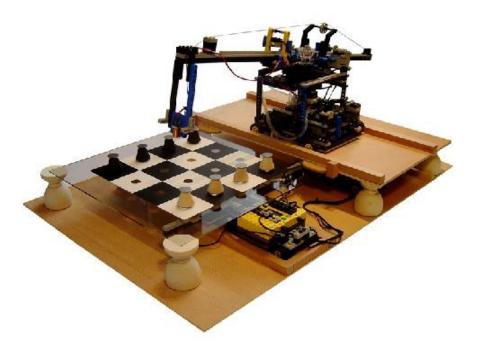
### Outline

- General Game Playing
- Propositional Logic
- First-Order Logic
- The Game Description Language GDL

# Introduction: *General* Game Playing

### **Computer Game Playing**



### Kasparov vs. Deep Blue (1997)



### **General Game Playing**

General Game Players are systems

- able to understand formal descriptions of arbitrary games
- able to learn to play these games effectively.

Translation: They don't know the rules until the game starts.

Unlike specialized game players (e.g. Deep Blue), they do not use algorithms designed in advance for specific games.

### Variety of Games



### **Noughts And Crosses**



### Chess

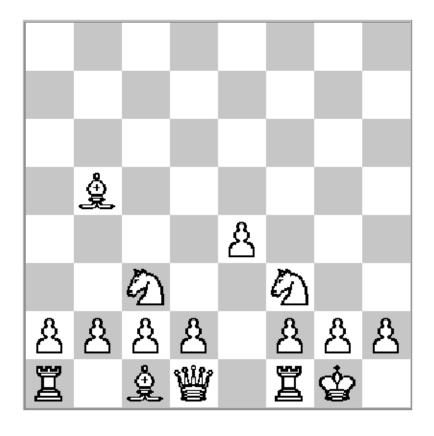


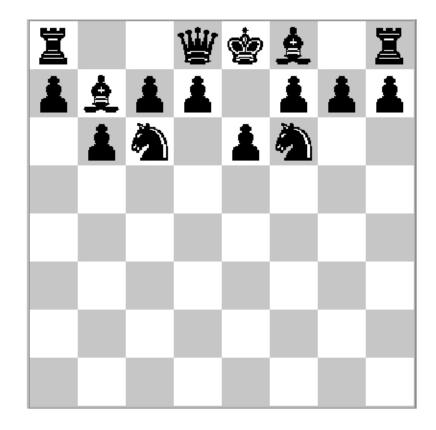
### **Bughouse Chess**



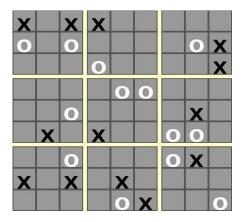


### Kriegspiel

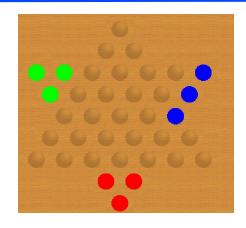


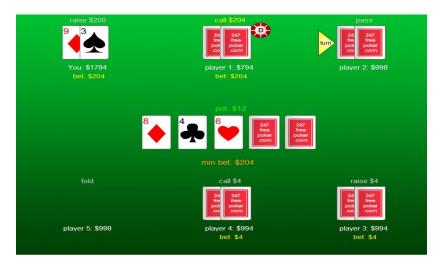


### **Other Games**



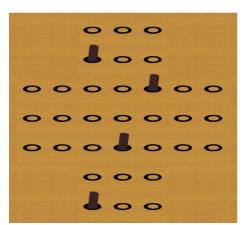




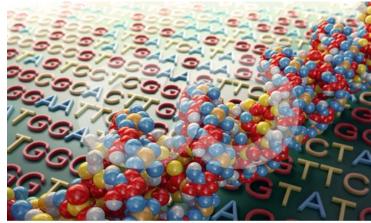


### Single-Player Games (aka. Planning)

7				1			4	
	2				9		5	6
		4		6		2		
		8	6		1		2	
		7				1		
	9		3		8	6		
		5		2		4		
8	4		1				6	
	1			8				2







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### **International Activities**

