Finite State Machine Maker

albab

Solution

Graph

1. Regular Expression To Epsilon-NFA

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Transition Table E-NFA

Transition Table				
Present State		Next State		
		ε	a	b
	q0		q1	
	ql	q9		
start	q8	q0,q2		
final	q9			
	q2			q3
	q3	q4		
	q4		q5	
	q5	q6		
	q6			q7
	q7	q9		

Graph

Transition Table E-NFA

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		ε	a	b
	q0		q1	
	ql	q9		
start	q8	q0,q2		
final	q9			
	q2			q3
	q3	q4		
	q4		q5	
	q5	q6		
	q6			q7
	q7	q9		

Step 1: ε-closure of each state

$$\epsilon$$
-closure(q0) = {q0}
 ϵ -closure(q1) = {q1, q9}
 ϵ -closure(q8) = {q8, q0, q2}
 ϵ -closure(q9) = {q9}
 ϵ -closure(q2) = {q2}
 ϵ -closure(q3) = {q3, q4}
 ϵ -closure(q4) = {q4}
 ϵ -closure(q5) = {q5, q6}
 ϵ -closure(q6) = {q6}
 ϵ -closure(q7) = {q7, q9}

Step 2: δ' transition for each state

$$\delta'(q0-a) = \{q1, q9\}$$

 $\delta'(q0-b) = \{\}$
 $\delta'(q1-a) = \{\}$
 $\delta'(q1-b) = \{\}$
 $\delta'(q8-a) = \{q1, q9\}$

$$\delta'(q8-b) = \{q3, q4\}$$

$$\delta'(q9-a) = \{\}$$

$$\delta'(q9-b) = \{\}$$

$$\delta'(q2-a) = \{\}$$

$$\delta'(q2-b) = \{q3, q4\}$$

$$\delta'(q3-a) = \{q5, q6\}$$

$$\delta'(q3-b) = \{\}$$

$$\delta'(q4-a) = \{q5, q6\}$$

$$\delta'(q4-b) = \{\}$$

$$\delta'(q5-a) = \{\}$$

$$\delta'(q5-b) = \{q7, q9\}$$

$$\delta'(q6-a) = \{\}$$

$$\delta'(q6-b) = \{q7, q9\}$$

$$\delta'(q7-a) = \{\}$$

Transition Table NFA

Transition Table			
Present State		Next State	
		а	b
start	q8	q1,q9	q3,q4
final	ql		
final	q9		
	q3	q5,q6	
	q4	q5,q6	
	q5,q6		
	q3,q4		
final	q1,q9		

NFA Graph

3. NFA to DFA Conversion

Transition Table				
Drocont Ctato		Next State		
riesei	Present State		b	
start	q8	q1,q9	q3,q4	
final	ql			
final	q9			
	q3	q5,q6		
	q4	q5,q6		
	q5,q6			
	q3,q4			
final	q1,q9			

DFA Transition Table

Transition Table				
Present State		Next State		
		a	b	
start	q8	q1,q9	q3,q4	
final	q1,q9	qd	qd	
	q3,q4	qd	qd	
	qd	qd	qd	

Graph

4. Minimization of DFA

step 1: remove unreachable states

{ qd }

Transition Table				
Present State		Next State		
		а	b	
start	q8	q1,q9	q3,q4	
final	q1,q9	qd	qd	
	q3,q4	qd	qd	
	qd	qd	qd	

step 3: Divide the states into partitions:

Partition: 1

{"q8" "q3,q4" } {"q1,q9" }

Partition: 2

{"q8" } {"q3,q4" } {"q1,q9" }

Partition: 3

{"q8" } {"q3,q4" } {"q1,q9" }

Minimized DFA Transition Table

Transition Table				
Present State		Next State		
		а	b	
start	q8	q1,q9	q3,q4	
	q3,q4	qd	qd	
final	q1,q9	qd	qd	

Graph