

Since $s \in \text{NP-hard}$, and $s \leq_k t$, then, for any problem p , such that $p \in \text{NP}$, we can have that $p \leq_k s$. Now, by the transitivity property, since $p \leq_k s$ and $s \leq_k t$, we can say that $p \leq_k t$. Now, by the definition of NP-hard, a problem p is NP-hard if for all $q \in \text{NP}$, $q \leq_k p$. Since for all problems $p \in \text{NP}$, we can have that $p \leq_k t$, it means that the problem t is also NP-hard.