Websites – www.general-game-playing.de games.stanford.edu

- Games
- Game Manager
- Reference Players
- Development Tools
- Literature

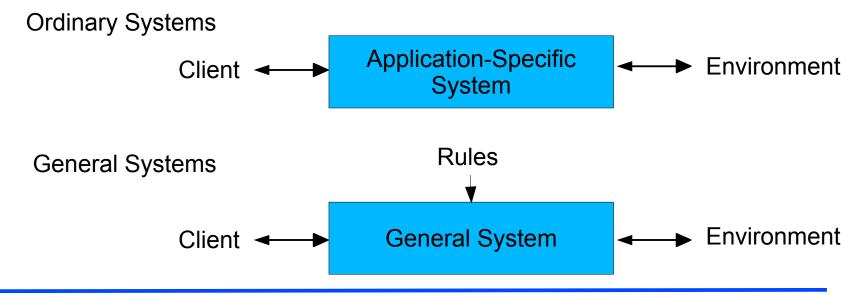
World Cup, administered by Stanford

- 2005 Cluneplayer (USA)
- 2006 Fluxplayer (Germany)
- 2007, 2008 Cadiaplayer (Iceland)
- 2009, 2010 Ary (France)
- 2011 TurboTurtle (USA)
- 2012 Cadiaplayer (Iceland)

### General Game Playing and Al

#### Why games?

- Many social, biological, political, and economic processes can be formalised as (multi-agent) games.
- General game-players are examples of systems that can adapt to radically different environments without human intervention.



### Finite Synchronous Games

#### Finite environment

- Environment with finitely many positions (= states)
- One initial state and one or more terminal states

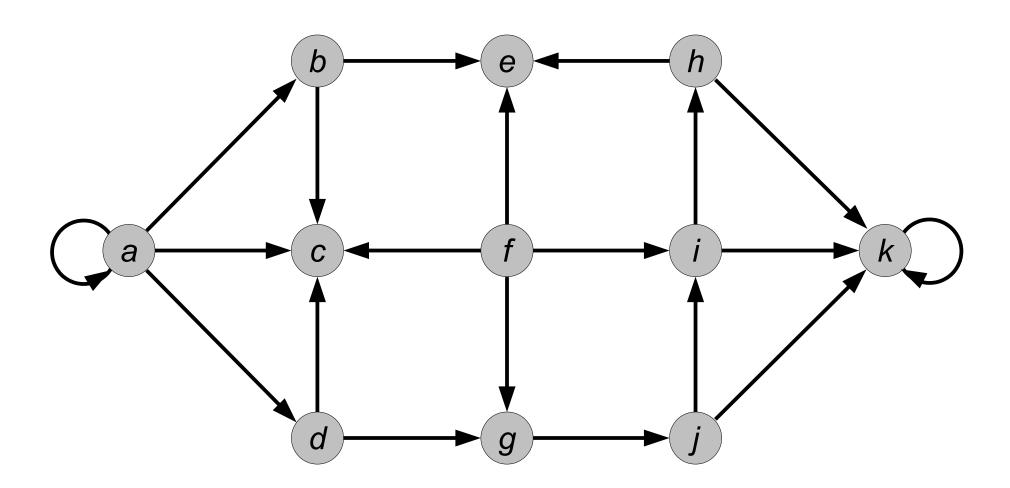
#### Finite Players

- Fixed finite number of players
- Each with finitely many "actions"
- Each with one or more goal states

