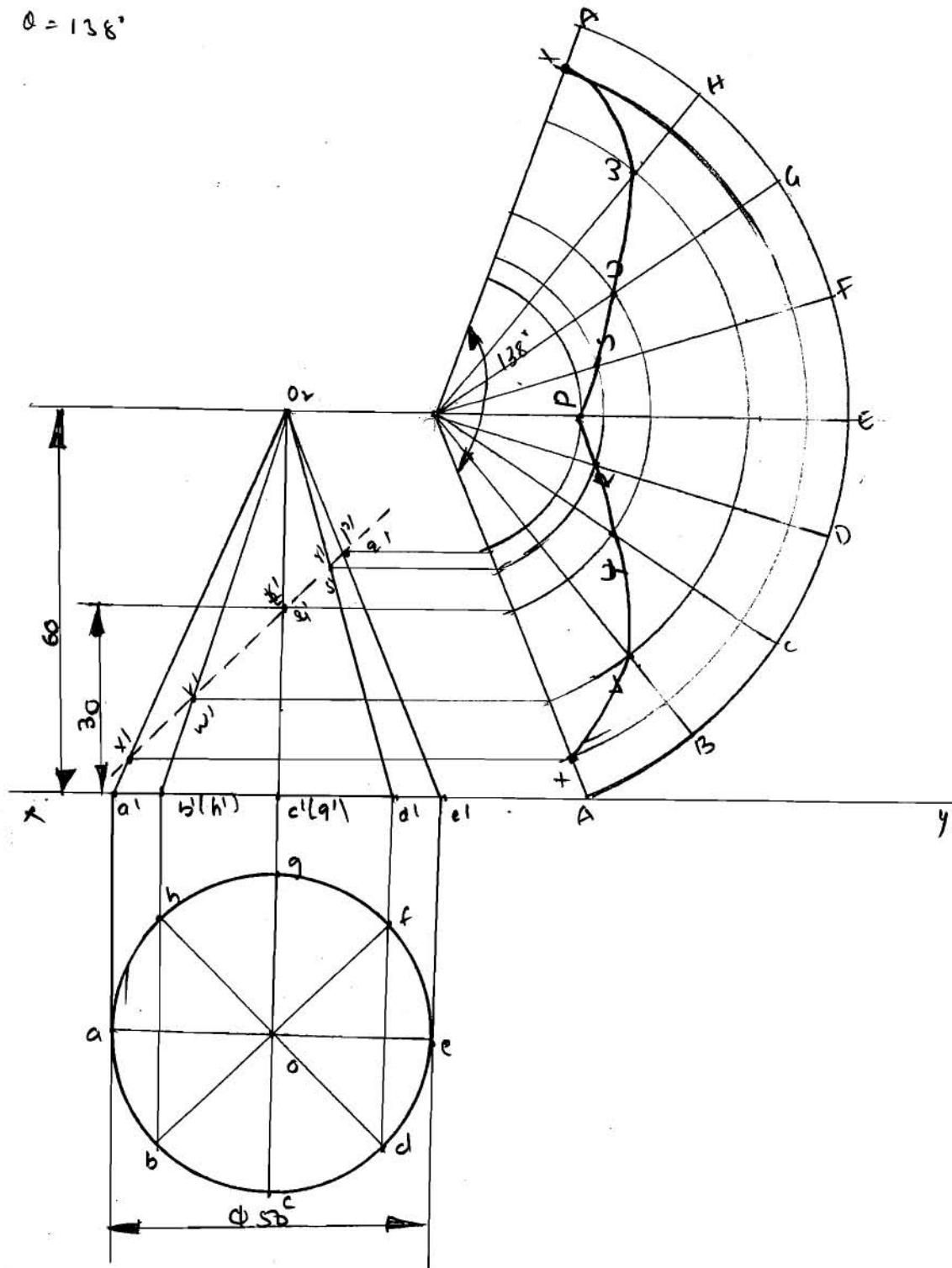
Q A cone of base diameter 50mm and axis's 60mm is resting on its base on the H.P., a sectional Plane lies to V.P. and inclined at  $45^\circ$  to H.P. bisecting the axis of the cone draw the development.

Cone

base diameter  $\phi = 50\text{mm}$

Axis's = 60mm

$\theta = 138^\circ$

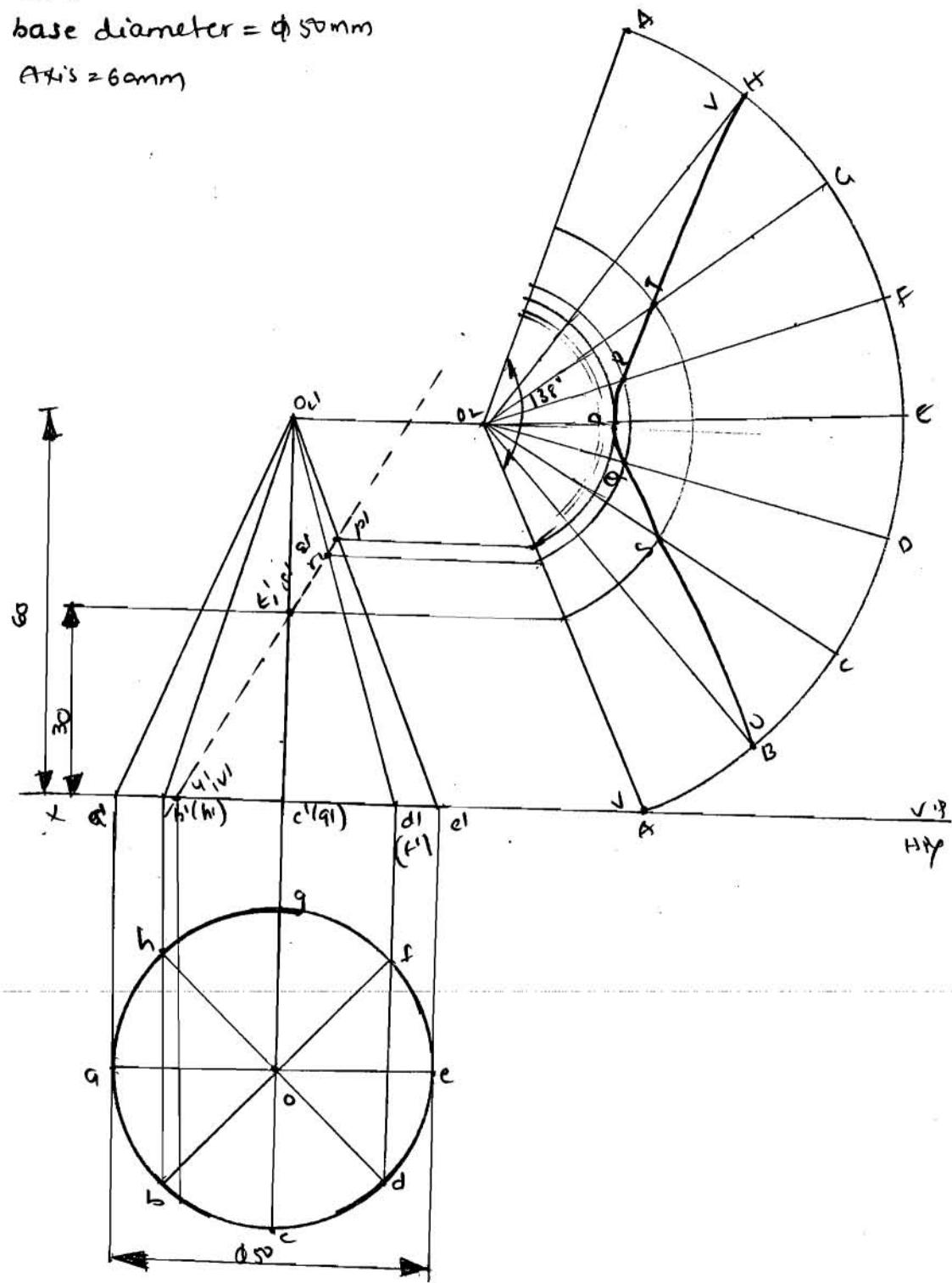


Q: A cone of base diameter 50mm and axis 60mm is resting on its base on the H.P. - a sectional Plane ter to v.p and inclined at 60° to H.P. bisectiong the axis of the cone draw the development of lateral surface of cone

Cone

base diameter = Ø 50 mm

Axis = 60 mm



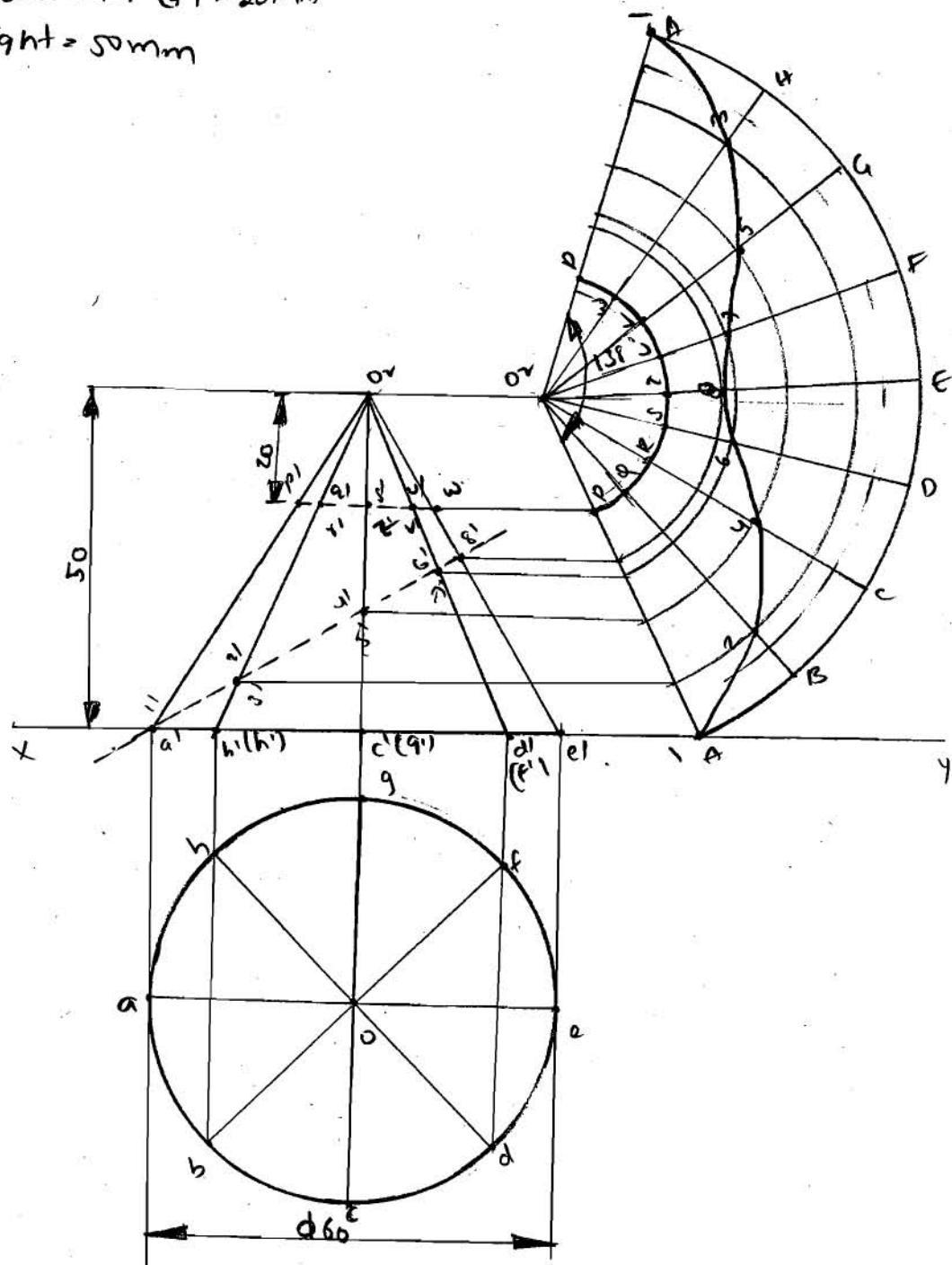
Q: The frustum of the cone of base diameter 60mm top diameter 20mm and height of the 50mm is resting on the base H.P. It is cut by A.I.P and inclined at  $30^\circ$  to the H.P. The H.T. of which is tangential to the base circle. Draw the development of the lateral surface of the retained frustum.

