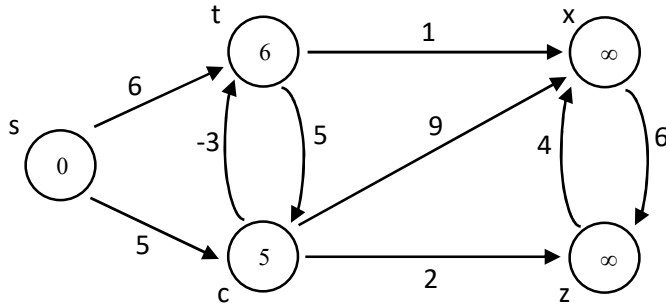


By considering the proof for Theorem 24.6, we can see that the proof builds on top of the loop invariant which is that: At the start of each iteration of the while loop of lines 4-8,  $d[v] = \delta(s, v)$  for each vertex  $v \in S$ . But when the graph has negative edge-weights, this invariant does not hold anymore. For the proof, where it really falls apart is that it says  $\delta(s, y) \leq \delta(s, u)$ . If the graph contain only positive edge-weights, then this is absolutely true, but since we allow the graph to contain negative edge-weights, it's possible that  $\delta(s, y) \geq \delta(s, u)$  if the path connecting  $y$  and  $u$  has negative edge-weights, and this would cause the followed proofs to be wrong. An example would be:



For this graph, after the first while loop,  $t$  and  $c$  would have their value being 6 and 5. And in this case, let  $t$  be the  $y$  in the proof, and let  $c$  be the  $u$  in the proof. If the graph contain only positive edge-weights, then  $\delta(s, y) \leq \delta(s, u) \rightarrow \delta(s, t) \leq \delta(s, c)$  is right, and the proof would be fine. But sin there exists negative edge-weights,  $\delta(s, c) = 3$ , and  $\delta(s, y) \geq \delta(s, u) \rightarrow \delta(s, t) \leq \delta(s, c)$ , and this is where the proof falls apart and the invariant doesn't hold.