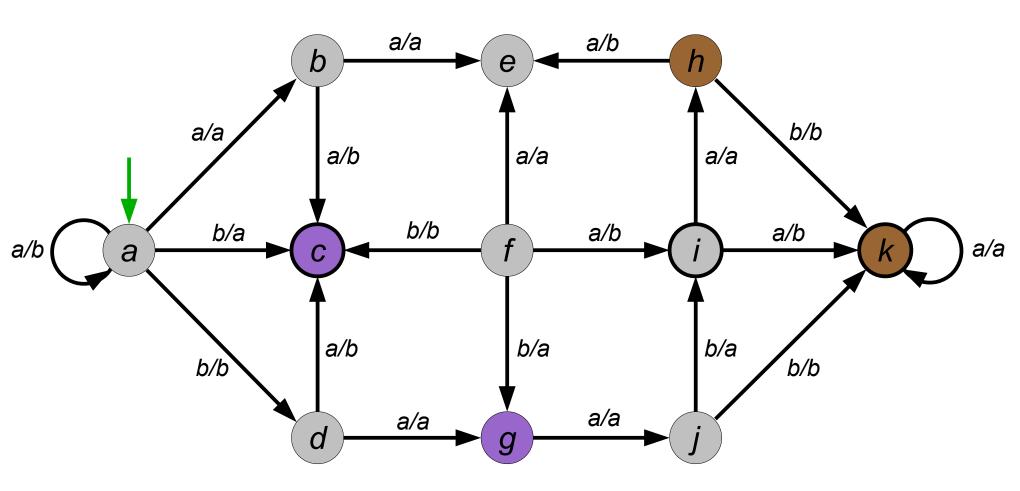
#### Synchronous Update

- All players move on all steps (possibly some "no-ops")
- Environment changes only in response to moves

### Games as State Machines



### Initial State, Terminal States, & Simultaneous Moves



### **Direct Description**

Since all of the games that we are considering are finite, it is possible in principle to communicate game information in the form of tables (for legal moves, update, etc.)

Problem: Size of description. Even though everything is finite, the necessary tables can be large (e.g. ~10<sup>44</sup> states in Chess)

#### Solutions:

- Reformulate in modular fashion
- Use compact encoding

### States versus Features

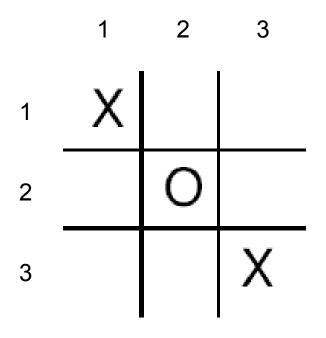
In many cases, worlds are best thought of in terms of **atomic features** that may change; e.g. "position-of-white-queen", "black-can-castle". Moves (a.k.a. actions) affect subsets of these features.

States represent all possible ways the world can be.

As such, the number of states is exponential in the number of features of the world, and the transition tables are correspondingly large.

Solution: Represent features directly and describe how actions change individual features rather than entire states

### **Example: Noughts And Crosses**



```
cell(1,1,x)
cell(1,2,b)
cell(1,3,b)
cell(2,1,b)
cell(2,2,o)
cell(2,3,b)
cell(3,1,b)
cell(3,2,b)
cell(3,3,x)
control(oplayer)
```

### Game Description Language (GDL): Facts and Rules

#### Some Facts

```
role(xplayer)
role(oplayer)

init(cell(1,1,b))
init(cell(1,2,b))
...
init(cell(3,3,b))
init(control(xplayer))
```

#### Some Rules

All highlighted expressions are pre-defined keywords in GDL.

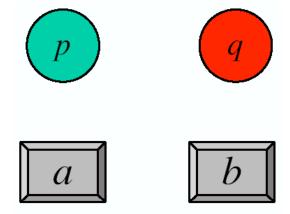
### Pure Logic: No Built-In Assumptions

#### What we see

#### What they see

## **Propositional Logic**

### A Simpler Example First: the Buttons-And-Light Game



Pressing button *a* toggles *p*.

Pressing button *b* interchanges *p* and *q*.

Initially, *p* and *q* are off. Goal: *p* and *q* are on.

### Propositional Logic: Vocabulary

Proposition Symbols: p, q, r

Logical Connectives: ¬p (negation, read: "not p")

p∧q (conjunction, read: "p and q")

p∨q (disjunction, read: "p or q")

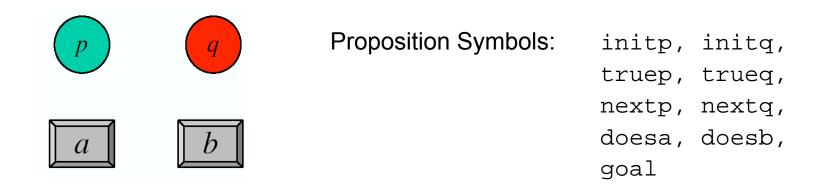
p<=q (implication, read: "p if q")

p<=>q (equivalence, read: "p if and only if q")