Cone

base diameter ( $d$ ) = 60mm

top diameter ( $d_1$ ) = 20mm

height = 50mm



(Q:-) Draw the development of lateral surface of square pyramid of base side 40mm and axis 60mm is resting on its base on the H.P. Such that

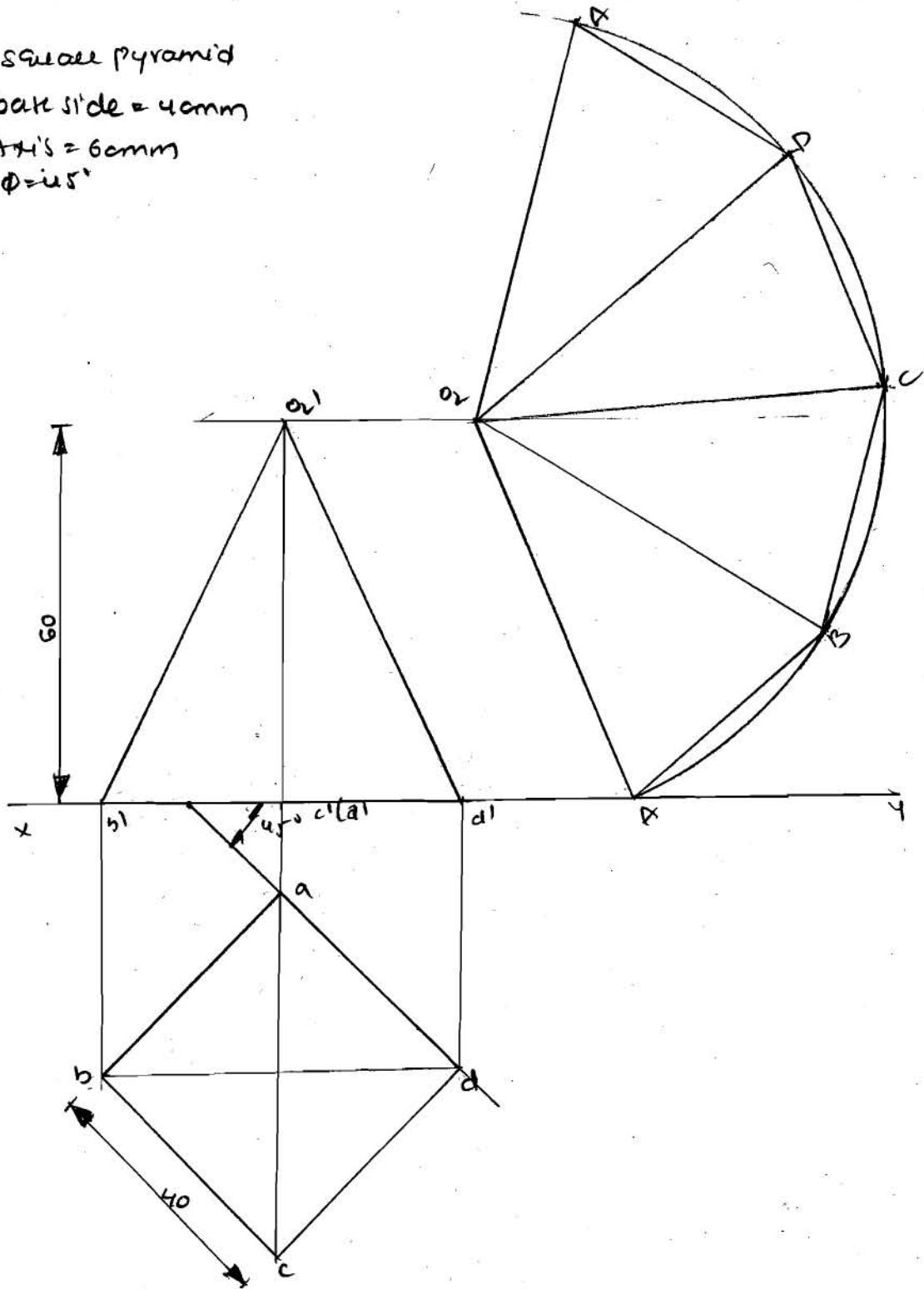
- all sides of the base are equally inclined to the V.P
- A side of the base is parallel to V.P

