

Assignment 1A

Name Ketan V. Choudhary

Class BE

Roll no 12

Subject AI

DOP	DoA	Marks	Sign

Q2) Consider following instance of 8 puzzle problem:

8	7	6
2	1	5
3	4	-

Initial

-	8	7
2	1	6
3	4	5

final configuration

Consider Heuristic function defined below:

h_1 = Missplaced tile Count except space

h_2 = Correctly placed files Count except space

h_3 = Sum of Manhattan distance between current and correct position of all tiles except space

Answer the following question

Q) In 8-puzzle problem we are concerned with getting to goal configuration within least number of steps. All moves are the equally costly. Define $g(n)$ in your own words. What will be the cost of 6 steps solution to some arbitrary 8-puzzle instance.

Ans:- The lowest path cost $g(n)$ can be the cost to reach the goal configuration in least steps. In our case, we can reach the final configuration in at least 4 moves: UP, LEFT, LEFT. Since all the moves are equally costly, we compute $g(n)$ as

$$g(n) = 1 + 1 + 1 + 1$$

$$g(n) = 4$$

Consider the following arbitrary 8-puzzle instance which gives solution in 6 steps.

8	7	6
2	1	5
-	3	4

The solution can be represented as:

$\{\{8, 7, 6\}, \{2, 1, 5\}, \{-, 3, 4\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, 5\}, \{3, -, 4\}\}$

$\rightarrow \{\{8, 7, 6\}, \{2, 1, 5\}, \{3, 4, -\}\} \rightarrow \{\{8, 7, 6\}, \{2, 1, -\}, \{3, 4, 5\}\} \rightarrow$
 $\{\{8, 7, -\}, \{2, 1, 6\}, \{3, 4, 5\}\} \rightarrow \{\{8, -, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\}$
 $\{\{-, 8, 7\}, \{2, 1, 6\}, \{3, 4, 5\}\}$

Since all the moves are equally costly, the cost could be $g(n) = 6$

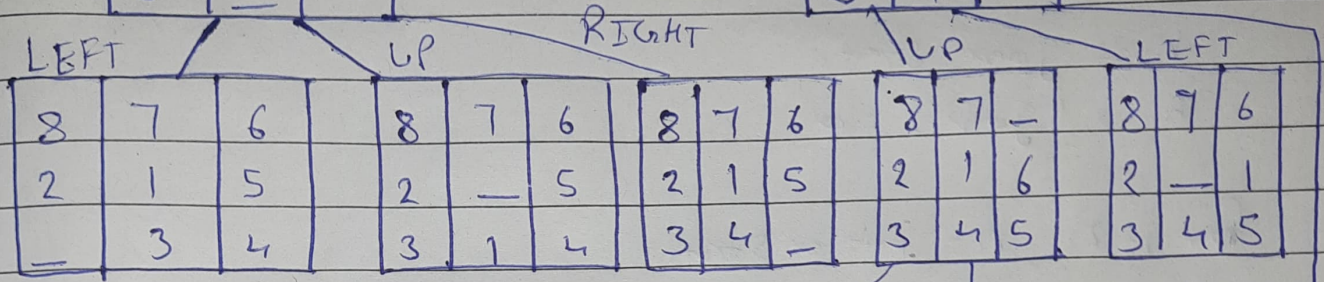
(c) Draw Exhaustive State Space tree of depth limited to 4 for instance of 8-puzzle problem in the question.

Ans c →

8	7	6
2	1	5
3	4	-

8	7	6
2	1	5
3	-	4

8	1	6
2	1	-
3	4	5



Down

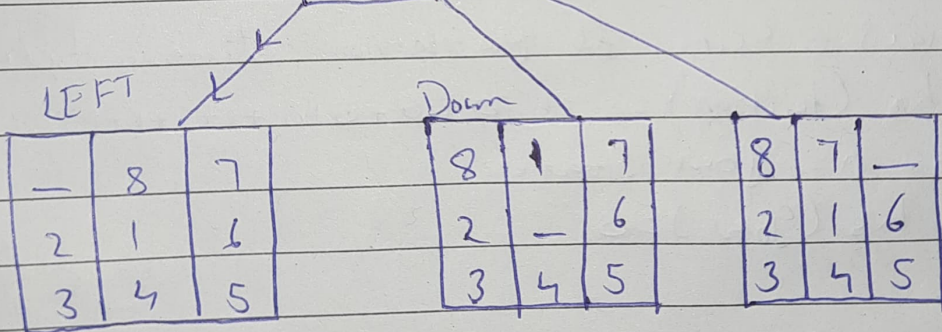
8	7	6
2	1	5
3	4	-

LEFT

8	-	7
2	1	6
3	4	5

Down

8	7	6
2	1	-
3	4	5



final
configuration

e) Compute $h_i(n)$ when $i=1,2,3$ And $n = \text{initial State}$
final / goal State question

Ans \rightarrow for $i=1$, $n = \text{initial State}$

$h_1(\text{initial}) = \text{this Placed tiles Count except space}$

$$h_1(\text{initial}) = 4$$

$n = \text{goal State}$

$$h_1(\text{goal}) = 0$$

for $i=2$, $n = \text{initial State}$

$h_2(\text{initial}) = \text{Correctly placed tiles Count except space}$

$$h_2(\text{initial}) = 4$$

for $n = \text{goal State}$

$$h_2(\text{goal}) = 8$$

for $i=3$, $n = \text{initial State}$

$h_3(\text{initial}) = \text{Sum of Manhattan distance between}$
~~current~~ $h_3(\text{initial}) = -1 + 0 + 0 + 0 + 1 + 1 + 1 + 1$

for $n = \text{goal State}$

$$h_3(\text{goal}) = 0$$