Sentences: built from proposition symbols and connectives

e.g. p<=>(q∧¬r)∨¬q

### **Example: Buttons and Lights**



#### The logic of this game:

```
nextp <=> (¬truep ∧ doesa) ∨ (trueq ∧ doesb)
nextq <=> (trueq ∧ doesa) ∨ (truep ∧ doesb)

¬initp
¬initq
qoal <=> (truep ∧ trueq)
```

### **Propositional Logic: Semantics**

#### Truth table

р	q	¬р	p∧q	p∨q	p<=q	p<=>q
false	false	true	false	false	true	true
false	true	true	false	true	false	false
true	false	false	false	true	true	false
true	true	false	true	true	true	true

Example  $\phi$   $\psi$ 

true	p trueq	doesa	doesb	¬truep	¬truep ∧ doesa	trueq ^ doesb	φνψ*
fals	e false	true	false	true	true	false	true
true	false	false	true	false	false	false	false

### **Knowing What Happens in Buttons-and-Lights**

nextp <=> (¬truep ∧ doesa) ∨ (trueq ∧ doesb)
nextq <=> (trueq ∧ doesa) ∨ (truep ∧ doesb)



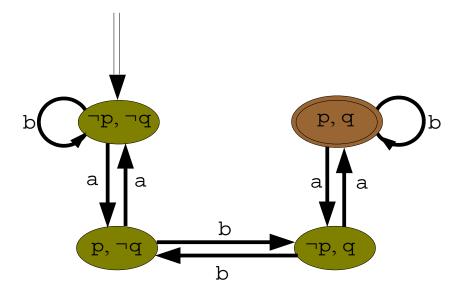






truep	trueq	doesa	doesb	nextp	nextq
false	false	true	false	true	false
false	false	false	true	false	false
true	false	true	false	false	false
true	false	false	true	false	true
false	true	true	false	true	true
false	true	false	true	true	false
true	true	true	false	false	true
true	true	false	true	true	true

### Summary: State Transitions for Buttons-and-Lights



### More on Semantics: Models

A model (in propositional logic) is an arbitrary subset of the proposition symbols.

M is a model for a sentence  $\varphi$  under the following conditions:

- M model for a proposition φ iff φ
- M model for ¬φ iff M not a model for φ
- M model for φ∧ψ iff M model for φ and model for ψ
- $\mathcal{M}$  model for  $\phi \lor \psi$  iff  $\mathcal{M}$  model for  $\phi$  or model for  $\psi$  (or both)
- M model for φ <= ψ iff M model for φ whenever M model for ψ</li>
- $\mathcal{M}$  model for  $\phi <=> \psi$  iff  $\mathcal{M}$  model for  $\phi$  just in case  $\mathcal{M}$  model for  $\psi$

If all models of sentences  $\Phi$  also satisfy  $\varphi$ , then  $\varphi$  is a logical consequence of  $\Phi$ .

# First-Order Logic

### First-Order Logic: Vocabulary

Object Variables: X, Y, Z

Object Constants: a, b, c

Functions: f, g, h

Predicates: p, q, r

Connectives:  $\neg$ ,  $\wedge$ ,  $\vee$ ,  $\langle =$ ,  $\langle = \rangle$ 

Quantifiers: ∀, ∃

The arity of a function or predicate is the number of arguments that can be supplied.

### First-Order Logic: Syntax

#### **Terms**

Variables:
x, y, z

• Constants: a, b, c

Functional terms: f(a), g(a,X), h(a,b,f(Y))

#### Sentences

• Atoms: p(X), q(a,q(a,b))

• Literals: p(X),  $\neg p(X)$  (i.e. atoms and negated atoms)

• Sentences: p(a) ∨ ¬p(a)

 $\forall X \exists Y p(X,Y) <= \exists Y \forall X p(X,Y)$ 

 $\forall X \ p(f(X)) \iff \exists Y \ q(X,f(Y)) \land \neg r(a)$ 

### Example

```
constant
role(xplayer)
role(oplayer)
init(cell(1,1,b)))
init(cell(1,2,b))
init(cell(3,3,b))
     control(xplayer))
         predicate
```

```
variable
```

### First-Order Logic: Semantics

The **Herbrand universe** for a logic language is the set of all terms without variables.

#### Example 1:

- Object Constants: a, b
- Herbrand Universe: {a, b}

#### Example 2:

- Object Constant: a
- Unary function:
- Herbrand Universe: {a, f(a), f(f(a)),...}

### Semantics (Cont'd)

The Herbrand base is the set of all variable-free atoms.