(a) Square Pyramid

base side = 40mm

Axis = 60mm

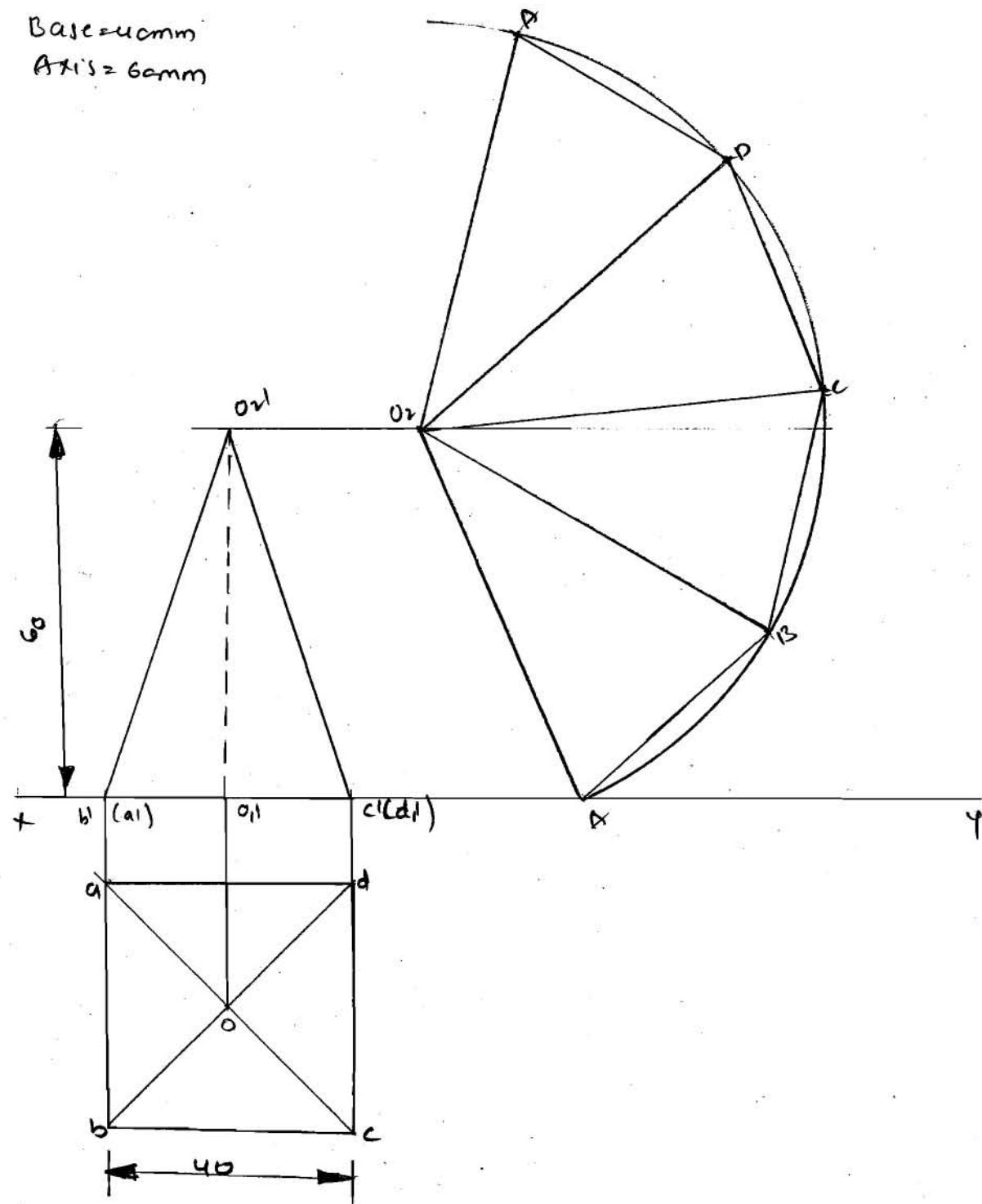
$\phi = 45^\circ$



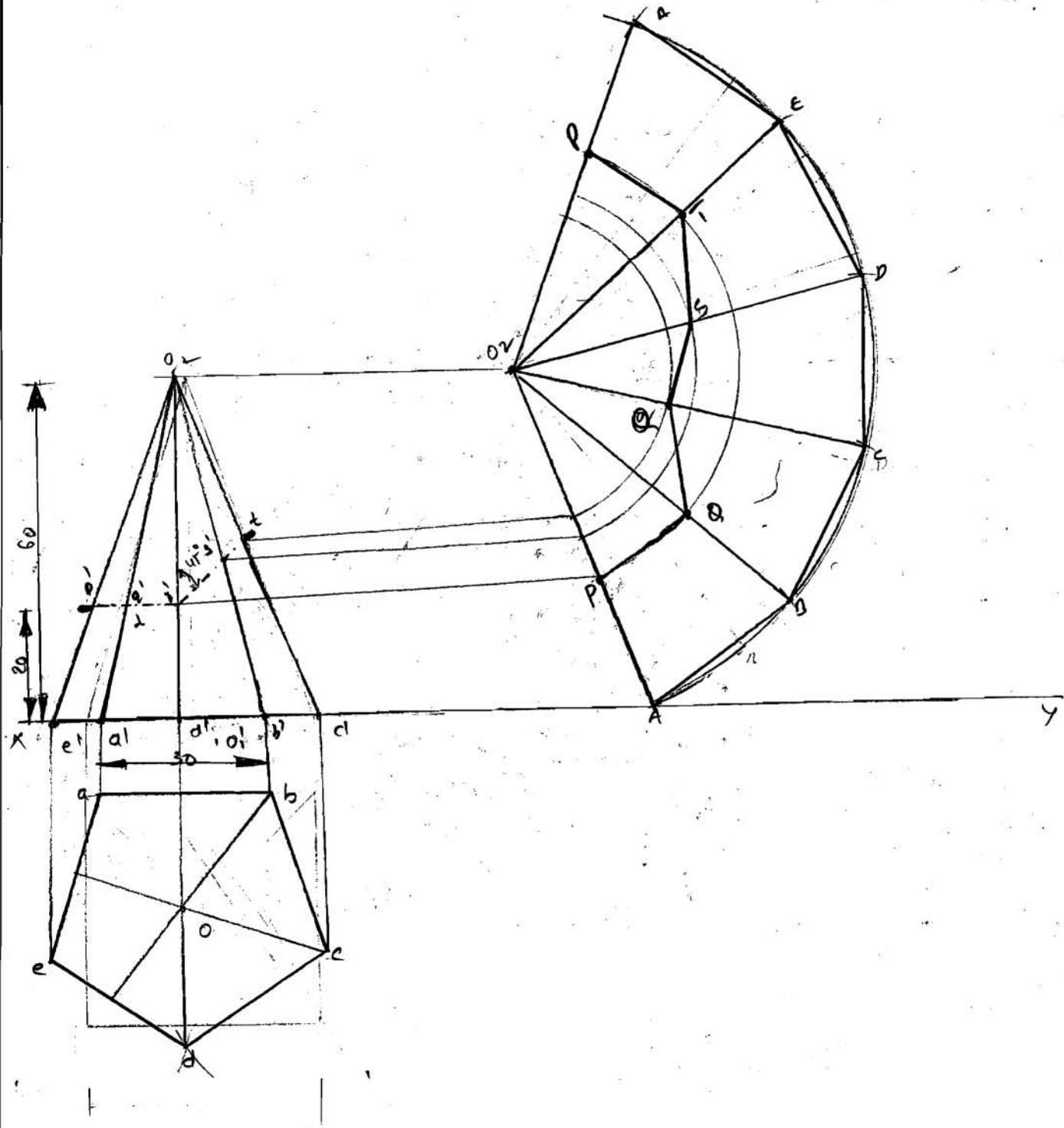
(b) Base is parallel to VP

Base=40mm

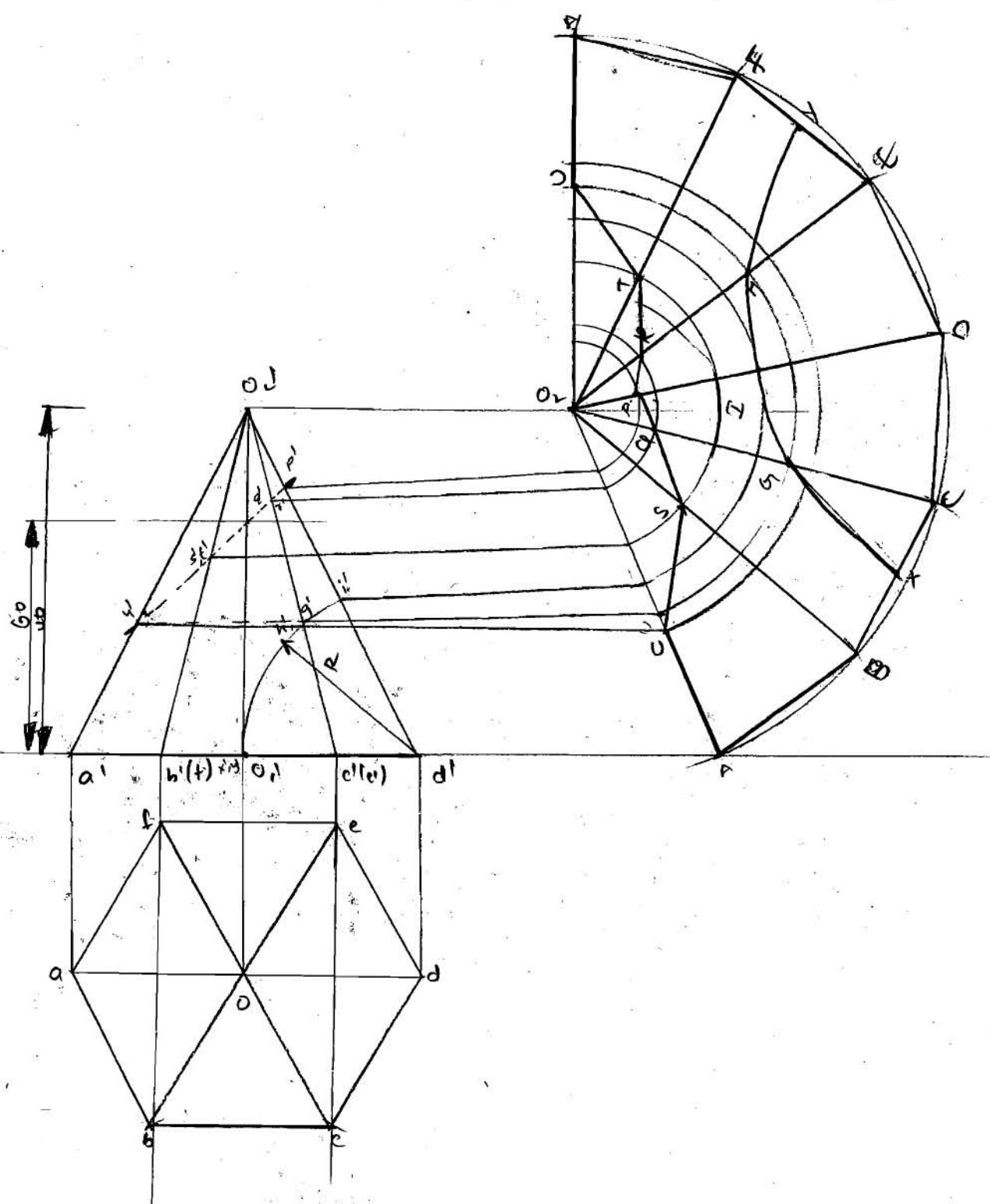
Axis=60mm



Q: A Pentagonal Pyramid Base side 30mm and axis 60mm - rest on its base on the H.P. with the side of the base is lkel to V.P. It is cut by two sectional planes meet at a height of 20mm from the base one of the sectional plane is horizontal while the other is an auxiliary inclined plane which U.T at 45° to H.P. Draw the development of Lateral surface of solid when apex is removed.



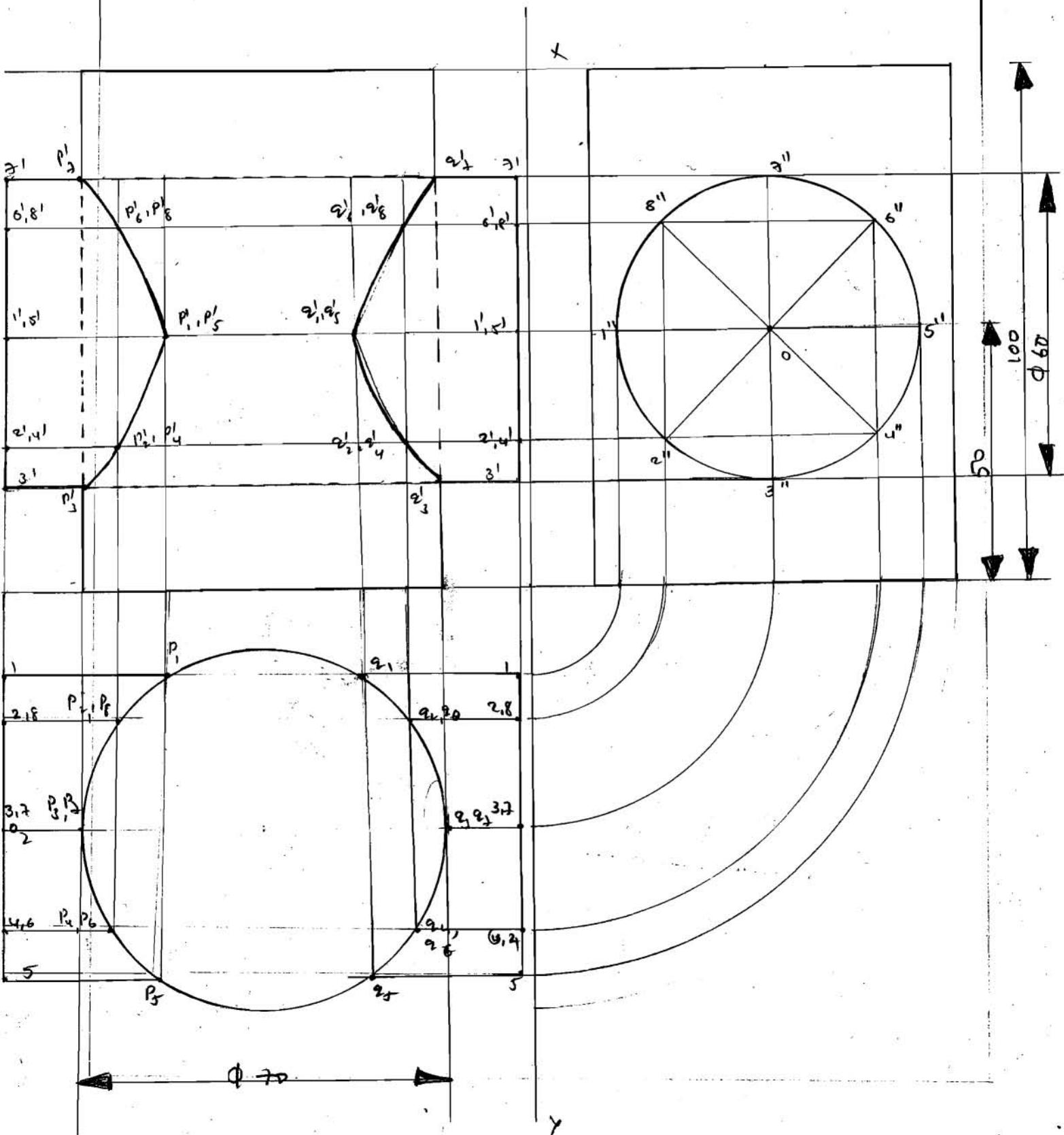
on its base on the H.P. with the side of the base parallel to V.P. It is cut by a planes perpendicular to V.P. To obtain the front view as shown in figure. Draw the development of lateral surface of the retained solid.



#### 4. INTERSECTION OF SOLIDS

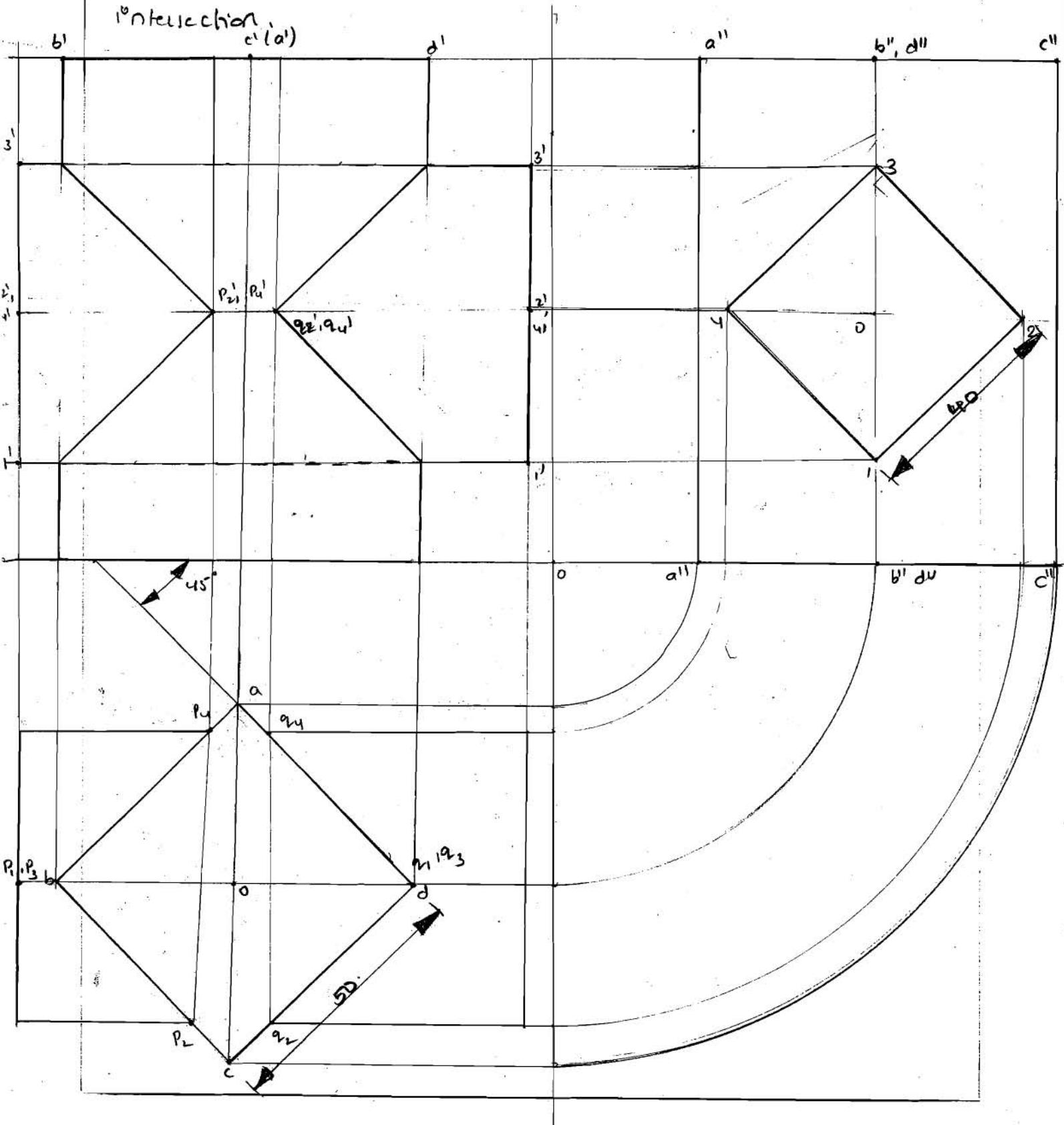
1. A cylinder of base diameter 70mm is resting on its base on the top. It is penetrated by another cylinder of base diameter 60mm such that their axes intersect each other at right angles. Draw the projections of the combination and show the curves of intersection.

Sol. Assume both cylinders height = 100mm



A square prism base side 50mm, is resting on its base on the H.P. It is completely penetrated by another square prism of base side 40mm. such that the axis of both prisms intersect each other at right-angles and faces of both prisms are equally inclined to V.P.

Draw the projections of the combination and show the lines of intersection.



