Specware to Isabelle Translator Manual

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Table of Contents

1. Concepts	
2. Usage	
2.1. Starting Up	
2.2. Using The Translator	
2.3. Proof Scripts in Specs	
2.4. Translation Tables	4

Chapter 1. Concepts

This is the initial experimental release of a Specware interface that allows the use of Isabelle/HOL to discharge proof obligations that arise in developing Specware specifications. The interface is essentially just an emacs command that converts a Specware spec to an Isabelle theory, along with extensions in the Specware syntax to allow Isabelle proof scripts to be embedded in Specware specs, and to allow the user to specify translation of Specware ops and types to existing Isabelle constants and types. The translation translates Specware declarations, definitions, axioms and theorems to the corresponding Isabelle versions. The logics are similar so it is usually straightforward to compare the source and target of the translations. In addition, Specware has implicit type obligations, particularly sub-type obligations, that are explicated in the Isabelle target.

We assume the user is familiar with Isabelle/HOL. See the tutorial at http://isabelle.in.tum.de/documentation.html. An example Specware spec with Isabelle proofs is given in Examples/IsabelleInterface/BoolEx.sw. This spec corresponds to the Isabelle theory in section 2.2.4 of the Isabelle/HOL tutorial. As another example, all of the proof obligations of the specs in Examples/Matching/MatchingSpecs.sw can be translated and proved by Isabelle without any user annotation.

To see examples of how to specify translation of Specware types and ops to existing Isabelle types and constants, see the bottom of the Specware Base library specs such as Library/Base/Integer.sw or Library/Base/List.sw.

A Specware definition may translate into one of three different kinds of Isabelle definitions: defs, recdefs and primrecs (primitive recursions). Simple recursion on coproduct constructors translates to primrec, but if the function has multiple arguments, only if the function is curried. Other recursion translates to recdef which, in general, requires a user-supplied measure function to prove termination. Non-recursive functions are translated to defs, except in some cases they are translated to recdefs which allow more pattern matching.

This initial translator has a number of limitations. It should translate all Specware specs but not all translated definitions and constructs will be accepted by Isabelle/HOL. In particular, only case expressions that involve a single level of pattern-matching on constructors are accepted. An exception, is that some nesting is allowed in top-level case expressions that are converted into definition cases. Local recursive functions in Specware are lambda-lifted to top-level functions in Isabelle/HOL. Mutual recursion is not currently supported.

Chapter 1. Concepts

Chapter 2. Usage

2.1. Starting Up

Specware and Isabelle can both be started up normally, each running under their own XEmacs job, but it convenient to run them under the same XEmacs. To do this run SpecwareIsabelle.

Currently Isabelle does not run under Windows so this script is not available there. However, the translator can run from Specware even if Isabelle is not running.

2.2. Using The Translator

The translator is called using the emacs command c-c c-i. The translation is written to a file in the Isa sub-directory of the current directory and the file is visited in a buffer. The user may then process the Isabelle theory providing proof steps as necessary. These proofs may then be copied back to the Specware spec so that the next time it is translated, the translation will include the proofs.

2.3. Proof Scripts in Specs

An embedded Isabelle proof script in a Specware spec consists of an introductory line beginning with proof Isa, the actual Isabelle script on subsequent lines terminated by the string end-proof. For example, the simple proof script apply(auto) can be embedded as follows:

```
proof Isa
  apply(auto)
end-proof
```

If the last command before end-proof is not done or sorry, the command done is inserted.

The proof script should occur immediately after the theorem that it applies to. If the script applies to a proof obligation that is not explicit in the spec, then the name of the obligation should appear after proof Isa, on the same line. Such named scripts may not occur immediately after a theorem or definition. Because of this restriction, it is

Chapter 2. Usage

sometime necessary to insert and empty proof annotation after a theorem or definition, as follows:

```
proof Isa end-proof
```

If the user does not supply a proof script for a theorem then the translator will supply the script apply(auto) which may be all that is required to prove simple theorems.

Annotations for theorems may be included on the proof Isa line. For example,

```
theorem Simplify_valif_normif is
   fa(b,env,t,e) valif (normif b t e) env = valif (IF(b, t, e)) env
proof Isa [simp]
   apply(induct_tac b)
   apply(auto)
   end-proof

translates to

theorem Simplify_valif_normif [simp]:
   "valif (normif b t e) env = valif (IF b t e) env"
   apply(induct_tac b)
   apply(auto)
   done
```

In this example we see that universal quantification in Specware becomes, by default, implicit quantification in Isabelle. This is normally what the user wants, but not always. The user may specify the variables that should be explicitly quantified by adding a clause like fate. to the proof Isa line. For example,

```
theorem Simplify_valif_normif is
   fa(b,env,t,e) valif (normif b t e) env = valif (IF(b, t, e)) env
   proof Isa [simp] fa t e.
       apply(induct_tac b)
       apply(auto)
   end-proof

translates to

theorem Simplify_valif_normif [simp]:
   "\<forall>t e. valif (normif b t e) env = valif (IF b t e) env"
       apply(induct_tac b)
```

```
apply(auto)
done
```

The \<forall> will be displayed as a universal quantification symbol using X-Symbol mode in Isabelle. Note that instead of fa in the proof Isa line the user may use the X-Symbol for universal quantification.

Recursive functions that are translated to recdefs can have a measure function specified on the proof Isa line, by including it between double-quotes. For example: proof Isa "measure ("\"<lambda>(wrd,sym). length wrd)" end-proof

2.4. Translation Tables

A translation table for Specware types and ops is introduced by a line beginning proof Isa Thy_Morphism followed optionally by an Isabelle theory (which will be imported into the translated spec), and terminated by the string end-proof. Each line gives the translation of a type or op. For example, for the Specware Integer theory we have:

```
proof Isa Thy_Morphism Presburger
  type Integer.Integer -> int
  type Nat.Nat -> nat (int,nat) [+,*,div,rem,<=,<,>=,>,abs,min,max]
  Integer.+ -> + Left 25
  Integer.- -> - Left 25
  IntegerAux.- -> -
  Integer.~ -> -
  Integer.* -> * Left 27
  Integer.div -> * Left 27
  Integer.rem -> * Left 27
  Integer.<= -> \<le> Left 20
  Integer.< -> < Left 20</pre>
  Integer.>= -> \<ge> Left 20
  Integer.> -> > Left 20
  Integer.min -> min curried
  Integer.max -> max curried
 end-proof
```

A type translation begins with the word type followed by the fully-qualified Specware name, \rightarrow and the Isabelle name. If the Specware type is a sub-type, you can specify coercion functions to and from the super-type in parentheses separated by commas.

Chapter 2. Usage

Note that by default, sub-types are represented by their super-type, so you would only specify a translation if you wanted them to be different, in which case coercion functions are necessary. Following the coercions functions can appear a list of overloaded functions within square brackets. These are used to minimize coercions back and forth between the two types.

An op translation begins with the fully-qualified Specware name, followed by -> and the Isabelle constant name. If the Isabelle constant is an infix operator, then it should be followed by Left or Right depending on whether it is left or right associative and a precedence number. Note that the precedence number is relative to Specware's precedence ranking, not Isabelle's. Also, an uncurried Specware op can be mapped to a curried Isabelle constant by putting curried after the Isabelle name, amd a binary op can be mapped with the arguments reversed by appending reversed to the line.