**Example**:  $\{p(a), p(b), q(a,a), q(a,b), q(b,a), q(b,b)\}$ 

A model is an arbitrary subset of the Herbrand base.

#### Examples:

- $M_1 = \{p(a), q(a,b), q(b,a)\}$
- $M_2 = \{p(a), p(b), q(a,a), q(a,b), q(b,a), q(b,b)\}$
- $\mathcal{M}_{3} = \{ \}$

### Semantics (Finished)

M is a model for a sentence  $\phi$  (in which all variables are bound by a quantifier) under the following conditions:

- M model for a variable-free atom φ iff φ
- M model for ¬φ iff M not a model for φ
- M model for φ \ ψ iff M model for φ and model for ψ
- M model for φ ∨ ψ iff M model for φ or model for ψ (or both)
- M model for φ <= ψ iff M model for φ whenever M model for ψ</li>
- M model for φ <=> ψ iff M model for φ just in case M model for ψ
- $\mathcal{M}$  model for  $\forall x \varphi$  iff  $\mathcal{M}$  model for  $\varphi\{x/t\}$  for all terms t in the Herbrand universe
- $\mathcal{M}$  model for  $\exists x \varphi$  iff  $\mathcal{M}$  model for  $\varphi\{x/t\}$  for some t in the Herbrand universe

 $\phi\{x/t\}$  means to replace each occurrence of x by t in  $\phi$ .

# **Examples**

#### Recall the models

- $M_1 = \{p(a), q(a,b), q(b,a)\}$
- $M_2 = \{p(a), p(b), q(a,a), q(a,b), q(b,a), q(b,b)\}$
- $\mathcal{M}_3 = \{ \}$

#### Some examples:

- $\mathcal{M}_1$  is a model for  $p(a) \land \neg p(b)$ , whereas  $\mathcal{M}_2$  and  $\mathcal{M}_3$  are not.
- $\mathcal{M}_2$  is a model for  $p(b) \le p(a)$ . So is  $\mathcal{M}_3$  (!)

If all models of sentences  $\Phi$  also satisfy  $\varphi$ , then  $\varphi$  is a logical consequence of  $\Phi$ .

## Logic Programs: A Subset of First-Order Logic

#### Clauses

Facts: atoms

Rules: Head <= Body</p>

Head: atom

Body: sentence built from  $\wedge$ ,  $\vee$ , literal

All variables in a clause are universally quantified (over the whole clause).

A logic program is a finite collection of clauses.

# General Game Description Language GDL

## Back to General Game Playing

In the Game Description Language (GDL), a game is a logic program. GDL uses the constants 0, 1, ..., 100 and the following predicates as keywords.

_				/ \	
	VI	$\neg$ $\Box$	$\triangle$	~ \	١
•	$\perp$	ノエ	. <del>–</del> 1	/	1

init(f)

true(f)

does(r,a)

next(f)

legal(r,a)

qoal(r,v)

terminal

means that  $\mathbf{r}$  is a role (i.e. a player) in the game

means that f is true in the initial position (state)

means that f is true in the current state

means that role r does action a in the current state

means that f is true in the next state

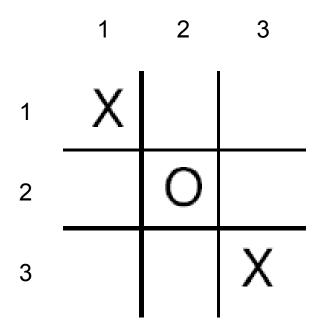
means that it is legal for r to play a in the current state

means that r gets goal value v in the current state

means that the current state is a terminal state

distinct(s,t) means that terms s and t are syntactically different

#### **Back to Noughts And Crosses**



```
cell(1,1,x)
cell(1,2,b)
cell(1,3,b)
cell(2,1,b)
cell(2,2,o)
cell(2,3,b)
cell(3,1,b)
cell(3,2,b)
cell(3,3,x)
control(oplayer)
```