# **UNIT-V**

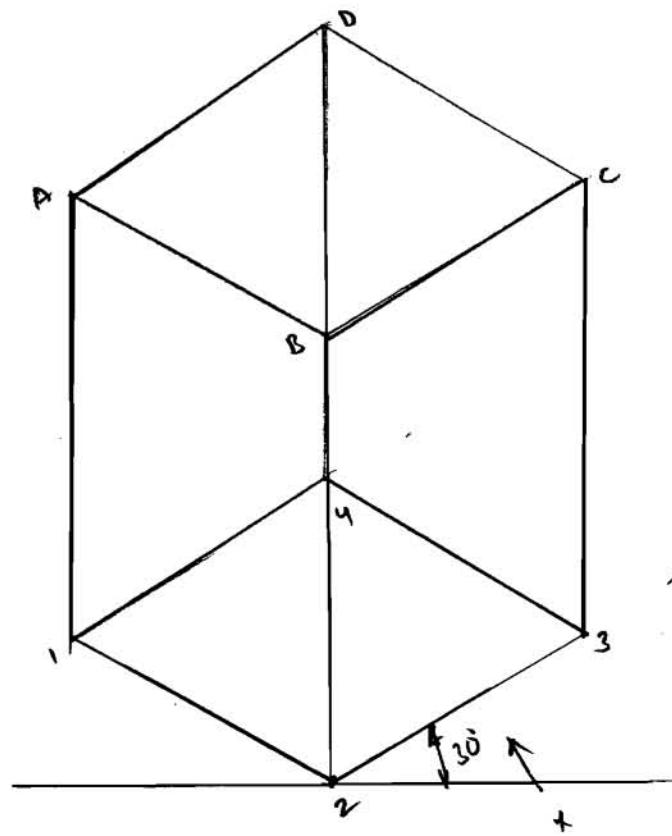
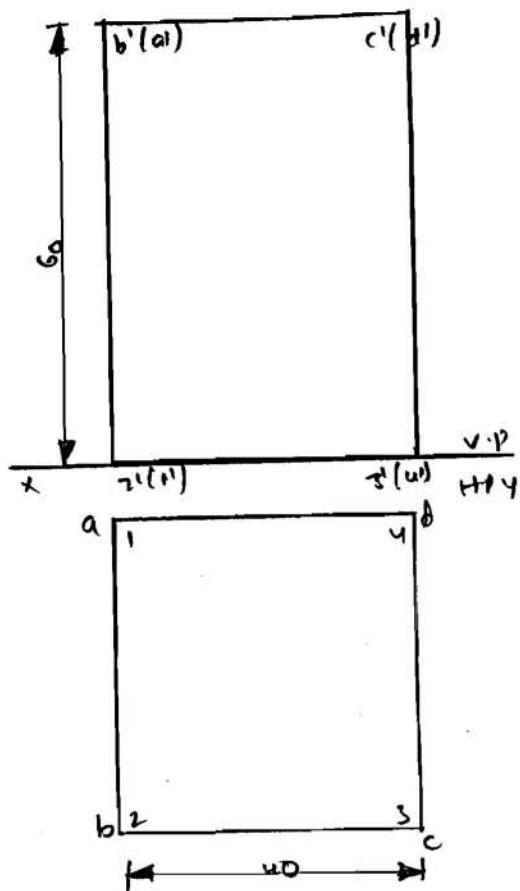
## **Content**

**Isometric Projections:** Principles of Isometric Projection – Isometric Scale – Isometric Views – Conventions – Isometric Views of Lines, Plane Figures, Simple and Compound Solids – Isometric Projection of objects having non-isometric lines. Isometric Projection of Spherical Parts.

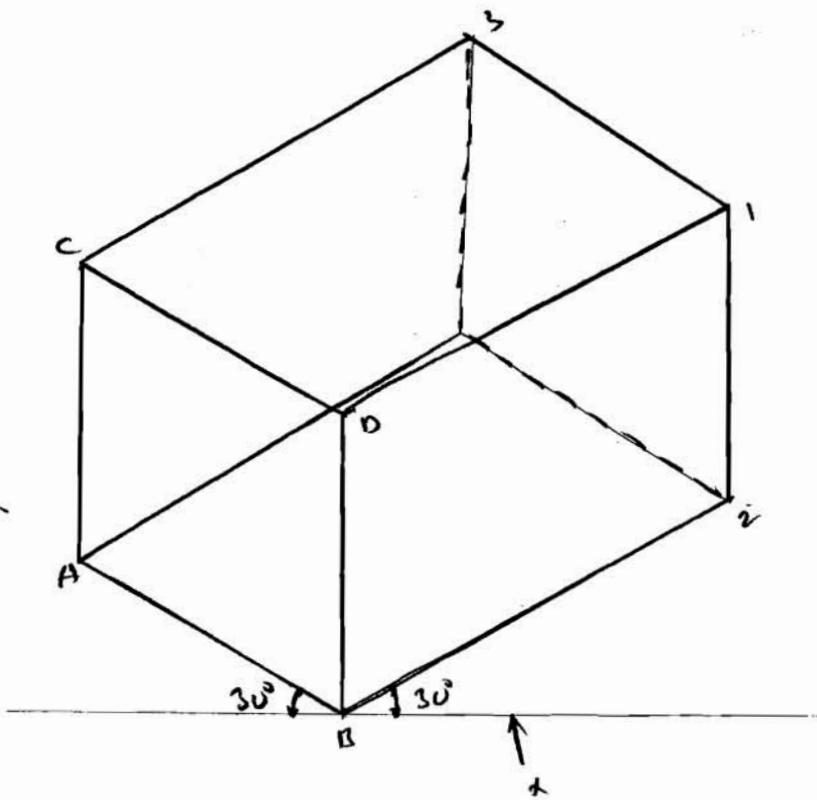
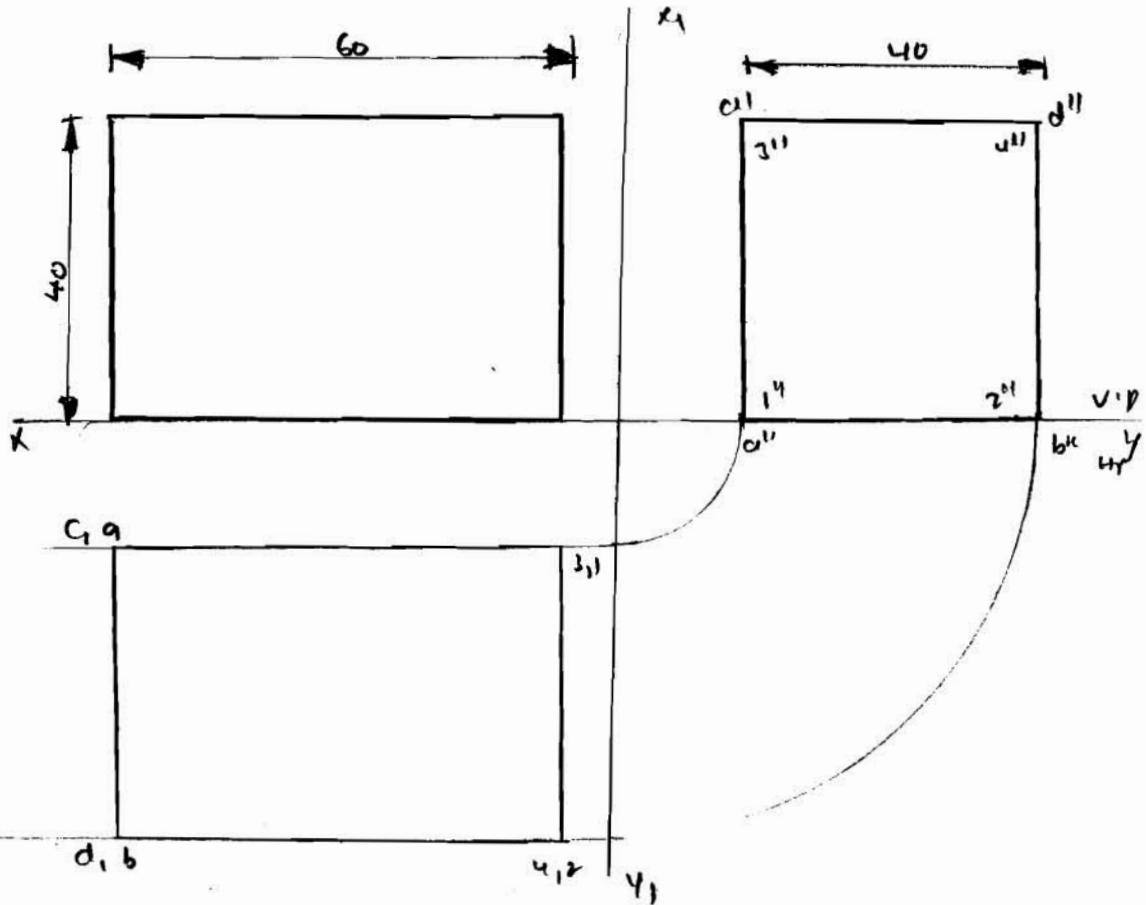
Conversion of Isometric Views to Orthographic Views and Vice-versa –Conventions

## Isometric Projections and Isometric Views-

- 1) Draw an isometric view of a square prism, back side view and OX's Gm's long section on the H.T.P  
 a) on its back with OX's perp to the H.T.P

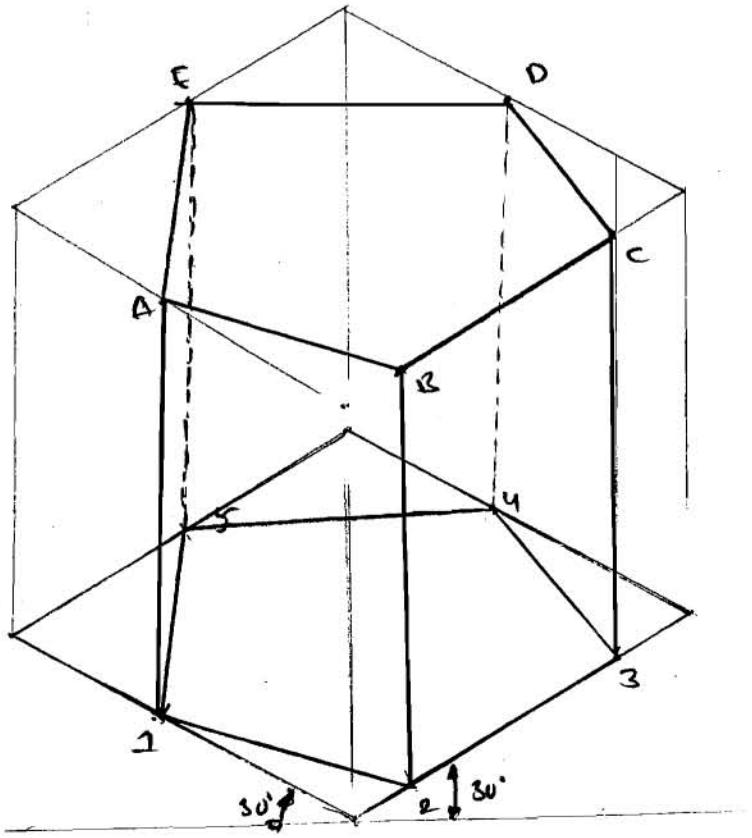
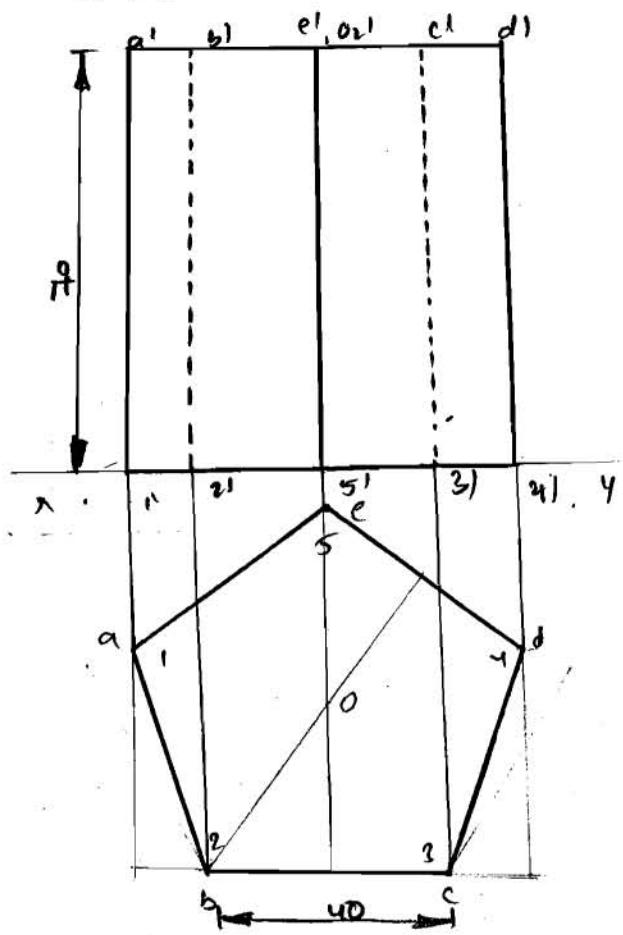


