

For this problem, will use proof by contradiction. For any correct, deterministic algorithm, to even read through the entire input array would take time  $\Omega(n)$ . So, if there's an algorithm for the problem that runs in time  $o(n)$ , there must exist some  $n_0 < n$  and array  $A[1, \dots, n_0]$  for which the algorithm does not even read all the array entries.

However, in order to guarantee the algorithm is correct, one must check each entry in  $A$  in order to make sure that they are sorted in non-decreasing order, which means that for each entry  $x_i \in A$ ,  $A[x_i] \leq A[x_{i+1}]$ . And this is the only way to make sure that the array is sorted in non-decreasing order as if the algorithm fails to check any entries in the input array, it can not guarantee that the array is sorted in non-decreasing order, for that missed entry  $x_i$  may be smaller than  $x_{i-1}$ .

As a result, any correct, deterministic algorithm must check all  $n$  entries in array  $A$ . Hence, there does not exist  $n_0 < n$  and array  $A[1, \dots, n_0]$  for which the algorithm does not even read all the array entries. And this is a contradiction, so for any correct, deterministic algorithm for this problem, it would run in time  $\Omega(n)$ .