## Noughts and Crosses: Elements of the Vocabulary

#### Object constants

```
xplayer, oplayer
x, o ,b
noop
```

Players Marks Move

#### Functions

```
cell(number,number,mark) Feature
control(player) Feature
mark(number,number) Move
```

#### Predicates

```
row(number,mark)
column(number,mark)
diagonal(mark)
line(mark)
open
draw
```

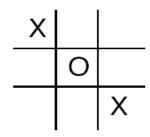
#### Players and Initial State

```
role(xplayer)
role(oplayer)
init(cell(1,1,b))
init(cell(1,2,b))
init(cell(1,3,b))
init(cell(2,1,b))
init(cell(2,2,b))
init(cell(2,3,b))
init(cell(3,1,b))
init(cell(3,2,b))
init(cell(3,3,b))
init(control(xplayer))
```

#### **Move Generator**

#### Conclusions:

```
legal(xplayer,noop)
legal(oplayer,mark(1,2))
...
legal(oplayer,mark(3,2))
```



```
true(cell(1,1,x))
true(cell(1,2,b))
true(cell(1,3,b))
true(cell(2,1,b))
true(cell(2,2,o))
true(cell(2,3,b))
true(cell(3,1,b))
true(cell(3,2,b))
true(cell(3,3,x))
true(control(oplayer))
```

#### Physics: Example

cell(1,1,x)cell(1,1,x)cell(1,2,b)cell(1, 2, b)cell(1,3,0)cell(1,3,b)cell(2,1,b)cell(2,1,b)cell(2,2,0)cell(2,2,0)oplayer cell(2,3,b)cell(2,3,b)mark(1,3) cell(3,1,b)cell(3,1,b)cell(3,2,b)cell(3,2,b)cell(3,3,x)cell(3,3,x)control(xplayer) control(oplayer)  $\circ$ O Χ

#### **Physics**

```
next(cell(M,N,x)) <= does(xplayer,mark(M,N))
next(cell(M,N,o)) <= does(oplayer,mark(M,N))</pre>
```

```
next(control(xplayer)) <= true(control(oplayer))
next(control(oplayer)) <= true(control(xplayer))</pre>
```

## **Supporting Concepts**

```
diagonal(W) <=
row(M,W) <=
                                      true(cell(1,1,W)) \(\Lambda\)
   true(cell(M,1,W)) \cap \)
                                      true(cell(2,2,W)) \times
   true(cell(M,2,W)) \cdot
                                      true(cell(3,3,W))
   true(cell(M, 3, W))
                                  diagonal(W) <=
column(N,W) <=
                                       true(cell(1,3,W)) \[ \lambda \]
   true(cell(1,N,W)) \
                                       true(cell(2,2,W)) \( \)
   true(cell(2,N,W)) ^
                                       true(cell(3,1,W))
   true(cell(3,N,W))
```

#### **Termination and Goal Values**

```
terminal <=
   line(x) \lor line(o)
terminal <=
   ←open
line(W) <=
   row(M,W) V
   column(N,W) V
   diagonal(W)
open <=
   true(cell(M,N,b))
```

```
goal(xplayer,100) <= line(x)</pre>
goal(xplayer, 50) <= draw</pre>
goal(xplayer, 0) <= line(o)</pre>
goal(oplayer,100) <= line(o)</pre>
goal(oplayer, 50) <= draw</pre>
goal(oplayer, 0) <= line(x)</pre>
draw <=
   \neg line(x) \land \neg line(o) \land \neg open
```

## Knowledge Interchange Format

Knowledge Interchange Format (a.k.a. KIF) is a standard for programmatic exchange of knowledge represented in relational logic.

Syntax is prefix version of standard syntax.

Some operators are renamed: not, and, or.

Case-independent. Variables are prefixed with ?.

```
r(X,Y) \le p(X,Y) \land \neg q(Y)
(<= (r ?x ?y) (and (p ?x ?y) (not (q ?y))))
```