c) on its rectangular face with axis u.v.w.p

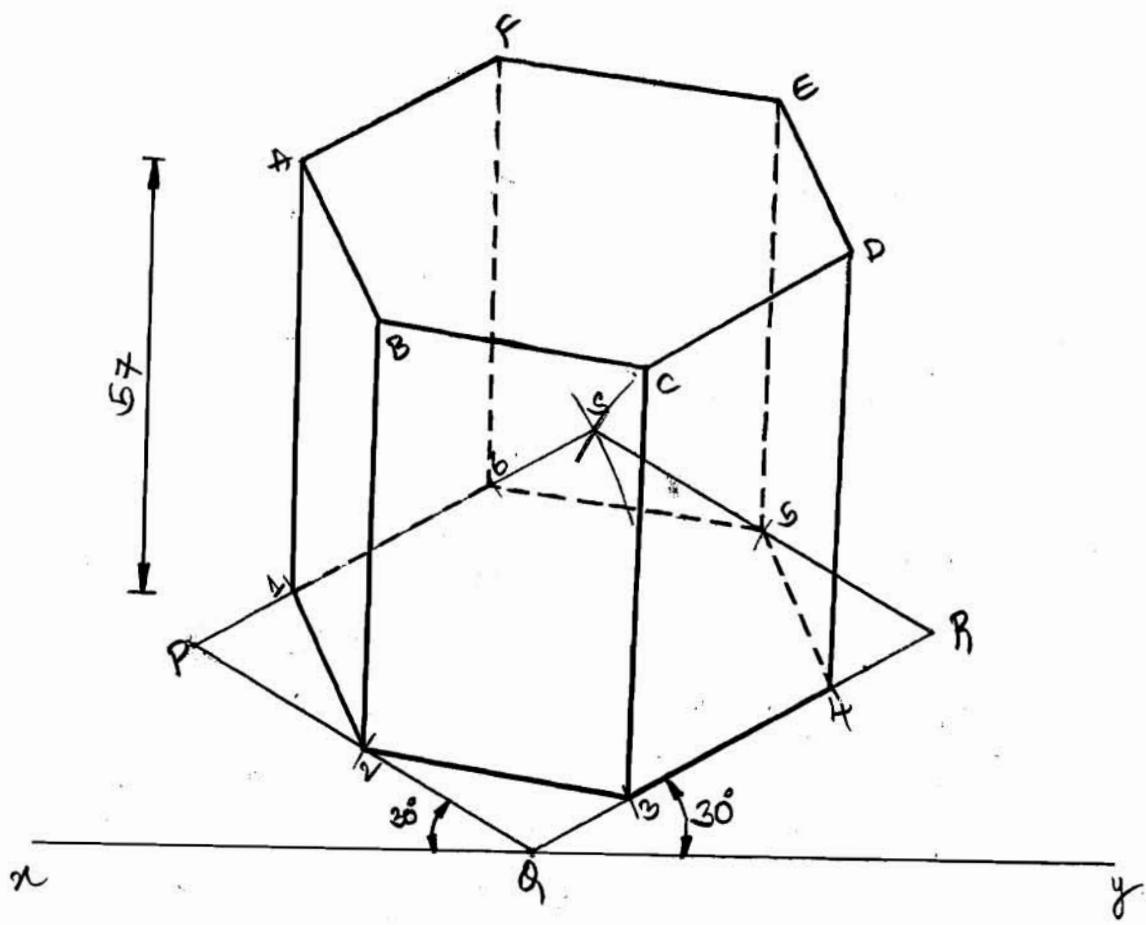


long axis resting on its back on the H.P. with an edge of the back is 161

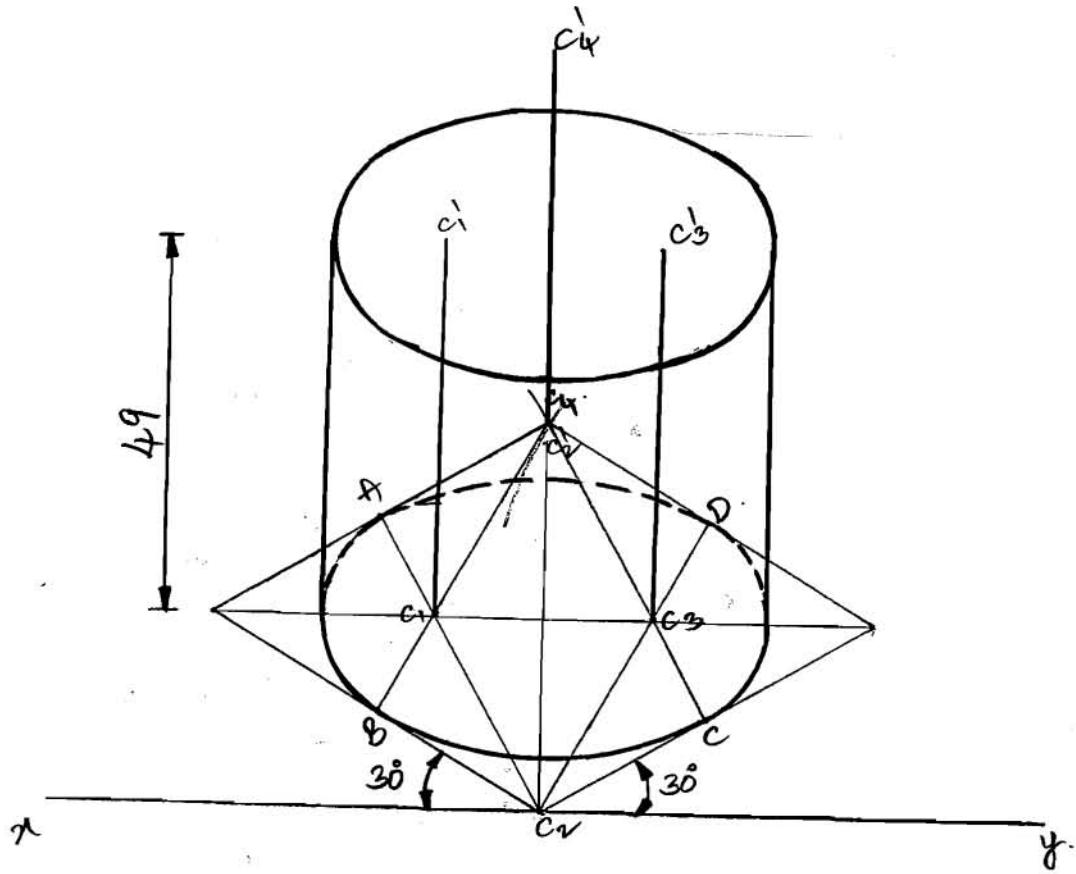
To V.P.



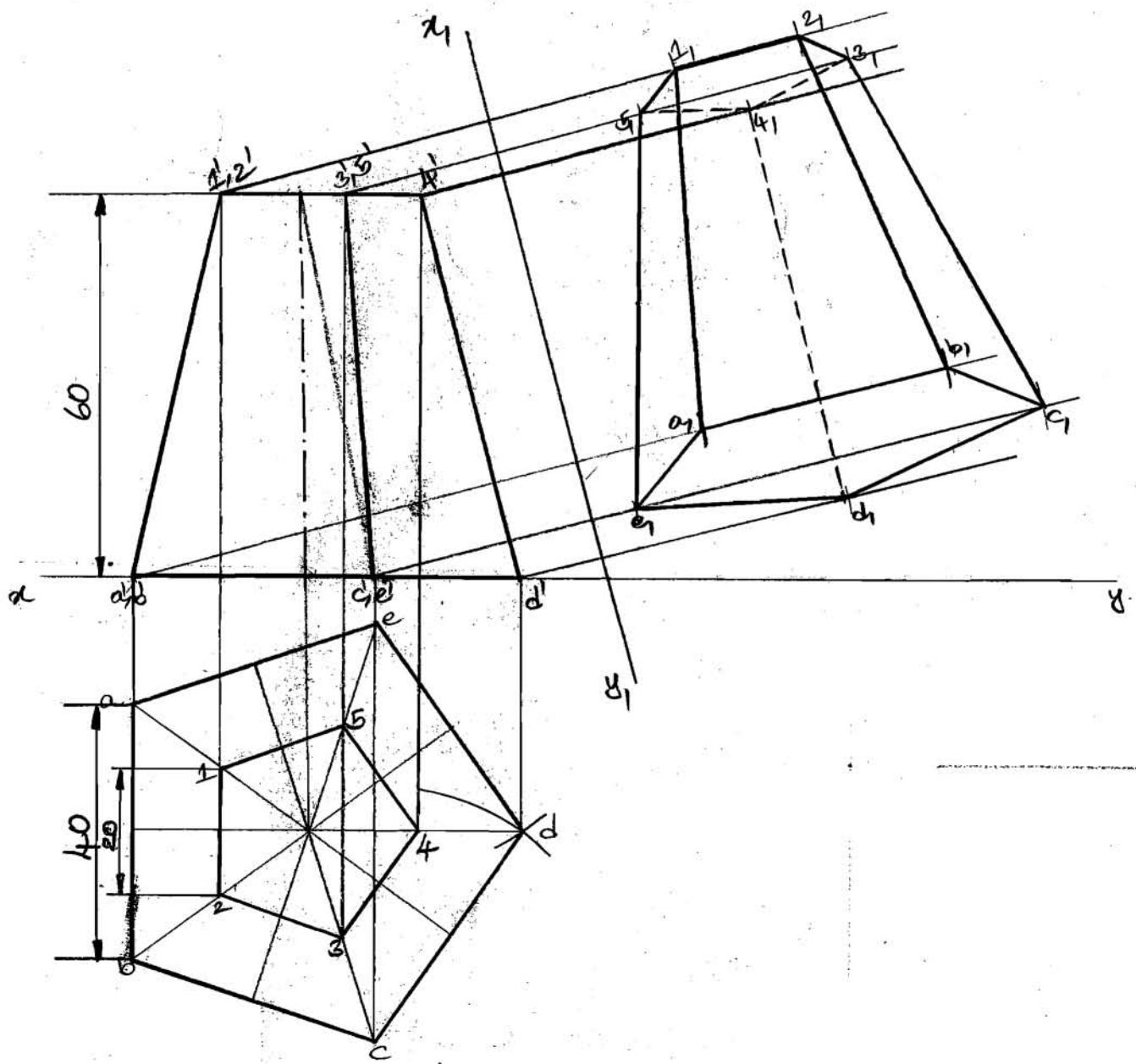
## \* Isometric View (Hexagonal Prism)