or, equivalently,

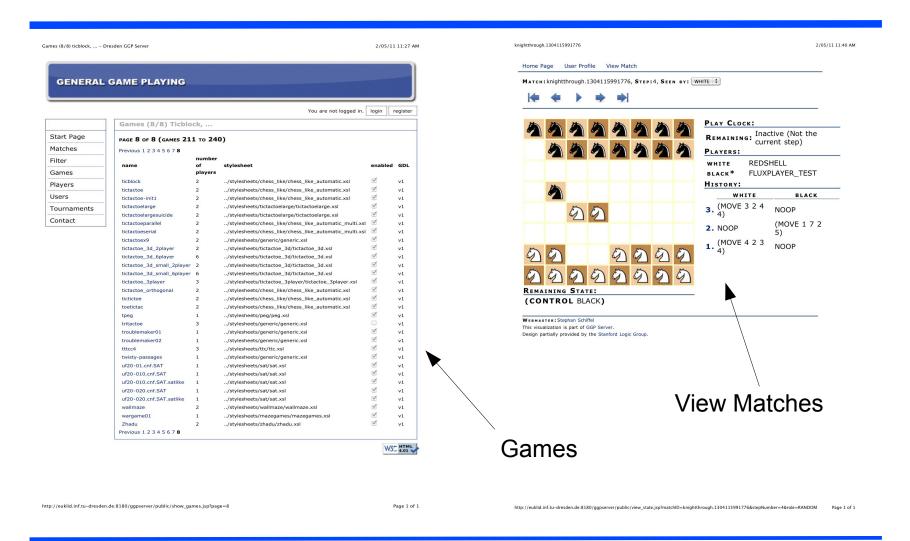
```
(<= (r ?x ?y) (p ?x ?y) (not (q ?y)))
```

Semantics is the same.

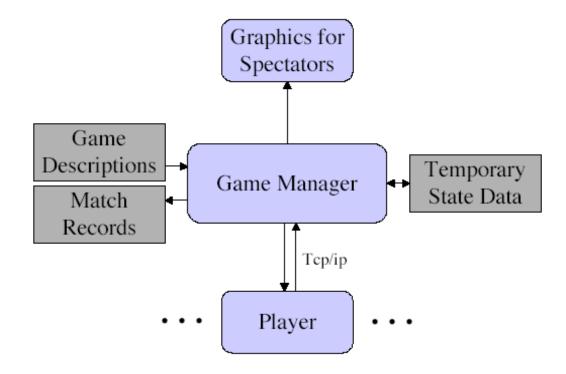
## Noughts And Crosses in KIF

```
(role xplayer)
                                      (<= (legal ?p (mark ?m ?n))</pre>
                                                                            (<= (line ?w)
(role(oplayer)
                                          (true (cell ?m ?n b))
                                                                                (or (row ?m ?w)
                                          (true (control ?p)))
                                                                                     (column ?n ?w)
(init (cell 1 1 b))
                                      (<= (legal xplayer noop)
                                                                                    (diagonal ?w)))
(init (cell 1 2 b))
                                           (true (control oplayer)))
(init (cell 1 3 b))
                                      (<= (legal oplayer noop)</pre>
                                                                            <= open
(init (cell 2 1 b))
                                          (true (control xplayer)))
                                                                                (true (cell ?m ?n b)))
(init (cell 2 2 b))
(init (cell 2 3 b))
                                      (<= (row ?m ?w)
                                                                            (<= terminal</pre>
(init (cell 3 1 b))
                                           (true (cell ?m 1 ?w))
                                                                                (or (line x) (line o)))
(init (cell 3 2 b))
                                                                            (<= terminal</pre>
                                           (true (cell ?m 2 ?w))
(init (cell 3 3 b))
                                           (true (cell ?m 3 ?w)))
                                                                                (not open))
(init (control xplayer))
                                      (<= (column ?n ?w)
                                            (true (cell 1 ?n ?w))
                                                                            (<= (goal xplayer 100)
(<= (next (cell ?m ?n x))</pre>
                                            (true (cell 2 ?n ?w))
                                                                                (line x))
    (does xplayer (mark ?m ?n))
                                            (true (cell 3 ?n ?w)))
                                                                            (<= (goal xplayer 50)</pre>
(<= (next (cell ?m ?n o))</pre>
                                      (<= (diagonal ?w)</pre>
                                                                                draw
    (does oplayer (mark ?m ?n))
                                            (true (cell 1 1 ?w))
                                                                            (<= (goal xplayer 0)</pre>
(<= (next (cell ?m ?n ?w))</pre>
                                            (true (cell 2 2 ?w))
                                                                                (line o))
    (true (cell ?m ?n ?w))
                                            (true (cell 3 3 ?w)))
                                                                            (<= (goal oplayer 100)
    (does ?p (mark ?j ?k))
                                      (<= (diagonal ?x)
                                                                                (line o))
    (or (distinct ?m ?j)
                                            (true (cell 1 3 ?w))
                                                                            (<= (goal oplayer 50)</pre>
         (distinct ?n ?k)))
                                            (true (cell 2 2 ?w))
                                                                                draw
(<= (next (control xplayer))</pre>
                                            (true (cell 3 1 ?w)))
                                                                           (<= (goal oplayer 0)</pre>
    (true (control oplayer)))
                                                                                (line x))
(<= (next (control oplayer))</pre>
    (true (control xplayer)))
```

# http://130.208.241.192/ggpserver/index.jsp



## Game Manager



#### **Communication Protocol**

Manager sends START message to players

```
(START <MATCH ID> <ROLE> <GAME DESCRIPTION> <STARTCLOCK> <PLAYCLOCK>)
```

- Match ID: the name of the game
- Role: the name of the role you are playing (e.g. xplayer or oplayer)
- Game description: the axioms describing the game
- Start/play clock: how much time you have before the game begins/per turn
- Manager sends PLAY message to players (PLAY <MATCH ID> <PRIOR MOVES>)

```
Prior moves is a list of moves, one per player
```

- The order is the same as the order of roles in the game description
- e.g. ((mark 1 1) noop)
- Special case: for the first turn, prior moves is nil
- Players send back a message of the form MOVE, e.g. (mark 3 2)
- When the previous turn ended the game, Manager sends a STOP message (STOP <MATCH ID> <PRIOR MOVES>)

# http://www.general-game-playing.de/downloads.html

Downloads - General Game Playing 2/05/11 12:25 PM Home We provide programs that might help you to implement your own General Game Playing system. All programs contain source code and are distributed under GPL. Activities Research GAMECONTROLLER Literature GameController is a standalone game master clone written entirely in Java and developed as part of the GGPServer Getting Started project. It is particularly useful for testing your own general game playing system. GameController comes with a simple GUI and a command line interface. Send bug reports and suggestions to Stephan Schiffel. Downloads Download the most recent version from the sourceforge project page Links **Download Manager** · Java 1.6 runtime environment java -jar gamecontroller-XY2.jar BASIC PROLOG PLAYER A basic player implemented in ECLiPSe Prolog based on code from FLUXPLAYER. Download current version (1.1) System requirements: . ECLiPSe Prolog version 5.10 or higher Changes since version 1.0 **Download Basic Players** · the port should be free now after stopping the player (last update: 12 March 2009) BASIC JAVA PLAYER A basic player implemented in Java which comes with a framework for implementing your strategies, analyzing the game, etc. It can be found on the Palamedes-IDE website. BASIC C++ PLAYER A basic player implemented in C++ with the reasoner of the prolog player above. Download current version (1.6) Linux/Unix (or any system which provides sockets) Page 1 of 2 http://www.general-game-playing.de/downloads.html

# GameControllerApp

000		GameController (tictactoe)					
		Startclock	TestMatch_1				
Role XPLAYER	Type RANDOM	Playclock	5 Port	Value 0	0		
OPLAYER	RANDOM	-		0	100		
INEO/12-42-1	15.123): match:To	Stop		r Log			
	.5.129): game:tic		GDL VI				
INFO(12:43:1 INFO(12:43:1	15.129): starting 15.131): step:1	game with st	artclock=10, playclo				
B)(CELL 2 2 B)	)(CELL 2 3 B)(CEL	L 3 1 B)(CELL	. 1 B)(CELL 1 2 B)(CELI . 3 2 B)(CELL 3 3 B)(CC yer: local(Random)				
INFO(12:43:1 INFO(12:43:1	.5.136): role: OPL .5.137): Sending	AYER => pla start messag	yer: local(Random) ges		4 +		
INEU/13-13-1	5 152) time after	er asmostart	c runThroads: Man M	27 U2 12-13-12 ECT	1		

## **Background Reading**

#### Logic

Russell & Norvig AIMA: Chapter 7 – Section 7.4
 Chapter 8 – Sections 8.1 and 8.2

#### General Game Playing

games.stanford.edu/competition/misc/aaai.pdf

# New Online Course on General Game Playing

www.coursera.org/courses/ggp

starts 1 Apr 2013