## Isometric View (Cylinder)

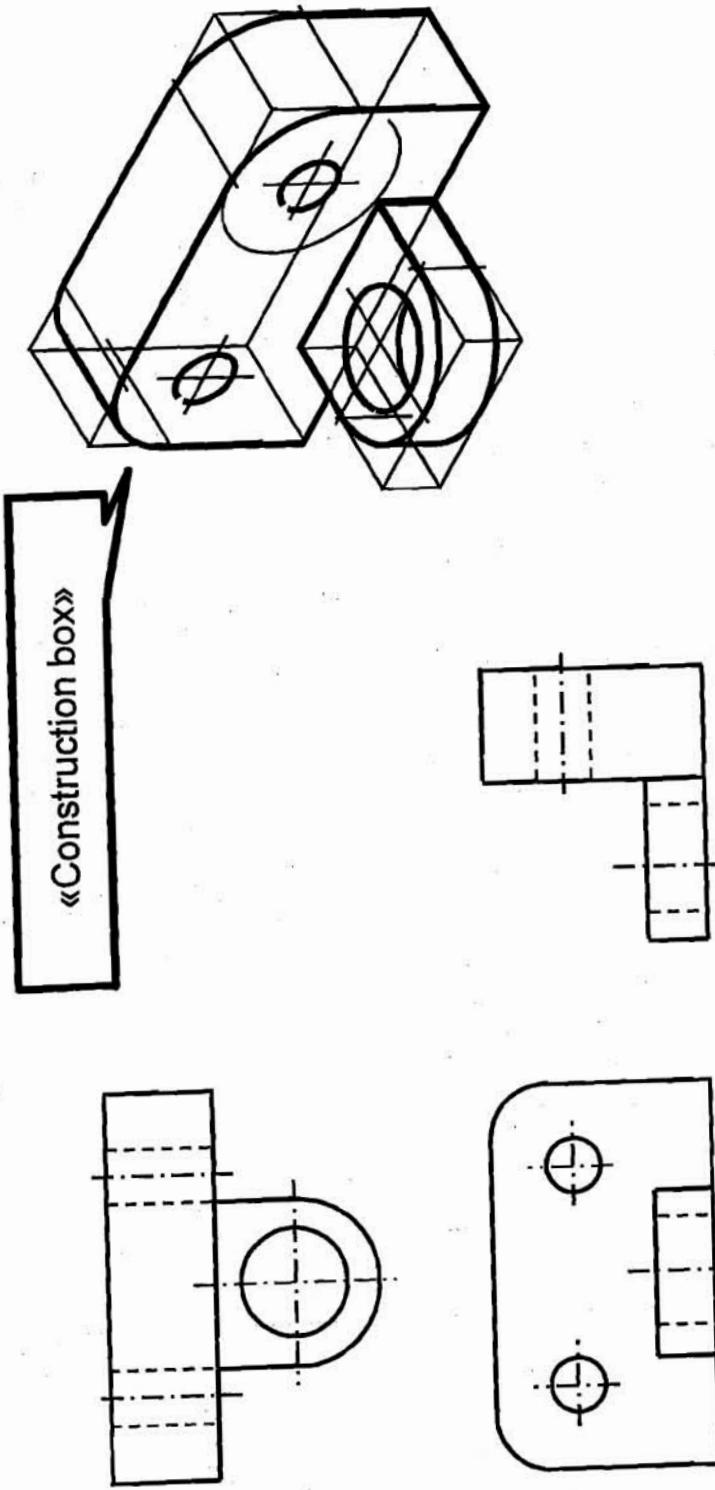


# \* Isometric View (Pentagonal Frustum)



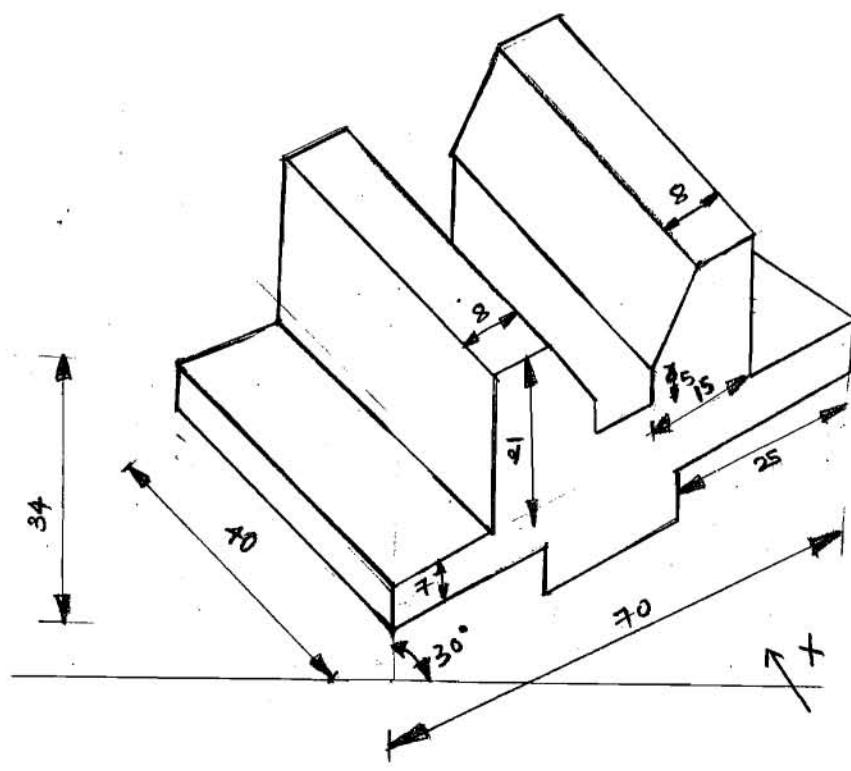
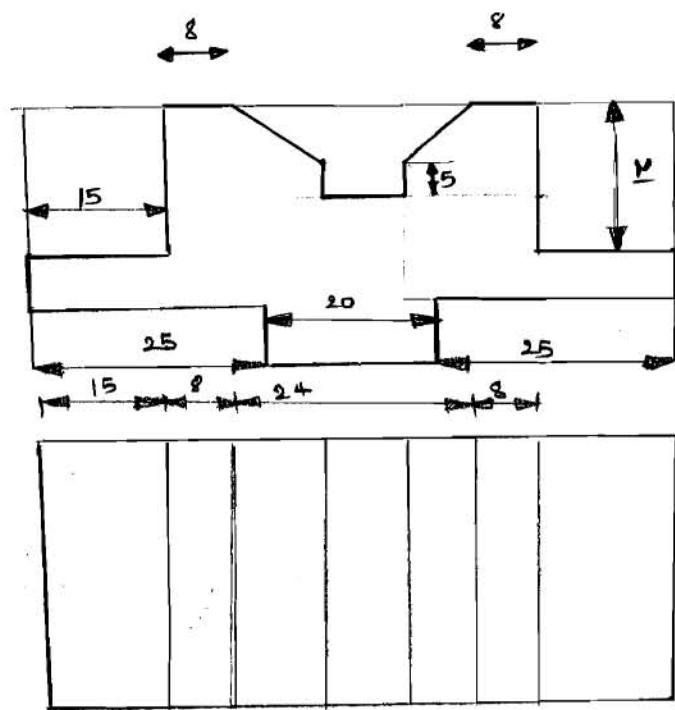
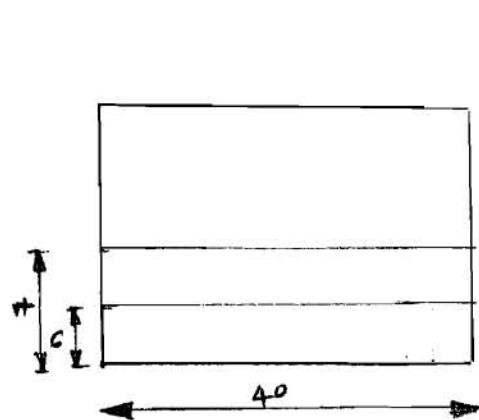
# Isometric drawing

How to draw an object containing rounded parts

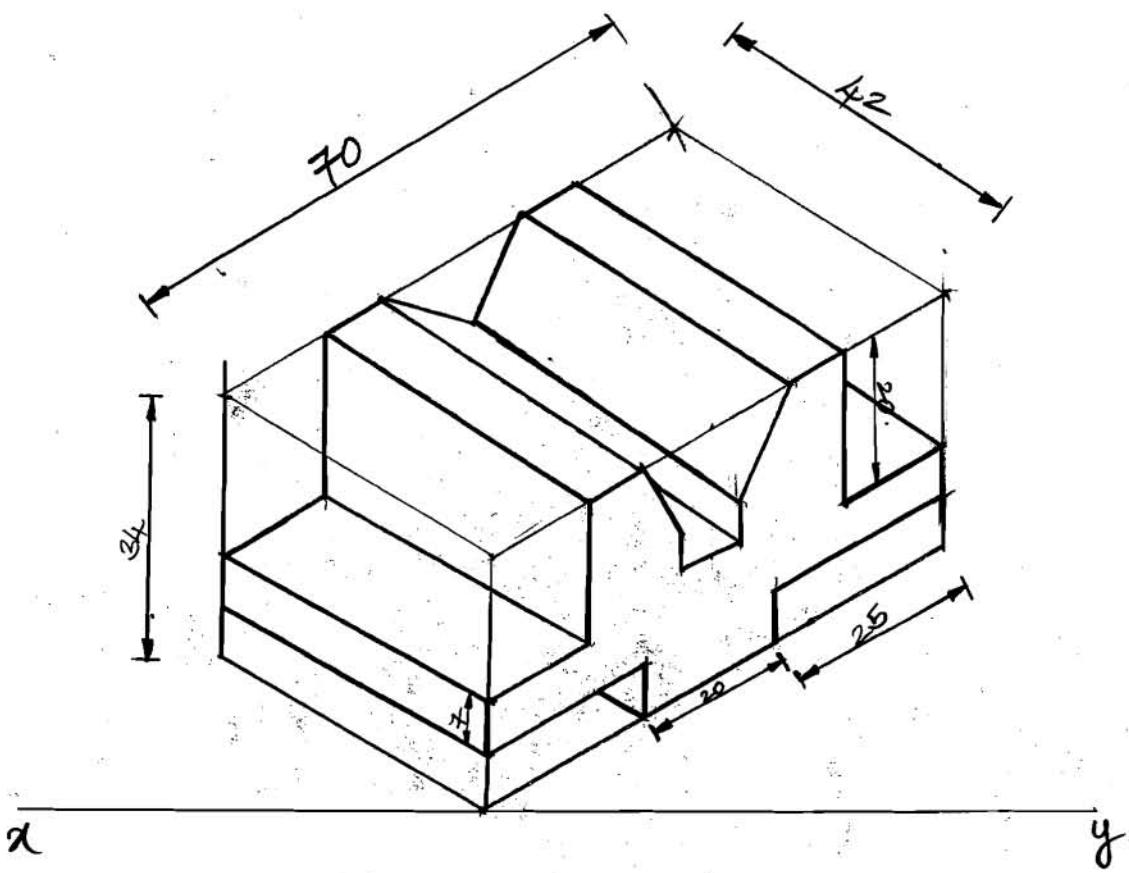


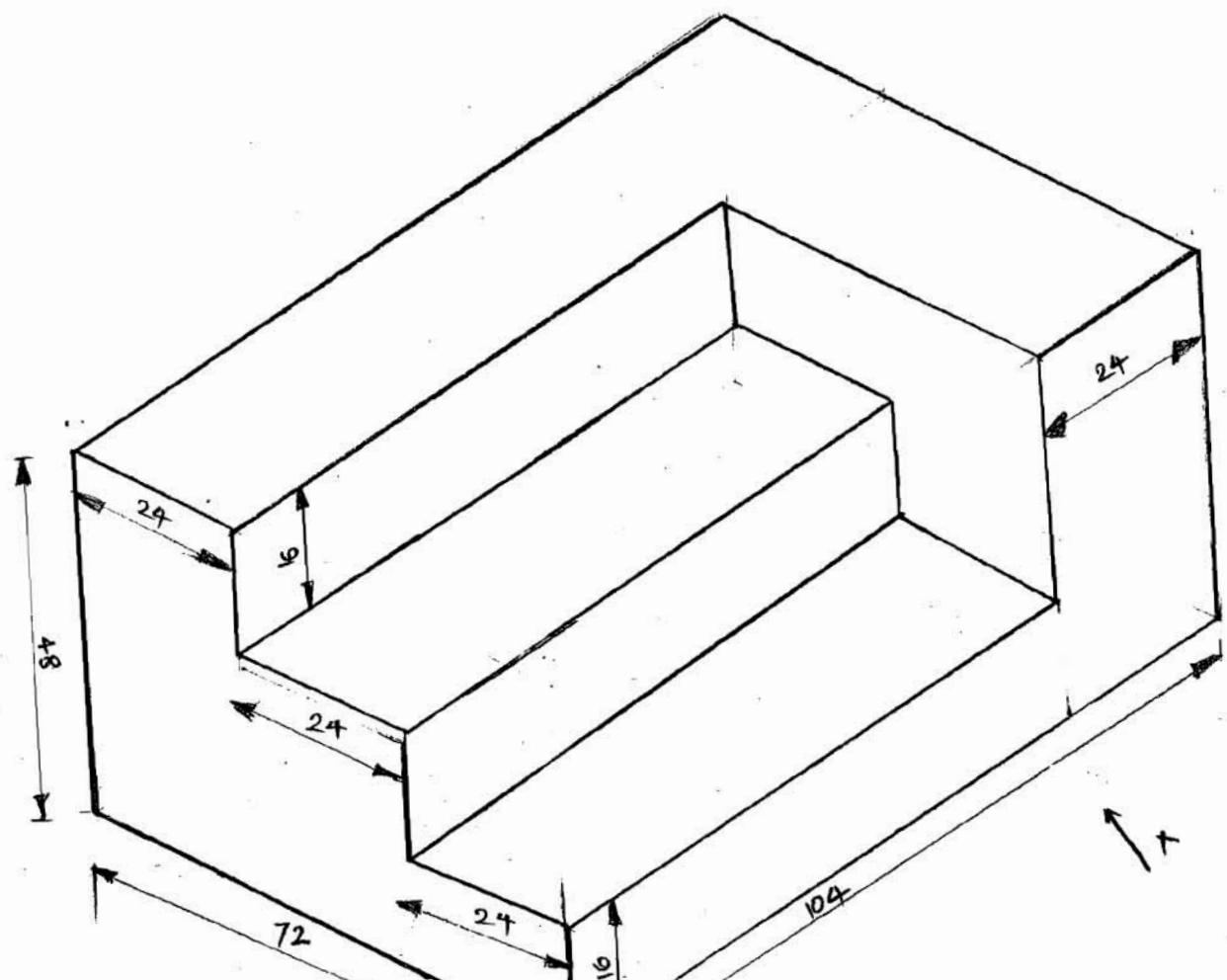
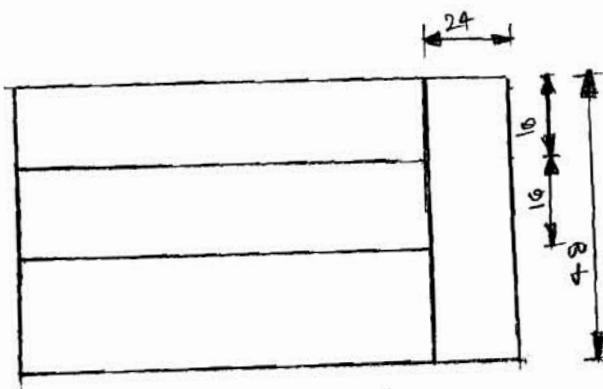
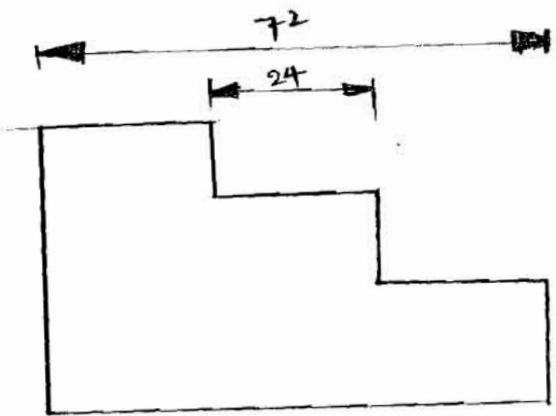
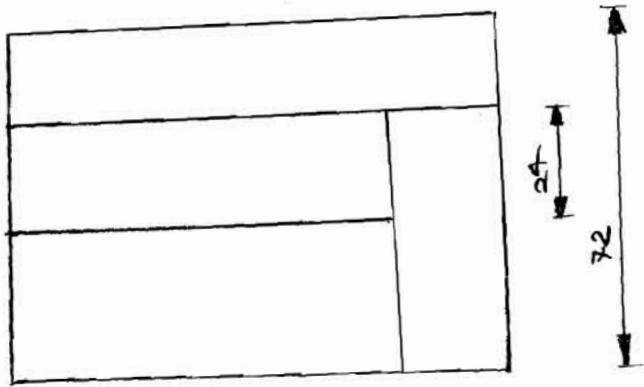
ISOMETRIC PROJECTION

ORTHOGRAPHIC MULTI-VIEW PROJECTION



8 Isometric View





## Example 1

### Steps to draw projections

- Identify surfaces perpendicular or inclined to the view
- Surfaces parallel to the view would not be visible in that view.
- First draw horizontal and vertical reference planes (easily identifiable on drawing)
- Start drawing from the reference planes.

Draw the orthographic projections of Fig. 1

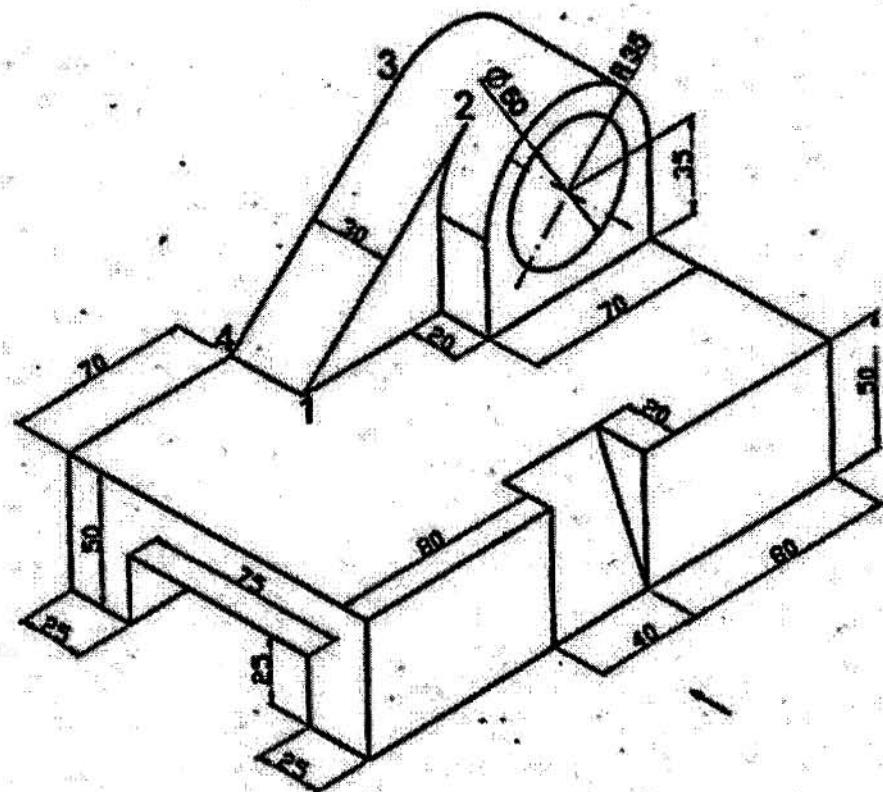
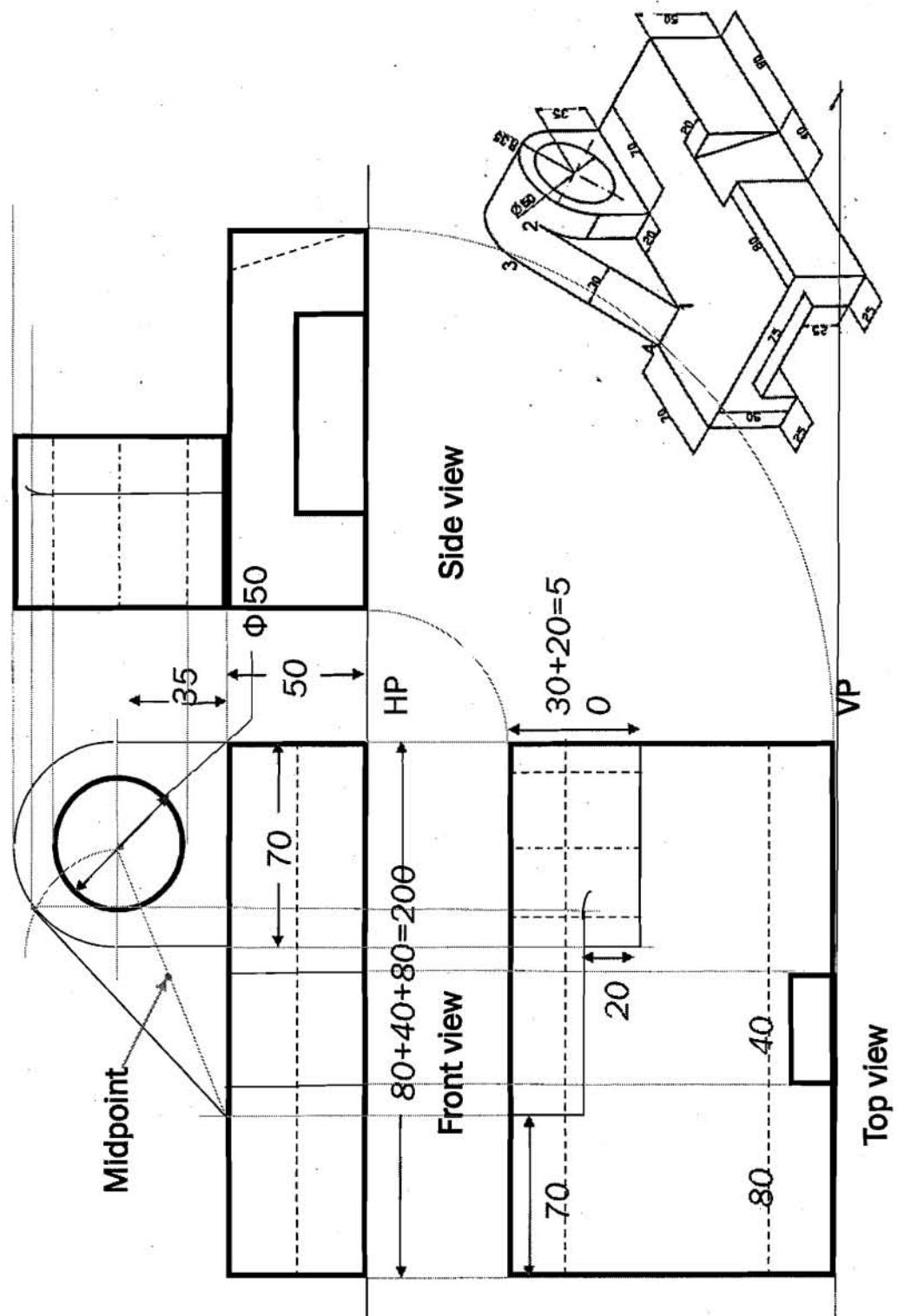
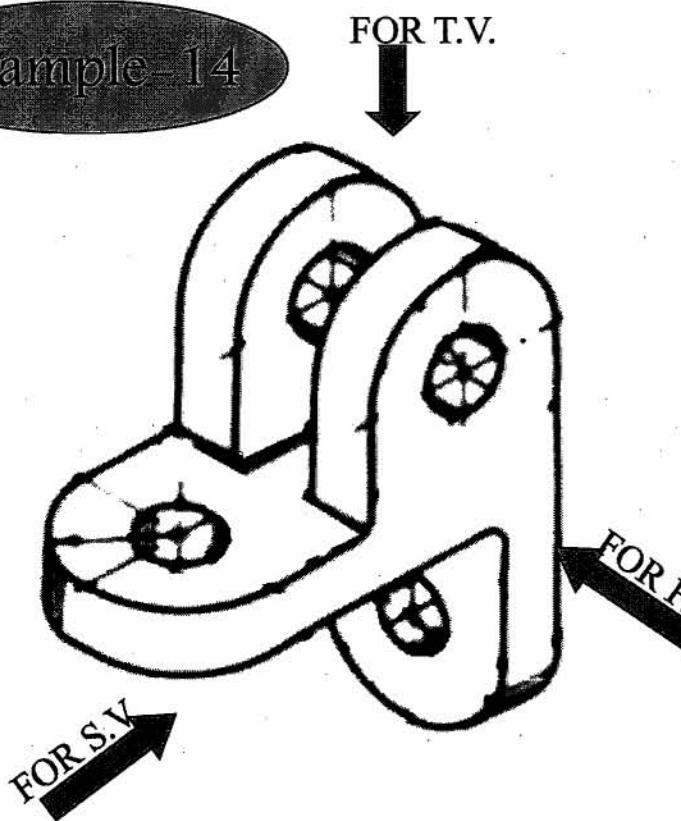


Fig. 1

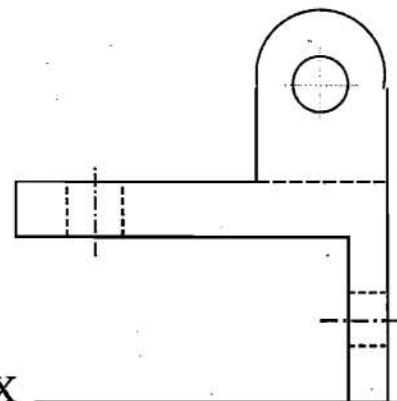


Example - 14

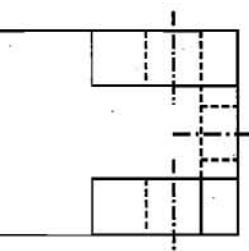
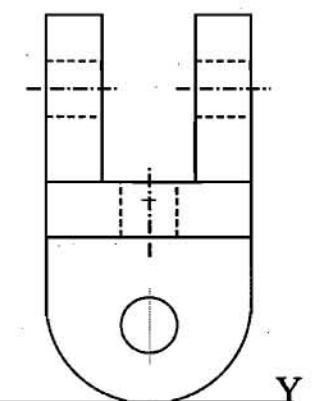


### ORTHOGRAPHIC PROJECTIONS

FRONT VIEW



L.H.SIDE VIEW



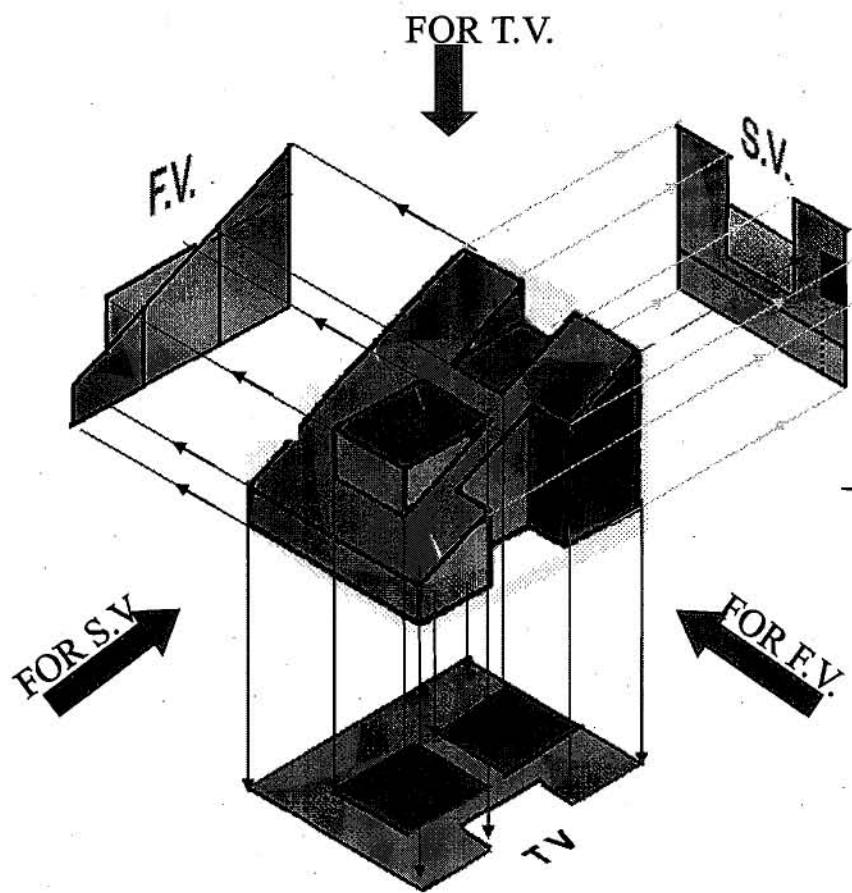
TOP VIEW

### **PICTORIAL PRESENTATION IS GIVEN**

DRAW THREE VIEWS OF THIS OBJECT  
BY FIRST ANGLE PROJECTION METHOD

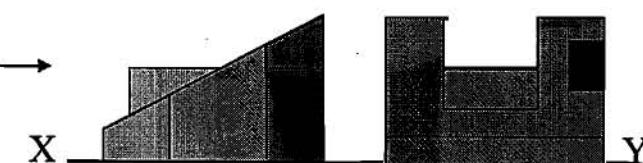
GEKKIN

## Example - 3

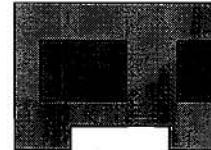


### ORTHOGRAPHIC PROJECTIONS

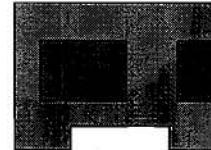
FRONT VIEW



L.H.SIDE VIEW



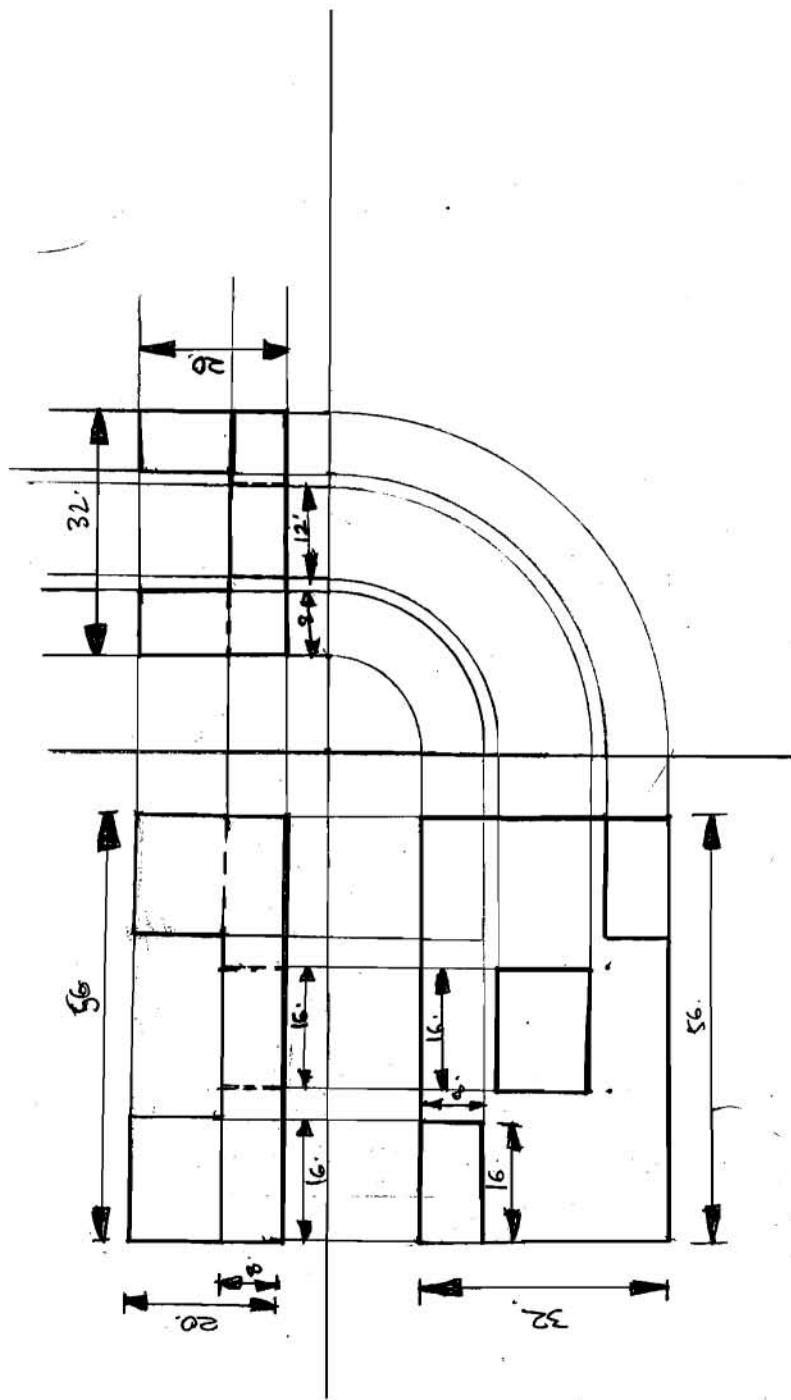
TOP VIEW



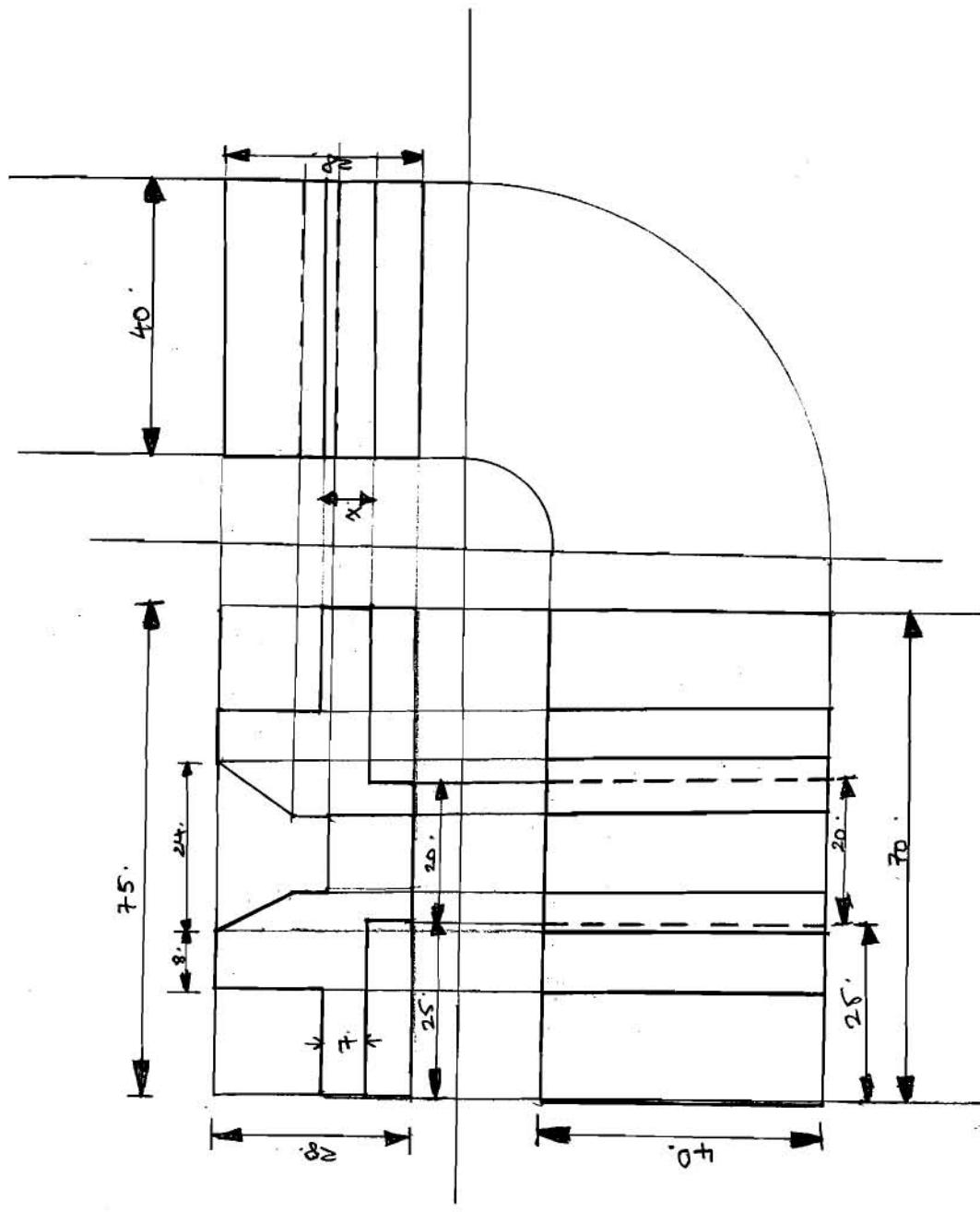
### PICTORIAL PRESENTATION IS GIVEN

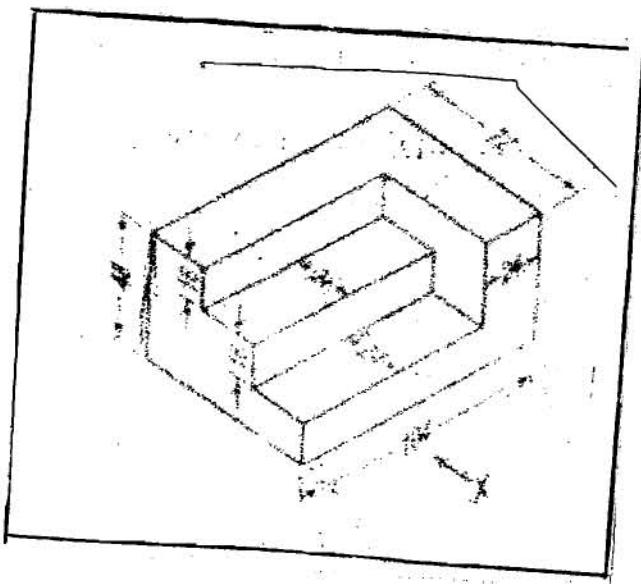
DRAW THREE VIEWS OF THIS OBJECT  
BY FIRST ANGLE PROJECTION METHOD

## \* Orthographics Views (First Angle Projection)



# \* Orthographic Views (First Angle Projection)





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